

# *Combining Leakage-Resilient PRFs and Shuffling Towards Bounded Security for Small Embedded Devices*



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# Outline

Background

Our construction

Evaluation setup

Results



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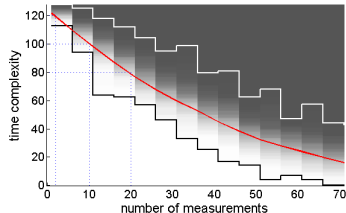
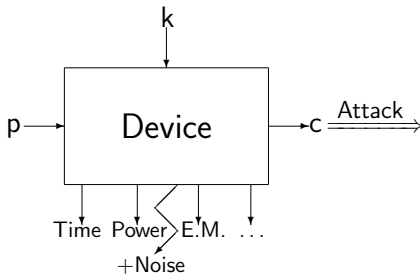
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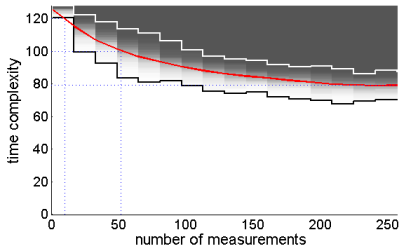


## Side channel attacks



- ▷ Rank of the key decreases exponentially with the number of measurements.

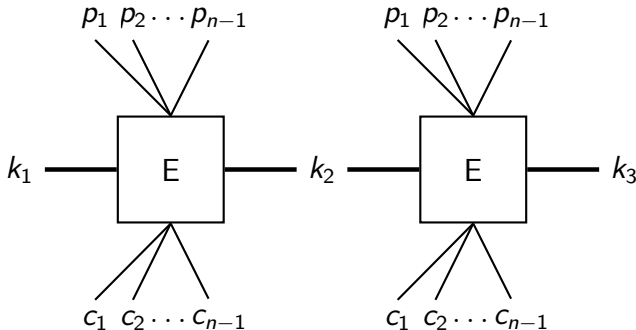
## *Ideal goal : bounded security*



- ▷ Limits the number of measurements/plaintexts for 1 key.
- ▷ Hope: bound on time complexity independent of the number of measurements.

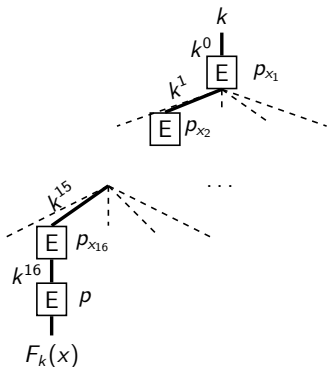


## Leakage resilient PRG [BM84]



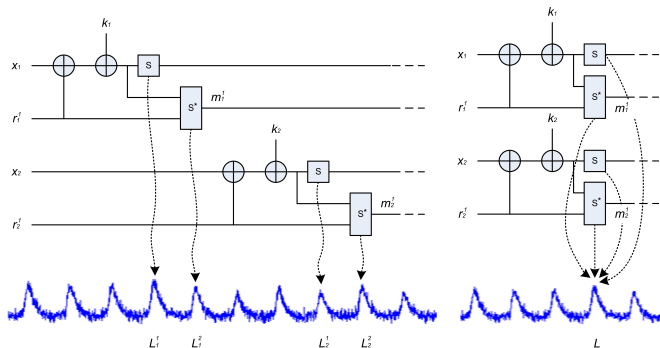
- ▷ The construction limits the number of measurements for one key 👍.
- ▷ But 2 parties need to be synchronized (stateful) 🚫.

## Leakage resilient PRF [GGM86]



- ▶ The data complexity is limited, not the number of measurements 🙅.
- ▶ The 2 parties do not need to be synchronized (stateless) 👍.

## Implementation hardware vs. software



- ▶ In software, the operations are done sequentially. At each time, the trace depends only on one operation.
- ▶ In hardware, the operations are done in parallel. The leakage on different operations are at the same time in the trace.



## *Previous results on leakage resilient primitives*

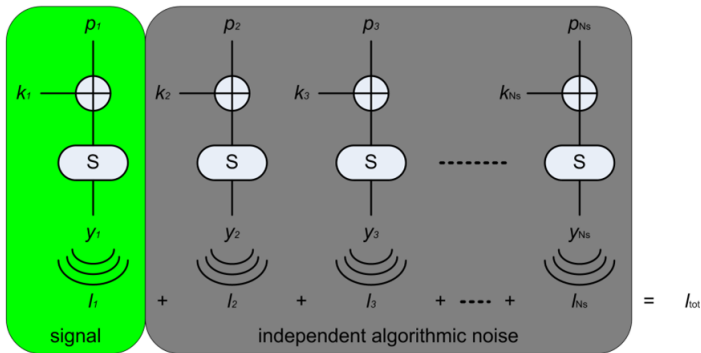
Belaïd et al. have shown that [BGS14]:

	Software	Hardware
LR PRG	bounded	bounded
LR PRF	unbounded	unbounded
LR-PRF+key dependent algorithmic noise [MJS12]	unbounded	bounded*

\* against specific, but realistic adversaries.

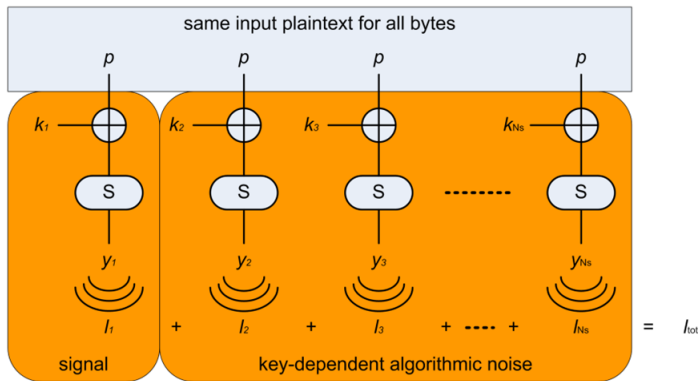


# Algorithmic noise in hardware



$P_i$  can be chosen randomly  $\Rightarrow$  Divide and conquer attacks could remove the algorithmic noise.

## Key dependent algorithmic noise in hardware



Divide and conquer attacks hardly apply in that case [MSJ12].

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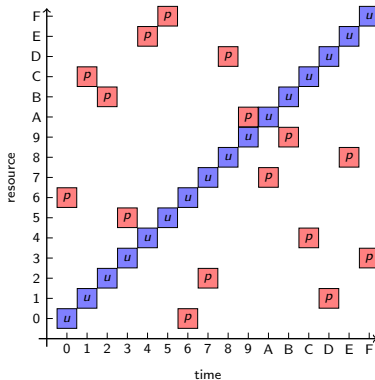
## *Research problem: bounded security in software*

Natural idea:

- ▷ Leakage resilient PRF.
- ▷ Shuffled implementation for algorithmic noise.
- ▷ Chosen plaintext for key dependent noise.



# Shuffling in software



- ▷ Randomize the order of the operations.
- ▷ Trivial attack: integration (sum over all the time)  $\Rightarrow$  algorithmic noise.



## *Key dependent algorithmic noise differences in software/hardware*

- ▷ There is some information on the permutation used  $\Rightarrow$  there is some indication on the subkey used 🙅.
- ▷ Shuffling can be done on all the operations  $\Rightarrow$  key dependent algorithmic noise in all the rounds 👍.



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# *Implementation of the counter-measure*

- ▷ Simulated experiments, parameters:
  - direct leakage on the permutation,
  - indirect resource dependent leakage,
  - indirect time dependent leakage,
  - noise level (not in this presentation).
  
- ▷ On real device, ATmega644p, parameters:
  - direct permutation leakage,
  - indirect leakage as well ( $16 \times 16 \times 256$  templates)
  - shuffling implementation (not in this presentation).



## Attacks against the target implementation

- ▷ Leakage on the S-box outputs:

$$\mathbf{L}_{\text{sprf}}^{r+t} = [\mathbf{L}_{p(t),t}(S(x \oplus k_{p(t)})) + N_t]_t.$$

- ▷ Direct permutation leakage:

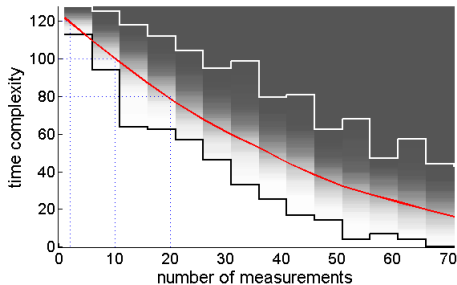
$$\mathbf{L}' = [\text{HW}(p(t)) + N_t]_t.$$

- ▷ Template attacks, worst case scenario [VCMKS12]:

$$\Pr[\mathbf{L} = \mathbf{l} | K_s = k] = \sum_t \frac{f(t, s, \mathbf{l}')}{\sum_{t'} f(t', s, \mathbf{l}')} \Pr[L_t = l_t | K_s = k].$$



## *Metric to evaluate attack*



Security margins evaluated thanks to security graph [VCGS13]

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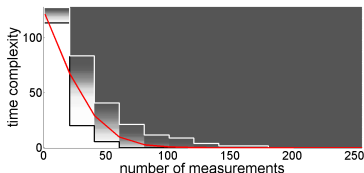
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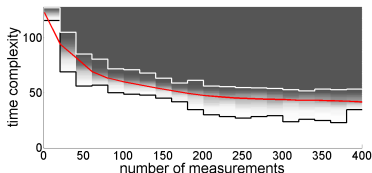
## *Simulated : indirect resource dependent leakage*

No direct leakage.  
No time dependency.

Correlation resource  
leakage : 0.75.



Correlation resource  
leakage : 0.99.



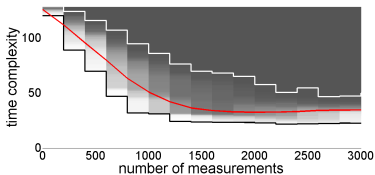
Bounded security if leakage functions are similar enough 🙌.

## *Simulated : indirect time dependent leakage*

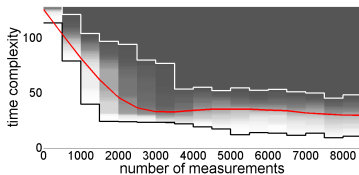
No direct leakage.

Correlation resource leakage : 0.75.

Correlation time leakage  
: 0.75.



Correlation time leakage  
: 0.99.



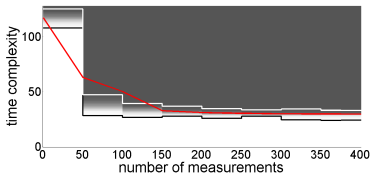
Bounded security when time adds confusion between leakage functions 🍷.

## *Simulated : direct leakage*

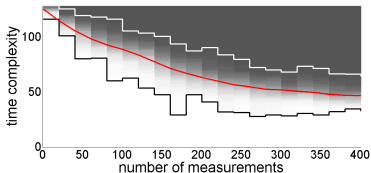
Direct leakage.

Correlation resource leakage : 0.75.

Correlation time leakage  
: 0.75.



Correlation time leakage  
: 0.99.



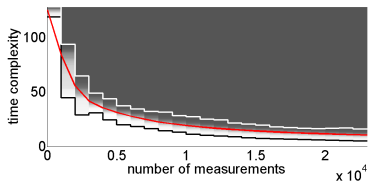
Bound on time complexity when direct leakages are available 🍏.

## On real device

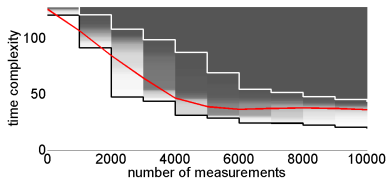
Correlation resource leakage : 0.86.

Correlation time leakage : 0.84.

Direct leakage.



No direct leakage.



Low bounded security 🖐️.



## Conclusion

- ▷ Goal achieved : security bounded stateless primitive in software 👍.
- ▷ S-box leakage only (since MixColumns is also protected same result should be observed) 👍.
- ▷ Concrete security level weak 👎.
- ▷ Against specific adversaries 👎.
- ▷ Would be interesting to look at other (more noisy) chips and other attack strategies.

# THANKS

