Lab 03: Logistic Regression

Thus far, the problems we've encountered have been *regression* problems, in which the target $y \in \mathbb{R}$.

Today we'll start experimenting with *classification* problems, beginning with *binary* classification problems, in which the target $y \in \{0, 1\}$.

Background

The simplest approach to classification, applicable when the input feature vector $\mathbf{x} \in \mathbb{R}^n$, is a simple generalization of what we do in linear regression. Recall that in linear regression, we assume that the target is drawn from a Gaussian distribution whose mean is a linear function of $\mathbf{x}$:

$$y \sim \mathcal{N}(\theta^\top \mathbf{x}, \sigma^2)$$

In logistic regression, similarly, we'll assume that the target is drawn from a Bernoulli distribution with parameter p being the probability of class 1:

$$y \sim \mathrm{Bernoulli}(p)$$

That's fine, but how do we model the parameter p? How is it related to $\mathbf{x}$?

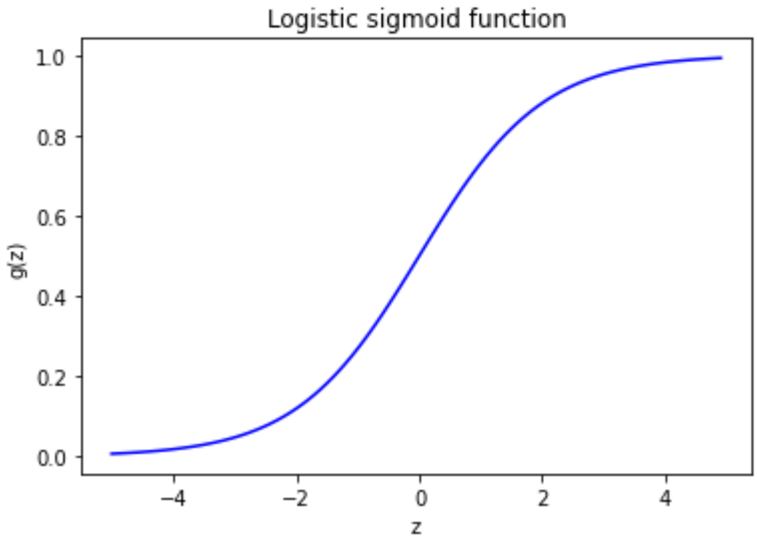
In linear regression, we assume that the mean of the Gaussian is $\theta^\top \mathbf{x}$, i.e., a linear function of $\mathbf{x}$.

In logistic regression, we'll assume that p is a "squashed" linear function of $\mathbf{x}$, i.e.,

$$p = \mathrm{sigmoid}(\theta^\top \mathbf{x}) = g(\theta^\top \mathbf{x}) = \frac{1}{1 + e^{-\theta^\top \mathbf{x}}}.$$

Later, when we introduce generalized linear models, we'll see why p should take this form. For now, though, we can simply note that the selection makes sense. Since p is a discrete probability, p is bounded by $0 \leq p \leq 1$. The sigmoid function $g(\cdot)$ conveniently obeys these bounds:

In [67]:
```
import numpy as np
import matplotlib.pyplot as plt

def f(z):
    return 1 / (1 + np.exp( -z ))

z = np.arange(-5, 5, 0.1)
plt.plot(z, f(z), 'b-')
plt.xlabel('z')
plt.ylabel('g(z)')
plt.title('Logistic sigmoid function')
plt.show()
```



We see that the sigmoid approaches 0 as its input approaches $-\infty$ and approaches 1 as its input approaches $+\infty$. If its input is 0, its value is 0.5.

Again, this choice of function may seem strange at this point, but bear with it! We'll derive this function from a more general principle, the generalized linear model, later.

OK then, we now understand that for logistic regression, the assumptions are:

1. The *data* are pairs $(\mathbf{x}, y) \in \mathbb{R}^n \times \{0, 1\}$.
2. The *hypothesis function* is $h_\theta(\mathbf{x}) = \frac{1}{1+e^{-\theta^\top \mathbf{x}}}$.

What else do we need... ? A cost function and an algorithm for minimizing that cost function!

Cost function for logistic regression

You can refer to the lecture notes to see the derivation, but for this lab, let's just skip to the chase. With the hypothesis $h_\theta(\mathbf{x})$ chosen as above, the log likelihood function $\ell(\theta)$ can be derived as

$$\ell(\theta) = \log \mathcal{L}(\theta) = \sum_{i=1}^{m} y^{(i)} \log(h_\theta(\mathbf{x}^{(i)})) + (1 - y^{(i)}) \log(1 - (h_\theta(\mathbf{x}^{(i)})).$$

Negating the log likelihood function to obtain a loss function, we have

$$J(\theta) = -\sum_{i=1}^{m} y^{(i)} \log h_\theta(\mathbf{x}^{(i)}) + (1 - y^{(i)}) \log(1 - h_\theta(\mathbf{x}^{(i)})).$$

There is no closed-form solution to this problem like there is in linear regression, so we have to use gradient descent to find θ minimizing $J(\theta)$. Luckily, the function *is* convex in θ so there is just a single global minimum, and gradient descent is guaranteed to get us there eventually if we take the right step size.

The *stochastic* gradient of J, for a single observed pair $(\mathbf{x}, y)$, turns out to be (see lecture notes)

$$\nabla_J(\theta) = (h_\theta(\mathbf{x}) - y)\mathbf{x}.$$

Give some thought as to whether following this gradient to increase the loss J would make a worse classifier, and vice versa!

Finally, we obtain the update rule for the jth iteration selecting training pattern i:

$$\theta^{(j+1)} \leftarrow \theta^{(j)} + \alpha(y^{(i)} - h_\theta(\mathbf{x}^{(i)}))\mathbf{x}^{(i)}.$$

Note that we can perform *batch gradient descent* simply by summing the single-pair gradient over the entire training set before taking a step, or *mini-batch gradient descent* by summing over a small subset of the data.

Example dataset 1: student admissions data

This example is from Andrew Ng's machine learning course on Coursera.

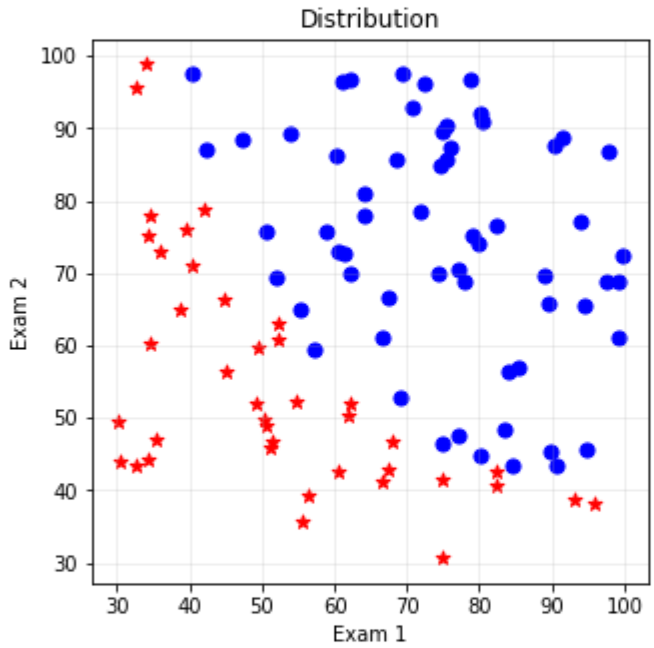
The data contain students' scores for two standardized tests and an admission decision (0 or 1).

In [68]:
```
# Load student admissions data. The data file does not contain he
aders,
# so we use hard coded indices for exam 1, exam2, and the admissi
on decision.

data = np.loadtxt('ex2data1.txt',delimiter = ',')
exam1_data = data[:,0]
exam2_data = data[:,1]
X = np.array([exam1_data, exam2_data]).T
y = data[:,2]

# Output some sample data

print('Exam scores', X[0:5,:])
print('-----------------------------')
print('Admission decision', y[0:5])
```

```
Exam scores [[34.62365962 78.02469282]
 [30.28671077 43.89499752]
 [35.84740877 72.90219803]
 [60.18259939 86.3085521 ]
 [79.03273605 75.34437644]]
-----------------------------
Admission decision [0. 0. 0. 1. 1.]
```

Let's plot the data...

In [69]:
```
# Plot the data

idx_0 = np.where(y == 0)
idx_1 = np.where(y == 1)

fig1 = plt.figure(figsize=(5, 5))
ax = plt.axes()
ax.set_aspect(aspect = 'equal', adjustable = 'box')
plt.title('Distribution')
plt.xlabel('Exam 1')
plt.ylabel('Exam 2')
plt.grid(axis='both', alpha=.25)
ax.scatter(exam1_data[idx_0], exam2_data[idx_0], s=50, c='r', mar
ker='*', label='Not Admitted')
ax.scatter(exam1_data[idx_1], exam2_data[idx_1], s=50, c='b', mar
ker='o', label='Admitted')
plt.show()
```



Let's see if we can find good values for θ without normalizing the data. We will definitely want to split the data into train and test, however...

In [70]:
```
import random
random.seed(12)

# Partion data into training and test datasets

m, n = X.shape
XX = np.insert(X, 0, 1, axis=1)
y = y.reshape(m, 1)
idx = np.arange(0, m)
random.shuffle(idx)
percent_train = .6
m_train = int(m * percent_train)
train_idx = idx[0:m_train]
test_idx = idx[m_train:]
X_train = XX[train_idx,:];
X_test = XX[test_idx,:];

y_train = y[train_idx];
y_test = y[test_idx];
```

All important functions are here

In [71]:
```
def sigmoid(z):
    return 1 / (1 + np.exp(-z))

def h(X, theta):
    return sigmoid(X @ theta)

def grad_j(X, y, y_pred):
    return X.T @ (y - y_pred) / X.shape[0]

def j(theta, X, y):
    y_pred = h(X, theta)
    error = (-y * np.log(y_pred)) - ((1 - y) * np.log(1 - y_pre
d))
    cost = sum(error) / X.shape[0]
    grad = grad_j(X, y, y_pred)
    return cost[0], grad
```

Initialize theta

In [72]:
```
# Get a feel for how h works
theta_initial = np.zeros((n+1, 1))

print('Initial theta:', theta_initial)
print('Initial predictions:', h(XX, theta_initial)[0:5,:])
print('Targets:', y[0:5,:])
```

```
Initial theta: [[0.]
 [0.]
 [0.]]
Initial predictions: [[0.5]
 [0.5]
 [0.5]
 [0.5]
 [0.5]]
Targets: [[0.]
 [0.]
 [0.]
 [1.]
 [1.]]
```

Batch training function for num_iters iterations

In [73]:
```
def train(X, y, theta_initial, alpha, num_iters):
    theta = theta_initial
    j_history = []
    for i in range(num_iters):
        cost, grad = j(theta, X, y)
        theta = theta + alpha * grad
        j_history.append(cost)
    return theta, j_history
```

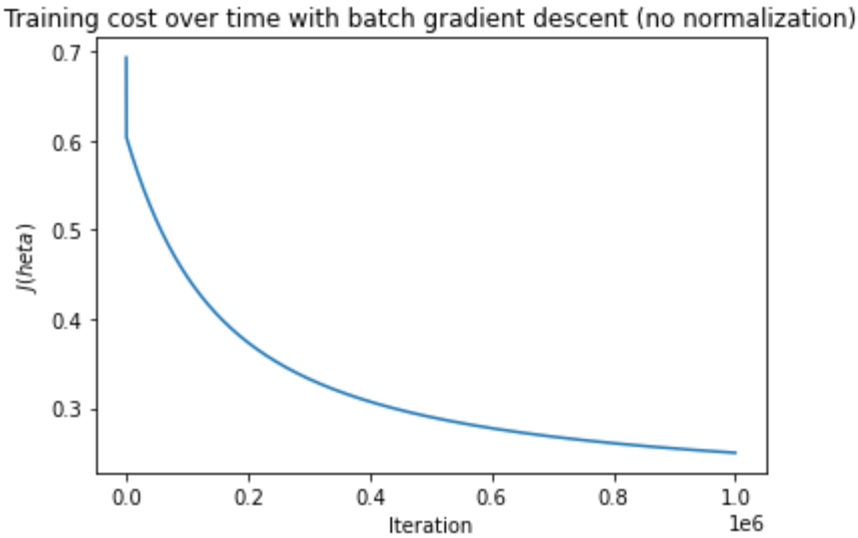
Train data

In [74]:
```
# Train for 3000 iterations on full training set

alpha = .0005
num_iters = 1000000
theta, j_history = train(X_train, y_train, theta_initial, alpha, 
num_iters)

print("Theta optimized:", theta)
print("Cost with optimized theta:", j_history[-1])
```

```
Theta optimized: [[-11.29380461]
 [  0.10678604]
 [  0.07994591]]
Cost with optimized theta: 0.24972975869900044
```

Plot graph

In [75]:
```
plt.plot(j_history)
plt.xlabel("Iteration")
plt.ylabel("$J(\theta)$")
plt.title("Training cost over time with batch gradient descent (n
o normalization)")
plt.show()
```



In-lab exercise from example 1 (Total 35 points)

That took a long time, right?

See if you can do better.

1. Try increasing the learning rate α and starting with a better initial θ. How much does it help?
   - Try at least 2 learning rate α with 2 difference θ (4 experiments)
   - Do not forget to plot the graph to compare youre results
2. Better yet, try *normalizing the data* and see if the training converges better. How did it go?
   - Do not forget to plot the graph to compare youre results between unnormalized and normalized data.
3. Discuss the effects of normalization, learning rate, and initial θ in your report.

Exercise 1.1 (5 points)

Fill α and θ

In [76]:
```
# grade task: change 'None' value to number(s) or function
### BEGIN SOLUTION
# declare your alphas
alpha1 = 0.001
alpha2 = 0.00001

# initialize thetas as you want
theta_initial1 = np.zeros((n+1, 1))
for i in range(n+1):
    theta_initial1[i] = random.random() / 10 - 0.05
theta_initial2 = np.zeros((n+1, 1))

num_iters = 10000
### END SOLUTION
# declare your alphas
alpha1 = None
alpha2 = None

# initialize thetas as you want
theta_initial1 = None
theta_initial2 = None

# define your num iterations
num_iters = None
```

In [77]:
```
alpha_list = [alpha1, alpha2]
print('alpha 1:', alpha1)
print('alpha 2:', alpha2)

theta_initial_list = [theta_initial1, theta_initial2]
print('theta 1:', theta_initial_list[0])
print('theta 2:', theta_initial_list[1])

print('Use num iterations:', num_iters)

# Test function: Do not remove
assert alpha_list[0] is not None and alpha_list[1] is not None, "
Alpha has not been filled"
chk1 = isinstance(alpha_list[0], (int, float))
chk2 = isinstance(alpha_list[1], (int, float))
assert chk1 and chk2, "Alpha must be number"
assert theta_initial_list[0] is not None and theta_initial_list
[1] is not None, "initialized theta has not been filled"
chk1 = isinstance(theta_initial_list[0], (list,np.ndarray))
chk2 = isinstance(theta_initial_list[1], (list,np.ndarray))
assert chk1 and chk2, "Theta must be list"
chk1 = ((n+1, 1) == theta_initial_list[0].shape)
chk2 = ((n+1, 1) == theta_initial_list[1].shape)
assert chk1 and chk2, "Theta size are incorrect"
assert num_iters is not None and isinstance(num_iters, int), "num
_iters must be integer"
print("success!")
# End Test function
```

```
alpha 1: 0.001
alpha 2: 1e-05
theta 1: [[-0.03219505]
 [ 0.01958955]
 [-0.04631539]]
theta 2: [[0.]
 [0.]
 [0.]]
Use num iterations: 10000
success!
```

Exercise 1.2 (5 points)

Train data

In [78]:
```
# grade task: change 'None, None' value to number(s) or function
j_history_list = []
theta_list = []
for alpha in alpha_list:
    for theta_initial in theta_initial_list:
        ### BEGIN SOLUTION
        theta_i, j_history_i = train(X_train, y_train, theta_init
ial, alpha, num_iters)
        ### END SOLUTION
        theta_i, j_history_i = None, None
        j_history_list.append(j_history_i)
        theta_list.append(theta_i)
```

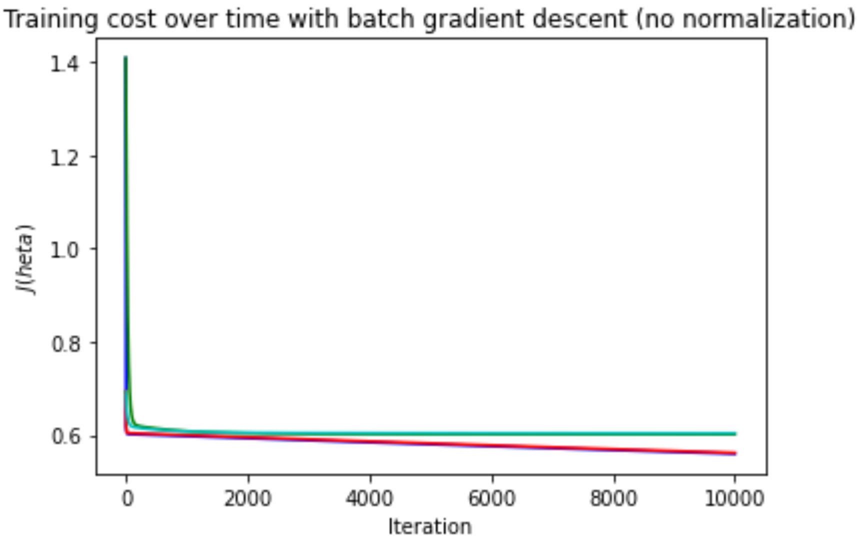
In [79]:
```
# Test function: Do not remove
assert theta_list[0] is not None and j_history_list[0] is not Non
e, "No values in theta_list or j_history_list"
chk1 = isinstance(theta_list[0], (list,np.ndarray))
chk2 = isinstance(j_history_list[0][0], (int, float))
assert chk1 and chk2, "Wrong type in theta_list or j_history_lis
t"
print("success!")
# End Test function
```

```
success!
```

Exercise 1.3 (10 points)

Plot graph

In [80]:
```
### BEGIN SOLUTION
color = ['b', 'r', 'g', 'c']
i = 0
for j_history in j_history_list:
    plt.plot(j_history, color[i])
    i = i+1
plt.xlabel("Iteration")
plt.ylabel("$J(\theta)$")
plt.title("Training cost over time with batch gradient descent (n
o normalization)")
plt.show()
### END SOLUTION
```



Exercise 1.4 (10 points)

- Repeat your training, but **normalized data** before run training
- Compare the results between **normalized data** and **unnormalized data**

In [ ]:
```
# code here
```

Exercise 1.5 (5 points)

Discuss the effects of normalization, learning rate, and initial θ in your report.

Report here

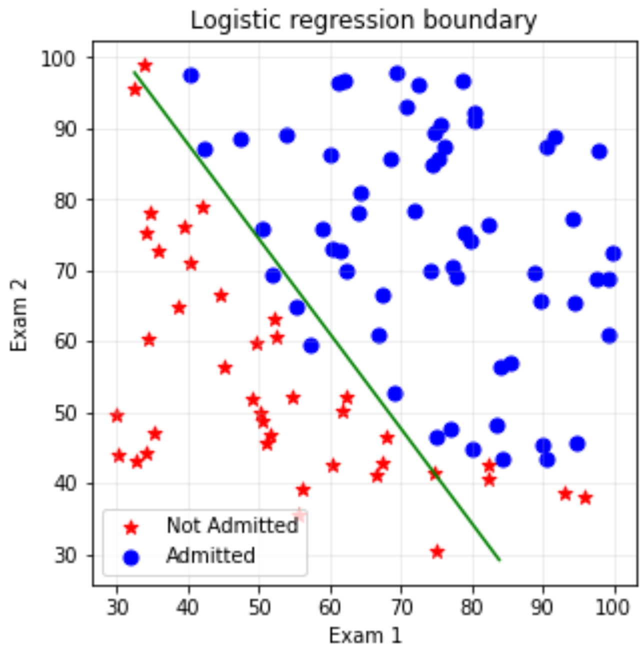
Decision boundary

Note that when $\theta^\top \mathbf{x} = 0$, we have $h_\theta(\mathbf{x}) = 0.5$. That is, we are equally unsure as to whether $\mathbf{x}$ belongs to class 0 or class 1. The contour at which $h_\theta(\mathbf{x}) = 0.5$ is called the classifier's *decision boundary*.

We know that in the plane, the equation
$$ax + by + c = 0$$
is the general form of a 2D line. In our case, we have
$$\theta_0 + \theta_1 x_1 + \theta_2 x_2 = 0$$
as our decision boundary, but clearly, this is just a 2D line in the plane. So when we plot x_1 against x_2, it is easy to plot the boundary line.

In [81]:
```
def boundary_points(X, theta):
    v_orthogonal = np.array([[theta[1,0]],[theta[2,0]]])
    v_ortho_length = np.sqrt(v_orthogonal.T @ v_orthogonal)
    dist_ortho = theta[0,0] / v_ortho_length
    v_orthogonal = v_orthogonal / v_ortho_length
    v_parallel = np.array([[-v_orthogonal[1,0]],[v_orthogonal[0,
0]]])
    projections = X @ v_parallel
    proj_1 = min(projections)
    proj_2 = max(projections)
    point_1 = proj_1 * v_parallel - dist_ortho * v_orthogonal
    point_2 = proj_2 * v_parallel - dist_ortho * v_orthogonal
    return point_1, point_2
```

In [82]:
```
fig1 = plt.figure(figsize=(5,5))
ax = plt.axes()
ax.set_aspect(aspect = 'equal', adjustable = 'box')
plt.title('Logistic regression boundary')
plt.xlabel('Exam 1')
plt.ylabel('Exam 2')
plt.grid(axis='both', alpha=.25)
ax.scatter(X[:,0][idx_0], X[:,1][idx_0], s=50, c='r', marker='*',
label='Not Admitted')
ax.scatter(X[:,0][idx_1], X[:,1][idx_1], s=50, c='b', marker='o',
label='Admitted')
point_1, point_2 = boundary_points(X, theta)
plt.plot([point_1[0,0], point_2[0,0]],[point_1[1,0], point_2[1,
0]], 'g-')
plt.legend(loc=0)
plt.show()
```



You'll have to adjust the above code to make it work with normalized data.

Test set performance

Now let's apply the learned classifier to the test data we reserved in the beginning:

In [83]:
```
def r_squared(y, y_pred):
    return 1 - np.square(y - y_pred).sum() / np.square(y - y.mean
()).sum()
```

In [84]:
```
y_test_pred_soft = h(X_test, theta)
y_test_pred_hard = (y_test_pred_soft > 0.5).astype(int)

test_rsq_soft = r_squared(y_test, y_test_pred_soft)
test_rsq_hard = r_squared(y_test, y_test_pred_hard)
test_acc = (y_test_pred_hard == y_test).astype(int).sum() / y_tes
t.shape[0]

print('Got test set soft R^2 %0.4f, hard R^2 %0.4f, accuracy %0.2
f' % (test_rsq_soft, test_rsq_hard, test_acc))
```

```
Got test set soft R^2 0.6636, hard R^2 0.6931, accuracy 0.93
```

For classification, accuracy is probably the more useful measure of goodness of fit.

Example 2: Loan prediction dataset

Let's take another example dataset and see what we can do with it.

This dataset is from [Kaggle (https://www.kaggle.com/altruistdelhite04/loan-prediction-problem-dataset)](https://www.kaggle.com/altruistdelhite04/loan-prediction-problem-dataset).

The data concern loan applications. It has 12 independent variables, including 5 categorical variables. The dependent variable is the decision "Yes" or "No" for extending a loan to an individual who applied.

One thing we will have to do is to clean the data, by filling in missing values and converting categorical data to reals. We will use the Python libraries pandas and sklearn to help with the data cleaning and preparation.

Read the data and take a look

In [85]:
```
# Import Pandas. You may need to run "pip3 install pandas" at the
console if it's not already installed

import pandas as pd

# Import the data

data_train = pd.read_csv('train_LoanPrediction.csv')
data_test = pd.read_csv('test_LoanPrediction.csv')

# Start to explore the data

print('Training data shape', data_train.shape)
print('Test data shape', data_test.shape)

print('Training data:\n', data_train)
```

```
Training data shape (614, 13)
Test data shape (367, 12)
Training data:
       Loan_ID  Gender Married Dependents     Education Self_Empl
oyed  \
0    LP001002    Male      No          0      Graduate
No
1    LP001003    Male     Yes          1      Graduate
No
2    LP001005    Male     Yes          0      Graduate
Yes
3    LP001006    Male     Yes          0  Not Graduate
No
4    LP001008    Male      No          0      Graduate
No
..        ...     ...     ...        ...           ...
...
609  LP002978  Female      No          0      Graduate
No
610  LP002979    Male     Yes         3+      Graduate
No
611  LP002983    Male     Yes          1      Graduate
No
612  LP002984    Male     Yes          2      Graduate
No
613  LP002990  Female      No          0      Graduate
Yes

     ApplicantIncome  CoapplicantIncome  LoanAmount  Loan_Amount_
Term  \
0               5849                0.0         NaN             3
60.0
1               4583             1508.0       128.0             3
60.0
2               3000                0.0        66.0             3
60.0
3               2583             2358.0       120.0             3
60.0
4               6000                0.0       141.0             3
60.0
..               ...                ...         ...
...
609             2900                0.0        71.0             3
60.0
610             4106                0.0        40.0             1
80.0
611             8072              240.0       253.0             3
60.0
612             7583                0.0       187.0             3
60.0
613             4583                0.0       133.0             3
60.0

     Credit_History Property_Area Loan_Status
0               1.0         Urban           Y
1               1.0         Rural           N
2               1.0         Urban           Y
3               1.0         Urban           Y
```

```
4              1.0        Urban          Y
..             ...          ...        ...
609            1.0        Rural          Y
610            1.0        Rural          Y
611            1.0        Urban          Y
612            1.0        Urban          Y
613            0.0    Semiurban          N

[614 rows x 13 columns]
```

In [86]:

```python
# Check for missing values in the training and test data

print('Missing values for train data:\n------------------------\n
', data_train.isnull().sum())
print('Missing values for test data \n ------------------------\n
', data_test.isnull().sum())
```

```
Missing values for train data:
------------------------
 Loan_ID              0
Gender              13
Married              3
Dependents          15
Education            0
Self_Employed       32
ApplicantIncome      0
CoapplicantIncome    0
LoanAmount          22
Loan_Amount_Term    14
Credit_History      50
Property_Area        0
Loan_Status          0
dtype: int64
Missing values for test data
 ------------------------
 Loan_ID              0
Gender              11
Married              0
Dependents          10
Education            0
Self_Employed       23
ApplicantIncome      0
CoapplicantIncome    0
LoanAmount           5
Loan_Amount_Term     6
Credit_History      29
Property_Area        0
dtype: int64
```

Handle missing values

We can see from the above table that the `Married` column has 3 missing values in the training dataset and 0 missing values in the test dataset. Let's take a look at the distribution over the datasets then fill in the missing values in approximately the same ratio.

You may be interested to look at the [documentation of the Pandas `fillna()` function (https://pandas.pydata.org/pandas-docs/stable/reference/api/pandas.DataFrame.fillna.html)](https://pandas.pydata.org/pandas-docs/stable/reference/api/pandas.DataFrame.fillna.html). It's great!

In [87]:
```
# Compute ratio of each category value
# Divide the missing values based on ratio
# Fillin the missing values
# Print the values before and after filling the missing values fo
r confirmation

print(data_train['Married'].value_counts())

married = data_train['Married'].value_counts()
print('Elements in Married variable', married.shape)
print('Married ratio ', married[0]/sum(married.values))

def fill_martial_status(data, yes_num_train, no_num_train):
    data['Married'].fillna('Yes', inplace = True, limit = yes_num
_train)
    data['Married'].fillna('No', inplace = True, limit = no_num_t
rain)

fill_martial_status(data_train, 2, 1)
print(data_train['Married'].value_counts())
print('Missing values for train data:\n------------------------\n
', data_train.isnull().sum())
```

```
Yes    398
No     213
Name: Married, dtype: int64
Elements in Married variable (2,)
Married ratio  0.6513911620294599
Yes    400
No     214
Name: Married, dtype: int64
Missing values for train data:
------------------------
 Loan_ID              0
Gender              13
Married              0
Dependents          15
Education            0
Self_Employed       32
ApplicantIncome      0
CoapplicantIncome    0
LoanAmount          22
Loan_Amount_Term    14
Credit_History      50
Property_Area        0
Loan_Status          0
dtype: int64
```

Now the number of examples missing the `Married` attribute is 0.

Excercise: Complete the data processing based on examples given and logistic regression model on training dataset. Estimate the Accuracy (goodness of fit) on test dataset.

In [88]:
```
# Another example of filling in missing values for the "number of
dependents" attribute.
# Here we see that categorical values are all numeric except one
value "3+"
# Create a new category value "4" for "3+" and ensure that all th
e data is numeric

print(data_train['Dependents'].value_counts())
dependent = data_train['Dependents'].value_counts()

print('Dependent ratio 1 ', dependent['0'] / sum(dependent.value
s))
print('Dependent ratio 2 ', dependent['1'] / sum(dependent.value
s))
print('Dependent ratio 3 ', dependent['2'] / sum(dependent.value
s))
print('Dependent ratio 3+ ', dependent['3+'] / sum(dependent.valu
es))

def fill_dependent_status(num_0_train, num_1_train, num_2_train,
num_3_train, num_0_test, num_1_test, num_2_test, num_3_test):
    data_train['Dependents'].fillna('0', inplace=True, limit = nu
m_0_train)
    data_train['Dependents'].fillna('1', inplace=True, limit = nu
m_1_train)
    data_train['Dependents'].fillna('2', inplace=True, limit = nu
m_2_train)
    data_train['Dependents'].fillna('3+', inplace=True, limit = n
um_3_train)
    data_test['Dependents'].fillna('0', inplace=True, limit = num
_0_test)
    data_test['Dependents'].fillna('1', inplace=True, limit = num
_1_test)
    data_test['Dependents'].fillna('2', inplace=True, limit = num
_2_test)
    data_test['Dependents'].fillna('3+', inplace=True, limit = nu
m_3_test)

fill_dependent_status(9, 2, 2, 2, 5, 2, 2, 1)

print(data_train['Dependents'].value_counts())

# Convert category value "3+" to "4"

data_train['Dependents'].replace('3+', 4, inplace = True)
data_test['Dependents'].replace('3+', 4, inplace = True)
```

```
0     345
1     102
2     101
3+     51
Name: Dependents, dtype: int64
Dependent ratio 1  0.5759599332220368
Dependent ratio 2  0.17028380634390652
Dependent ratio 3  0.1686143572621035
Dependent ratio 3+  0.08514190317195326
0     354
1     104
2     103
3+     53
Name: Dependents, dtype: int64
```

Once missing values are filled in, you'll want to convert strings to numbers.

Finally, here's an example of replacing missing values for a numeric attribute. Typically, we would use the mean of the attribute over the training set.

In [89]:
```
print(data_train['LoanAmount'].value_counts())

LoanAmt = data_train['LoanAmount'].value_counts()

print('mean loan amount ', np.mean(data_train["LoanAmount"]))

loan_amount_mean = np.mean(data_train["LoanAmount"])

data_train['LoanAmount'].fillna(loan_amount_mean, inplace=True, l
imit = 22)
data_test['LoanAmount'].fillna(loan_amount_mean, inplace=True, li
mit = 5)
```

```
120.0    20
110.0    17
100.0    15
187.0    12
160.0    12
         ..
570.0     1
300.0     1
376.0     1
117.0     1
311.0     1
Name: LoanAmount, Length: 203, dtype: int64
mean loan amount  146.41216216216216
```

Take-home exercise (65 points)

Using the data from Example 2 above, finish the data cleaning and preparation. Build a logistic regression model based on the cleaned dataset and report the accuracy on the test and training sets.

- Setup X and Y data (10 points)
- Train data and return theta and J value. Find the good α and you may normalized data before train. (30 points)
- Use θ and implement in test set. (10 points)
- Summarize what did you do and how to find the best result in this take home exercise. (15 points)

To turn in

Turn in a brief report in the form of a Jupyter notebook explaining what you did for the in-lab exercise and the take-home exercise. Discuss what you learned in terms of normalization and data cleaning and the results you obtained.

In [ ]:

```

```