

n -Sample Test Classifier on Binary Outcomes of Stratified Randomized Experiments

MA 590 Special Topics: Causal Inference

Aukkawut Ammartayakun

Worcester Polytechnic Institute

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Two-Sample Case

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Let say we have two group of data D : D_t and D_c . We want to test whether there is a difference between the two groups.

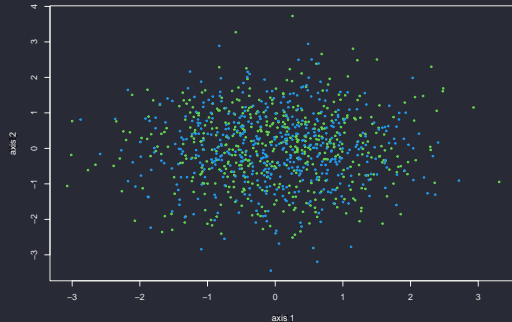
Classifier Two-Sample Test (Lopez-Paz and Oquab 2017)

- Combined two dataset into one dataset D .
- Split the dataset into training and testing set.
- Fit the classifier (like logistic regression) to the training set and predict the testing set.
- Calculate the empirical loss l_e of the classifier. If $|l_e - 0.5| < \epsilon$, then $\bar{\tau} = 0$.

Testing the Algorithm

```
set.seed(590)
# generate random multivariate gaussian data
n <- 1000
d <- 2
X <- matrix(rnorm(n*d), n, d)
y <- c(rep(0, n/2), rep(1, n/2))
c2st(X, y, echo = TRUE)
```

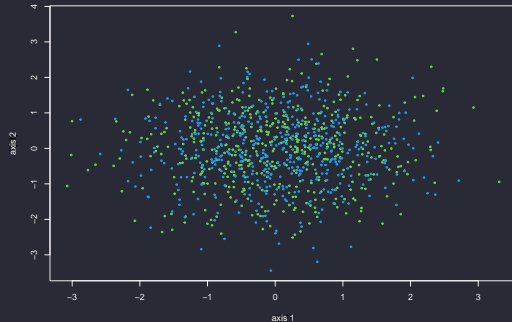
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[1] Empirical loss: 0.57
[1] p-value: 0.282762829938323
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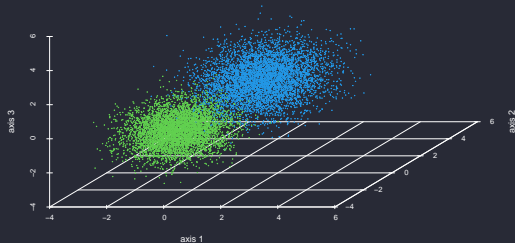
It is the *impossible* classification problem. Thus, the result should be close to near-chance level.

Testing the Algorithm

```
set.seed(590)
# generate two dataset: two gaussians
n <- 5000
d <- 3
X0 <- matrix(rnorm(n*d, -1,0.8), n, d)
X1 <- matrix(rnorm(n*d, 1,1), n, d)
y <- c(rep(0, n), rep(1, n))
c2st(rbind(X0, X1), y, echo = TRUE)
```

```
[1] Empirical loss: 0.0285
```

```
[1] p-value: 0
```

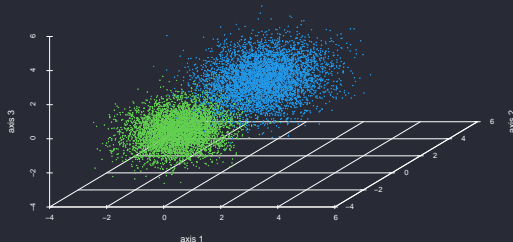


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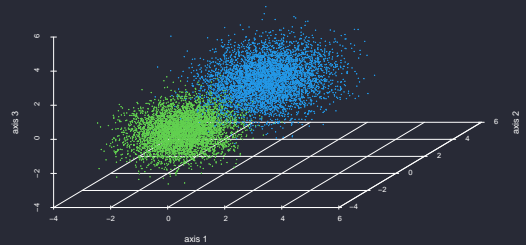
[1] p-value: 0



Test statistic diverges from near-chance level as there is an exist of “linear” decision boundary. The dimensionality problem in homogeneity test is solved.

Question: Does changing from GLM to other models increases (widen the range of) the testing power, β ?

Testing the Algorithm



Comparison to Maximum Mean Discrepancy

Use C2ST on Causal Inference

- But, how can we use C2ST on causal inference?

Example:

Generalization of n -Sample Case

Possible Solution

- Combine both treatment and control group within each stratum into one dataset D_i^s .
- For each group, fit the classifier (like logistic regression) to the training set and predict the testing set.
- Calculate the empirical loss l_e of the classifier. If $|l_e - 0.5| < \epsilon$, then $\bar{\tau}_{\text{within}} = 0$
- Find the way to infer $\bar{\tau}_{\text{between}}$

References

References

Lopez-Paz, David, and Maxime Oquab. 2017. “Revisiting Classifier Two-Sample Tests.”
In *International Conference on Learning Representations*.
<https://openreview.net/forum?id=SJkXfE5xx>.