Comparison of Priori and Brute Force Algorithms for Frequent Items Mining Midterm Project **Aurel Sahiti** UCID: as4579 as4579@njit.edu In [2]: import random import pandas as pd from itertools import combinations import time Introduction This document details the implementation and comparison of two algorithms: the Priori algorithm and the Brute Force method for mining frequent item sets and generating association rules from transaction data. We will explore how both methods work and compare their performance based on their execution times. **Creating Transaction Data** In [3]: # Create 30 items from supermarkets items = ['milk', 'bread', 'butter', 'eggs', 'cheese', 'chicken', 'beef', 'fish', 'apples', 'bananas', 'oranges', 'grapes', 'cereal', 'pasta', 'rice', 'tomatoes', 'onions', 'potatoes', 'broccoli', 'carrots', 'shampoo', 'floss', 'toothpaste', 'detergent', 'cleaning_wipes', 'diapers', 'napkins', 'paper_towels', 'dish_soap', 'toilet_paper' # Create a function that will generate random transactions def generate_transactions(num_transactions=20): transactions = [] for _ in range(num_transactions): # Randomly choose a subset of items for each transaction (1-10 items) num_items = random.randint(1, 10) transaction = random.sample(items, num_items) transactions.append(transaction) return transactions # Generate 5 databases with 20 transactions each databases = [generate_transactions() for _ in range(5)] - We started by defining 30 items commonly purchased in supermarkets. - The "generate_transactions" function generates a list of transactions, where each transaction contains anywhere from 1 up to 10 items. - In total, 5 databases were created with 20 transactions in each. **Creating Functions** In [4]: # Calculate support for a given itemset def calculate_support(itemset, transactions): count = sum(1 for transaction in transactions if itemset.issubset(transaction)) return count / len(transactions) # Filter itemsets by support def filter_itemsets_by_support(itemsets, transactions, min_support): filtered_itemsets = {} for itemset in itemsets: support = calculate_support(itemset, transactions) if support >= min_support: filtered_itemsets[itemset] = support return filtered_itemsets # Generate candidate itemsets of size 1 def get_itemsets_size_1(transactions): itemset = set() for transaction in transactions: for item in transaction: itemset.add(frozenset([item])) return itemset # Generate candidate itemsets of larger size by combining frequent itemsets def generate_candidate_itemsets(frequent_itemsets, k): candidates = set() frequent_itemsets_list = list(frequent_itemsets) for i in range(len(frequent_itemsets_list)): for j in range(i + 1, len(frequent_itemsets_list)): 11 = list(frequent_itemsets_list[i]) 12 = list(frequent_itemsets_list[j]) 11.sort() **if** 11[:k-2] == 12[:k-2]: # Only combine if first k-2 items are the same candidates.add(frozenset(frequent_itemsets_list[i] | frequent_itemsets_list[j])) return candidates # Generate association rules def generate_association_rules(frequent_itemsets, transactions, min_confidence): rules = [] for itemset in frequent_itemsets: if len(itemset) < 2:</pre> continue for consequence in itemset: antecedent = itemset - frozenset([consequence]) if len(antecedent) == 0: continue # Calculate confidence support_itemset = calculate_support(itemset, transactions) support_antecedent = calculate_support(antecedent, transactions) confidence = support_itemset / support_antecedent if support_antecedent > 0 else 0 if confidence >= min confidence: rules.append((antecedent, frozenset([consequence]), confidence)) return rules - Support is calculated as the fraction of transactions containing the given item-set. - The "calculate" support" function is used in both algorithms to check if an item-set is frequent (if its support is above the specified minimum threshold). The "filter_itemsets_by_support" function loops through each item-set in the input "itemsets". For each item-set, it calculates its support using the "calculate_support" function. If the support is greater than or equal to the specified "min_support", the item-set is added to the "filtered itemsets" dictionary along with its support value. Finally, the function returns the filtered itemsets dictionary, which contains only itemsets that meet the minimum support criteria. - The "get_itemsets_size_1" function is created to generate the initial set of 1-itemsets (combinations of single items) from a list of transactions. - The use of the "frozenset" ensures that the itemsets are immutable, which is useful when storing these itemsets as keys in a dictionary for support calculations or when further processing them to generate larger itemsets. - The "generate_candidate_itemsets" function generates candidate itemsets of size "k" by combining frequent itemsets of size k-1. - The "generate_association_rules" function generates association rules from frequent item-sets by calculating the confidence of each rule (based on the support of the item-set and its antecedent). - It also checks if the confidence meets the specified minimum threshold and stores the rules that satisfy that condition. **Apriori Algorithm Implementation** In [5]: # Main Apriori algorithm def apriori(transactions, items, min_support=0.2, min_confidence=0.6): # Step 1: Generate itemsets of size 1 candidate_itemsets = get_itemsets_size_1(transactions) # Step 2: Filter itemsets by support frequent_itemsets = filter_itemsets_by_support(candidate_itemsets, transactions, min_support) all_frequent_itemsets = dict(frequent_itemsets) k = 2 while frequent_itemsets: # Step 3: Generate candidate itemsets of size k candidate_itemsets = generate_candidate_itemsets(frequent_itemsets, k) # Step 4: Filter itemsets by support frequent_itemsets = filter_itemsets_by_support(candidate_itemsets, transactions, min_support) all_frequent_itemsets.update(frequent_itemsets) k **+=** 1 # Step 5: Generate association rules rules = generate_association_rules(all_frequent_itemsets.keys(), transactions, min_confidence) return all_frequent_itemsets, rules In [6]: # Apriori results def apriori_results(databases, min_support, min_confidence, items): for i, transactions in enumerate(databases): print(f"\nDatabase {i + 1}:") # Apriori start_time = time.time() frequent_itemsets_apriori, rules_apriori = apriori(transactions, items, min_support, min_confidence) apriori_time = time.time() - start_time # Output frequent itemsets from Apriori print("\nApriori Frequent Itemsets:") for itemset, support in frequent_itemsets_apriori.items(): print(f"Itemset: {set(itemset)}, Support: {support:.4f}") # Output association rules from Apriori print("\nApriori Association Rules:") for antecedent, consequent, confidence in rules_apriori: print(f"Rule: {set(antecedent)} -> {set(consequent)}, Confidence: {confidence:.4f}") # Set minimum support and confidence min_support = 0.2 min_confidence = 0.6 # Compare the two algorithms on all 5 databases apriori_results(databases, min_support, min_confidence, items) Database 1: Apriori Frequent Itemsets: Itemset: {'rice'}, Support: 0.2000 Itemset: {'butter'}, Support: 0.2000 Itemset: {'chicken'}, Support: 0.2000 Itemset: {'cleaning_wipes'}, Support: 0.3000 Itemset: {'onions'}, Support: 0.2000 Itemset: {'eggs'}, Support: 0.2000 Itemset: {'carrots'}, Support: 0.2500 Itemset: {'detergent'}, Support: 0.3500 Itemset: {'grapes'}, Support: 0.3500 Itemset: {'milk'}, Support: 0.2000 Itemset: {'bananas'}, Support: 0.3000 Itemset: {'oranges'}, Support: 0.2000 Itemset: {'floss'}, Support: 0.2500 Itemset: {'broccoli'}, Support: 0.2500 Itemset: {'dish_soap'}, Support: 0.2000 Itemset: {'tomatoes'}, Support: 0.3000 Itemset: {'detergent', 'grapes'}, Support: 0.2500 Itemset: {'chicken', 'grapes'}, Support: 0.2000 Itemset: {'cleaning_wipes', 'milk'}, Support: 0.2000 Apriori Association Rules: Rule: {'grapes'} -> {'detergent'}, Confidence: 0.7143 Rule: {'detergent'} -> {'grapes'}, Confidence: 0.7143 Rule: {'chicken'} -> {'grapes'}, Confidence: 1.0000 Rule: {'milk'} -> {'cleaning_wipes'}, Confidence: 1.0000 Rule: {'cleaning_wipes'} -> {'milk'}, Confidence: 0.6667 Database 2: Apriori Frequent Itemsets: Itemset: {'beef'}, Support: 0.2000 Itemset: {'cereal'}, Support: 0.2000 Itemset: {'apples'}, Support: 0.2500 Itemset: {'onions'}, Support: 0.2000 Itemset: {'eggs'}, Support: 0.4000 Itemset: {'bread'}, Support: 0.3000 Itemset: {'detergent'}, Support: 0.2000 Itemset: {'oranges'}, Support: 0.2500 Itemset: {'broccoli'}, Support: 0.3000 Itemset: {'napkins'}, Support: 0.2500 Itemset: {'tomatoes'}, Support: 0.2000 Itemset: {'shampoo'}, Support: 0.2500 Itemset: {'toilet_paper'}, Support: 0.2000 Apriori Association Rules: Database 3: Apriori Frequent Itemsets: Itemset: {'rice'}, Support: 0.2000 Itemset: {'butter'}, Support: 0.2500 Itemset: {'cleaning_wipes'}, Support: 0.2500 Itemset: {'cereal'}, Support: 0.2000 Itemset: {'diapers'}, Support: 0.2000 Itemset: {'apples'}, Support: 0.3000 Itemset: {'onions'}, Support: 0.2500 Itemset: {'eggs'}, Support: 0.3500 Itemset: {'pasta'}, Support: 0.2500 Itemset: {'detergent'}, Support: 0.2000 Itemset: {'paper_towels'}, Support: 0.2000 Itemset: {'grapes'}, Support: 0.3500 Itemset: {'milk'}, Support: 0.2000 Itemset: {'bananas'}, Support: 0.3500 Itemset: {'toothpaste'}, Support: 0.2000 Itemset: {'oranges'}, Support: 0.2000 Itemset: {'broccoli'}, Support: 0.2000 Itemset: {'napkins'}, Support: 0.2500 Itemset: {'fish'}, Support: 0.2500 Itemset: {'potatoes'}, Support: 0.2500 Itemset: {'toilet_paper'}, Support: 0.2500 Itemset: {'diapers', 'bananas'}, Support: 0.2000 Itemset: {'grapes', 'bananas'}, Support: 0.2000 Apriori Association Rules: Rule: {'diapers'} -> {'bananas'}, Confidence: 1.0000 Database 4: Apriori Frequent Itemsets: Itemset: {'beef'}, Support: 0.3000 Itemset: {'butter'}, Support: 0.2000 Itemset: {'cereal'}, Support: 0.2000 Itemset: {'diapers'}, Support: 0.2500 Itemset: {'apples'}, Support: 0.3000 Itemset: {'pasta'}, Support: 0.2000 Itemset: {'grapes'}, Support: 0.3000 Itemset: {'bananas'}, Support: 0.2000 Itemset: {'toothpaste'}, Support: 0.2500 Itemset: {'floss'}, Support: 0.2500 Itemset: {'napkins'}, Support: 0.3000 Itemset: {'fish'}, Support: 0.2500 Itemset: {'potatoes'}, Support: 0.2500 Itemset: {'toilet_paper'}, Support: 0.2000 Apriori Association Rules: Database 5: Apriori Frequent Itemsets: Itemset: {'butter'}, Support: 0.2000 Itemset: {'cleaning_wipes'}, Support: 0.3500 Itemset: {'diapers'}, Support: 0.2000 Itemset: {'apples'}, Support: 0.4000 Itemset: {'onions'}, Support: 0.3500 Itemset: {'eggs'}, Support: 0.2500 Itemset: {'carrots'}, Support: 0.3000 Itemset: {'bread'}, Support: 0.2000 Itemset: {'paper_towels'}, Support: 0.2000 Itemset: {'milk'}, Support: 0.3000 Itemset: {'bananas'}, Support: 0.2500 Itemset: {'toothpaste'}, Support: 0.3000 Itemset: {'oranges'}, Support: 0.2500 Itemset: {'floss'}, Support: 0.3000 Itemset: {'broccoli'}, Support: 0.4000 Itemset: {'napkins'}, Support: 0.2000 Itemset: {'dish_soap'}, Support: 0.2500 Itemset: {'shampoo'}, Support: 0.3000 Itemset: {'potatoes'}, Support: 0.2500 Itemset: {'broccoli', 'dish_soap'}, Support: 0.2000 Itemset: {'shampoo', 'potatoes'}, Support: 0.2000 Itemset: {'apples', 'broccoli'}, Support: 0.2000 Itemset: {'broccoli', 'milk'}, Support: 0.2000 Itemset: {'apples', 'toothpaste'}, Support: 0.2000 Itemset: {'broccoli', 'eggs'}, Support: 0.2000 Itemset: {'cleaning_wipes', 'milk'}, Support: 0.2000 Itemset: {'shampoo', 'onions'}, Support: 0.2000 Apriori Association Rules: Rule: {'dish_soap'} -> {'broccoli'}, Confidence: 0.8000 Rule: {'potatoes'} -> {'shampoo'}, Confidence: 0.8000 Rule: {'shampoo'} -> {'potatoes'}, Confidence: 0.6667 Rule: {'milk'} -> {'broccoli'}, Confidence: 0.6667 Rule: {'toothpaste'} -> {'apples'}, Confidence: 0.6667 Rule: {'eggs'} -> {'broccoli'}, Confidence: 0.8000 Rule: {'milk'} -> {'cleaning_wipes'}, Confidence: 0.6667 Rule: {'shampoo'} -> {'onions'}, Confidence: 0.6667 - The Apriori algorithm works by generating candidate itemsets of size 1, then iteratively combining frequent itemsets to form larger itemsets. - After generating itemsets, it filters them based on the minimum support. - Once all frequent itemsets are found, it generates association rules by calculating their confidence and comparing it to the minimum confidence threshold. **Brute Force Method Implementation** In [7]: # Part 2: Brute Force Method # Brute force method for finding frequent itemsets def brute_force(transactions, min_support=0.2, min_confidence=0.6): transactions = list(map(set, transactions)) # Convert transactions to sets all_frequent_itemsets = {} # To store all frequent itemsets k = 1 # Start with 1-itemsets while True: # Step 1: Generate all possible k-itemsets items_in_transactions = set(item for transaction in transactions for item in transaction) candidate_itemsets = list(combinations(items_in_transactions, k)) # Step 2: Filter itemsets by support frequent_itemsets = {} for itemset in candidate_itemsets: itemset = frozenset(itemset) support = calculate_support(itemset, transactions) if support >= min_support: frequent_itemsets[itemset] = support # Step 3: Terminate if no frequent itemsets found if not frequent_itemsets: break # Add to all frequent itemsets all_frequent_itemsets.update(frequent_itemsets) k += 1 # Increase the size of the itemset return all_frequent_itemsets In [8]: # Brute Force results def brute_results(databases, min_support, min_confidence, items): for i, transactions in enumerate(databases): print(f"\nDatabase {i + 1}:") # Brute Force start_time = time.time() frequent_itemsets_brute = brute_force(transactions, min_support) brute_time = time.time() - start_time # Output frequent itemsets from Brute print("\nBrute Frequent Itemsets:") for itemset, support in frequent_itemsets_brute.items(): print(f"Itemset: {set(itemset)}, Support: {support:.4f}") # Generate and output association rules from Brute print("\nBrute Force Association Rules:") rules_bruteforce = generate_association_rules(frequent_itemsets_brute.keys(), transactions, min_confidence) for antecedent, consequent, confidence in rules_bruteforce: print(f"Rule: {set(antecedent)} -> {set(consequent)}, Confidence: {confidence:.4f}") # Set minimum support and confidence $min_support = 0.2$ $min_confidence = 0.6$ # Compare the two algorithms on all 5 databases brute_results(databases, min_support, min_confidence, items) Database 1: Brute Frequent Itemsets: Itemset: {'detergent'}, Support: 0.3500 Itemset: {'carrots'}, Support: 0.2500 Itemset: {'grapes'}, Support: 0.3500 Itemset: {'butter'}, Support: 0.2000 Itemset: {'floss'}, Support: 0.2500 Itemset: {'eggs'}, Support: 0.2000 Itemset: {'tomatoes'}, Support: 0.3000 Itemset: {'chicken'}, Support: 0.2000 Itemset: {'rice'}, Support: 0.2000 Itemset: {'broccoli'}, Support: 0.2500 Itemset: {'onions'}, Support: 0.2000 Itemset: {'dish_soap'}, Support: 0.2000 Itemset: {'cleaning_wipes'}, Support: 0.3000 Itemset: {'oranges'}, Support: 0.2000 Itemset: {'bananas'}, Support: 0.3000 Itemset: {'milk'}, Support: 0.2000 Itemset: {'detergent', 'grapes'}, Support: 0.2500 Itemset: {'chicken', 'grapes'}, Support: 0.2000 Itemset: {'cleaning_wipes', 'milk'}, Support: 0.2000 Brute Force Association Rules: Rule: {'grapes'} -> {'detergent'}, Confidence: 0.7143 Rule: {'detergent'} -> {'grapes'}, Confidence: 0.7143 Rule: {'chicken'} -> {'grapes'}, Confidence: 1.0000 Rule: {'milk'} -> {'cleaning_wipes'}, Confidence: 1.0000 Rule: {'cleaning_wipes'} -> {'milk'}, Confidence: 0.6667 Database 2: Brute Frequent Itemsets: Itemset: {'apples'}, Support: 0.2500 Itemset: {'detergent'}, Support: 0.2000 Itemset: {'cereal'}, Support: 0.2000 Itemset: {'eggs'}, Support: 0.4000 Itemset: {'tomatoes'}, Support: 0.2000 Itemset: {'beef'}, Support: 0.2000 Itemset: {'toilet_paper'}, Support: 0.2000 Itemset: {'broccoli'}, Support: 0.3000 Itemset: {'onions'}, Support: 0.2000 Itemset: {'napkins'}, Support: 0.2500 Itemset: {'shampoo'}, Support: 0.2500 Itemset: {'oranges'}, Support: 0.2500 Itemset: {'bread'}, Support: 0.3000 Brute Force Association Rules: Database 3: Brute Frequent Itemsets: Itemset: {'detergent'}, Support: 0.2000 Itemset: {'apples'}, Support: 0.3000 Itemset: {'potatoes'}, Support: 0.2500 Itemset: {'grapes'}, Support: 0.3500 Itemset: {'butter'}, Support: 0.2500 Itemset: {'toothpaste'}, Support: 0.2000 Itemset: {'cereal'}, Support: 0.2000 Itemset: {'eggs'}, Support: 0.3500 Itemset: {'pasta'}, Support: 0.2500 Itemset: {'toilet_paper'}, Support: 0.2500 Itemset: {'paper_towels'}, Support: 0.2000 Itemset: {'fish'}, Support: 0.2500 Itemset: {'rice'}, Support: 0.2000 Itemset: {'broccoli'}, Support: 0.2000 Itemset: {'onions'}, Support: 0.2500 Itemset: {'napkins'}, Support: 0.2500 Itemset: {'cleaning_wipes'}, Support: 0.2500 Itemset: {'oranges'}, Support: 0.2000 Itemset: {'diapers'}, Support: 0.2000 Itemset: {'bananas'}, Support: 0.3500 Itemset: {'milk'}, Support: 0.2000 Itemset: {'grapes', 'bananas'}, Support: 0.2000 Itemset: {'diapers', 'bananas'}, Support: 0.2000 Brute Force Association Rules: Rule: {'diapers'} -> {'bananas'}, Confidence: 1.0000 Database 4: Brute Frequent Itemsets: Itemset: {'apples'}, Support: 0.3000 Itemset: {'potatoes'}, Support: 0.2500 Itemset: {'grapes'}, Support: 0.3000 Itemset: {'butter'}, Support: 0.2000 Itemset: {'floss'}, Support: 0.2500 Itemset: {'toothpaste'}, Support: 0.2500 Itemset: {'cereal'}, Support: 0.2000 Itemset: {'pasta'}, Support: 0.2000 Itemset: {'beef'}, Support: 0.3000 Itemset: {'toilet_paper'}, Support: 0.2000 Itemset: {'fish'}, Support: 0.2500 Itemset: {'napkins'}, Support: 0.3000 Itemset: {'diapers'}, Support: 0.2500 Itemset: {'bananas'}, Support: 0.2000 Brute Force Association Rules: Database 5: Brute Frequent Itemsets: Itemset: {'apples'}, Support: 0.4000 Itemset: {'potatoes'}, Support: 0.2500 Itemset: {'carrots'}, Support: 0.3000 Itemset: {'butter'}, Support: 0.2000 Itemset: {'floss'}, Support: 0.3000 Itemset: {'toothpaste'}, Support: 0.3000 Itemset: {'eggs'}, Support: 0.2500 Itemset: {'paper_towels'}, Support: 0.2000 Itemset: {'broccoli'}, Support: 0.4000 Itemset: {'onions'}, Support: 0.3500 Itemset: {'dish_soap'}, Support: 0.2500 Itemset: {'napkins'}, Support: 0.2000 Itemset: {'shampoo'}, Support: 0.3000 Itemset: {'cleaning_wipes'}, Support: 0.3500 Itemset: {'oranges'}, Support: 0.2500 Itemset: {'bread'}, Support: 0.2000 Itemset: {'diapers'}, Support: 0.2000 Itemset: {'bananas'}, Support: 0.2500 Itemset: {'milk'}, Support: 0.3000 Itemset: {'apples', 'toothpaste'}, Support: 0.2000 Itemset: {'apples', 'broccoli'}, Support: 0.2000 Itemset: {'potatoes', 'shampoo'}, Support: 0.2000 Itemset: {'broccoli', 'eggs'}, Support: 0.2000 Itemset: {'broccoli', 'dish_soap'}, Support: 0.2000 Itemset: {'broccoli', 'milk'}, Support: 0.2000 Itemset: {'shampoo', 'onions'}, Support: 0.2000 Itemset: {'cleaning_wipes', 'milk'}, Support: 0.2000 Brute Force Association Rules: Rule: {'toothpaste'} -> {'apples'}, Confidence: 0.6667 Rule: {'shampoo'} -> {'potatoes'}, Confidence: 0.6667 Rule: {'potatoes'} -> {'shampoo'}, Confidence: 0.8000 Rule: {'eggs'} -> {'broccoli'}, Confidence: 0.8000 Rule: {'dish_soap'} -> {'broccoli'}, Confidence: 0.8000 Rule: {'milk'} -> {'broccoli'}, Confidence: 0.6667 Rule: {'shampoo'} -> {'onions'}, Confidence: 0.6667 Rule: {'milk'} -> {'cleaning_wipes'}, Confidence: 0.6667 - The Brute Force method generates all possible itemsets of increasing size (starting from size 1). - It filters itemsets based on support but does not use any optimizations (like Apriori) to limit the number of candidate itemsets. This results in a much higher computational cost. - The following function takes the results and prints for each database. Comparison of Algorithms In [9]: # Comparing brute force and apriori def compare_algorithms(databases, min_support, min_confidence, items): for i, transactions in enumerate(databases): print(f"\nComparison for Database {i + 1}:") # Apriori method start_time = time.time() frequent_itemsets_apriori, rules_apriori = apriori(transactions, items, min_support, min_confidence) apriori_time = time.time() - start_time print(f"Apriori Association Rules Count: {len(rules_apriori)}, Time: {apriori_time:.6f} seconds") # Brute force method start_time = time.time() frequent_itemsets_bruteforce = brute_force(transactions, min_support) rules_bruteforce = generate_association_rules(frequent_itemsets_bruteforce.keys(), transactions, min_confidence) bruteforce_time = time.time() - start_time print(f"Brute Force Association Rules Count: {len(rules_bruteforce)}, Time: {bruteforce_time:.6f} seconds") # Set minimum support and confidence for comparison $min_support = 0.2$ $min_confidence = 0.6$ # Compare the two algorithms (Apriori and Brute) on all 5 databases compare_algorithms(databases, min_support, min_confidence, items) Comparison for Database 1: Apriori Association Rules Count: 5, Time: 0.001103 seconds Brute Force Association Rules Count: 5, Time: 0.011115 seconds Comparison for Database 2: Apriori Association Rules Count: 0, Time: 0.000779 seconds Brute Force Association Rules Count: 0, Time: 0.000789 seconds Comparison for Database 3: Apriori Association Rules Count: 1, Time: 0.001988 seconds Brute Force Association Rules Count: 1, Time: 0.009172 seconds Comparison for Database 4: Apriori Association Rules Count: 0, Time: 0.000917 seconds Brute Force Association Rules Count: 0, Time: 0.000914 seconds Comparison for Database 5: Apriori Association Rules Count: 8, Time: 0.001774 seconds Brute Force Association Rules Count: 8, Time: 0.006785 seconds - This function compares the Apriori and Brute Force methods on multiple databases. - For each database, it prints the number of association rules generated and the time taken by each algorithm. - The output shows how Apriori is faster while generating the same number of association rules as the Brute Force method. Conclusion In this comparison, both the Apriori algorithm and the Brute Force method generate the same number of association rules for each database, as they are both designed to find all rules that meet the specified minimum support and confidence thresholds. However, the Apriori algorithm significantly outperforms the Brute Force method in terms of execution time due to its optimization of candidate generation.