

Deep Learning

Content

- Vanishing Gradient & Activation Functions
- Dropout
- Batch Normalization

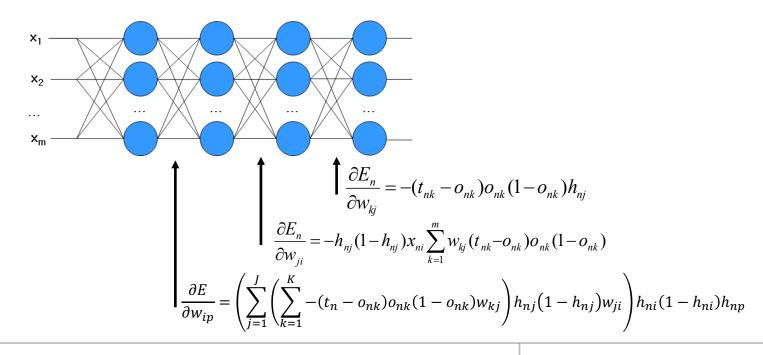


Gradient Vanishing & Activation Functions

Gradient Vanishing & Exploding

Gradient is easy to vanish or explode

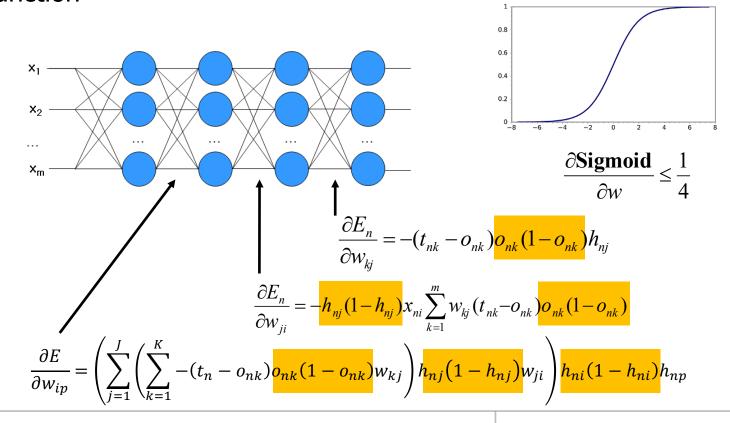
- To many terms are multiplied.
- If some are small numbers, gradient becomes very small.
- If some are large numbers, gradient becomes very large.



Activation Function

Vanishing Gradient

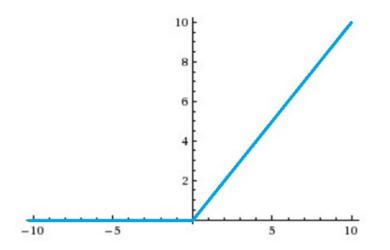
The major terms are the derivatives of the activation function



Activation Function

Using another functions instead of sigmoid

Rectified Linear Unit (ReLU)



$$f(x) = \begin{cases} x & \text{if } x > 0\\ 0 & \text{otherwise} \end{cases}$$

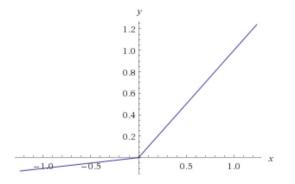
$$\frac{df(x)}{dx} = \begin{cases} 1 & \text{if } x > 0 \\ 0 & \text{otherwise} \end{cases}$$

Activation Function

You may use another

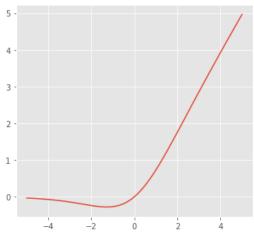
Leaky ReLU

$$f(x) = \begin{cases} x & \text{if } x > 0\\ 0.01x & \text{otherwise} \end{cases}$$



Swish (or SiLU-Sigmoid Linear Unit)

$$f(x) = \frac{x}{1 + e^{-x}}$$

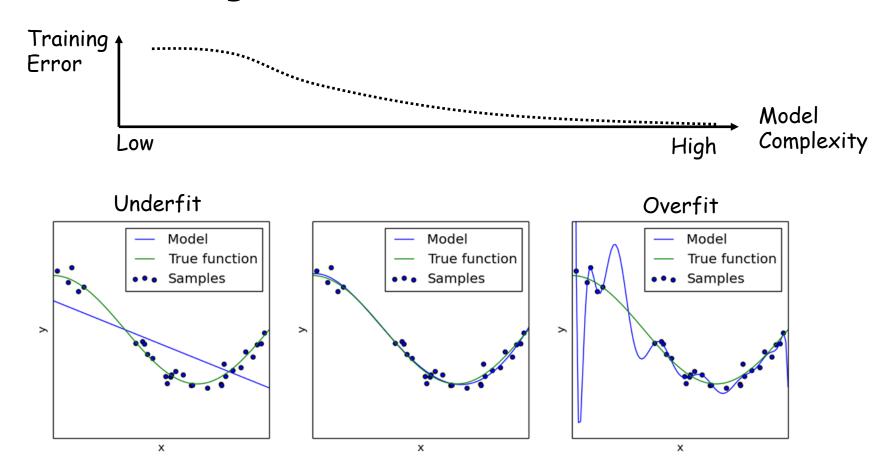




Regularization

Overfitting

Overfitting



Regularization

What is Regularization

Introducing additional information to prevent over-fitting

Approaches

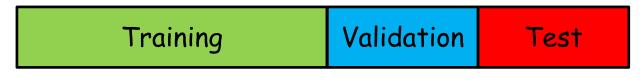
Proper Learning: Early stopping

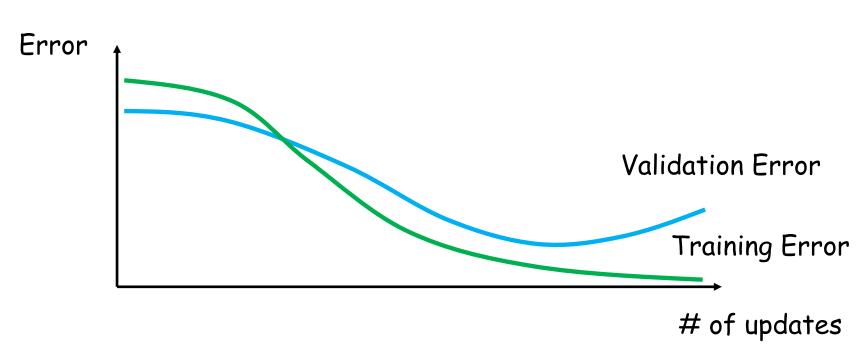
Proper Structure: Weight decay, Dropout,

DropConnect, Stochastic pooling

Early Stopping

Split data into 3 groups





L1 Regularization

- Leading most weights very close to zero
- Choosing a small subset of most important inputs

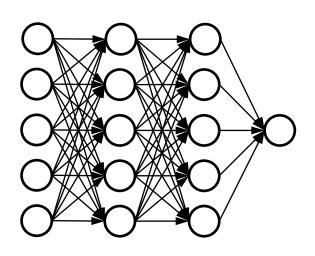
$$\widetilde{E}(\mathbf{w}) = E(\mathbf{w}) + \frac{\lambda}{2} |\mathbf{w}|$$

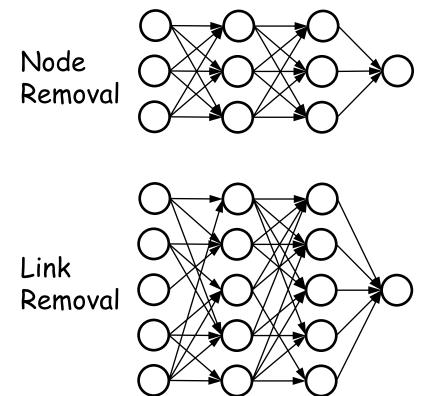
L2 Regularization

- Penalizing peaky weights
- Encouraging to use all of its inputs

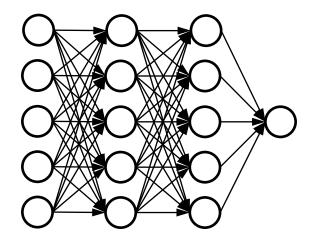
$$\widetilde{E}(\mathbf{w}) = E(\mathbf{w}) + \frac{\lambda}{2} \mathbf{w}^T \mathbf{w}$$

Complex Structure vs Simple Structure





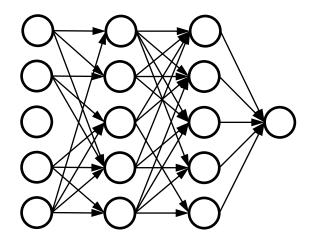
Complex Structure vs Simple Structure



Complex

Dense Connections

 $\sum |\mathbf{w}|$ is large

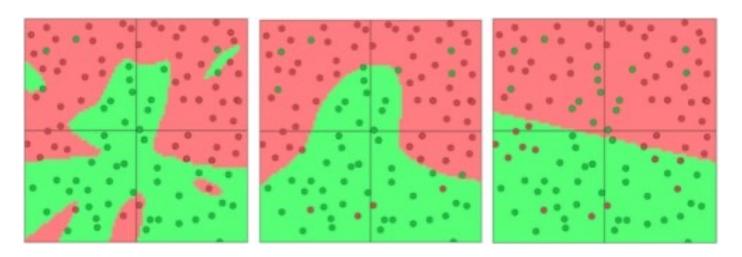


Simple

Most Connections close to O

 $\sum |w|$ is small

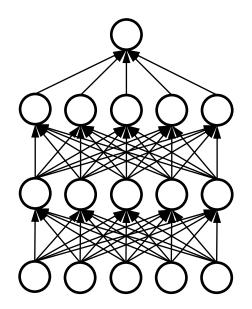
Example: Separating green and red

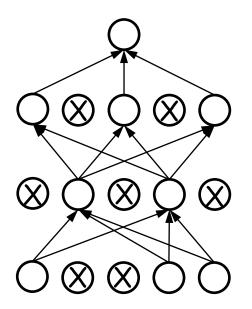


L2 regularization strengths of 0.01, 0.1, and 1

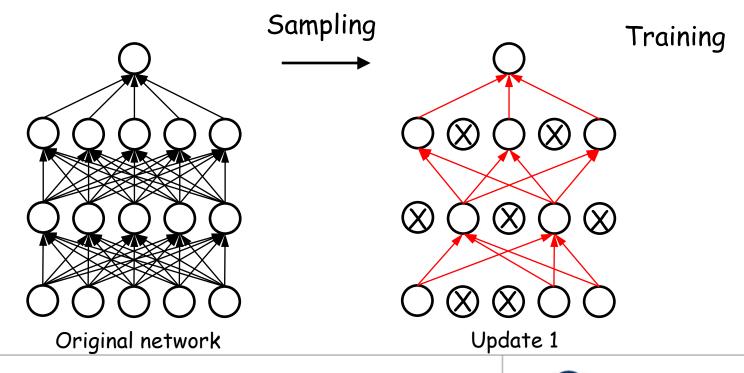
How can we reduce the structural complexity?

- Let's simply remove some nodes, and
- Train the simplified neural network
- Hmm??

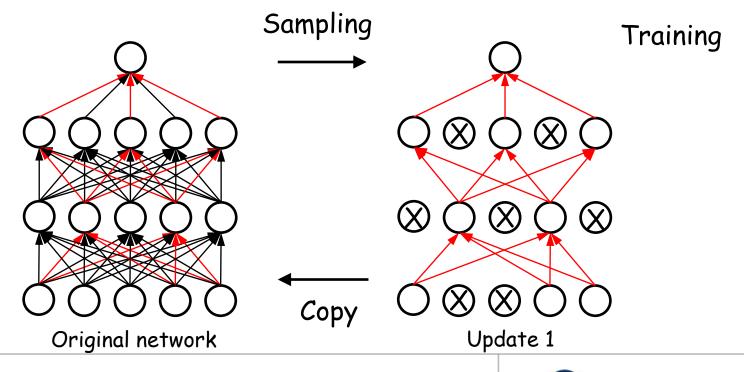




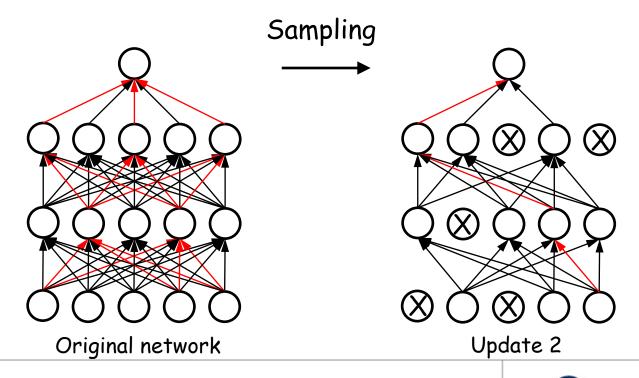
- How can we reduce the structural complexity without removing nodes?
 - Hmm??



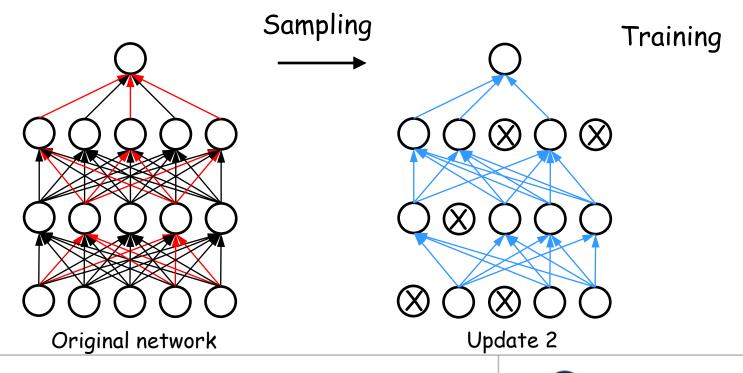
- How can we reduce the structural complexity without removing nodes?
 - Hmm??



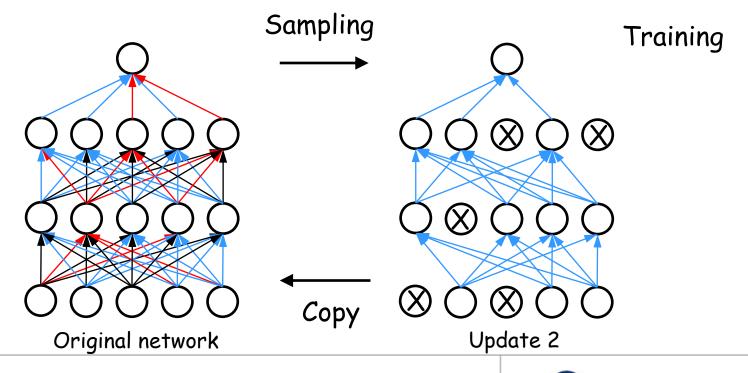
- How can we reduce the structural complexity without removing nodes?
 - Hmm??



- How can we reduce the structural complexity without removing nodes?
 - Hmm??

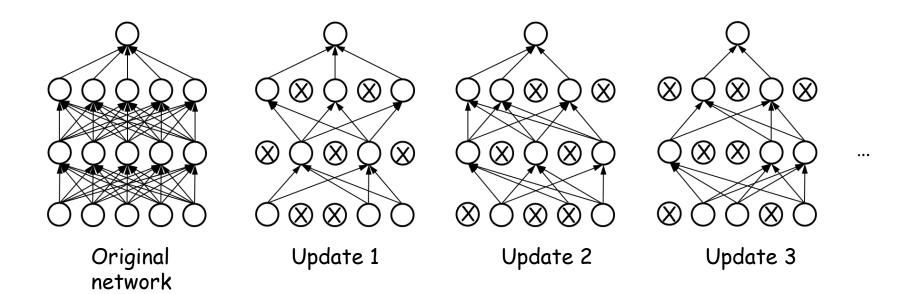


- How can we reduce the structural complexity without removing nodes?
 - Hmm??



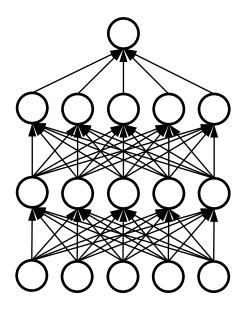
Do this at every epoch

- Randomly choose nodes with a probability of p
 - Usually p = 0.5
- Train the simplified neural network



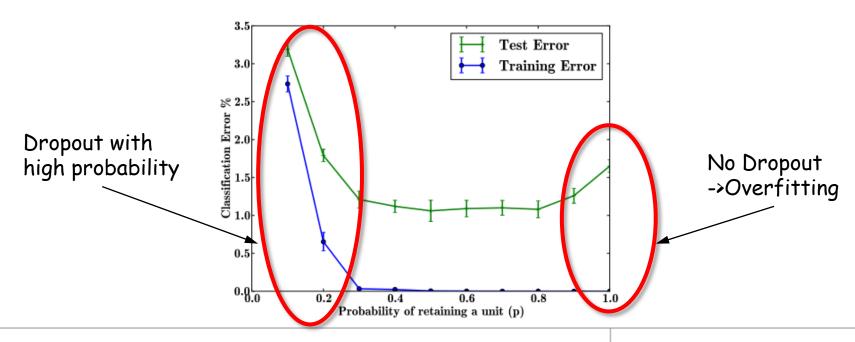
Testing

Use all the nodes without dropout



The effect of the dropout rate p:

- An architecture of 784-2048-2048-2048-10 is used on the MNIST dataset.
- The dropout rate p is changed from small numbers (most units are dropped out) to 1.0 (no dropout).



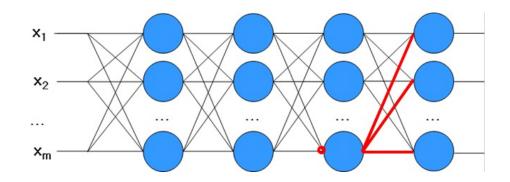
Summary

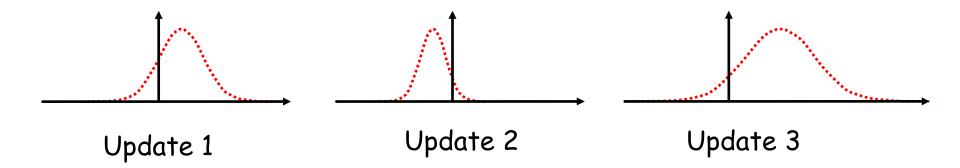
- Dropout is a very good and fast regularization method.
- Dropout is a bit slow to train (2-3 times slower than without dropout).
- If the amount of data is average-large dropout excels.
 When data is big enough, dropout does not help much.
- Dropout achieves better results than former used regularization methods (Weight Decay).



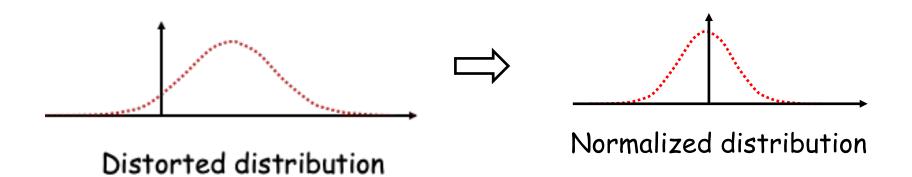
Distribution Shift

Output distribution of the red node

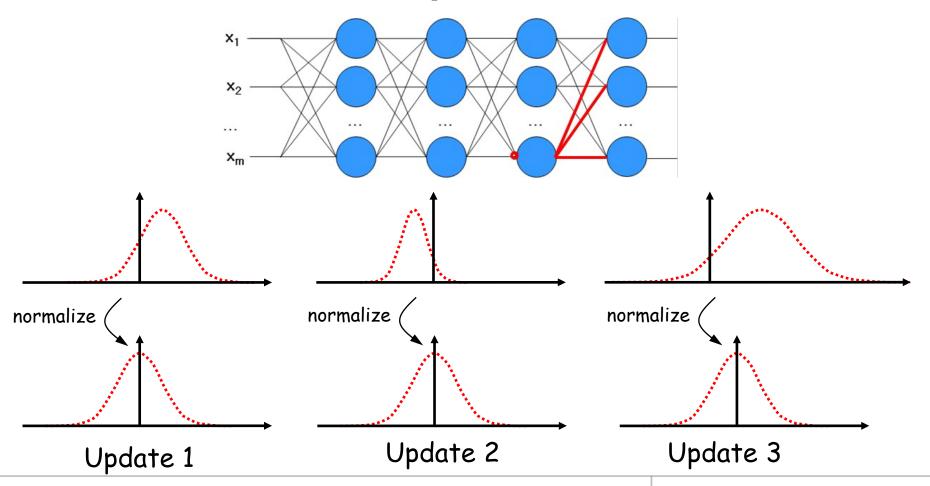




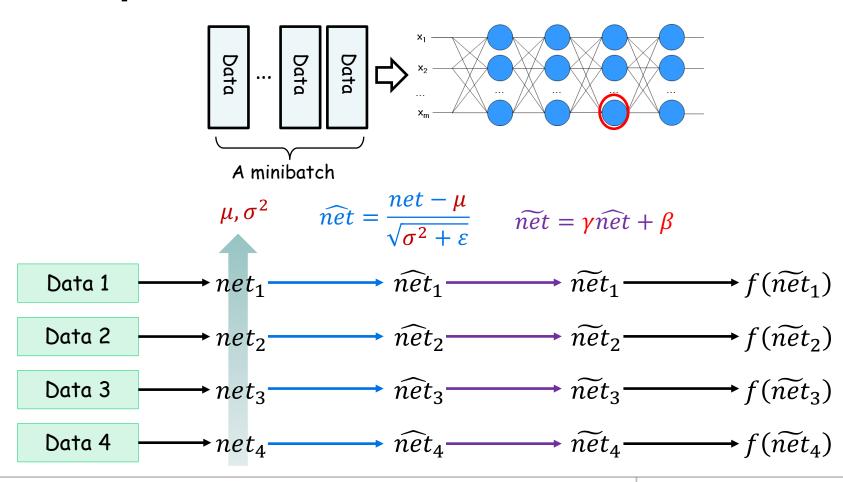
- Distribution Shift
 - It disturbs the learning process,
 - Learning is getting slow down
- Why don't we normalize the distribution of inputs



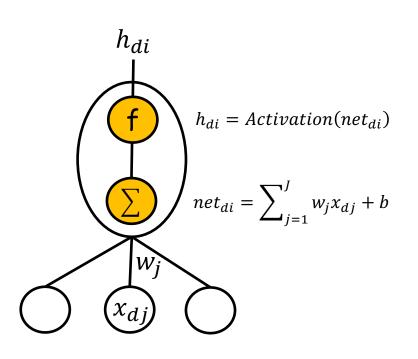
Normalization of outputs

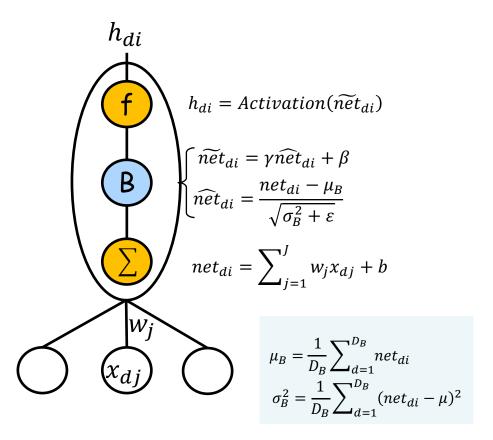


Input Normalization



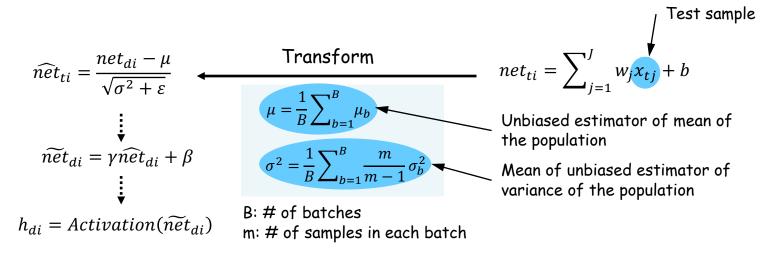
For a Single Node





Testing

- For Training, the mean and variance of each batch are used for normalization
- For Testing, of which data the mean and variance will be used?
 - Estimated with those of batches in the training



Advantage

- Reduces internal covariant shift.
- Reduces the dependence of gradients on the scale of the connection weights.
- Regularizes the model and reduces the need for regularization techniques.
 - It adds some stochastic noise to the activations as a result of using noisy estimates computed on the mini-batches. This has a regularization effect in some applications.