Einführung in die Neuroinformatik

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1 Backpropagation [Pen and Paper]

1.1

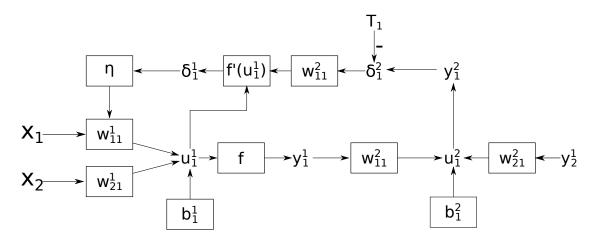


Abbildung 1: Ablauf graphisch dargestellt

1.2

1. Forwärts propagieren:

$$u_{1}^{(1)} = x_{1} \cdot w_{11}^{(1)} + x_{2} \cdot w_{21}^{(1)} + b_{1}^{(1)}$$

$$y_{1}^{(1)} = f_{1}(u_{1}^{(1)})$$

$$u_{1}^{(2)} = y_{1}^{(1)} \cdot w_{11}^{(2)} + y_{2}^{(1)} \cdot w_{21}^{(2)} + b_{1}^{(2)}$$

$$y_{1}^{(2)} = f_{2}(u_{1}^{(2)})$$

2. Fehler in der Ausgabeschicht bestimmen:

$$\delta_1^{(2)} = y_1^{(2)} - T_1$$

3. Backpropagation

$$\delta_1^{(1)} = \delta_1^{(2)} w_{11}^{(2)} f'\left(u_i^{(1)}\right)$$

4. Gewichte adaptieren

$$w_{11}^{(1)} = w_{11}^{(1)} + \eta x_1 \delta_1^{(1)}$$

2 Backpropagation [Matlab]

2.1

```
1 function [weights] = initWeights(inputDimensions, hiddenNeurons,
       output Dimensions)
  %initWeights initializes the weights of the network
3 %
      Arguments:
          - inputDimensions: number of input neurons
4 %
          - hiddenNeurons: number of hidden neurons
6 %
          - output Dimensyions: number of output neurons
  %
 %
      Returns:
  %
          - weights: struct with the parameters w1, w2, theta1 and
       theta2
  %
10
      rng(1337, 'combRecursive');
11
       weights.w1 = rand (hiddenNeurons, inputDimensions) - 0.5;
12
       weights .w2 = rand(outputDimensions, hiddenNeurons) - 0.5;
       weights.theta1 = rand(hiddenNeurons, 1) - 0.5;
14
       weights.theta2 = rand(outputDimensions, 1) - 0.5;
15
16 end
  2.2
function [y2, u2, y1, u1] = forward(inputX, weights, trans)
2 %forward calculates the network output
      Arguments:
3 %
4 %

    inputX: input data organized as samples x dimensions (

     each row denotes a point)
```

```
5 %
          - weights: struct with the parameters w1, w2, theta1 and
      theta2
6 %
          - trans: activation function f(x) of the hidden layer
7 %
      u1 = weights.w1 * inputX + weights.theta1;
      v1 = trans(u1):
      u2 = weights.w2 * y1 + weights.theta2;
      y2 = u2;
_{12} end
  2.3
function [delta1, delta2] = propagateError(T, y2, w2, u1Diff)
  %propagateError calculates the error of the network (delta1 and
     delta2)
3 %
      Arguments:
4 %
          - T: teacher signal
          - y2: output of the last neuron
          - w2: weights matrix of the second layer
6 %
  %
          - u1Diff: f'(u1)
8 %
      delta2 = T-y2;
      delta1 = delta2 * (transpose(w2) .* u1Diff);
11 end
  function y = transDiff(x)
      y = ones(size(x))./(cosh(x).^2);
3 end
  2.4
  function [weights, errors] = train(hiddenNeurons, learnRate,
     inputX, outputT, epochs, trans, transDiff)
2 %train trains the neural network
з %
      Arguments:
4 %
          - hiddenNeurons: number of hidden neurons
          - learnRate: learning rate \eta
5 %
          - inputX: input data organized as samples x dimensions (
     each row denotes a point)
  %
          - outputT: teacher signal as column vector
8 %
          - epochs: number of epochs to train the network
  %
          - trans: transfer function to use in the hidden layer (
     activation function)
10 %
          - transDiff: derivative of the transfer function
```

```
%
11
       assert (iscolumn (outputT), 'T must be a column vector');
12
       assert (size (inputX, 1) == size (outputT, 1), 'Each data point
13
           must have an associated label');
       rng(1337, 'combRecursive'); % For reproducibility (does also
14
           work with parfor: http://de.mathworks.com/help/distcomp
          /control-random-number-streams.html#btms9o
       weights = initWeights(size(inputX,2), hiddenNeurons, size(
15
          outputT, 2));
       errors = zeros(epochs, 1);
16
17
       for e=1:epochs
18
           indexSet = randperm(size(inputX,1));
19
           for c=indexSet
               currentInput = transpose(inputX(c,:));
21
                trainerOutput = transpose(outputT(c,:));
22
                [mlpOutput, u2, hiddenOutput, u1] = forward(
23
                   currentInput , weights , trans );
                [delta1, delta2] = propagateError(trainerOutput,
24
                   mlpOutput, weights.w2, transDiff(u1));
25
                weights.w1 = weights.w1 + learnRate * (delta1 *
26
                   transpose (currentInput));
                weights.w2 = weights.w2 + learnRate * delta2 *
27
                   transpose (hiddenOutput);
                weights.theta1 = weights.theta1 + learnRate * delta1
                weights.theta2 = weights.theta2 + learnRate * delta2
29
           end;
30
           [mlpOutput, u2, hiddenOutput, u1] = forward (transpose (
32
              inputX), weights, trans);
           diff = norm(mlpOutput-transpose(outputT))^2;
33
           errors(c) = diff;
34
       end;
35
  _{
m end}
  2.5
1 % Initialization
2 % Generate data
s = 31;
[x, y, z] = peaks(s);
```

```
data = [x(:) y(:) z(:)];
_{6} X = data(:, 1:2);
  T = data(:, 3);
  eta = 0.01;
  [weights, E] = train (100, eta, X, T, 1000, @tanh, @transDiff);
10
11
  figure();
  subplot(2,2,1);
  surf(x,y,z);
   xlabel("x 1");
15
   ylabel("x_2");
16
   zlabel("peaks(x 1, x 2)");
   title ("Peaks-Funktion");
19
  subplot(2,2,2);
20
  output = forward (transpose (X), weights, @tanh);
21
  output = reshape(output, size(z));
   surf(x,y,output);
  xlabel("x 1");
  ylabel("x 2");
^{25}
   zlabel("f(x_1, x_2)");
   title ("Netz-Ausgabe");
27
28
29
  subplot(2,2,3);
   surf(x,y,abs(output-z));
31
  xlabel("x 1");
   ylabel("x_2");
   zlabel("|peaks(x_1, x_2) - f(x_1, x_2)|");
   title ("Differenz der beiden Funktionen");
36
^{37}
  subplot(2,2,4);
  plot (E);
39
  xlabel("i");
40
  ylabel("E(i)");
  title ("Fehlerverlauf");
43
  print("Plot.eps", "-depsc");
```

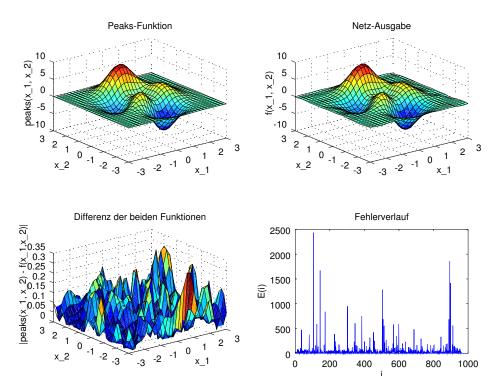


Abbildung 2: Ausgabe des Matlab-Skripts