

Dividulet

P(U,t) & V(L,t) & V

$$\frac{\partial V}{\partial t} = -\frac{1}{e} \frac{\partial \rho}{\partial t} - \frac{f}{20} |V|V$$

$$\frac{\partial \rho}{\partial t} + \rho c^{2} \frac{\partial V}{\partial t} = 0$$

V(lit) => volocity at location L and time t

p(lit) => pressure at location L and time t

Space hiserthization: t= hat hat have one equally spaced segments

1 time discretization: t= hat have one of the segments.

Using central differences method: (Referred paper uses backward forward difference method. The rouls are more noisy)

For the velocity:

$$\frac{V(i,k+1)-V(i,k)}{\Delta t} = \frac{1}{e} \frac{P(i+1,k)-P(i+1,k)}{2\Delta t} = \frac{1}{2D} \left[V(i,k)\right]V(i,k)$$

$$V(i,k+1) = \frac{\Delta t}{e} \frac{P(i+1,k)-P(i+1,k)}{2\Delta t} + \frac{\Delta t}{2D} \left[V(i,k)\right]V(i,k) + V(i,k)$$

For the pressure

$$\frac{P(i,k+1) \cdot P(i,k)}{\Delta t} = -Pc^2 \frac{V(i+1,k) \cdot V(i-1,k)}{\Delta t}$$

$$P(i,k+1) = -Pc^2 \Delta t \frac{V(i+1,k) \cdot V(i-1,k)}{\Delta t} + P(i,k)$$

Initial Conditions

Upstream Boundary Conditions

$$V(o,k+1) = P_o = P(o,k)$$

$$V(o,k+1) = -\frac{\Delta t}{P \Delta L} \left(P(1,k) - P_o \right) - \frac{\Delta t f}{2D} \left| V(o,k) \right| V(o,k)$$

Down stream boundary condition
$v(m,k+1) = T(k) u_{max}$ The is the command size to the value, where $0 \le T \le 1$
P(m,k+1) = - Perst (v(m,k) - v(m-1,k))+p(m,k)
Nomen clarive
p: pressure (Pa) P: flow density (kg/m3)
or variety (M/S) f: Darry - Weishach frichen factor
c. vare velocity (m18) D: pipe d'ameter (m)
Simulation Scenario and parameter (see sec. 4 of the paper)
Po = 2.105 Pa T = 10 seconds
L = 200 m
D = lwmm
P = 1000 kg/m3
C = hwm/s
f = 0.03
T: value dosing, function of time
T(t): 1 -> value is fully clusted
T(1)=0 -> value is fully open
Contractive on the contractive of the contractive o
Constant closure tate as countril simulation
1 fully closed
oper D tos
fulls time hari war
American mariners

value is slowly closed with a constant closure - rate k=0 4=1 k=m-1 k=m , and fimulation time T = 6 seconds m = 16 Let us take For the optimization process, we will record the pressure data every 1 second! later, this pressure days will be used as basis to the cost function 2.6 × 10⁵ Pipeline node #16 2.35 × 10⁵ Pressure at t = 10s 2.4 2.3 2.2 2.25 2.2 $p(\ell)$ 2.15 2.1 1.2 2.05 10 2 3 6 8 9 50 100 150 200 to Time(s) t=T 0 = L



