

# Lista 2 - Análise de Sobrevida

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## Exercício 1

### Item (a)

$$P(T > 1) = 1 - P(T < 1) = 1 - \int_0^1 2t * \exp\{-t^2\} dt = 1 - (1 - \exp\{-1\}) \approx 0,3679$$

### Item (b)

$$h(t) = \frac{f(t)}{S(t)} = \frac{2t * \exp\{-t^2\}}{\exp\{-t^2\}} \Rightarrow \lim_{t \rightarrow \infty} h(t) = \infty$$

## Exercício 2

##	tempos.ex2	censuras.ex2
## [1,]	7	0
## [2,]	34	0
## [3,]	42	0
## [4,]	63	0
## [5,]	64	0
## [6,]	74	1
## [7,]	83	0
## [8,]	84	0
## [9,]	91	0
## [10,]	108	0
## [11,]	112	0
## [12,]	129	0
## [13,]	133	0
## [14,]	133	0
## [15,]	139	0
## [16,]	140	0
## [17,]	140	0
## [18,]	146	0
## [19,]	149	0
## [20,]	154	0
## [21,]	157	0
## [22,]	160	0
## [23,]	160	0
## [24,]	165	0
## [25,]	173	0
## [26,]	176	0
## [27,]	185	1
## [28,]	218	0
## [29,]	225	0
## [30,]	241	0
## [31,]	248	0
## [32,]	273	0

```
## [33,]      279      1
## [34,]      297      0
## [35,]      319      1
## [36,]      405      0
## [37,]      417      0
## [38,]      420      0
## [39,]      440      0
## [40,]      523      0
## [41,]      523      1
## [42,]      583      0
## [43,]      594      0
## [44,]     1101      0
## [45,]     1116      1
## [46,]     1146      0
## [47,]     1226      1
## [48,]     1349      1
## [49,]     1412      1
## [50,]     1417      0
```

## Item (a)

```
require(survival)
```

```
## Loading required package: survival
```

```
KM.ex2 <-
survfit(Surv(time = tempos.ex2, event = censuras.ex2) ~ 1, conf.int = F)
NA.ex2 <-
survfit(coxph(Surv(tempos.ex2, censuras.ex2) ~ 1, method = "breslow"))
summary(KM.ex2)
```

```
## Call: survfit(formula = Surv(time = tempos.ex2, event = censuras.ex2) ~
##      1, conf.int = F)
##
##   time n.risk n.event survival std.err
##    74     45      1    0.978  0.0220
##   185     24      1    0.937  0.0451
##   279     18      1    0.885  0.0661
##   319     16      1    0.830  0.0819
##   523     11      1    0.754  0.1035
##  1116      6      1    0.629  0.1436
##  1226      4      1    0.471  0.1735
##  1349      3      1    0.314  0.1728
##  1412      2      1    0.157  0.1407
```

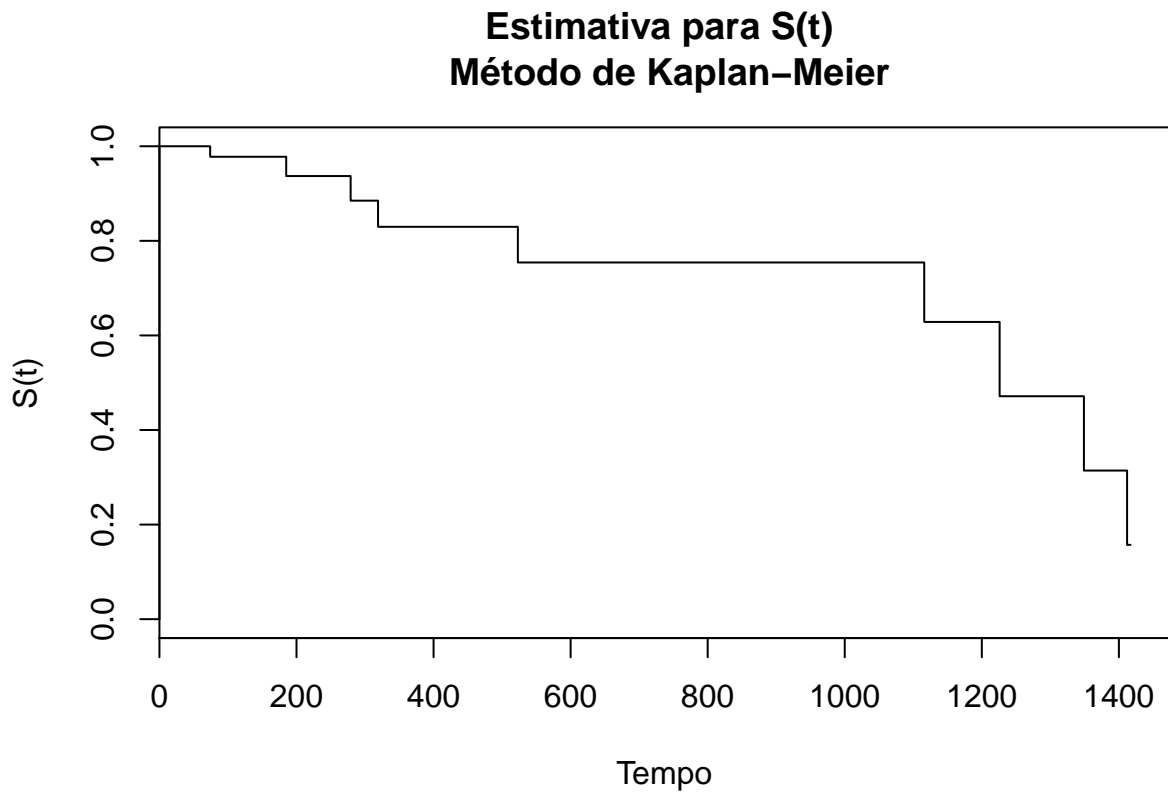
```
summary(NA.ex2)
```

```
## Call: survfit(formula = coxph(Surv(tempos.ex2, censuras.ex2) ~ 1, method = "breslow"))
##
##   time n.risk n.event survival std.err lower 95% CI upper 95% CI
##    74     45      1    0.978  0.0217      0.936      1.000
##   185     24      1    0.938  0.0443      0.855      1.000
##   279     18      1    0.887  0.0647      0.769      1.000
##   319     16      1    0.834  0.0801      0.691      1.000
```

##	523	11	1	0.761	0.1007	0.587	0.986
##	1116	6	1	0.644	0.1371	0.425	0.978
##	1226	4	1	0.502	0.1647	0.264	0.955
##	1349	3	1	0.360	0.1682	0.144	0.900
##	1412	2	1	0.218	0.1493	0.057	0.835

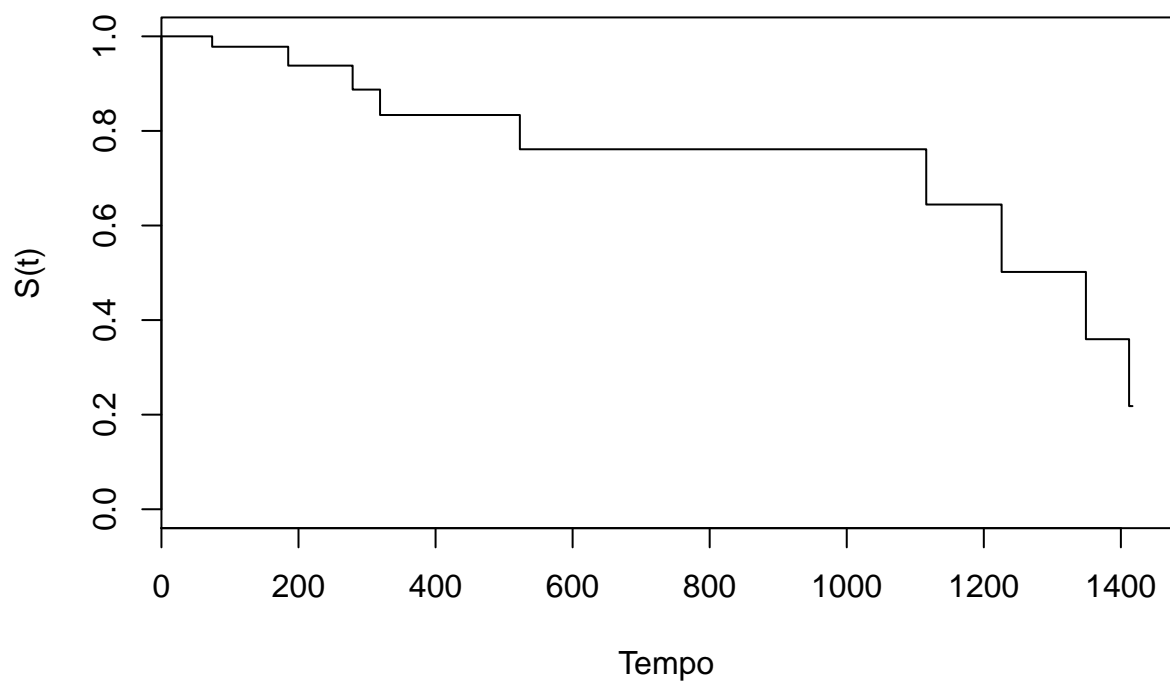
### Item (b)

```
plot(
  KM.ex2,
  conf.int = FALSE,
  xlab = "Tempo",
  ylab = "S(t)",
  main = "Estimativa para S(t) \n Método de Kaplan-Meier"
)
```



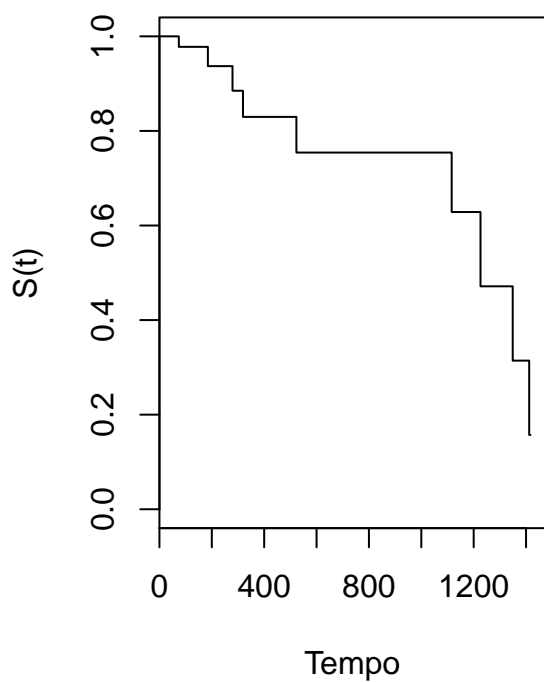
```
plot(
  NA.ex2,
  conf.int = FALSE,
  xlab = "Tempo",
  ylab = "S(t)",
  main = "Estimativa para S(t) \n Método de Nelson-Aalen"
)
```

## Estimativa para $S(t)$ Método de Nelson-Aalen

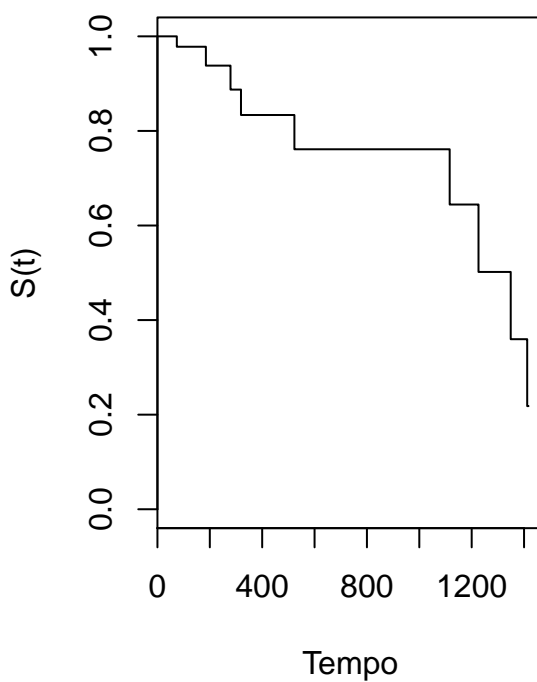


```
par(mfrow=c(1,2))
plot(
  KM.ex2,
  conf.int = FALSE,
  xlab = "Tempo",
  ylab = "S(t)",
  main = "Estimativa para S(t) \n Método de Kaplan-Meier"
)
plot(
  NA.ex2,
  conf.int = FALSE,
  xlab = "Tempo",
  ylab = "S(t)",
  main = "Estimativa para S(t) \n Método de Nelson-Aalen"
)
```

**Estimativa para  $S(t)$   
Método de Kaplan-Meier**

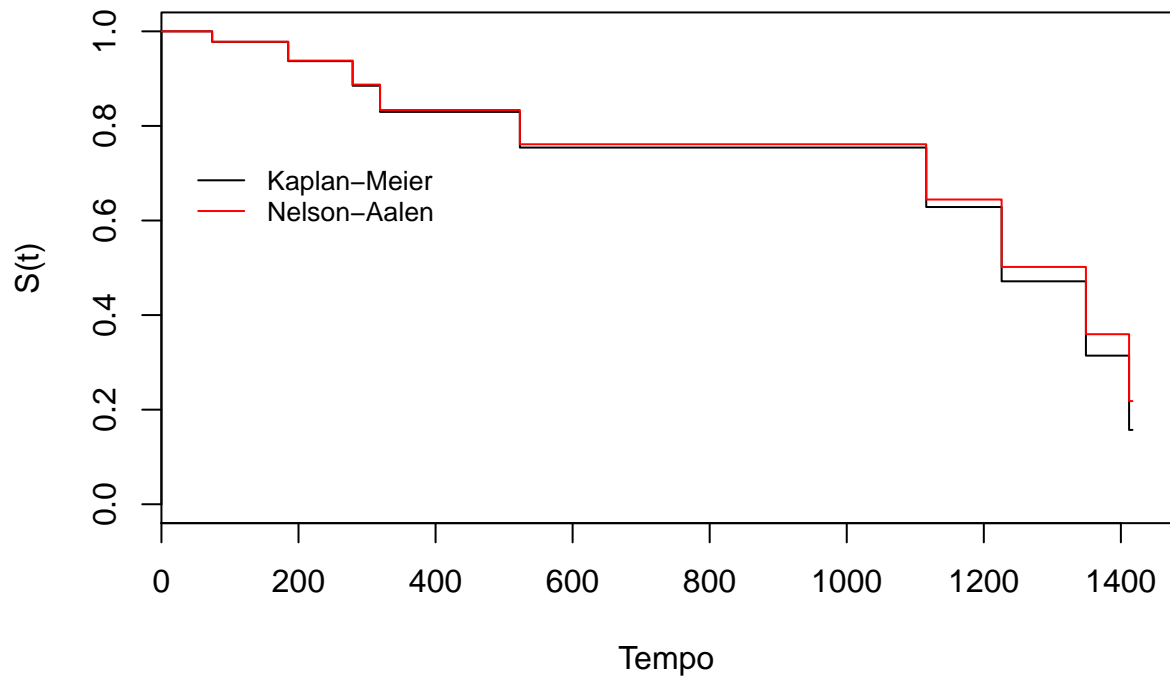


**Estimativa para  $S(t)$   
Método de Nelson-Aalen**



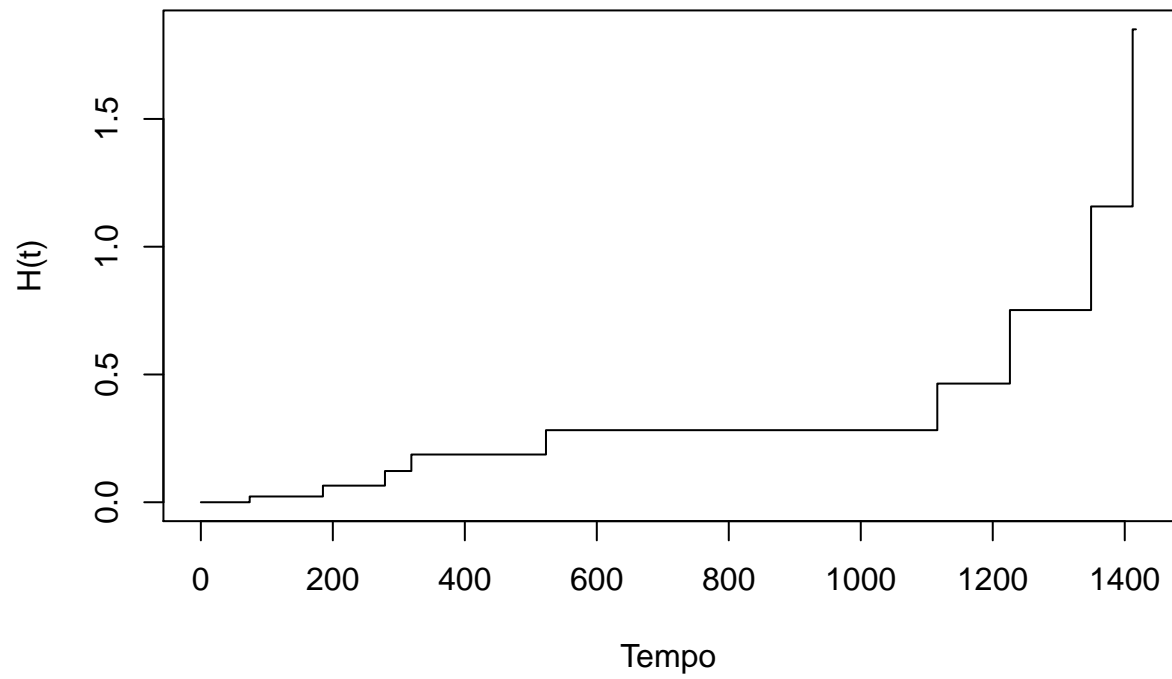
```
par(mfrow = c(1,1))
plot(
  KM.ex2,
  conf.int = FALSE,
  xlab = "Tempo",
  ylab = "S(t)",
  main = "Estimativas para S(t) \n "
)
lines(NA.ex2, col = 2, conf.int = F)
legend(20,0.75,lty=c(1,1),c("Kaplan-Meier","Nelson-Aalen"),bty="n",cex=0.8,col=c(1,2))
```

## Estimativas para $S(t)$



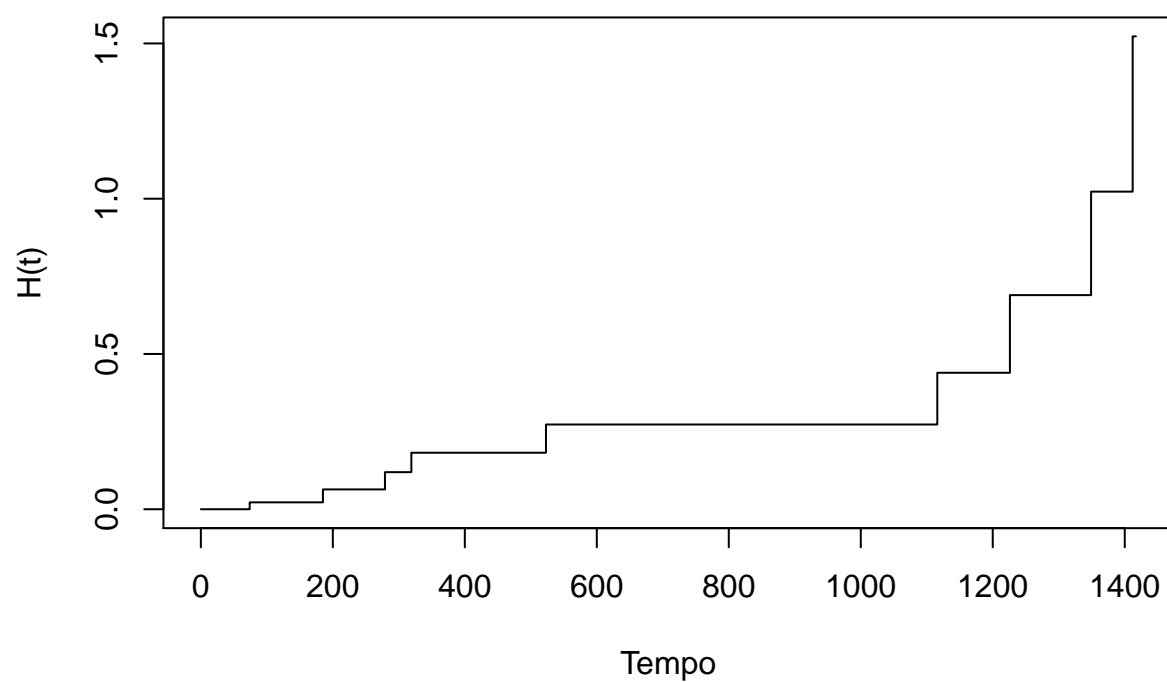
```
plot(KM.ex2, fun = "cumhaz", xlab = "Tempo", ylab = "H(t)", main = "Estimativa para H(t) \n Método de K
```

### Estimativa para $H(t)$ Método de Kaplan-Meier



```
plot(NA.ex2, conf.int = F, fun = "cumhaz", xlab = "Tempo", ylab = "H(t)", main = "Estimativa para H(t) ")
```

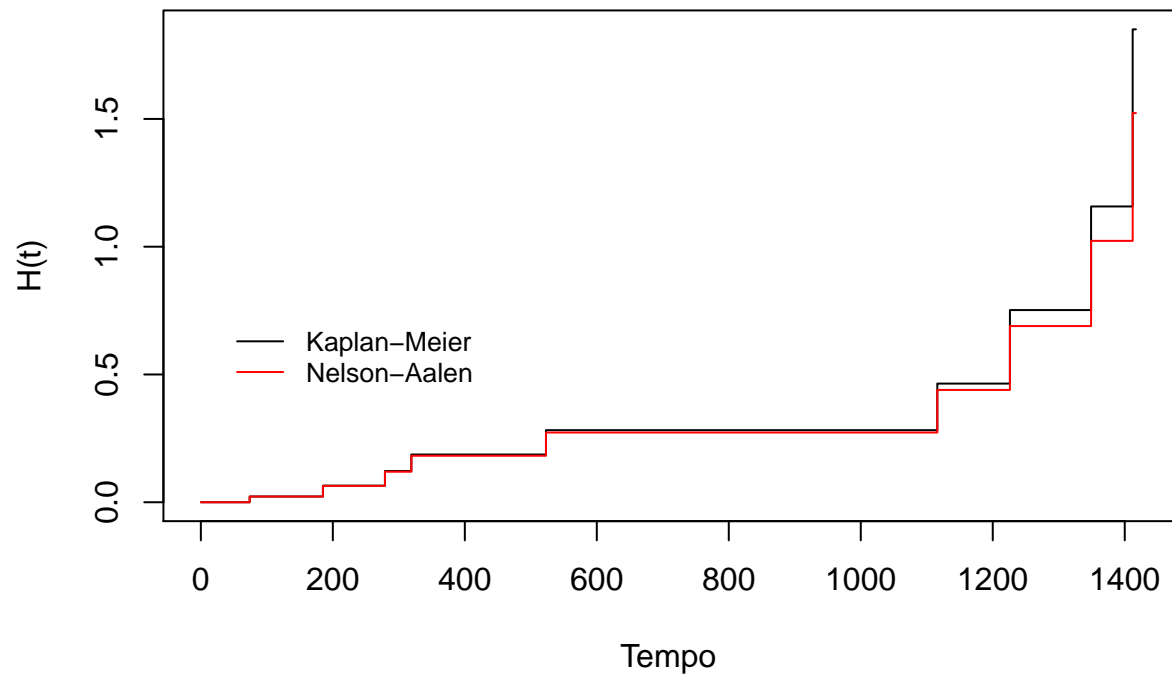
## Estimativa para $H(t)$ Método de Nelson-Aalen



```
plot(KM.ex2, fun = "cumhaz", xlab = "Tempo", ylab = "H(t)", main = "Estimativa para H(t)")  
lines(NA.ex2, col = 2, fun = "cumhaz", conf.int = F)  
legend(20, 0.75, lty = c(1, 1), c("Kaplan-Meier", "Nelson-Aalen"), bty = "n", cex = 0.8, col = c(1, 2))
```



### Estimativa para $H(t)$



Item (c)