Analytical solution