

Chapter 2 The Regression Line

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Exercise Set A

Problem 1

In the Pearson-Lee data, the average height of the fathers was 67.78 inches; the SD was 2.74 inches. The average height of the sons was 68.7 inches; the SD was 2.81 inches. The correlation was .501.

Part a

True or false and explain: because the sons average an inch taller than the fathers, if the father is 72 inches tall, it's 50-50 whether the son is taller than 73 inches.

False. The statement as given states that given the point (\bar{x}, \bar{y}) , moving to $\bar{x} + c$ causes the conditional mean of y to increase to $\bar{y} + c$. This is incorrect. The correct statement is that by moving to $\bar{x} + SD_x$, the conditional mean of y increases to $\bar{y} + rSD_y$.

Part b

Find the regression line of son's height on father's height, and its RMS error.

The line is

$$y - 68.7 = .501 \frac{2.81}{2.74} (x - 67.7)$$

From the formulas, the MSE is

$$MSE = (1 - .501^2)(2.81)^2 = 1.966$$

and RMS is $\sqrt{1.966} = 1.402$.