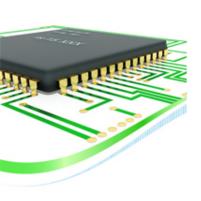


### **Definition**

In a typical language processor implementation, syntactic analysis is the attempt to recognize string of tokens as a sentence in a given language

Parser is the general term for the component that performs the syntactic analysis.



## **Syntactic Validity**

Yes, valid program is a sentence. Usually, validity transcends syntax.

- Declarative Integrity
- Parameter Matching
- Type Conformance
- Operator Applicability
- Statement Applicability
- ...





# Grammars CFG and (E)BNF

Context Free Grammar (Type 2: Grammars)

$$G = (V, \Sigma, R, S)$$

V: Set of non-terminal (Variables)

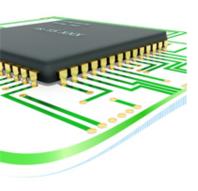
Σ: Set of terminals (Reported by lexical analyzer)

R: Rule set (Production rules, productions)

S: Start variable

Backus-Naur Form (Notation)





### **RFC 822**

### Grammars

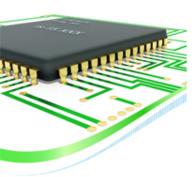
### **BNF for Human Reader**

The syntax of the standard, in RFC #733, was originally specified in the Backus-Naur Form (BNF) meta-language. Ken L. Harrenstien, of SRI International, was responsible for re-coding the BNF into an augmented BNF that makes the representation smaller and easier to understand.

. . . .

```
dtext
           = <any CHAR excluding "[", ; => may be folded
               "]", "\" & CR, & including
               linear-white-space>
           = "(" *(ctext / quoted-pair / comment) ")"
comment
           = <any CHAR excluding "(", ; => may be folded
ctext
               ")", "\" & CR, & including
               linear-white-space>
quoted-pair = "\" CHAR
                                          ; may quote any char
phrase
           = 1*word
                                          ; Sequence of words
          = atom / quoted-string
word
```





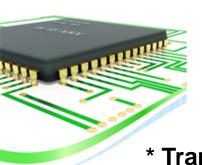
### **Grammars**

(E)BNF for a Language Processor

### From a Parser Generator Project

```
Lexical elements and rules referenced by both RFC822 and MIME.
: Matches(<:LessThan) addr_spec Matches(>:GreaterThan);
msg id
            : local part AtSign domain;
addr spec
            : word *(Dot word);
local part
word
            : Matches(+!{#0-#32,specials} :atom) |
             Matches(" *(!{#0,",\\,#13}|\\{#1-#255}) ":quoted string);
            : sub_domain *(Dot sub_domain);
domain
            : domain_ref | Matches([*(!{#0,[,],\\,#13}|\\{#1-#255})]:domain_literal);
sub domain
domain ref
            : atom;
```





# Grammars BNF Simplified

### \* Transformation

 $u e^* w \rightarrow u e' w$ 

e': e'e | ε (Left recursive form)

e': e e' | ε (Right recursive form)

#### + Transformation

 $u e+ w \rightarrow u e e' w$ 

e': e'e | ε (Left recursive form)

e': e e' | ε (Right recursive form)

### ? Transformation

 $u e? w \rightarrow u e' w$  $e' : e \mid \epsilon$ 

#### **Parentheses**

 $u (e) w \rightarrow u e' w$ e' : e

### **Alternative Notations**

[e], {e}, prefix, postfix, etc...

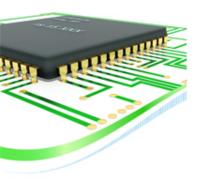




# **Derivation**Definition

Derivation is a sequence of rewriting steps that begins with the grammar's start symbol and ends with a sentence in the language.





## Sentential Form

**Definition** 

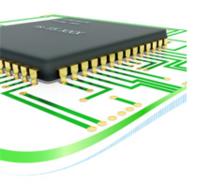
Sentential form is a string of symbols that occurs as a <u>step</u> in a valid derivation.

A step is making use of a rule on the latest sentential form.

- Choose a variable.
- Replace with the associated production.

$$G = (V, \Sigma, R, S)$$
 
$$f_n = uAv \qquad A \in V \qquad A \to w \in R \qquad f_{n+1} = uwv \qquad uAv, \ uwv \in S^*$$
 
$$u, \ v \in (V \ U \ \Sigma)^*$$





### **Derivation**

 $S^* \Rightarrow \alpha$  means  $\alpha$  can be found as a sentence starting from S by zero or more derivation steps.

 $\alpha \Longrightarrow \beta$  means  $\beta$  is reachable from  $\alpha$  by zero or more derivation steps.

 $\alpha \Rightarrow \beta$  means  $\beta$  is reachable from  $\alpha$  by one or more derivation steps.

 $\alpha \Longrightarrow \beta$  and  $\beta \Longrightarrow \gamma$  then  $\alpha \Longrightarrow \gamma$ 

**Example: Input: aaba** 

**G**<sub>1</sub>:

 $S \rightarrow aA \mid abC$ 

 $A \rightarrow aA \mid bA \mid C \mid \epsilon$ 

 $C \rightarrow c$ 

**G**<sub>1</sub>:

 $S \rightarrow aA$ 

 $S \rightarrow abC$ 

 $A \rightarrow aA$ 

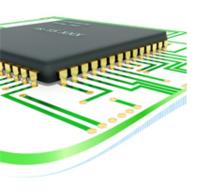
 $A \rightarrow bA$ 

 $A \rightarrow C$ 

 $A \rightarrow \epsilon$ 

 $C \rightarrow c$ 





### **Derivations**

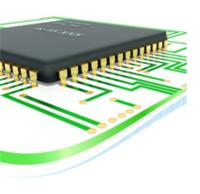
### LMD, RMD, Left and Right Sentential Forms

Leftmost Derivation (LMD) chooses the leftmost variable. Rightmost Derivation (RMD) chooses the rightmost variable. Any step in LMD is leftmost sentential form. Any step in RMD is rightmost sentential form.

### Finding sentence aaba by G1

S use S  $\rightarrow$  aA aA use A  $\rightarrow$  aA aaA use A  $\rightarrow$  bA aabA use A  $\rightarrow$  aA aabaA use A  $\rightarrow$   $\epsilon$ aaba





### **Parse Trees**

Successive steps taken in a derivation can be represented with help of trees, which are known as parse trees.

$$G: E \rightarrow E + E \mid E * E \mid - E \mid (E) \mid id$$

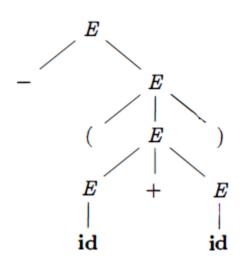
$$E \rightarrow E + E$$

$$E \rightarrow E * E$$

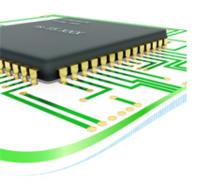
$$E \rightarrow - E$$

$$E \rightarrow (E)$$

$$E \rightarrow id$$







## **Ambiguity**

A grammar that produces more than one parse tree for some sentence is said to be ambiguous.

$$G: E \rightarrow E + E \mid E * E \mid - E \mid (E) \mid id$$

 $E \rightarrow E + E$ 

 $E \rightarrow E * E$ 

 $E \rightarrow - E$ 

 $E \rightarrow (E)$ 

 $E \rightarrow id$ 

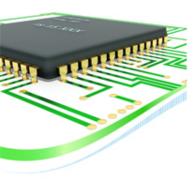
Input: id + id \* id

Create leftmost derivations for this sentence!









### Rewriting

G: 
$$E \rightarrow E + E \mid E * E \mid - E \mid (E) \mid id$$

$$E \rightarrow E + E$$

$$E \rightarrow E * E$$

$$E \rightarrow -E$$

$$E \rightarrow (E)$$

$$E \rightarrow id$$

$$E \rightarrow E + T I T$$

$$T \rightarrow T * F | F$$

$$F \rightarrow -E \mid (E) \mid id$$

$$E \rightarrow E + T$$

$$E \rightarrow T$$

$$T \rightarrow T * F$$

$$T \rightarrow F$$

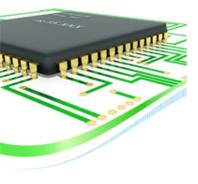
$$F \rightarrow -E$$

$$F \rightarrow (E)$$

$$F \rightarrow id$$

**Inputs:** id + id \* id, id + id + id, id \* id \* id





# Parsing as Tree Building Method

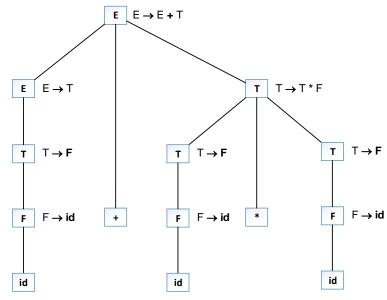
### **Top-Down Parsing**

Begins with the root and grows the tree toward the leaves.

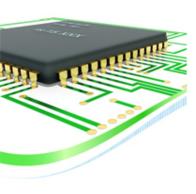
### **Bottom-Up Parsing**

Begins with the leaves and grows the tree toward the root.

Input: id + id \* id







## **Top Down Parsing**

#### The Left Recursion Problem

G:

 $E \rightarrow E + T I T$ 

 $T \rightarrow T * F | F$ 

 $F \rightarrow -EI(E)Iid$ 

 $E \rightarrow E + T$ 

 $E \rightarrow T$ 

 $T \rightarrow T * F$ 

 $T \rightarrow F$ 

 $F \rightarrow -E$ 

 $F \rightarrow (E)$ 

 $F \rightarrow id$ 

Input: id + id \* id

### **Immediate Recursions**

 $A \rightarrow A \alpha \mid \beta$ 

### **Elimination**

 $A \rightarrow \beta A'$  $A' \rightarrow \alpha A' \mid \epsilon$ 





### **Left Recursion**

**Elimination** 

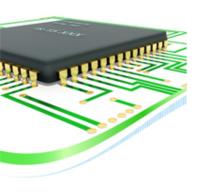
When Grammar has no Cycles and no ε-productions

### **General Elimination Algorithm**

```
arrange the nonterminals in some order A_1, A_2, \ldots, A_n.

for ( each i from 1 to n ) {
	for ( each j from 1 to i-1 ) {
	replace each production of the form A_i \to A_j \gamma by the
	productions A_i \to \delta_1 \gamma \mid \delta_2 \gamma \mid \cdots \mid \delta_k \gamma, where
	A_j \to \delta_1 \mid \delta_2 \mid \cdots \mid \delta_k are all current A_j-productions
}
eliminate the immediate left recursion among the A_i-productions
}
```





### **Left Recursion**

Elimination

### **General Elimination Algorithm**

 $E \rightarrow E + T \mid T$  $T \rightarrow T * F \mid F$ 

 $F \rightarrow -E \mid (E) \mid id$ 

 $E \rightarrow E + T$ 

 $E \rightarrow T$ 

 $T \rightarrow T * F$ 

 $T \rightarrow F$ 

 $F \rightarrow -E$ 

 $F \rightarrow (E)$ 

 $F \rightarrow id$ 

Input: id + id \* id

 $E \rightarrow E + T I T$ 

 $T \rightarrow T * F | F$ 

 $F \rightarrow -E \mid (E) \mid id$ 

 $E \rightarrow T E'$ 

 $E' \rightarrow +T E' \mid \epsilon$ 

 $T \rightarrow F T'$ 

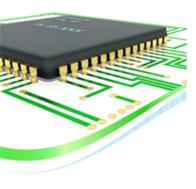
 $T' \rightarrow * F T' \mid \epsilon$ 

 $F \rightarrow -E$ 

 $F \rightarrow (E)$ 

 $F \rightarrow id$ 



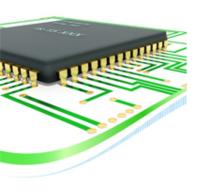


# The leftmost, top-down parser

## Backtracking

```
root \leftarrow node for the start symbol. S:
focus \leftarrow root:
push(null);
word \leftarrow NextWord():
while (true) do:
    if (focus is a nonterminal) then begin;
       pick next rule to expand focus (A \to \beta_1, \beta_2, ..., \beta_n);
        build nodes for \beta_1, \beta_2 \dots \beta_n as children of focus;
       push (\beta_n, \beta_{n-1}, \ldots, \beta_2);
        focus \leftarrow \beta_1;
    end:
    else if (word matches focus) then begin;
       word \leftarrow NextWord():
        focus \leftarrow pop()
    end:
    else if (word = eof and focus = null)
        then accept the input and return root;
       else backtrack:
end:
```





## Backtracking

Backtrack-free Grammar / Predictive Grammar a CFG for which the leftmost, top-down parser can always predict the correct rule with lookahead of at most one word.

### **Elimination Using First and Follow Sets**

#### **FIRST Set**

For a grammar symbol  $\alpha$ , FIRST( $\alpha$ ) is the set of <u>terminals</u> that can appear at the start of a sentence derived from  $\alpha$ .

#### **FOLLOW Set**

For a nonterminal  $\alpha$ , FOLLOW( $\alpha$ ) contains the set of <u>words</u> that can occur immediately after  $\alpha$  in a sentence.





 $G = (V, \Sigma, R, S)$ 

What are T, NT,

**P?** 

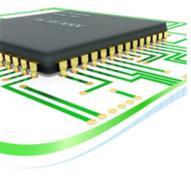
## First Set

```
for each \alpha \in (T \cup eof \cup \epsilon) do;
                                                                              Construction
      FIRST(\alpha) \leftarrow \alpha;
end:
for each A \in NT do:
      FIRST(A) \leftarrow \emptyset:
end:
while (FIRST sets are still changing) do;
    for each p \in P, where p has the form A \rightarrow \beta do;
           if \beta is \beta_1\beta_2...\beta_k, where \beta_i \in T \cup NT, then begin;
              rhs \leftarrow FIRST(\beta_1) - \{\epsilon\};
              i \leftarrow 1:
              while (\epsilon \in FIRST(\beta_i)) and i \leq k-1 do;
                     rhs \leftarrow rhs \cup (FIRST(\beta_{i+1}) - \{\epsilon\});
                    i \leftarrow i + 1:
              end:
           end:
         if i = k and \epsilon \in FIRST(\beta_k)
                 then rhs \leftarrow rhs \cup \{\epsilon\};
         FIRST(A) \leftarrow FIRST(A) \cup rhs;
    end:
end:
```





### First Set **Example**



### G:

$$E \rightarrow E + T \mid T$$
  
 $T \rightarrow T * F \mid F$   
 $F \rightarrow -E \mid (E) \mid id$ 

$$E \rightarrow T E'$$
  
 $E' \rightarrow +T E'$   
 $E' \rightarrow \epsilon$ 

$$T \rightarrow F T'$$

$$T' \rightarrow * F T'$$

$$T' \rightarrow \epsilon$$

$$F \rightarrow - E$$
  
 $F \rightarrow (E)$   
 $F \rightarrow id$ 

### **Build the first sets!**





### **Follow Set**

### Construction

```
for each A \in NT do:
      FOLLOW(A) \leftarrow \emptyset:
end:
FOLLOW(S) \leftarrow \{eof\};
while (FOLLOW sets are still changing) do;
    for each p \in P of the form A \to \beta_1 \beta_2 \cdots \beta_k do;
           TRAILER \leftarrow FOLLOW(A);
           for i \leftarrow k down to 1 do:
                  if \beta_i \in NT then begin;
                       FOLLOW(\beta_i) \leftarrow FOLLOW(\beta_i) \cup TRAILER;
                       if \epsilon \in FIRST(\beta_i)
                            then Trailer \leftarrow Trailer \cup (first(\beta_i) -\epsilon);
                           else TRAILER \leftarrow FIRST(\beta_i);
                 end:
                 else TRAILER \leftarrow FIRST(\beta_i); // is \{\beta_i\}
           end:
    end:
end:
```



### **Follow Set**

**Example** 

### G:

$$E \rightarrow E + T \mid T$$
  
 $T \rightarrow T * F \mid F$   
 $F \rightarrow -E \mid (E) \mid id$ 

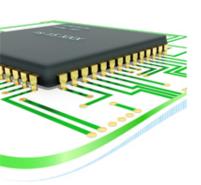
$$E \rightarrow T E'$$
  
 $E' \rightarrow +T E'$   
 $E' \rightarrow \epsilon$ 

$$T \rightarrow F T'$$
 $T' \rightarrow * F T'$ 
 $T' \rightarrow \epsilon$ 

$$F \rightarrow - E$$
  
 $F \rightarrow (E)$   
 $F \rightarrow id$ 

**Build the follow sets!** 





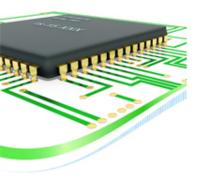
# Backtrack-free Test

### Test each non-terminal with multiple RHS!

$$First^{+}(A \rightarrow \beta) = \begin{cases} First(\beta), & \varepsilon \notin First(\beta) \\ First(\beta) \cup Follow(A), & otherwise \end{cases}$$

$$First^+(A \to \beta_i) \cap First^+(A \to \beta_i) = \emptyset, \quad \forall 1 \le i, j \le n, \quad i \ne j$$





G:

 $E \rightarrow E + T \mid T$ 

 $T \rightarrow T * F | F$ 

 $E \rightarrow T E'$ 

 $E' \rightarrow \epsilon$ 

 $T' \rightarrow \epsilon$ 

 $F \rightarrow -E$ 

 $F \rightarrow id$ 

 $F \rightarrow (E)$ 

 $F \rightarrow id (E)$ 

 $F \rightarrow id [E]$ 

 $T \rightarrow F T'$ 

 $T' \rightarrow * F T'$ 

 $E' \rightarrow +T E'$ 

 $F \rightarrow -E \mid (E) \mid id$ 

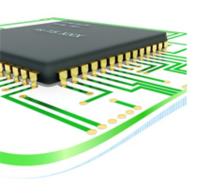
## Left Factoring

When array and function call like structures added!

### G: $E \rightarrow E + T I T$ $T \rightarrow T * F | F$ $F \rightarrow -E \mid (E) \mid id$ $F \rightarrow -E$ $F \rightarrow (E)$ $F \rightarrow id G$ $G \rightarrow (E)$ $G \rightarrow [E]$

 $G \rightarrow \epsilon$ 





### **Predictive Parsers**

### **Stages of Test & Elimination**

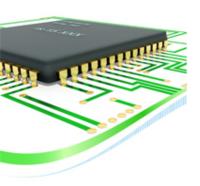
- Ambiguity
- Left Recursion
- Backtracking
- Left Factoring

Can you revise the leftmost, top-down parser?

### Now, we can focus on

- Recursive Descent Parsers
- Table Driven LL(1) Parser





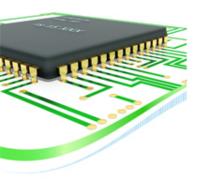
## Recursive Descent Parsing

```
Expr()
   /\star Expr \rightarrow Term Expr' \star /
   if (Term())
        then return EPrime():
        else Fail():
EPrime()
   /* Expr' \rightarrow + Term Expr' */
   /* Expr' \rightarrow - Term Expr' */
   if (word = + or word = -)
        then begin;
          word \leftarrow NextWord():
          if (Term())
               then return EPrime():
               else Fail():
        end:
```

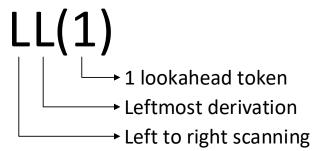
### A procedure for each NT

- Hand coded
- Or, automatically generated based on grammar
- Ease of customization, debugging





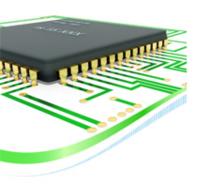
## LL(1) Parsing



### LL(1) Parsers

- Use standard skeleton procedure
- Use parse tables
- Can be generated by parser generators





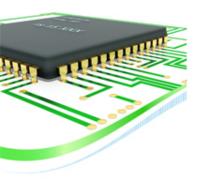
### The leftmost, top-down parser

(non-predictive)

## LL(1) Parsing

```
root \leftarrow node for the start symbol, S;
focus \leftarrow root:
push(null);
word \leftarrow NextWord():
while (true) do:
    if (focus is a nonterminal) then begin;
       pick next rule to expand focus (A \to \beta_1, \beta_2, ..., \beta_n);
        build nodes for \beta_1, \beta_2 \dots \beta_n as children of focus;
        push (\beta_n, \beta_{n-1}, \ldots, \beta_2):
        focus \leftarrow \beta_1;
    end:
    else if (word matches focus) then begin;
        word \leftarrow NextWord():
        focus \leftarrow pop()
    end:
    else if (word = eof and focus = null)
        then accept the input and return root;
       else backtrack;
                       Sample pseudo-code from "Cooper, K.D., Torczon, L.; Engineering A Compiler"
end:
```





### LL(1) Parser

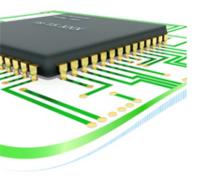
**Predictive** 

No backtracking

## LL(1) Parsing

```
word \leftarrow NextWord():
push eof onto Stack:
push the start symbol, S, onto Stack;
focus \leftarrow top of Stack;
loop forever:
   if (focus = eof and word = eof)
        then report success and exit the loop;
   else if (focus \in T or focus = eof) then begin;
      if focus matches word then begin;
          pop Stack;
          word \leftarrow NextWord():
      end:
      else report an error looking for symbol at top of stack;
   end:
   else begin: /* focus is a nonterminal */
      if Table[focus,word] is A \rightarrow B_1B_2\cdots B_k then begin;
          pop Stack:
          for i \leftarrow k to 1 by -1 do:
             if (B_i \neq \epsilon)
                then push B_i onto Stack;
          end:
      end:
      else report an error expanding focus;
     end:
     focus \leftarrow top of Stack;
end:
                    Sample pseudo-code from "Cooper, K.D., Torczon, L.; Engineering A Compiler"
```





### LL(1) Parser

**Predictive** 

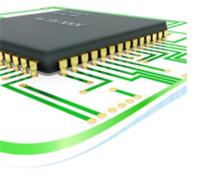
No backtracking

# LL(1) Parsing Parse Table

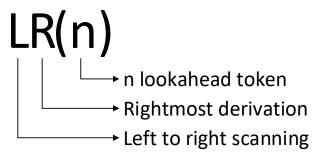
### **Use First+ to create the parse table!**

|        | eof | + | - | × | ÷ | ( | ) | name | num |
|--------|-----|---|---|---|---|---|---|------|-----|
| Goal   | _   | _ | _ | _ | _ | 0 | _ | 0    | 0   |
| Expr   | _   | _ | _ | _ | _ | 1 | _ | 1    | 1   |
| Expr'  | 4   | 2 | 3 | _ | _ | _ | 4 | _    | _   |
| Term   | _   | _ | _ | _ | _ | 5 | _ | 5    | 5   |
| Term'  | 8   | 8 | 8 | 6 | 7 | _ | 8 | _    | _   |
| Factor | _   | _ | _ | _ | _ | 9 | _ | 11   | 10  |





# Bottom Up Parsing LR Grammars



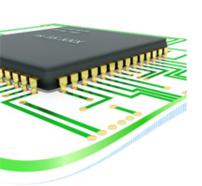
### **Bottom-Up Parsing**

Begins with the leaves and grows the tree toward the root.

#### **LR Grammars**

- Shift Reduce Parsing
- LR(0) Automaton
- Using Follow: SLR Parsing
- Using Lookahead: LR(1) Canonical Items
- Saving Resources: LALR





**Shift Reduce Parsing** 

### **Grammar:**

| 1 |    | P | _             | F |
|---|----|---|---------------|---|
|   | ۱. |   | $\overline{}$ | ᆫ |

2. 
$$E \rightarrow E + T$$

3. 
$$E \rightarrow T$$

4. 
$$T \rightarrow id (E)$$

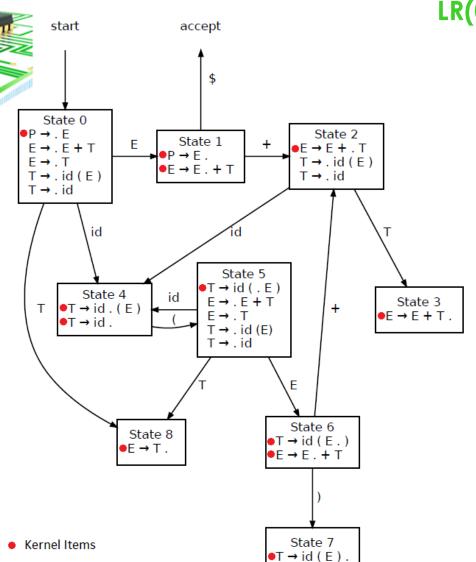
5.  $T \rightarrow id$ 

Input: id(id+id)

| Stack       | Input           | Action  |
|-------------|-----------------|---|
|             | id (id + id) \$ | shift   |
| id          | (id + id)\$     | shift   |
| id (        | id + id)\$      | shift   |
| id ( id     | + id ) \$       | reduce $T \rightarrow id$                                     |
| id ( T      | + id ) \$       | reduce $E \rightarrow T$                                      |
| id (E       | + id ) \$       | shift   |
| id (E+      | id)\$           | shift   |
| id (E + id) | ) \$            | reduce $T \rightarrow id$                                     |
| id (E + T)  | )\$             | reduce $E \rightarrow E + T$                                  |
| id (E       | ) \$            | shift   |
| id ( E )    | \$              | reduce $T \rightarrow id(E)$                                  |
| T           | \$              | reduce $E \rightarrow T$                                      |
| E           | \$              | $\operatorname{reduce} \operatorname{P} \to \operatorname{E}$ |
| P           | \$              | accept  |



LR(0) Items / Automaton



### **Position Notation**

Dot augmentation

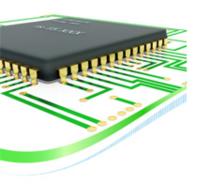
### **Kernel Items**

Ex:  $P \rightarrow .E$ 

#### Closure

Ex:





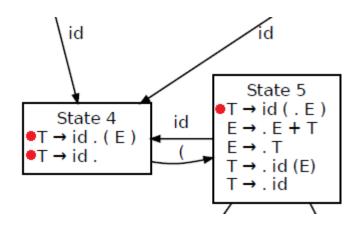
**Conflicts** 

### **Shift - Reduce Conflicts**

From the example grammar (State 4)

 $T \rightarrow id . E$ 

 $T \rightarrow id$ .



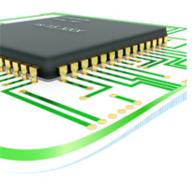
### **Reduce – Reduce Conflicts**

Ex: If we had followings on a state

 $S \rightarrow id (E)$ .

 $E \rightarrow id (E)$ .





**SLR Parsing** 

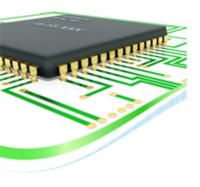
### **Prediction Using Follow Sets**

| State | Goto |    |    | ACTION |    |    |    |  |
|-------|------|----|----|--------|----|----|----|--|
|       | E    | T  | id | (      | )  | +  | \$ |  |
| 0     | G1   | G8 | S4 |        |    |    |    |  |
| 1     |      |    |    |        |    | S2 | R1 |  |
| 2     |      | G3 | S4 |        |    |    |    |  |
| 3     |      |    |    |        | R2 | R2 | R2 |  |
| 4     |      |    |    | S5     | R5 | R5 | R5 |  |
| 5     | G6   | G8 | S4 |        |    |    |    |  |
| 6     |      |    |    |        | S7 | S2 |    |  |
| 7     |      |    |    |        | R4 | R4 | R4 |  |
| 8     |      |    |    |        | R3 | R3 | R3 |  |

#### **Grammar:**

- 1.  $P \rightarrow E$
- 2.  $E \rightarrow E + T$
- 3.  $E \rightarrow T$
- 4.  $T \rightarrow id (E)$
- 5.  $T \rightarrow id$





# Bottom Up Parsing SLR Parsing

SLR Parsing Algorithm.

Let S be a stack of LR(0) automaton states. Push  $S_0$  onto S. Let a be the first input token.

### Loop:

Let *s* be the top of the stack.

If ACTION[s, a] is accept:

Parse complete.

Else if ACTION[s, a] is **shift** t:

Push state t on the stack.

Let a be the next input token.

Else if ACTION[s, a] is **reduce** A  $\rightarrow \beta$ :

Pop states corresponding to  $\beta$  from the stack.

Let t be the top of stack.

Push GOTO[t, A] onto the stack.

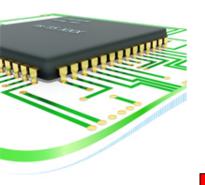
Otherwise:

Halt with a parse error.





**SLR Parsing** 



| _ |    |   |   |   |   |   |
|---|----|---|---|---|---|---|
| G | ra | m | m | 2 | r | • |

| 1 |  | Ρ. | $\rightarrow$ | Ε |
|---|--|----|---------------|---|
|---|--|----|---------------|---|

2. 
$$E \rightarrow E + T$$

3. 
$$E \rightarrow T$$

4. 
$$T \rightarrow id (E)$$

5. 
$$T \rightarrow id$$

Input: id(id+id)

| Stack          | Symbols     | Input            | Action                       |
|----------------|-------------|------------------|------------------------------|
| <br>0          |             | id ( id + id) \$ | shift 4                      |
| 0 4            | id          | ( id + id ) \$   | shift 5                      |
| 0 4 5          | id (        | id + id ) \$     | shift 4                      |
| 0 4 5 <u>4</u> | id ( id     | + id ) \$        | $reduce \ T \rightarrow id$  |
| 0 4 5 <u>8</u> | id ( T      | + id ) \$        | $reduce \ E \rightarrow T$   |
| 0 4 5 <u>6</u> | id (E       | + id ) \$        | shift 2                      |
| 04562          | id (E+      | id ) \$          | shift 4                      |
| 045624         | id (E + id) | )\$              | $reduce \ T \rightarrow id$  |
| 045 <u>623</u> | id (E + T)  | )\$              | reduce $E \rightarrow E + T$ |
| 0456           | id (E       | )\$              | shift 7                      |
| 0 <u>4567</u>  | id (E)      | \$               | reduce $T \rightarrow id(E)$ |
| 0 <u>8</u>     | T           | \$               | $reduce \ E \rightarrow T$   |
| 0 1            | E           | \$               | accept                       |





LR(1) Items

### SLR fails when follow sets are not distinct on the same state

|   | First | Follow |
|---|-------|--------|
| S | id    | \$     |
| V | id    | =\$)   |
| E | Id    | \$)    |

#### **Grammar:**

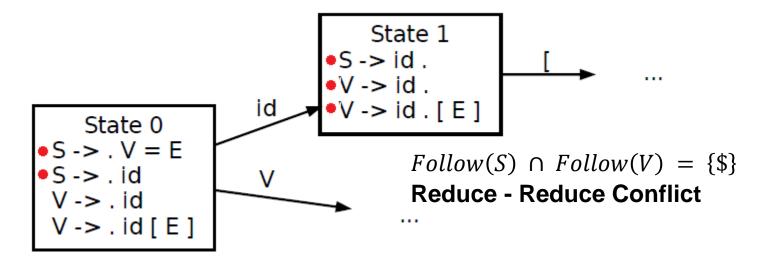
| 1 |  | S | $\rightarrow$ | ٧ | = | Ε |
|---|--|---|---------------|---|---|---|
|---|--|---|---------------|---|---|---|

2. 
$$S \rightarrow id$$

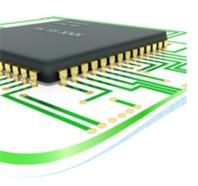
3. 
$$V \rightarrow id$$

4. 
$$V \rightarrow id (E)$$

5. 
$$E \rightarrow V$$







# Bottom Up Parsing LR(1) Items

### **Canonical Form**

Like LR(0), Augmented by Lookahead

#### **Grammar:**

- 1.  $S \rightarrow V = E$
- 2.  $S \rightarrow id$
- 3.  $V \rightarrow id$
- 4.  $V \rightarrow id (E)$
- 5.  $E \rightarrow V$

### Writing Lookahead for Each Item in State

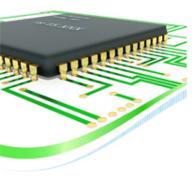
In case A  $\rightarrow \alpha$  . B, {L} create B  $\rightarrow$  .  $\gamma$ , {L}

In case A  $\rightarrow \alpha$  . B  $\beta$ , {L}

create B  $\rightarrow$  .  $\gamma$ , First( $\beta$ ) if  $\beta$  cannot be  $\epsilon$ 

create B  $\rightarrow$  .  $\gamma$ , First( $\beta$ ) U {L} if  $\beta$  can be  $\epsilon$ 





### **Grammar:**

- 1.  $P \rightarrow E$
- 2.  $E \rightarrow E + T$
- 3.  $E \rightarrow T$
- 4.  $T \rightarrow id (E)$
- 5.  $T \rightarrow id$

## **Bottom Up Parsing**

LR(1) Items

### **Example Case for P (State 0)**

As kernel item add (1)  $P \rightarrow . E$ , {\$}

Using (1) add (2)  $E \rightarrow .E + T$ , {\$}

Using (1) add (3)  $E \rightarrow . T$ , {\$}

Using (2) add (4)  $E \rightarrow .E + T$ ,  $\{+\}$ 

Using (3) add (5)  $T \rightarrow .$  id ( E ), {\$}

Using (3) add (6)  $T \rightarrow .id, \{\$\}$ 

Using (4) add (7)  $E \rightarrow . T$ ,  $\{+\}$ 

No new item using (5), (6)

Using (7) add (8)  $T \rightarrow .id (E), \{+\}$ 

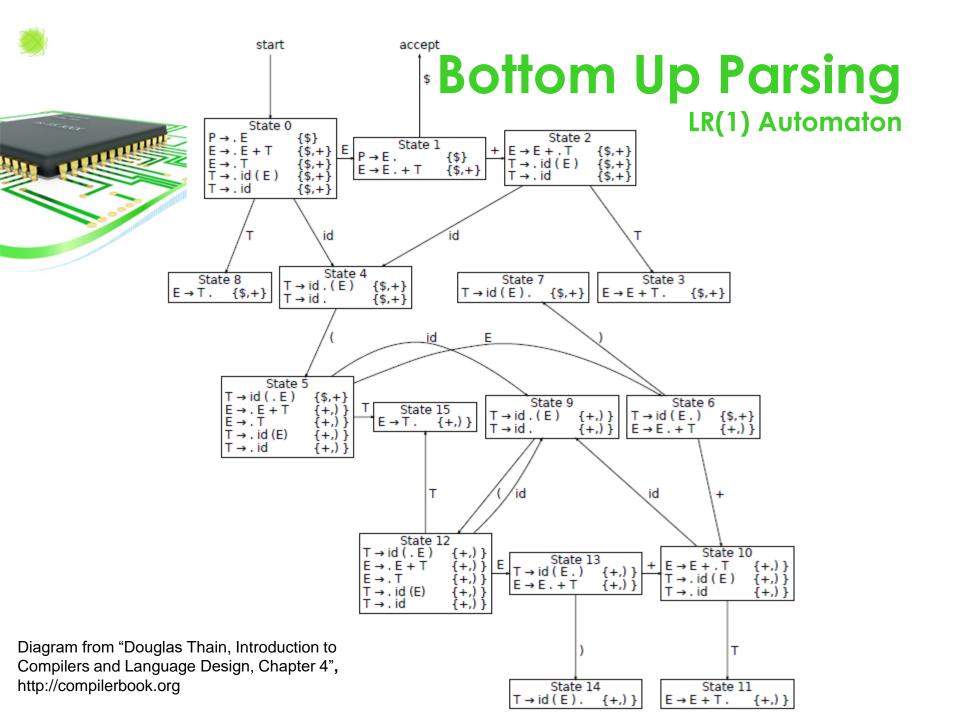
Using (7) add (9)  $T \rightarrow .id, \{+\}$ 

No new items using (8), (9)

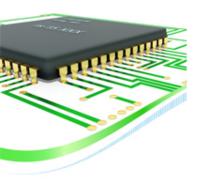
Merge the items having common LR(0) items.

### Closure

 $P \rightarrow . E, \{\$\}$   $E \rightarrow . E + T, \{\$ +\}$   $E \rightarrow . T, \{\$ +\}$   $T \rightarrow . id (E), \{\$ +\}$  $T \rightarrow . id, \{\$ +\}$ 







# Bottom Up Parsing LALR Parsing

### **Merge States Having Common Cores**

Identify the States Having Common Cores
Write a New State with LR(0) items and Union Lookaheads

**Example:** Not from the Previous Diagram!

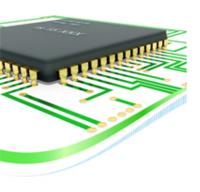
Identify the states that can be merged in the previous diagram!

Reconstruct the diagram!

**Note on Grammars:** 

$$LL(1) \subset SLR \subset LALR \subset LR(1) \subset CFG$$





### **Final Words**

### **Other Parsing Strategies**

- LL(\*)
- Parse Expression Grammars (PEG)
- ...more

"BOTTOM LINE: We do all this math to ensure that the source code is translated to internal representation unambiguously, predictably." (\*)