New York City - Green Taxis Data **Analysis**

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I am analyzing the data from New York City Taxi and Limousine commission for Green Taxis. The green taxis are not allowed to pick up passengers inside of the densely populated areas of Manhattan.

I will be analyzing the September 2015 data set, available from below link:

http://www.nyc.gov/html/tlc/html/about/trip record data.shtml (http://www.nyc.gov/html/tlc/html/about/trip_record_data.shtml).

Data dictionary: http://www.nyc.gov/html/tlc/downloads/pdf/data dictionary trip records green.pdf (http://www.nyc.gov/html/tlc/downloads/pdf/data dictionary trip records green.pdf) Rate information:

http://www.nyc.gov/html/tlc/html/passenger/taxicab_rate.shtml (http://www.nyc.gov/html/tlc/html/passenger/taxicab_rate.shtml)

I will be using R for data analysis and visualization.

I will also be submitting the nyc taxi.rmd markdown file, when knit can be used to reproduce the results, includes the r-code, its output and my write-up

```
As a first step, all the necessary libraries are downloaded and loaded to memory.
 ## randomForest 4.6-12
 ## Type rfNews() to see new features/changes/bug fixes.
 ## Attaching package: 'ggplot2'
 ## The following object is masked from 'package:randomForest':
 ##
 ##
        margin
 ##
 ## Attaching package: 'data.table'
 ## The following objects are masked from 'package:reshape2':
 ##
 ##
         dcast, melt
 ##
 ## Attaching package: 'lubridate'
```

```
## The following objects are masked from 'package:data.table':
##
##
       hour, isoweek, mday, minute, month, quarter, second, wday,
##
       week, yday, year
## The following object is masked from 'package:base':
##
##
       date
## Loading required package: boot
##
## Attaching package: 'pastecs'
## The following objects are masked from 'package:data.table':
##
##
       first, last
## Loading required package: lattice
##
## Attaching package: 'lattice'
## The following object is masked from 'package:boot':
##
##
       melanoma
## Loading required package: survival
##
## Attaching package: 'survival'
## The following object is masked from 'package:caret':
##
##
       cluster
## The following object is masked from 'package:boot':
##
##
       aml
## Loading required package: splines
## Loading required package: parallel
```

```
## Loaded gbm 2.1.3

##
## Attaching package: 'tidyr'

## The following object is masked from 'package:pastecs':
##
## extract

## The following object is masked from 'package:reshape2':
##
## smiths
```

Question 1 - Loading Data

To begin the analysis, I will be loading the file in R. If the file is not available in current location, it will be downloaded from https://s3.amazonaws.com/nyc-tlc/trip+data/green_tripdata_2015-09.csv (https://s3.amazonaws.com/nyc-tlc/trip+data/green_tripdata_2015-09.csv) and loaded.

The number of rows, columns and summary statistics per feature of the green taxis trip data is displayed.

```
## [1] Loading the file..

##
##
##
## Number of rows in the file: 1494926

##
##
## Number of columns in the file: 21

##
##
##
##
## Summary of the green taxi NYC data:
```

```
##
       VendorID
                               lpep_pickup_datetime
            :1.000
##
    Min.
                     2015-09-20 02:00:32:
##
    1st Qu.:2.000
                     2015-09-05 14:57:48:
                                                 8
##
    Median :2.000
                     2015-09-10 17:43:49:
                                                 8
##
            :1.782
                     2015-09-13 00:27:28:
                                                 8
    Mean
    3rd Ou.:2.000
##
                     2015-09-13 01:06:29:
                                                 8
##
    Max.
           :2.000
                     2015-09-26 22:48:40:
                                                 8
##
                     (Other)
                                          :1494877
##
             Lpep_dropoff_datetime Store_and_fwd_flag
                                                           RateCodeID
    2015-09-28 00:00:00:
                                    N:1486192
##
                              172
                                                        Min.
                                                                : 1.000
##
    2015-09-13 00:00:00:
                              153
                                    Υ:
                                          8734
                                                         1st Ou.: 1.000
##
    2015-09-19 00:00:00:
                              141
                                                        Median : 1.000
##
    2015-09-14 00:00:00:
                              126
                                                        Mean
                                                                : 1.098
    2015-09-21 00:00:00:
                              125
##
                                                         3rd Qu.: 1.000
    2015-09-12 00:00:00:
                              119
##
                                                        Max.
                                                                :99.000
##
    (Other)
                        :1494090
    Pickup longitude Pickup latitude Dropoff longitude Dropoff latitude
##
##
    Min.
           :-83.32
                      Min.
                              : 0.00
                                       Min.
                                               :-83.43
                                                           Min.
                                                                  : 0.00
    1st Qu.:-73.96
                      1st Qu.:40.70
                                                           1st Qu.:40.70
##
                                       1st Qu.:-73.97
    Median :-73.95
                                       Median :-73.95
                      Median :40.75
                                                           Median :40.75
##
##
    Mean
            :-73.83
                      Mean
                              :40.69
                                       Mean
                                               :-73.84
                                                           Mean
                                                                  :40.69
##
    3rd Ou.:-73.92
                      3rd Ou.:40.80
                                        3rd Ou.:-73.91
                                                           3rd Ou.:40.79
##
    Max.
            : 0.00
                      Max.
                              :43.18
                                       Max.
                                                  0.00
                                                           Max.
                                                                  :42.80
##
##
    Passenger_count Trip_distance
                                         Fare_amount
                                                                Extra
                                                :-475.00
##
    Min.
            :0.000
                     Min.
                             :
                                0.000
                                        Min.
                                                            Min.
                                                                    :-1.0000
    1st Qu.:1.000
                     1st Qu.:
                                1.100
                                        1st Qu.:
                                                    6.50
                                                            1st Qu.: 0.0000
##
##
    Median :1.000
                     Median :
                                1.980
                                        Median :
                                                    9.50
                                                            Median : 0.5000
##
    Mean
            :1.371
                     Mean
                                2.968
                                        Mean
                                                   12.54
                                                            Mean
                                                                   : 0.3513
##
    3rd Qu.:1.000
                     3rd Qu.:
                                3.740
                                         3rd Qu.:
                                                   15.50
                                                            3rd Qu.: 0.5000
##
    Max.
            :9.000
                     Max.
                             :603.100
                                        Max.
                                                : 580.50
                                                            Max.
                                                                    :12.0000
##
##
       MTA_tax
                         Tip amount
                                            Tolls amount
                                                               Ehail fee
                                                               Mode:logical
##
                               :-50.000
                                                  :-15.2900
    Min.
            :-0.5000
                       Min.
                                           Min.
                                                               NA's:1494926
##
    1st Qu.: 0.5000
                       1st Qu.:
                                  0.000
                                           1st Qu.:
                                                     0.0000
    Median : 0.5000
                       Median :
                                  0.000
                                           Median :
##
                                                     0.0000
                                  1.236
##
    Mean
            : 0.4866
                       Mean
                                           Mean
                                                     0.1231
##
    3rd Qu.: 0.5000
                       3rd Qu.:
                                  2.000
                                           3rd Qu.:
                                                     0.0000
##
    Max.
           : 0.5000
                       Max.
                               :300.000
                                           Max.
                                                  : 95.7500
##
##
    improvement surcharge Total amount
                                                Payment type
                                                                  Trip type
                                                       :1.000
                                                                Min.
##
    Min.
            :-0.3000
                           Min.
                                   :-475.00
                                               Min.
                                                                        :1.000
##
    1st Qu.: 0.3000
                           1st Qu.:
                                       8.16
                                               1st Qu.:1.000
                                                                1st Qu.:1.000
    Median : 0.3000
##
                           Median :
                                      11.76
                                               Median :2.000
                                                                Median :1.000
            : 0.2921
                                      15.03
##
    Mean
                           Mean
                                               Mean
                                                       :1.541
                                                                Mean
                                                                        :1.022
    3rd Qu.: 0.3000
##
                            3rd Qu.:
                                      18.30
                                               3rd Ou.:2.000
                                                                3rd Qu.:1.000
##
    Max.
           : 0.3000
                           Max.
                                   : 581.30
                                               Max.
                                                       :5.000
                                                                Max.
                                                                        :2.000
##
                                                                NA's
                                                                        :4
```

Question 2 - Histogram & Structure

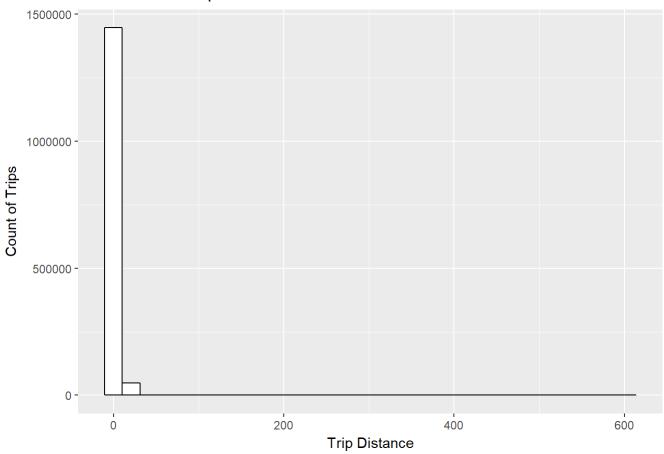
The distribution of trip distance is analyzed using a histogram.

```
## [1] 0
```

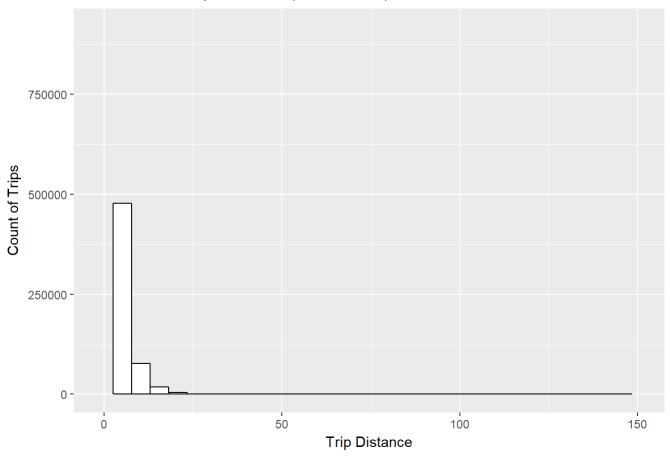
[1] 603.1

`stat_bin()` using `bins = 30`. Pick better value with `binwidth`.

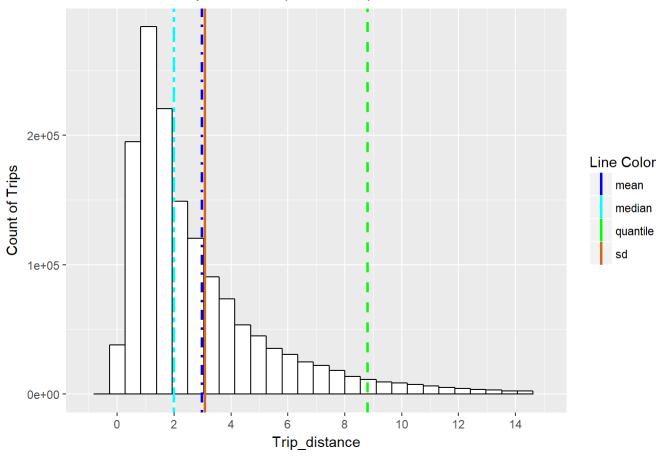
Distribution of Trip Distance



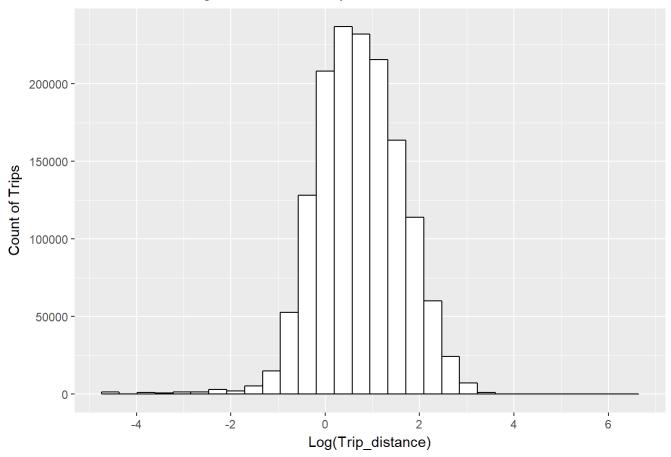
Distribution of Trip Distance (0-150 miles)



Distribution of Trip Distance (0-15 miles)



Distribution of Log Transformed Trip Distance



From the histogram of the complete trip distance, I found the most of the data clustered around 0 to 150 miles. But, due to the presence of outliers we are not able to view the complete distribution. Zooming in on trip distance, between 0 and 150 miles, I find the data to be distributed within 15 miles.

Limiting the trip distance to 15 miles and plotting the mean, median, standard deviation and quantiles, I find the distribution asymmetric and positively skewed. The structure of the distribution is lognormal (http://people.stern.nyu.edu/adamodar/New_Home_Page/StatFile/statdistns.htm (http://people.stern.nyu.edu/adamodar/New_Home_Page/StatFile/statdistns.htm) - Figure 6A.9: Lognormal distribution). It's standard deviation is 3.07 miles, which is higher than mean (2.96 miles) and the median (1.98 miles). From the 95th quantile, I found 95% of trip distance to be within 8.8 miles.

From the histogram, I found most of the data to be clustered around 0 to 4 miles. My hypothesis - most people tend to use the green taxis for short range distances as nearly 14000 passengers tend to commute within 8 miles. So, these passengers most often be rushing for work or to airports (distance between Queens and JFK, Queens and LaGuardia airport is nearly 6 miles), where the green taxis operate.

Question 3 - Mean & Median by group

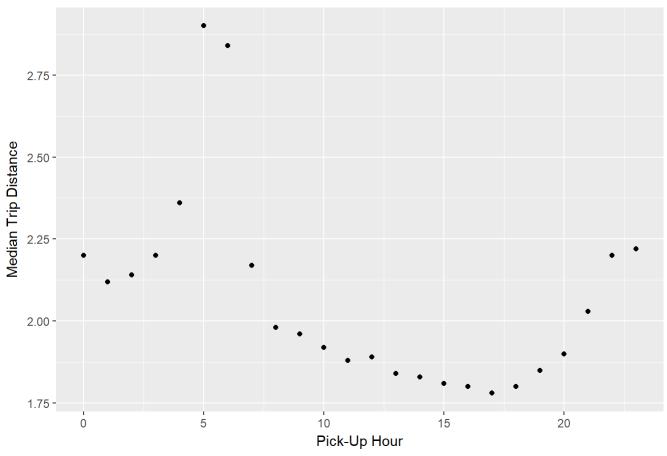
For the next part of my analysis, I will be looking at the trip distance grouped by the hour of day.

Assumptions: The pickUp_datetime feature contains the date and time a passenger boarded the taxi and will be used for for calculating the hour of day. As we are not considering the travel time, dropOff_datetime will not be considered for calculating the hour of day.

##	
##	
##	Median Trip Distance by Pick-up hour is:

pickUpHour <int></int>	Trip_distance <dbl></dbl>
0	2.20
1	2.12
2	2.14
3	2.20
4	2.36
5	2.90
6	2.84
7	2.17
8	1.98
9	1.96
1-10 of 24 rows	Previous 1 2 3 Next

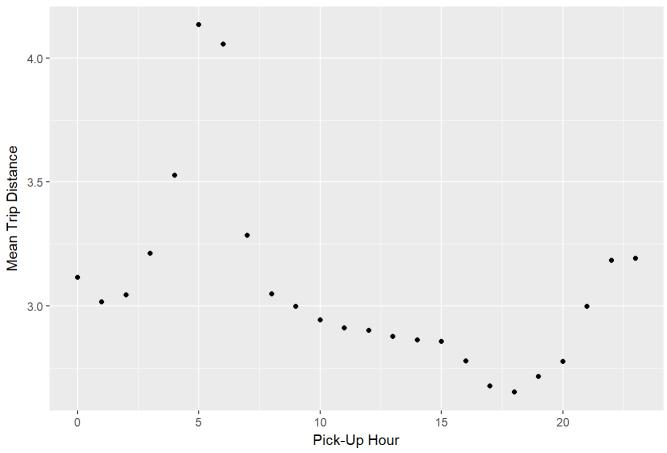
Median Trip Distance for each Pick-Up Hour



##	
##	
	Moon Thin Distance by Disk up houn is:
##	Mean Trip Distance by Pick-up hour is:

pickUpHour <int></int>	Trip_distance <dbl></dbl>
0	3.115276
1	3.017347
2	3.046176
3	3.212945
4	3.526555
5	4.133474
6	4.055149
7	3.284394
8	3.048450
9	2.999105
1-10 of 24 rows	Previous 1 2 3 Next

Mean Trip Distance for each Pick-Up Hour



Plotting the mean and median of the trip distance grouping by hour, I find that people tend to travel during the peak hours - early morning between 5:00 AM to 8:00 AM and at night after 8:00 PM.

My hypothesis Passengers tend to travel more distance at the early hour peak - say, rushing to catch flights or going to work (early shift or a presentation and don't want to be late), and at night after 8:00 PM - say, after working late hours at office. Based on the http://www.businessinsider.com/heres-why-new-york-city-air-traffic-is-so-congested-2015-7 (http://www.businessinsider.com/heres-why-new-york-city-air-traffic-is-so-congested-2015-7), travelers at NYC consider the best time to fly out at early mornings (6:00 AM) which justifies the peak at around 5:00 AM for long distance commute (distance between NYC and Newark is 20 miles).

Question 3 - Airport trip report

Now I will be looking at the characteristics of the trips originating and terminating at the airports.

Assumptions

- Newark airport is generally considered as NYC airport (all google searches yielded this) even though it is in New Jersey
- http://www.nyc.gov/html/tlc/html/passenger/taxicab_rate.shtml
 (http://www.nyc.gov/html/tlc/html/passenger/taxicab_rate.shtml) taxi cabs having a RateCodeID of '02' and '03' have pick-up or drop-off points at JFK and Newark airport respectively
- Got the co-ordinates of Newark, LaGuardia and JFK airports using google and derived a boundary (given below) that covers the area around these airports

JFK Airport:

Minimum Latitude is 40.63 Maximum Latitude is 40.65 Minimum Longitude is -73.82 Maximum Longitude is -73.75

LaGuardia Airport:

Minimum Latitude is 40.76 Maximum Latitude is 40.78 Minimum Longitude is -73.89 Maximum Longitude is -73.85

Newark Airport:

Minimum Latitude is 40.67
Maximum Latitude is 40.71
Minimum Longitude is -74.19
Maximum Longitude is -74.15

Initially, I specified the bounding co-ordinates of the airports for analysis and found the data points to be very less. Looking at the data dictionary (http://www.nyc.gov/html/tlc/downloads/pdf/data_dictionary_trip_records_green.pdf (http://www.nyc.gov/html/tlc/downloads/pdf/data_dictionary_trip_records_green.pdf)), I found the rate code id to be a good indicator for identifying trips that originated or terminated at one of the NYC area airports. Finally, I merged the data from rate code id and co-ordinates to derive the final value.

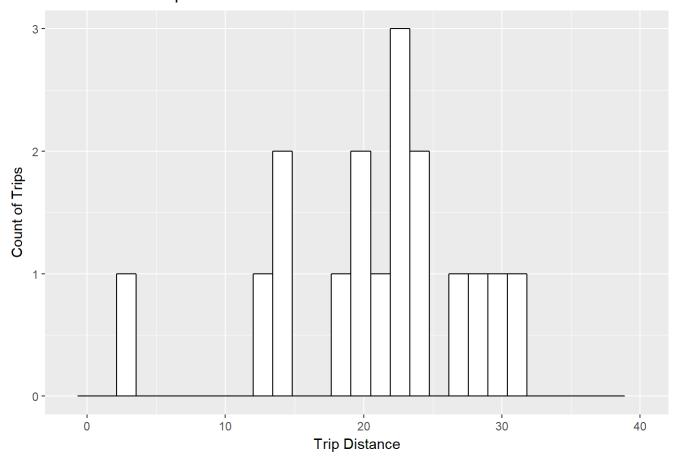
```
##
##
## Number of Transactions that originate or terminate at
##
       one of the NYC area airports (only latitude & longitude): 372
##
##
## Average fair amount that originate or terminate at
       one of the NYC area airports per trip (only latitude & longitude): $ 32.56546
##
##
##
## Number of Transactions that originate or terminate at one of the NYC area airports
       (only rate code id): 5552
##
##
##
## Average fair amount that originate or terminate at one of the NYC area airports per
       trip (only rate code id): $ 48.97695
##
##
##
## Number of Transactions that originate or terminate at
##
       one of the NYC area airports (latitude, longitude and rate code id): 5897
##
##
## Average fair amount that originate or terminate at
       one of the NYC area airports per trip (latitude, longitude and rate code id): $ 47.8928
##
```

Other important characteristics considered are:

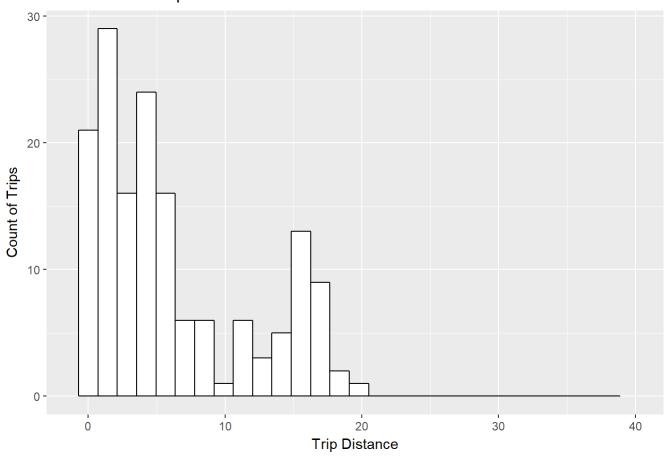
- · Distribution of Trip Duration
- · Distribution of Trip Distance
- Distribution of Trip Pick-up hour

```
## `stat_bin()` using `bins = 30`. Pick better value with `binwidth`.
```

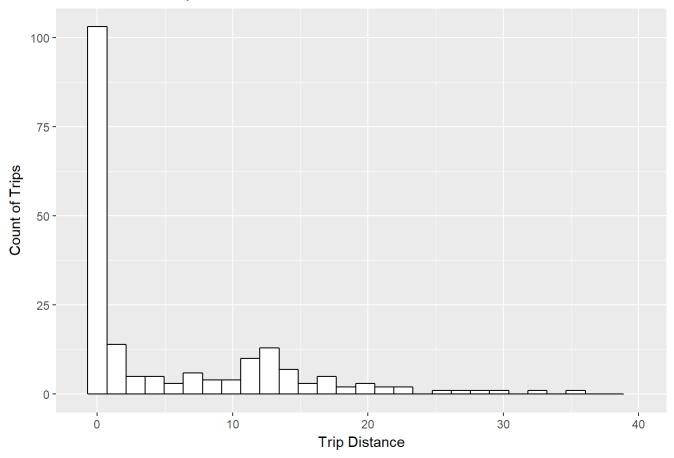
Distribution of Trip Distance - JFK



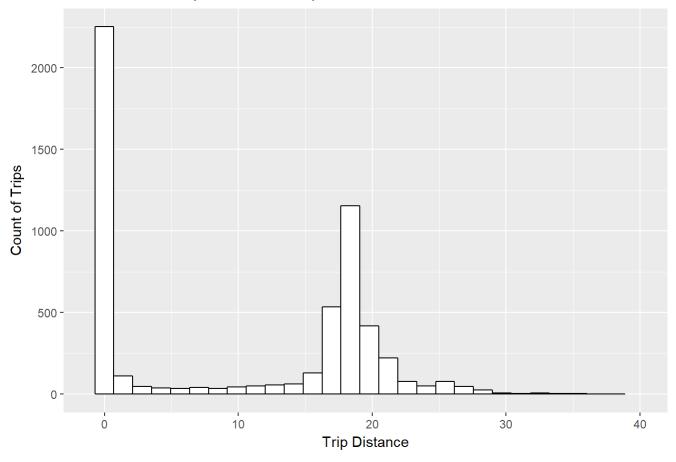
Distribution of Trip Distance - LaGuardia



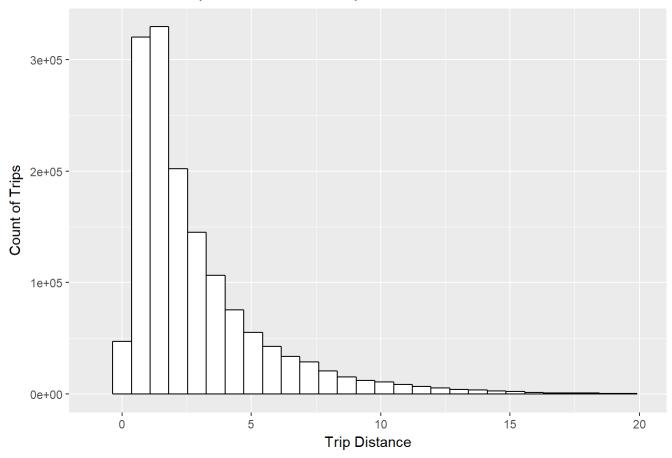
Distribution of Trip Distance - Newark



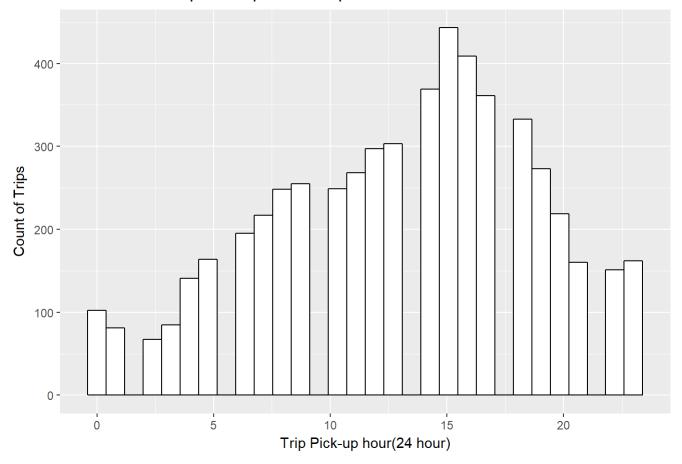
Distribution of Trip Distance - Airport Area



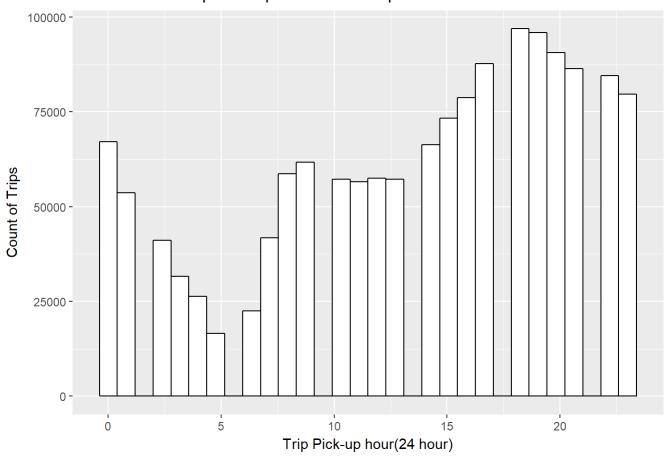
Distribution of Trip Distance - Non-Airport Area



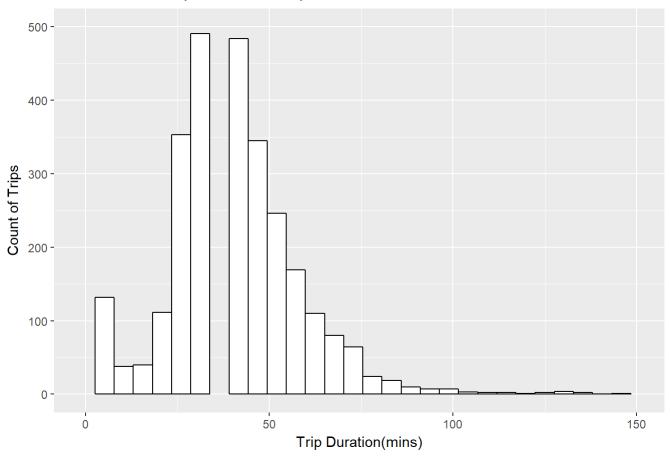
Distribution of Trip Pick-up hour - Airport Area



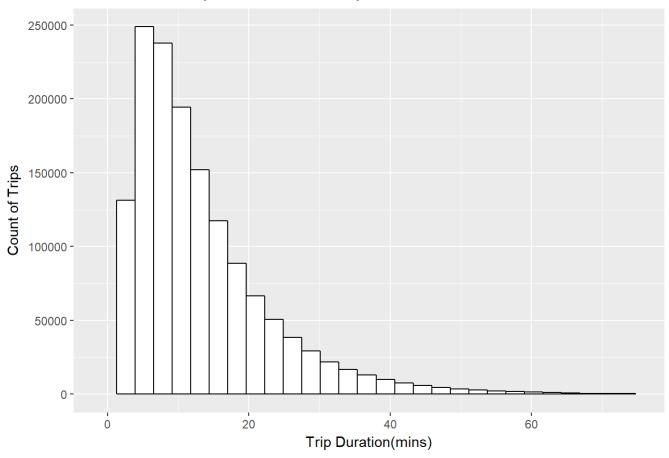
Distribution of Trip Pick-up hour - Non-Airport Area



Distribution of Trip Duration - Airport Area



Distribution of Trip Duration - Non-Airport Area



Based on the graphs above, we can see that

- Passengers tend to travel to and from LaGuardia using green taxis as they are closer to the NYC boroughs
 and have a shorter travel distance as well. Passengers using JFK and Newark have a high travel distance
 and lesser count, comparatively.
- Trips distances to and from airports tend to be around 20 miles (with a minimum of 12 miles from NYC to LaGuardia and a maximum of 20 miles from NYC to Newark), while trips not originating or terminating at airports cover shorter distances with most travels within 5 miles.
- The distribution for the pick-up hour is nearly the same for airport and non-airport pick-ups, with airport pick-up hour peaking at 03:00 PM and non-airport pick-ups peaking at around 07:00 PM. I can hypothesise that passengers commuting within city, tend to take taxis when they need late night travel and commuters to airports (based on the http://www.businessinsider.com/heres-why-new-york-city-air-traffic-is-so-congested-2015-7 (http://www.businessinsider.com/heres-why-new-york-city-air-traffic-is-so-congested-2015-7) report) like to travel from early hours to mid-day, this trend can be found in the graphs.
- The distribution of trip duration shows how travelling in the city for shorter distances takes shorter time (with most data points around 0 to 20 mins) and the airport trips last longer (with most data points around 50 mins). The longer travel distance for Airport area can be credit to the tourists, most of whom on a tight schedule would want to cover attractions or have a stop-over at friends before their destination, or a passenger opting for a round-about trip while dropping off or picking up their friends or relatives at airports.

Question 4 - Tip Percent

Now I will analyze the derived variable - tip percent, tip amount as a percentage of the total fare amount.

Summarizing the tip percentage, we find 4172 records having 'NA' as their tip percentage.

Decoding further, I found the presence of a data points having the total amount as a negative value (with 0 tip) and 0.

Looking at the NYC taxi minimum fare amount from http://nymag.com/nymetro/urban/features/taxi/n_20286/ (http://nymag.com/nymetro/urban/features/taxi/n_20286/) &

http://www.nyc.gov/html/tlc/html/passenger/taxicab rate.shtml

(http://www.nyc.gov/html/tlc/html/passenger/taxicab_rate.shtml) - I found an initial charge of \$2.00 charged for a ride (with airports having a minimum fixed cost), which had been increased to 2.50\$.

And so, I filter on the total amount that have a value either equal or more than the initial charge.

```
## Min. 1st Qu. Median Mean 3rd Qu. Max. NA's
## 0.000 0.000 0.000 6.654 16.667 100.000 4172
```

```
## The following objects are masked from greenTrip (pos = 3):
##

## Dropoff_latitude, Dropoff_longitude, Ehail_fee, Extra,
## Fare_amount, improvement_surcharge, Lpep_dropoff_datetime,
## lpep_pickup_datetime, MTA_tax, Passenger_count, Payment_type,
## Pickup_latitude, Pickup_longitude, RateCodeID,
## Store_and_fwd_flag, Tip_amount, Tolls_amount, Total_amount,
## Trip_distance, Trip_type, VendorID
```

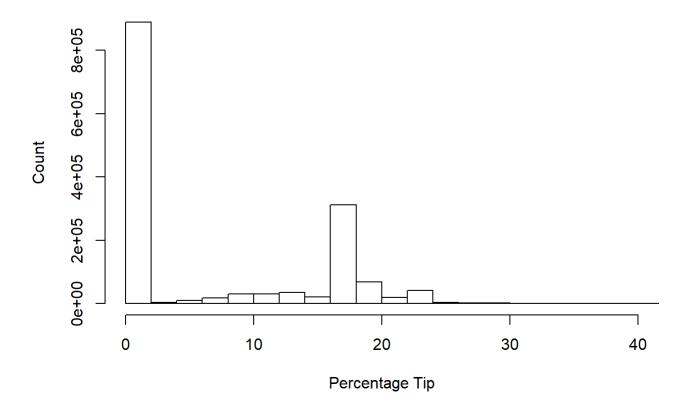
```
## Min. 1st Qu. Median Mean 3rd Qu. Max.
## 0.000 0.000 0.000 6.666 16.667 100.000
```

```
## [1] 1487889
```

```
## [1] 6.665601
```

```
## [1] 8.876661
```

Histogram of Percentage Tip



Looking at the data distribution, I find most of the passengers giving no tip and mean of tip percent at 17%, which is a good predictor of USA's tipping culture, generally people tend to tip around 20% for good service.

Question 4 - Predictive Model

Now I begin building the predictive model for tip percentage.

As the first step, I will start performing data cleansing.

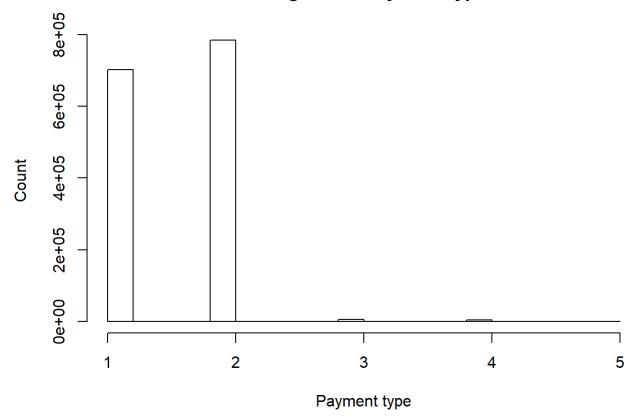
Displaying the statistical information of green taxis data -

	VendorID <dbl></dbl>	Ipep_pickup_datetime < g >	Lpep_dropoff_datetime < g >	Store_and_fv
nbr.val	1.494926e+06	NA	NA	
nbr.null	0.000000e+00	NA	NA	
nbr.na	0.000000e+00	NA	NA	
min	1.000000e+00	NA	NA	
max	2.000000e+00	NA	NA	
range	1.000000e+00	NA	NA	
sum	2.664025e+06	NA	NA	

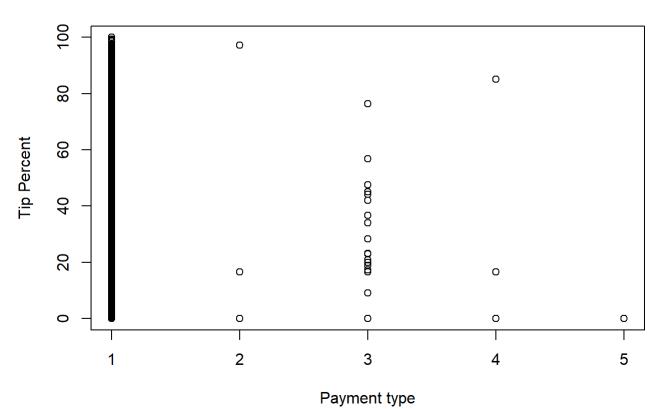
	VendorID <dbl></dbl>	Ipep_pickup_datetime < g >	Lpep_dropoff_datetime < g >	Store_and_fw
median	2.000000e+00	NA	NA	
mean	1.782045e+00	NA	NA	
SE.mean	3.376679e-04	NA	NA	
1-10 of 14 rows	s 1-5 of 23 columns		Previous	1 2 Next

As we can see from the statistical information, the data for ehail_fee is all N/A, we can drop the feature from dataset.

Histogram of Payment type



Plot of Payment type vs Tip Percent



Analyzing the dataset I found approximately 40% of the transactions having a tip. Looking at the scatter plot of payment type against the tip percentage, I found more than 90% of the tip received has been from credit card.

There are hardly any passengers tipping by cash. We will not consider payment type 3, 4 or 5 as they do not charge the customer, have a dispute or voided trip. None of these payment types (2, 3, 4 or 5) will contribute to a tip. Any tip wherein the customer is not charged for the ride can be considered as a "gesture of good will", but it not a good explanatory parameter.

And so, I have dropped the payment method field after filtering the data on credit card.

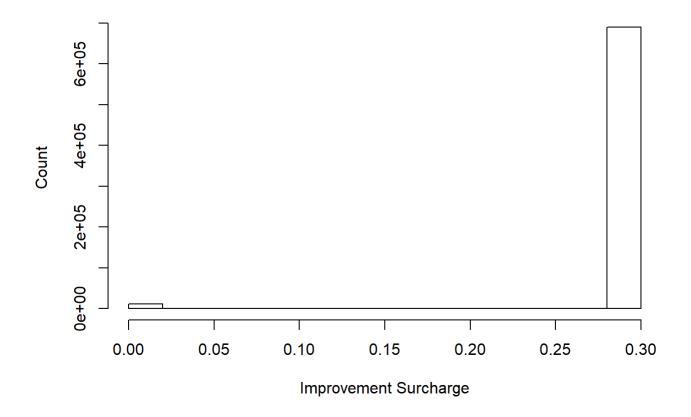
Next, I move on to cleansing the amount fields since the amounts cannot be negative. No additional information is available so as why the amount is negative, the below filters are applied:

- NYC taxi minimum fare amount from http://nymag.com/nymetro/urban/features/taxi/n_20286/
 (http://nymag.com/nymetro/urban/features/taxi/n_20286/) &
 http://www.nyc.gov/html/tlc/html/passenger/taxicab_rate.shtml
 (http://www.nyc.gov/html/tlc/html/passenger/taxicab_rate.shtml) initial charge of \$2.00 charged for a ride.
 (0.49% of data has negative amount)
- Analyzing on the Tip_amount, I found nearly 2000 records have tip amount more than the total charge (Fare_amount+Extra+MTA_tax+improvement_surcharge). These might have happened by chance (someone must have gotten lucky or it could be an outlier). These records are filtered.

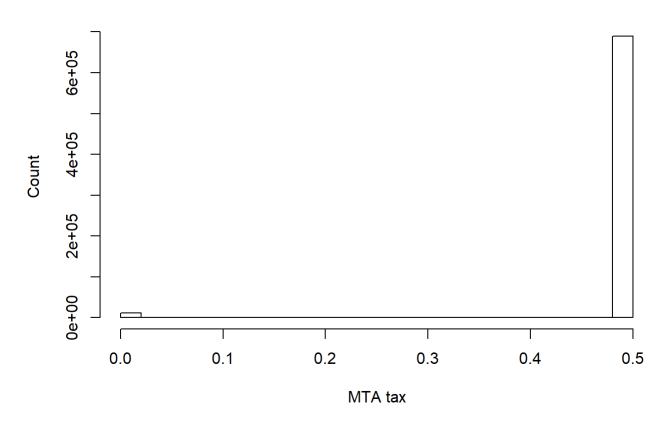
After applying the above filter, I found no negative amounts in improvement_surcharge, MTA_tax, Tolls_amount and so no filters are applied on these fields.

Percentage tip is re-calculated for the new subset of data as a derivative of fare_amount, MTA_tax and improvement surcharge (I have not used the total amount as the total amount is inclusive of tip amount).

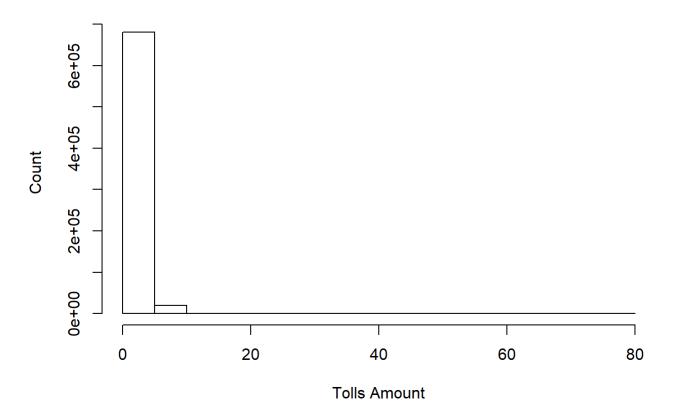
Histogram of Improvement Surcharge



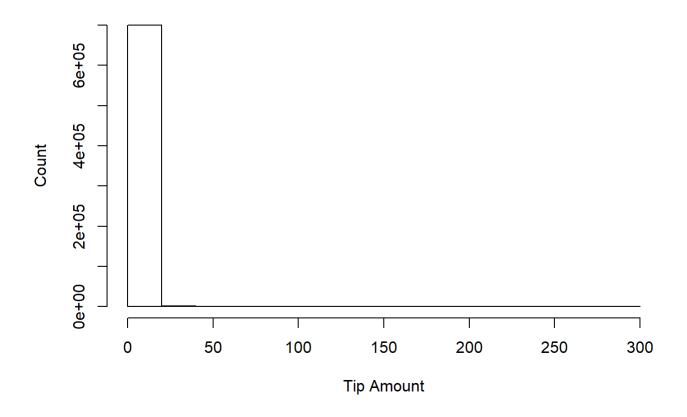
Histogram of MTA tax



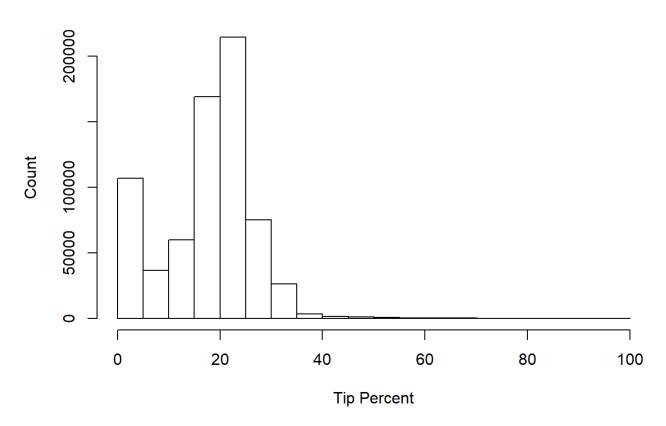
Histogram of Tolls Amount



Histogram of Tip Amount



Histogram of Tip Percent



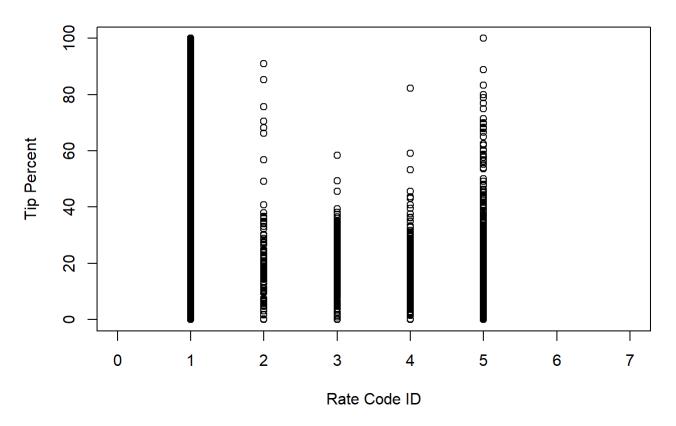
The scatter plot of tip percent against trip distance shows that, as the distance increases, which in turn increases the fare amount, the number of passengers and trip percent decrease.

Next I move on to cleansing the rate code id, passenger count and geographic co-ordinates fields,

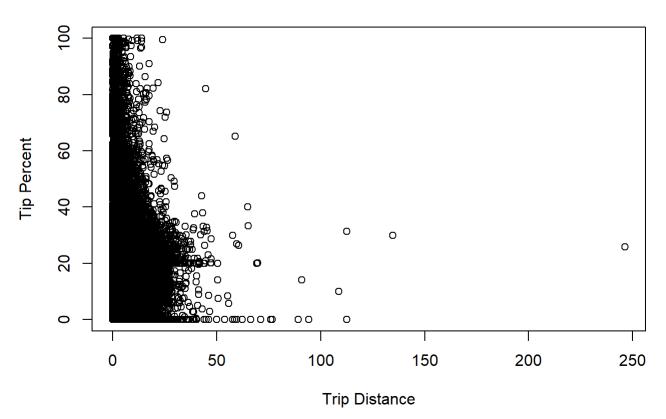
- Count of passengers with RateCodeID greater than 4 are 473 with 81 of them tipping, a tiny sample
- Count of passengers in group of 6 or more are 36 with 28 of them tipping, a tiny sample
- New York City does not encompass longitude and latitudes of 0 degree (this can be due to a faulty device or incorrect caliberation)
- Using http://www.mapdevelopers.com/geocode_bounding_box.php
 (http://www.mapdevelopers.com/geocode_bounding_box.php), the bounding co-ordinates of New York city are determined

Records matching the above conditions are filtered out.

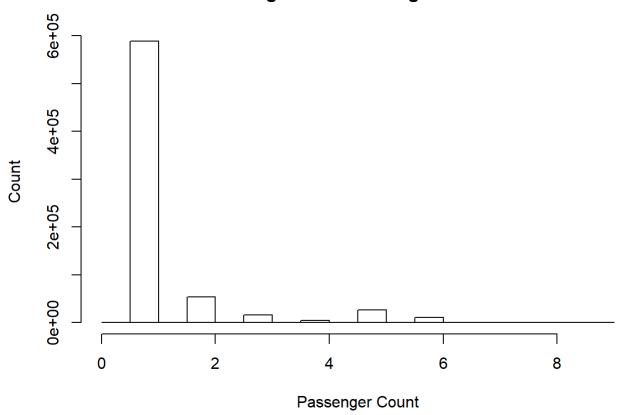
Plot of Rate Code ID vs Tip Percent



Plot of Trip Distance ID vs Tip Percent



Histogram of Passenger Count



```
##
## Number of transactions with rate code id 4 & greater than 6: 473

##
## Number of transactions with rate code id 4 & greater than 6 who tip: 392

##
## Number of transactions with more than 6 passengers: 36

##
## Number of transactions with more than 6 passengers who tip: 8
```

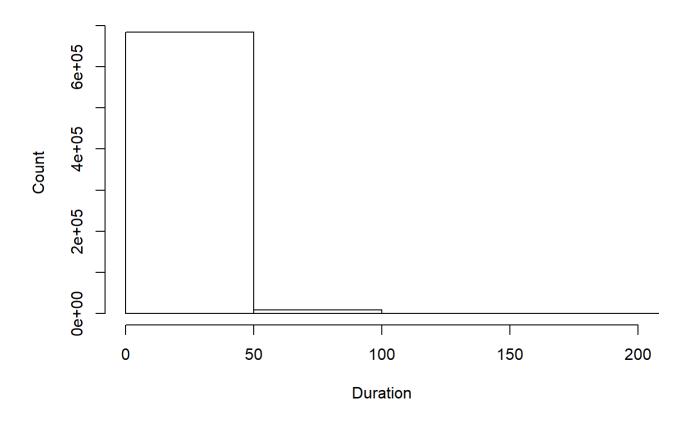
As part of feature engineering, the below fields are derived:

- trip_duration difference of drop-off and pick-up times in minutes
- dayOfWeek of the trip
- dayOfMonth of the trip
- · hour of the trip
- speed of the trip in miles per hour

The below filters are applied on derived variables:

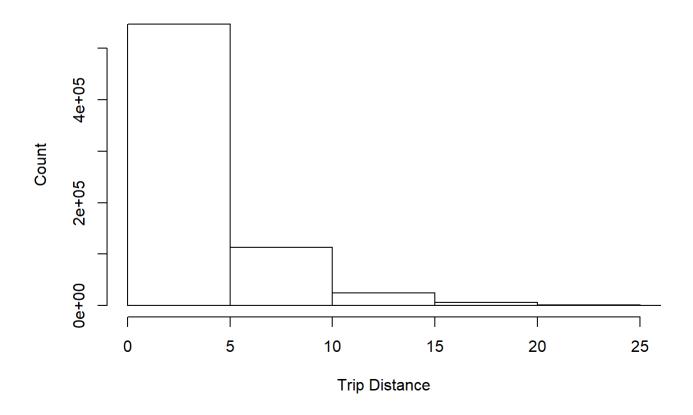
- Trips longer than 200 minutes are discarded as these may be tourist trips, out of city trips which can be considered as outliers
- The maximum speed limit in New York City is 50 mph and in United States is 137 mph. Trips with Speed more than 140 miles per hour are discarded as this can be attributed to a faulty device or incorrect calibration, and the sample size is small.

Histogram of Duration



##
Number of transactions with duration greater than 200 miles: 3556

Histogram of Trip Distance



##
Number of transactions with Speed greater than 140 miles: 692520

Building the model:

Now that data cleansing and engineering is complete, I begin to test the data for linearity.

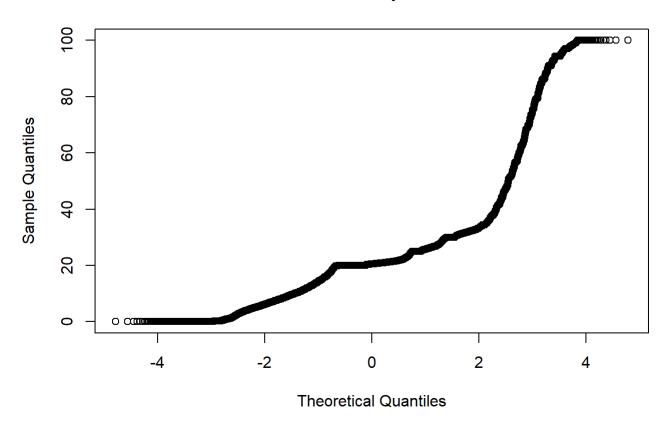
The scatter plot of tip_percent against rate code id, trip distance and payment type (displayed during data analysis), show that the independent and the dependent variables are not linearly related. Histogram of explanatory variables - payment_type, trip_distance and amount fields show the data points to be log linearly distributed.

To confirm linear regression model doesn't fit, I rum Im function on the features and determine the value of r-squared to be 0.04, which is too low for accuracy prediction.

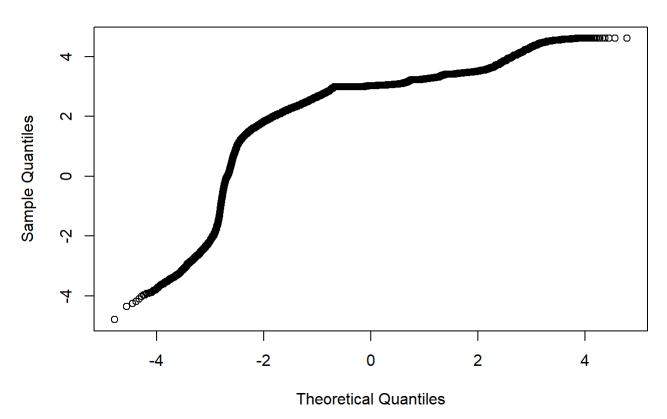
Code for making predictions (logistic and loglinear) is provided in the rmd file along with instructions to run at the top of this file.

```
##
## Call:
  lm(formula = percTip ~ VendorID + RateCodeID + Pickup longitude +
       Pickup latitude + Dropoff longitude + Dropoff latitude +
##
##
       Passenger_count + Trip_distance + Fare_amount + Extra + MTA_tax +
       Tolls amount + improvement surcharge + duration + Speed +
##
##
       day + hour + dayOfWeek + Trip_type, data = modelData)
##
## Residuals:
##
      Min
               1Q Median
                               3Q
                                      Max
##
  -85.939 -4.914
                    2.105
                            4.534 94.455
##
## Coefficients:
##
                          Estimate Std. Error t value Pr(>|t|)
                        -5.564e+02 2.707e+01 -20.558 < 2e-16 ***
## (Intercept)
## VendorID
                        -2.887e-01 2.818e-02 -10.243 < 2e-16 ***
## RateCodeID
                        -6.060e-01 1.254e-01 -4.834 1.34e-06 ***
## Pickup_longitude
                        -1.108e+01 3.879e-01 -28.568 < 2e-16 ***
                        -9.625e+00 3.442e-01 -27.963 < 2e-16 ***
## Pickup latitude
## Dropoff longitude
                        -6.810e+00 3.087e-01 -22.059 < 2e-16 ***
## Dropoff latitude
                        -8.852e+00 3.472e-01 -25.496 < 2e-16 ***
## Passenger_count
                         7.733e-02 1.109e-02
                                                6.976 3.04e-12 ***
## Trip_distance
                        -4.866e-02 1.146e-02 -4.248 2.16e-05 ***
## Fare amount
                        -1.734e-02 3.039e-03 -5.706 1.15e-08 ***
## Extra
                         1.231e+00 3.337e-02 36.898 < 2e-16 ***
## MTA tax
                                                9.355 < 2e-16 ***
                         9.496e+00 1.015e+00
## Tolls amount
                         8.326e-01 1.202e-02 69.262 < 2e-16 ***
## improvement surcharge 2.397e+00 1.514e+00
                                                1.584 0.11322
## duration
                        -6.042e-02 2.376e-03 -25.431 < 2e-16 ***
## Speed
                         8.554e-03 3.036e-03
                                                2.817 0.00485 **
## day
                         1.089e-02 1.355e-03
                                                8.038 9.18e-16 ***
                         2.056e-02 1.742e-03 11.801 < 2e-16 ***
## hour
## dayOfWeek
                        -1.278e-02 5.642e-03 -2.265
                                                      0.02348 *
                        -1.888e-01 6.338e-01 -0.298 0.76583
## Trip_type
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 9.522 on 691754 degrees of freedom
## Multiple R-squared: 0.045, Adjusted R-squared: 0.04497
## F-statistic: 1715 on 19 and 691754 DF, p-value: < 2.2e-16
```

QQ Plot for Tip Percent



QQ Plot for Log transfmored Tip Percent



The qqplot of tip percentage indicates that data is not normal. Applying a log transformation on the data, we can see that the tip percent approaches normality.

Analyzing the data, we find that most of the data points have a tip of 0. This prompted me to build a logistic regression model to predict if passengers are likely to tip and then apply loglinear models to predict the percentage of tip.

Conditional Probability is used to determine the final tip percent:

$$P(A) = P(A|B) * P(B)$$

where,

P(A|B) - tip percent given the customer tips

P(B) - customer tips

Logistic Model

- A classification model is used for predicting whether a passenger will tip.
- A factor variable "willTip" is created to know if the passenger will tip set to "1" if tip_amount is greater than zero, else 1.
- · Logistic regression model is used for training and making predictions.
- A random sample of 80% of the data from the input dataset is used for training and 20% for testing.
- We use stepAIC function to derive the final list of features that can be used for improving the accuracy of the model. Before applying the stepAIC, AIC value was 421009 and after applying the function stepAIC reduced to 421000.
 - stepAIC Performs stepwise model selection by AIC. The model specified is re-run each time with a feature eliminated to determine, which model gives a good prediction for tip percentage.
- Based on the output of stepAIC the best features used for prediction are VendorID, RateCodeID,
 Pickup_longitude, Pickup_latitude, Dropoff_longitude, Dropoff_latitude, Passenger_count, Trip_distance,
 Extra, MTA_tax Tolls_amount, duration, Speed, day, hour, dayOfWeek, and Trip_type.
- The features specified by stepAIC make sense -
 - one vendor may provide better service,
 - passengers from certain area may be more leaned towards tipping,
 - passengers travelling at rush hour may tend to tip when they reach destination on time,
 - if the driver drives rashly passengers do not tend to tip.
- Using the testing data set, we make predictions if the customer will tip.

```
##
## Call:
  glm(formula = willTip ~ VendorID + RateCodeID + Pickup longitude +
##
       Pickup latitude + Dropoff longitude + Dropoff latitude +
##
       Passenger_count + Trip_distance + Fare_amount + Extra + MTA_tax +
       Tolls amount + improvement surcharge + duration + Speed +
##
##
       day + hour + dayOfWeek + Trip_type, family = binomial(link = "logit"),
##
       data = train)
##
## Deviance Residuals:
##
      Min
                 1Q
                     Median
                                  3Q
                                          Max
##
  -3.8887
            0.3937
                     0.4721
                              0.5725
                                       2.2060
##
## Coefficients:
##
                          Estimate Std. Error z value Pr(>|z|)
## (Intercept)
                        -4.322e+02 8.156e+00 -52.989 < 2e-16 ***
## VendorID
                        -3.285e-01 1.075e-02 -30.568 < 2e-16 ***
## RateCodeID
                        -1.554e-01 3.497e-02 -4.444 8.85e-06 ***
                        -2.948e+00 1.341e-01 -21.989 < 2e-16 ***
## Pickup longitude
## Pickup latitude
                        -1.670e+00 1.288e-01 -12.968 < 2e-16 ***
## Dropoff_longitude
                        -5.326e+00 1.108e-01 -48.053 < 2e-16 ***
## Dropoff latitude
                        -2.730e+00 1.286e-01 -21.226 < 2e-16 ***
                                               6.364 1.97e-10 ***
## Passenger_count
                         2.513e-02 3.949e-03
## Trip_distance
                         3.741e-02 3.580e-03 10.450 < 2e-16 ***
## Fare_amount
                         1.278e-04 7.651e-04
                                               0.167
                                                        0.8673
                         -5.033e-02 1.158e-02 -4.345 1.39e-05 ***
## Extra
## MTA tax
                                               8.014 1.11e-15 ***
                         2.746e+00 3.427e-01
## Tolls amount
                         5.848e-02 4.965e-03 11.778 < 2e-16 ***
## improvement surcharge 5.000e-01 4.909e-01
                                                1.018
                                                        0.3085
                         -3.277e-03 7.495e-04 -4.373 1.23e-05 ***
## duration
## Speed
                         1.229e-02 9.194e-04 13.370 < 2e-16 ***
                                                9.800 < 2e-16 ***
## day
                         4.632e-03 4.726e-04
## hour
                         8.311e-03 6.103e-04 13.619 < 2e-16 ***
## dayOfWeek
                        -3.851e-03 1.995e-03 -1.931
                                                        0.0535 .
## Trip type
                         3.471e-01 2.015e-01
                                                1.723
                                                        0.0849 .
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## (Dispersion parameter for binomial family taken to be 1)
##
##
       Null deviance: 444559 on 553418 degrees of freedom
## Residual deviance: 420384 on 553399 degrees of freedom
## AIC: 420424
##
## Number of Fisher Scoring iterations: 5
```

```
## Start: AIC=420423.8
## willTip ~ VendorID + RateCodeID + Pickup longitude + Pickup latitude +
##
       Dropoff_longitude + Dropoff_latitude + Passenger_count +
       Trip distance + Fare amount + Extra + MTA tax + Tolls amount +
##
##
       improvement surcharge + duration + Speed + day + hour + dayOfWeek +
##
       Trip type
##
##
                          Df Deviance
                                        AIC
## - Fare_amount
                           1 420384 420422
## - improvement_surcharge 1 420385 420423
## <none>
                              420384 420424
## - Trip_type
                           1 420387 420425
## - dayOfWeek
                           1 420388 420426
## - duration
                           1 420403 420441
## - Extra
                           1 420403 420441
## - RateCodeID
## - Passenger_count
                           1 420403 420441
                           1 420425 420463
## - MTA tax
                           1 420443 420481
## - day
                           1 420480 420518
## - Trip_distance
                           1 420491 420529
## - Tolls_amount
                           1 420533 420571
## - Pickup_latitude
                           1 420552 420590
## - Speed
                           1 420568 420606
## - hour
                           1 420568 420606
## - Dropoff_latitude
## - Pickup_longitude
                           1 420829 420867
                           1 420859 420897
## - VendorID
                           1 421367 421405
## - Dropoff longitude
                           1 422687 422725
##
## Step: AIC=420421.8
## willTip ~ VendorID + RateCodeID + Pickup_longitude + Pickup_latitude +
##
      Dropoff_longitude + Dropoff_latitude + Passenger_count +
       Trip_distance + Extra + MTA_tax + Tolls_amount + improvement_surcharge +
##
##
       duration + Speed + day + hour + dayOfWeek + Trip_type
##
##
                          Df Deviance
                                        AIC
## - improvement surcharge 1 420385 420421
## <none>
                               420384 420422
## - Trip type
                           1 420387 420423
## - dayOfWeek
                           1 420388 420424
## + Fare_amount
                           1 420384 420424
## - Extra
                           1 420403 420439
## - RateCodeID
                           1 420403 420439
## - duration
                           1 420404 420440
## - Passenger_count
                           1 420425 420461
## - MTA tax
                           1 420443 420479
## - day
                           1 420480 420516
## - Trip distance
                           1 420520 420556
## - Tolls_amount
                           1 420533 420569
## - Pickup_latitude
                           1 420553 420589
## - hour
                           1 420568 420604
## - Speed
                           1 420568 420604
## - Dropoff_latitude
                           1
                               420829 420865
```

```
## - Pickup longitude
                           1 420859 420895
                            1 421367 421403
## - VendorID
## - Dropoff longitude
                           1 422688 422724
##
## Step: AIC=420420.8
  willTip ~ VendorID + RateCodeID + Pickup_longitude + Pickup_latitude +
##
       Dropoff longitude + Dropoff latitude + Passenger count +
##
##
       Trip_distance + Extra + MTA_tax + Tolls_amount + duration +
##
       Speed + day + hour + dayOfWeek + Trip_type
##
##
                          Df Deviance
                                         AIC
## - Trip type
                               420387 420421
## <none>
                               420385 420421
## + improvement surcharge 1
                               420384 420422
## - dayOfWeek
                           1
                               420389 420423
## + Fare amount
                           1 420385 420423
                           1 420404 420438
## - Extra
## - duration
                           1
                              420404 420438
## - RateCodeID
                           1 420405 420439
## - Passenger_count
                           1 420426 420460
                               420444 420478
## - MTA tax
                            1
## - day
                            1
                               420481 420515
## - Trip_distance
                            1
                               420521 420555
## - Tolls_amount
                           1 420534 420568
## - Pickup_latitude
                           1
                               420554 420588
## - hour
                            1 420569 420603
## - Speed
                            1
                               420569 420603
## - Dropoff_latitude
                            1 420831 420865
## - Pickup longitude
                           1 420860 420894
## - VendorID
                            1 421367 421401
## - Dropoff_longitude
                            1
                               422688 422722
##
## Step: AIC=420420.8
  willTip ~ VendorID + RateCodeID + Pickup_longitude + Pickup_latitude +
##
##
       Dropoff_longitude + Dropoff_latitude + Passenger_count +
       Trip_distance + Extra + MTA_tax + Tolls_amount + duration +
##
       Speed + day + hour + dayOfWeek
##
##
##
                          Df Deviance
                                         AIC
## <none>
                               420387 420421
## + Trip_type
                            1
                               420385 420421
## - dayOfWeek
                           1
                               420390 420422
## + improvement_surcharge 1
                               420387 420423
                               420387 420423
## + Fare_amount
                            1
## - RateCodeID
                            1
                               420405 420437
## - Extra
                            1
                               420406 420438
                            1
## - duration
                               420406 420438
## - Passenger_count
                            1
                               420428 420460
## - MTA tax
                           1
                               420467 420499
## - day
                            1
                               420483 420515
## - Trip distance
                           1 420521 420553
## - Tolls_amount
                           1 420534 420566
## - Pickup latitude
                           1 420556 420588
## - hour
                            1
                               420571 420603
```

```
## - Speed 1 420572 420604

## - Dropoff_latitude 1 420832 420864

## - Pickup_longitude 1 420864 420896

## - VendorID 1 421368 421400

## - Dropoff_longitude 1 422688 422720
```

```
##
## Call: glm(formula = willTip ~ VendorID + RateCodeID + Pickup longitude +
##
       Pickup_latitude + Dropoff_longitude + Dropoff_latitude +
##
       Passenger_count + Trip_distance + Extra + MTA_tax + Tolls_amount +
##
       duration + Speed + day + hour + dayOfWeek, family = binomial(link = "logit"),
##
       data = train)
##
## Coefficients:
##
         (Intercept)
                               VendorID
                                                 RateCodeID
          -4.315e+02
                              -3.279e-01
##
                                                 -1.448e-01
##
    Pickup_longitude
                        Pickup_latitude Dropoff_longitude
##
          -2.953e+00
                              -1.670e+00
                                                 -5.321e+00
##
    Dropoff_latitude
                        Passenger_count
                                              Trip_distance
##
          -2.729e+00
                               2.515e-02
                                                  3.740e-02
##
                                               Tolls_amount
               Extra
                                MTA_tax
          -5.043e-02
                               2.440e+00
                                                  5.785e-02
##
##
            duration
                                   Speed
                                                        day
##
          -3.189e-03
                               1.232e-02
                                                  4.632e-03
##
                hour
                               day0fWeek
##
           8.307e-03
                              -3.846e-03
##
## Degrees of Freedom: 553418 Total (i.e. Null); 553402 Residual
## Null Deviance:
                        444600
## Residual Deviance: 420400
                                 AIC: 420400
```

```
##
## Call:
  glm(formula = willTip ~ VendorID + RateCodeID + Pickup longitude +
##
      Pickup latitude + Dropoff longitude + Dropoff latitude +
##
      Passenger_count + Trip_distance + Extra + MTA_tax + Tolls_amount +
      duration + Speed + day + hour, family = binomial(link = "logit"),
##
##
      data = train)
##
## Deviance Residuals:
                1Q Median
##
      Min
                                 3Q
                                         Max
## -3.8780 0.3937 0.4721 0.5725
                                      2.2134
##
## Coefficients:
##
                     Estimate Std. Error z value Pr(>|z|)
## (Intercept)
                   -4.317e+02 8.144e+00 -53.003 < 2e-16 ***
## VendorID
                   -3.278e-01 1.074e-02 -30.533 < 2e-16 ***
## RateCodeID
                   -1.447e-01 3.377e-02 -4.286 1.82e-05 ***
## Pickup_longitude -2.950e+00 1.340e-01 -22.015 < 2e-16 ***
## Pickup_latitude -1.670e+00 1.287e-01 -12.979 < 2e-16 ***
## Dropoff longitude -5.325e+00 1.108e-01 -48.068 < 2e-16 ***
## Dropoff latitude -2.728e+00 1.286e-01 -21.211 < 2e-16 ***
## Passenger_count
                    2.514e-02 3.949e-03 6.367 1.93e-10 ***
## Trip_distance 3.748e-02 3.187e-03 11.760 < 2e-16 ***
## Extra
                    -5.055e-02 1.158e-02 -4.365 1.27e-05 ***
## MTA_tax
                   2.441e+00 2.700e-01 9.039 < 2e-16 ***
                    5.777e-02 4.941e-03 11.693 < 2e-16 ***
## Tolls_amount
## duration
                   -3.224e-03 7.192e-04 -4.483 7.37e-06 ***
## Speed
                   1.237e-02 9.178e-04 13.479 < 2e-16 ***
## day
                    4.706e-03 4.710e-04 9.993 < 2e-16 ***
## hour
                     8.256e-03 6.097e-04 13.540 < 2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## (Dispersion parameter for binomial family taken to be 1)
##
##
      Null deviance: 444559 on 553418 degrees of freedom
## Residual deviance: 420390 on 553403 degrees of freedom
## AIC: 420422
##
## Number of Fisher Scoring iterations: 5
```

Log Linear Model:

- A regression model is used for predicting tip percentage.
- Loglinear model with gaussian distribution used as the predictor is a continous variable.
- The training and testing data set from logistic regression is reused for making prediction the percentage of tip, if passenger will tip.
- We use stepAIC function to derive the final list of features that can be used for improving the accuracy of the model. AIC reduced from 3205026 to 3205000.
- Using the testing data set, we make predictions the percentage of tip from the passenger.

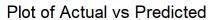
```
##
## Call:
## glm(formula = percTip ~ VendorID + RateCodeID + Pickup longitude +
##
      Pickup latitude + Dropoff longitude + Dropoff latitude +
##
      Passenger_count + Trip_distance + Fare_amount + Extra + MTA_tax +
      Tolls_amount + duration + Speed + Trip_type, family = gaussian(link = "log"),
##
##
      data = trainlm)
##
## Deviance Residuals:
##
      Min
                1Q
                    Median
                                 3Q
                                        Max
##
  -70.063
            -1.712
                    -0.095
                              2.738
                                     87.289
##
## Coefficients:
##
                     Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                   41.3103335 1.1785815 35.051 < 2e-16 ***
## VendorID
                    0.0235804 0.0012024 19.610 < 2e-16 ***
## RateCodeID
                                          1.815 0.069511 .
                    0.0109933 0.0060566
## Pickup_longitude -0.0940595 0.0174193 -5.400 6.68e-08 ***
                   ## Pickup latitude
## Dropoff longitude 0.3299460 0.0140980 23.404 < 2e-16 ***
## Dropoff latitude -0.1146157 0.0159341 -7.193 6.34e-13 ***
## Passenger_count
                    0.0012269 0.0004666 2.629 0.008552 **
## Trip_distance
                   ## Fare amount
                   -0.0019959  0.0002244  -8.895  < 2e-16 ***
## Extra
                    0.0763121 0.0013517 56.457 < 2e-16 ***
                                          3.416 0.000634 ***
## MTA tax
                    0.1581345 0.0462859
## Tolls_amount
                    0.0379755 0.0004312 88.069 < 2e-16 ***
## duration
                   -0.0043591  0.0001395  -31.241  < 2e-16 ***
                   -0.0024584   0.0001558   -15.783   < 2e-16 ***
## Speed
## Trip type
                    0.0201636 0.0222348
                                          0.907 0.364487
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## (Dispersion parameter for gaussian family taken to be 48.6655)
##
##
      Null deviance: 24543157 on 476946 degrees of freedom
## Residual deviance: 23209959 on 476931 degrees of freedom
## AIC: 3206457
##
## Number of Fisher Scoring iterations: 6
```

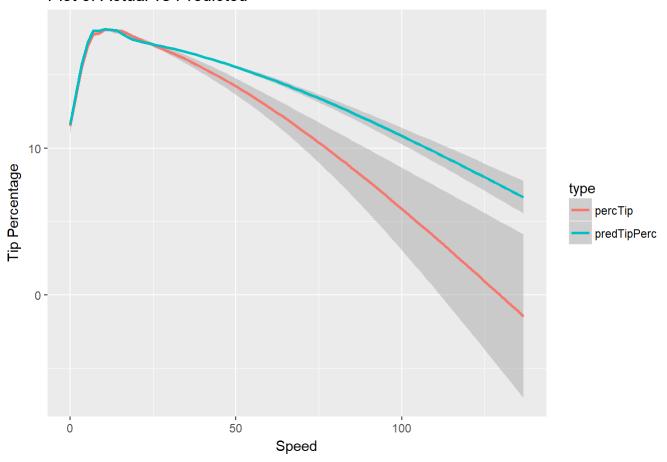
```
## Start: AIC=3206457
## percTip ~ VendorID + RateCodeID + Pickup longitude + Pickup latitude +
      Dropoff_longitude + Dropoff_latitude + Passenger_count +
##
      Trip distance + Fare amount + Extra + MTA tax + Tolls amount +
##
##
      duration + Speed + Trip_type
##
##
                    Df Deviance
                                   AIC
## - Trip type
                     1 23210000 3206456
                       23209959 3206457
## <none>
## - RateCodeID
                     1 23210124 3206459
## - Passenger_count
                     1 23210294 3206462
## - MTA tax
                     1 23210546 3206467
## - Fare_amount
                     1 23214142 3206541
## - Speed
                     1 23221489 3206692
## - VendorID
                     1 23228912 3206845
## - Dropoff longitude 1 23236062 3206991
## - Pickup_latitude
                     1 23240957 3207092
## - duration
                     1 23246038 3207196
## - Extra
                     1 23363622 3209603
## - Tolls_amount
                     1 23509024 3212562
##
## Step: AIC=3206456
## percTip ~ VendorID + RateCodeID + Pickup longitude + Pickup latitude +
      Dropoff_longitude + Dropoff_latitude + Passenger_count +
##
##
      Trip distance + Fare amount + Extra + MTA tax + Tolls amount +
##
      duration + Speed
##
##
                    Df Deviance
                                   AIC
                       23210000 3206456
## <none>
## + Trip_type
                     1 23209959 3206457
## - RateCodeID
                     1 23210318 3206461
## - Passenger_count
                     1 23210335 3206461
## - Trip_distance
                     1 23210382 3206462
## - MTA tax
                     1 23210560 3206466
## - Pickup_longitude
                     1 23211404 3206483
## - Dropoff latitude
                     1 23212474 3206505
## - Fare amount
                     1 23214249 3206541
## - Speed
                     1 23221492 3206690
## - VendorID
                     1 23228967 3206844
## - Dropoff_longitude 1 23236252 3206993
## - Pickup latitude
                     1 23241132 3207093
## - duration
                     1 23246467 3207203
## - Extra
                     1 23363634 3209601
## - Tolls amount
                     1 23514891 3212679
```

```
##
## Call: glm(formula = percTip ~ VendorID + RateCodeID + Pickup_longitude +
##
       Pickup_latitude + Dropoff_longitude + Dropoff_latitude +
       Passenger_count + Trip_distance + Fare_amount + Extra + MTA_tax +
##
##
       Tolls_amount + duration + Speed, family = gaussian(link = "log"),
##
       data = trainlm)
##
## Coefficients:
##
         (Intercept)
                               VendorID
                                                 RateCodeID
##
           41.356849
                               0.023588
                                                   0.013484
##
    Pickup_longitude
                        Pickup_latitude Dropoff_longitude
##
           -0.094285
                              -0.398935
                                                   0.330534
    Dropoff_latitude
##
                        Passenger_count
                                             Trip_distance
##
           -0.113884
                               0.001227
                                                  -0.002091
##
         Fare_amount
                                  Extra
                                                   MTA_tax
##
           -0.002014
                               0.076303
                                                   0.139820
##
        Tolls_amount
                               duration
                                                      Speed
                              -0.004342
##
            0.037914
                                                  -0.002447
##
## Degrees of Freedom: 476946 Total (i.e. Null); 476932 Residual
## Null Deviance:
                        24540000
## Residual Deviance: 23210000 AIC: 3206000
```

```
##
## Call:
## glm(formula = percTip ~ VendorID + Pickup_longitude + Pickup_latitude +
     Dropoff longitude + Dropoff latitude + Fare amount + Tolls amount +
##
##
     duration + Speed, family = gaussian(link = "log"), data = trainlm)
##
## Deviance Residuals:
##
     Min
              1Q
                  Median
                             3Q
                                   Max
          -2.195
## -68.567
                   0.007
                          2.641
                                 87.520
##
## Coefficients:
                   Estimate Std. Error t value Pr(>|t|)
##
## (Intercept)
                 45.5122267 1.1755987 38.714 < 2e-16 ***
## VendorID
                  ## Pickup_longitude -0.0866297 0.0173038 -5.006 5.55e-07 ***
## Pickup_latitude
                 ## Dropoff longitude 0.3542768 0.0138024 25.668 < 2e-16 ***
## Dropoff_latitude -0.1489131 0.0158154 -9.416 < 2e-16 ***
                 ## Fare amount
## Tolls amount
                  0.0373579  0.0004234  88.233  < 2e-16 ***
                 ## duration
## Speed
                 ## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## (Dispersion parameter for gaussian family taken to be 48.99158)
##
##
     Null deviance: 24543157 on 476946 degrees of freedom
## Residual deviance: 23365846 on 476937 degrees of freedom
## AIC: 3209638
##
## Number of Fisher Scoring iterations: 6
```

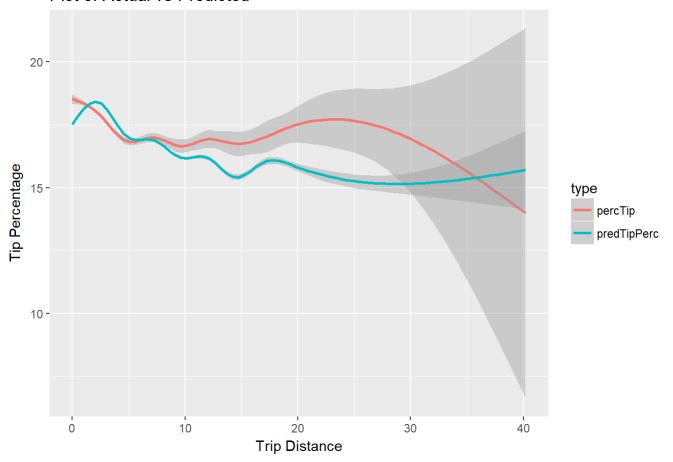
```
## `geom_smooth()` using method = 'gam'
```





`geom_smooth()` using method = 'gam'

Plot of Actual vs Predicted



- Response variable from logistic and log linear regression models in stored in test dataset.
- The tip percentage is calculated by multiplying the response value of logistic with log linear regression, using the conditional probability defined.
- We then, plot the actual vs the predicted tip percentage and can see that,
 - The model does a good job of predicting values that have low standard deviation in the actual data
 - Points where the actual data has high standard deviation, there model is predicting low values of tip.
 This is again valid, as from the scatter plot of Fare Amount against Percentage Tip, we found most of
 the passengers tend to tip a either no or a lower amount as the duration increases (which in turn
 increases the trip fare amount).

Future direction:

As part of future work, I would prefer to do predictions using random forest model with stratified cross validation to achieve a better accuracy. Below is sample execution of random forest and random forest with cross validation.

- The below testing is performed using 1% of random sample cleansed data that is not a good representation
 of the overall data set.
- Currently, the models are generating a very low r^2 (or) % variance explained. Using a bigger dataset with atleast 10 cross validations, we would be able to achieve a better predictive model.

Also, as the dependent variable is not perfectly normal, it would be a good idea to use a generalized additive model with gamma distribution.

Given more time and better processor, we can also run random forest with cross validation to generate models with higher accuracy.

```
##
## Call:
## randomForest(formula = percTip ~ VendorID + RateCodeID + Pickup_longitude +
                                                                                      Pickup lati
tude + Dropoff longitude + Dropoff latitude +
                                                   Passenger count + Trip distance + Fare amount
+ Extra + MTA tax +
                         Tolls_amount + improvement_surcharge + duration + Speed +
                                                                                         day + ho
ur + dayOfWeek, data = train, importance = TRUE,
                                                      ntree = 250)
##
                  Type of random forest: regression
##
                        Number of trees: 250
## No. of variables tried at each split: 6
##
##
             Mean of squared residuals: 88.52365
##
                       % Var explained: 7.49
```

```
## used (Mb) gc trigger (Mb) max used (Mb)
## Ncells 3723654 198.9 6861544 366.5 6861544 366.5
## Vcells 81119541 618.9 270045065 2060.3 337539465 2575.3
```

```
## Random Forest
##
## 6917 samples
     18 predictor
##
##
## No pre-processing
## Resampling: Cross-Validated (5 fold)
## Summary of sample sizes: 5534, 5533, 5532, 5535, 5534
##
  Resampling results across tuning parameters:
##
##
     mtry RMSE
                                 MAE
                     Rsquared
     2
##
           9.396208 0.07673230 6.937509
##
     10
           9.462128 0.07054979 6.995045
##
     18
           9.493197 0.06767893 7.023920
##
## RMSE was used to select the optimal model using the smallest value.
## The final value used for the model was mtry = 2.
```

```
## used (Mb) gc trigger (Mb) max used (Mb)
## Ncells 3734141 199.5 6861544 366.5 6861544 366.5
## Vcells 64300888 490.6 172828841 1318.6 337539465 2575.3
```

Question 5 - Distribution - Average Speed

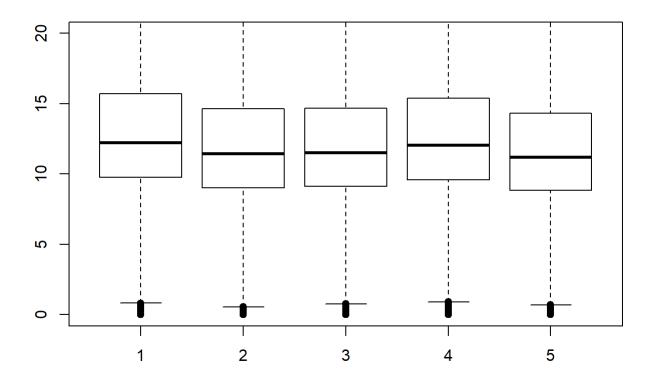
Now I derive Speed, distance (trip_distance) by time (trip_duration), a new explanatory variable for analysis.

The derived variable has nearly 4000 records as NA's or infinite. This is associated to most of the trips having 0 trip distance. Speed also has a maximum value of 2000 mph.

Using google search, I found the maximum speed limit in New York City to be 50 mph and in United States to be 137 mph. And so, data is cleansed to include records having Speed within 140 miles per hour.

speedSubset\$week <dbl></dbl>	speedSubset\$Speed <dbl></dbl>
1	13.46063
2	12.47781
3	12.54530
4	13.15193
5	12.19162
5 rows	

speedSubset\$week <dbl></dbl>	speedSubset\$Speed <dbl></dbl>
1	6.406365
2	6.112889
3	6.074027
4	6.298078
5	5.882751
5 rows	



Analyzing:

If the average trip speeds are materially the same in all weeks of September.

Test Used:

I have used ANOVA test with the null hypothesis that the average trip speeds are same in all weeks.

```
##
##
## t.test(Speed[week == 1 ], Speed[week == 2 ])
##
##
   Welch Two Sample t-test
##
##
## data: x and y
## t = 65.639, df = 693560, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to \theta
## 95 percent confidence interval:
## 0.9534768 1.0121708
## sample estimates:
## mean of x mean of y
   13.46063 12.47781
##
##
##
##
## t.test(Speed[week == 1], Speed[week == 3])
##
##
##
    Welch Two Sample t-test
##
## data: x and y
## t = 61.391, df = 693780, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to \boldsymbol{\theta}
## 95 percent confidence interval:
## 0.8861069 0.9445526
## sample estimates:
## mean of x mean of y
##
   13.46063 12.54530
##
##
##
## t.test(Speed[week == 1 ], Speed[week == 4 ])
##
##
##
   Welch Two Sample t-test
##
## data: x and y
## t = 20.013, df = 678340, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
## 0.2784646 0.3389286
## sample estimates:
## mean of x mean of y
   13.46063 13.15193
##
##
##
##
## t.test(Speed[week == 1 ], Speed[week == 5 ])
##
##
```

```
Welch Two Sample t-test
##
##
## data: x and y
## t = 56.483, df = 151460, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
  1.224977 1.313047
##
## sample estimates:
## mean of x mean of y
   13.46063 12.19162
##
##
##
##
## t.test(Speed[week == 2], Speed[week == 3])
##
##
   Welch Two Sample t-test
##
##
## data: x and y
## t = -4.7083, df = 722660, p-value = 2.498e-06
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
   -0.09559046 -0.03939765
## sample estimates:
## mean of x mean of y
##
   12.47781 12.54530
##
##
##
## t.test(Speed[week == 2], Speed[week == 4])
##
##
   Welch Two Sample t-test
##
##
## data: x and y
## t = -45.335, df = 692000, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to \theta
## 95 percent confidence interval:
   -0.7032717 -0.6449826
## sample estimates:
## mean of x mean of y
   12.47781 13.15193
##
##
##
##
## t.test(Speed[week == 2 ], Speed[week == 5 ])
##
##
##
   Welch Two Sample t-test
##
## data: x and y
## t = 12.956, df = 142620, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to \theta
## 95 percent confidence interval:
```

```
## 0.2428921 0.3294839
## sample estimates:
## mean of x mean of y
   12.47781 12.19162
##
##
##
## t.test(Speed[week == 3], Speed[week == 4])
##
##
##
   Welch Two Sample t-test
##
## data: x and y
## t = -40.972, df = 692370, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to \theta
## 95 percent confidence interval:
  -0.6356527 -0.5776136
## sample estimates:
## mean of x mean of y
   12.54530 13.15193
##
##
##
##
## t.test(Speed[week == 3 ], Speed[week == 5 ])
##
##
##
   Welch Two Sample t-test
##
## data: x and y
## t = 16.042, df = 141620, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
## 0.3104702 0.3968939
## sample estimates:
## mean of x mean of y
   12.54530 12.19162
##
##
##
## t.test(Speed[week == 4 ], Speed[week == 5 ])
##
##
##
   Welch Two Sample t-test
##
## data: x and y
## t = 42.874, df = 149770, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
## 0.9164146 1.0042157
## sample estimates:
## mean of x mean of y
## 13.15193 12.19162
```

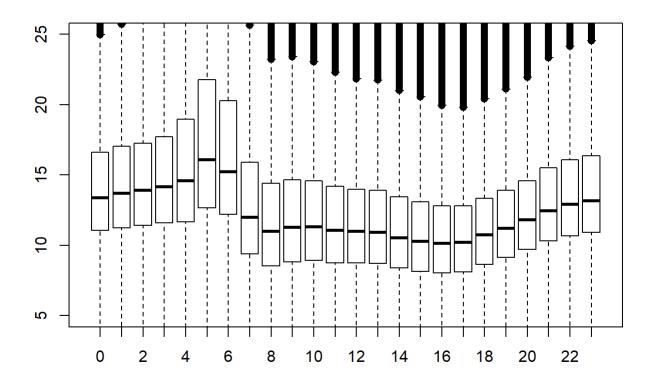
The p-value of the ANOVA test is very small and close to 0. Thus, the null hypothesis is rejected - the average trip speeds are not same in all weeks.

A 2-sample t-test, with significance value set at 0.05, is performed on all the weeks, to check if the means are same between any two weeks, but the p-vale is again close to 0 for all t-tests and no two weeks have the same means.

My hypothesis for average speed variation (based on the boxplot) is below:

- Week 1 Includes the Labor Day (September 7) long weekend. People would be entering or leaving the city
 for vacation on different dates. There would be less than normal traffic on these dates causing the average
 speed to be higher comparatively.
- Week 2 People would be returning or leaving from vacation after the long weekend, causing traffic jam on Tuesday, whereby reducing the average speed of the week
- Week 3 Most of the people would have returned to their daily routine and few people would still be returning from a long vacation, average speed of the week would be returning to normal
- Week 4 People would have returned to their daily routines and traffic would be less as daily commuters in NYC tend to take public transports and so the average speed is more compared to previous weeks. This would be a good approximate of the average speed of the week
- Week 5 Has only two days with peak Monday traffic which is why the average traffic is more.

To analyze, if the average trip speeds are same in the hours of day, I have used ANOVA test with the null hypothesis that the average trip speeds are same in all hours.



```
##
##
## t.test(Speed[hour == 0], Speed[hour == 1])
##
##
    Welch Two Sample t-test
##
##
## data: x and y
## t = -6.6388, df = 113400, p-value = 3.177e-11
## alternative hypothesis: true difference in means is not equal to \theta
## 95 percent confidence interval:
## -0.3219430 -0.1751774
## sample estimates:
## mean of x mean of y
   14.56728 14.81584
##
##
##
##
## t.test(Speed[hour == 0 ], Speed[hour == 2 ])
##
##
##
    Welch Two Sample t-test
##
## data: x and y
## t = -10.62, df = 85070, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to \boldsymbol{\theta}
## 95 percent confidence interval:
   -0.5097389 -0.3509069
## sample estimates:
## mean of x mean of y
##
   14.56728 14.99760
##
##
##
## t.test(Speed[hour == 0], Speed[hour == 3])
##
##
##
   Welch Two Sample t-test
##
## data: x and y
## t = -17.521, df = 56899, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
   -0.9034305 -0.7216389
##
## sample estimates:
## mean of x mean of y
   14.56728 15.37981
##
##
##
##
## t.test(Speed[hour == 0], Speed[hour == 4])
##
##
```

```
Welch Two Sample t-test
##
##
## data: x and y
## t = -29.786, df = 40127, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
   -1.745432 -1.529901
##
## sample estimates:
## mean of x mean of y
   14.56728 16.20494
##
##
##
##
## t.test(Speed[hour == 0 ], Speed[hour == 5 ])
##
##
   Welch Two Sample t-test
##
##
## data: x and y
## t = -46.23, df = 20959, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
   -3.552364 -3.263385
## sample estimates:
## mean of x mean of y
   14.56728 17.97515
##
##
##
##
## t.test(Speed[hour == 0], Speed[hour == 6])
##
##
   Welch Two Sample t-test
##
##
## data: x and y
## t = -41.086, df = 32760, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to \theta
## 95 percent confidence interval:
   -2.523921 -2.294077
## sample estimates:
## mean of x mean of y
   14.56728 16.97628
##
##
##
##
## t.test(Speed[hour == 0], Speed[hour == 7])
##
##
##
   Welch Two Sample t-test
##
## data: x and y
## t = 26.051, df = 82220, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to \theta
## 95 percent confidence interval:
```

```
## 1.017176 1.182686
## sample estimates:
## mean of x mean of y
   14.56728 13.46735
##
##
##
## t.test(Speed[hour == 0 ], Speed[hour == 8 ])
##
##
   Welch Two Sample t-test
##
##
## data: x and y
## t = 63.462, df = 123260, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to \theta
## 95 percent confidence interval:
## 2.224413 2.366191
## sample estimates:
## mean of x mean of y
##
   14.56728 12.27198
##
##
##
## t.test(Speed[hour == 0 ], Speed[hour == 9 ])
##
##
##
   Welch Two Sample t-test
##
## data: x and y
## t = 55.991, df = 127070, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to \theta
## 95 percent confidence interval:
## 1.953407 2.095127
## sample estimates:
## mean of x mean of y
   14.56728 12.54301
##
##
##
##
## t.test(Speed[hour == 0], Speed[hour == 10])
##
##
##
   Welch Two Sample t-test
##
## data: x and y
## t = 57.103, df = 121420, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
  1.991616 2.133194
## sample estimates:
## mean of x mean of y
##
   14.56728 12.50487
##
##
```

```
##
## t.test(Speed[hour == 0], Speed[hour == 11])
##
##
##
   Welch Two Sample t-test
##
## data: x and y
## t = 65.227, df = 120780, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to \theta
## 95 percent confidence interval:
## 2.277553 2.418669
## sample estimates:
## mean of x mean of y
   14.56728 12.21917
##
##
##
##
## t.test(Speed[hour == 0], Speed[hour == 12])
##
##
   Welch Two Sample t-test
##
##
## data: x and y
## t = 69.654, df = 123240, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to \theta
## 95 percent confidence interval:
## 2.388750 2.527076
## sample estimates:
## mean of x mean of y
   14.56728 12.10937
##
##
##
##
## t.test(Speed[hour == 0], Speed[hour == 13])
##
##
   Welch Two Sample t-test
##
##
## data: x and y
## t = 71.904, df = 122760, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
## 2.471749 2.610276
## sample estimates:
## mean of x mean of y
   14.56728 12.02627
##
##
##
##
## t.test(Speed[hour == 0], Speed[hour == 14])
##
##
##
   Welch Two Sample t-test
##
```

```
## data: x and y
## t = 91.856, df = 132110, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
## 2.974063 3.103749
## sample estimates:
## mean of x mean of y
   14.56728 11.52837
##
##
##
##
## t.test(Speed[hour == 0 ], Speed[hour == 15 ])
##
##
##
   Welch Two Sample t-test
##
## data: x and y
## t = 108.44, df = 131280, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
  3.353215 3.476661
## sample estimates:
## mean of x mean of y
   14.56728 11.15234
##
##
##
##
## t.test(Speed[hour == 0], Speed[hour == 16])
##
##
##
   Welch Two Sample t-test
##
## data: x and y
## t = 118.03, df = 129800, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to \theta
## 95 percent confidence interval:
## 3.581497 3.702450
## sample estimates:
## mean of x mean of y
##
   14.56728 10.92530
##
##
##
## t.test(Speed[hour == 0], Speed[hour == 17])
##
##
   Welch Two Sample t-test
##
##
## data: x and y
## t = 124.01, df = 121820, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to \theta
## 95 percent confidence interval:
  3.610165 3.726118
## sample estimates:
```

```
## mean of x mean of y
   14.56728 10.89914
##
##
##
##
##
  t.test(Speed[hour == 0], Speed[hour == 18])
##
##
##
   Welch Two Sample t-test
##
## data: x and y
## t = 105, df = 121450, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to \theta
## 95 percent confidence interval:
## 3.028330 3.143541
## sample estimates:
## mean of x mean of y
   14.56728 11.48134
##
##
##
##
## t.test(Speed[hour == 0], Speed[hour == 19])
##
##
##
   Welch Two Sample t-test
##
## data: x and y
## t = 84.866, df = 125600, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to \theta
## 95 percent confidence interval:
   2.472340 2.589236
## sample estimates:
## mean of x mean of y
   14.56728 12.03649
##
##
##
##
  t.test(Speed[hour == 0], Speed[hour == 20])
##
##
##
##
   Welch Two Sample t-test
##
## data: x and y
## t = 59.864, df = 131970, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to \theta
## 95 percent confidence interval:
## 1.775138 1.895310
## sample estimates:
## mean of x mean of y
##
   14.56728 12.73205
##
##
##
## t.test(Speed[hour == 0 ], Speed[hour == 21 ])
```

```
##
##
##
   Welch Two Sample t-test
##
## data: x and y
## t = 31.593, df = 136410, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to \theta
## 95 percent confidence interval:
  0.9314992 1.0547196
## sample estimates:
## mean of x mean of y
   14.56728 13.57417
##
##
##
##
## t.test(Speed[hour == 0], Speed[hour == 22])
##
##
##
   Welch Two Sample t-test
##
## data: x and y
## t = 16.231, df = 139760, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
## 0.4582726 0.5841466
## sample estimates:
## mean of x mean of y
   14.56728 14.04607
##
##
##
##
## t.test(Speed[hour == 0], Speed[hour == 23])
##
##
##
   Welch Two Sample t-test
##
## data: x and y
## t = 7.2732, df = 140440, p-value = 3.529e-13
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
## 0.1743982 0.3030648
## sample estimates:
## mean of x mean of y
   14.56728 14.32855
##
##
##
##
## t.test(Speed[hour == 1 ], Speed[hour == 2 ])
##
##
   Welch Two Sample t-test
##
##
## data: x and y
## t = -4.2419, df = 88437, p-value = 2.218e-05
```

```
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
   -0.26574660 -0.09777881
## sample estimates:
## mean of x mean of y
##
   14.81584 14.99760
##
##
##
  t.test(Speed[hour == 1], Speed[hour == 3])
##
##
##
##
   Welch Two Sample t-test
##
## data: x and y
## t = -11.646, df = 62683, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to \theta
## 95 percent confidence interval:
## -0.6588872 -0.4690618
## sample estimates:
## mean of x mean of y
##
   14.81584 15.37981
##
##
##
## t.test(Speed[hour == 1 ], Speed[hour == 4 ])
##
##
##
   Welch Two Sample t-test
##
## data: x and y
## t = -24.49, df = 44202, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to \theta
## 95 percent confidence interval:
##
   -1.500281 -1.277932
## sample estimates:
## mean of x mean of y
##
   14.81584 16.20494
##
##
##
  t.test(Speed[hour == 1 ], Speed[hour == 5 ])
##
##
##
##
   Welch Two Sample t-test
##
## data: x and y
## t = -42.112, df = 22383, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
## -3.306363 -3.012265
## sample estimates:
## mean of x mean of y
   14.81584 17.97515
##
```

```
##
##
##
## t.test(Speed[hour == 1 ], Speed[hour == 6 ])
##
##
   Welch Two Sample t-test
##
##
## data: x and y
## t = -35.848, df = 35927, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to \theta
## 95 percent confidence interval:
   -2.278563 -2.042314
## sample estimates:
## mean of x mean of y
   14.81584 16.97628
##
##
##
##
  t.test(Speed[hour == 1], Speed[hour == 7])
##
##
##
##
   Welch Two Sample t-test
##
## data: x and y
## t = 30.328, df = 86688, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to \theta
## 95 percent confidence interval:
## 1.261343 1.435639
## sample estimates:
## mean of x mean of y
##
   14.81584 13.46735
##
##
##
## t.test(Speed[hour == 1 ], Speed[hour == 8 ])
##
##
##
   Welch Two Sample t-test
##
## data: x and y
## t = 65.629, df = 111100, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
##
   2.467891 2.619833
## sample estimates:
## mean of x mean of y
   14.81584 12.27198
##
##
##
##
## t.test(Speed[hour == 1 ], Speed[hour == 9 ])
##
##
```

```
Welch Two Sample t-test
##
##
## data: x and y
## t = 58.658, df = 113390, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
## 2.196883 2.348771
## sample estimates:
## mean of x mean of y
   14.81584 12.54301
##
##
##
##
## t.test(Speed[hour == 1 ], Speed[hour == 10 ])
##
##
   Welch Two Sample t-test
##
##
## data: x and y
## t = 59.694, df = 109850, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
  2.235087 2.386843
## sample estimates:
## mean of x mean of y
   14.81584 12.50487
##
##
##
##
## t.test(Speed[hour == 1 ], Speed[hour == 11 ])
##
##
   Welch Two Sample t-test
##
##
## data: x and y
## t = 67.265, df = 109190, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to \theta
## 95 percent confidence interval:
## 2.521009 2.672334
## sample estimates:
## mean of x mean of y
   14.81584 12.21917
##
##
##
##
## t.test(Speed[hour == 1 ], Speed[hour == 12 ])
##
##
##
   Welch Two Sample t-test
##
## data: x and y
## t = 71.334, df = 108970, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to \theta
## 95 percent confidence interval:
```

```
## 2.632110 2.780837
## sample estimates:
## mean of x mean of y
   14.81584 12.10937
##
##
##
## t.test(Speed[hour == 1], Speed[hour == 13])
##
##
   Welch Two Sample t-test
##
##
## data: x and y
## t = 73.432, df = 108820, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to \theta
## 95 percent confidence interval:
## 2.715116 2.864029
## sample estimates:
## mean of x mean of y
##
   14.81584 12.02627
##
##
##
## t.test(Speed[hour == 1 ], Speed[hour == 14 ])
##
##
##
   Welch Two Sample t-test
##
## data: x and y
## t = 91.573, df = 107150, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to \theta
## 95 percent confidence interval:
## 3.217103 3.357829
## sample estimates:
## mean of x mean of y
   14.81584 11.52837
##
##
##
##
## t.test(Speed[hour == 1], Speed[hour == 15])
##
##
##
   Welch Two Sample t-test
##
## data: x and y
## t = 106.38, df = 101010, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
  3.595999 3.730998
## sample estimates:
## mean of x mean of y
##
   14.81584 11.15234
##
##
```

```
##
## t.test(Speed[hour == 1 ], Speed[hour == 16 ])
##
##
##
    Welch Two Sample t-test
##
## data: x and y
## t = 114.91, df = 97940, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to \theta
## 95 percent confidence interval:
## 3.824173 3.956895
## sample estimates:
## mean of x mean of y
   14.81584 10.92530
##
##
##
##
## t.test(Speed[hour == 1 ], Speed[hour == 17 ])
##
##
   Welch Two Sample t-test
##
##
## data: x and y
## t = 119.78, df = 89895, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to \boldsymbol{\theta}
## 95 percent confidence interval:
## 3.852611 3.980793
## sample estimates:
## mean of x mean of y
##
   14.81584 10.89914
##
##
##
## t.test(Speed[hour == 1 ], Speed[hour == 18 ])
##
##
   Welch Two Sample t-test
##
##
## data: x and y
## t = 102.51, df = 89012, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
## 3.270740 3.398251
## sample estimates:
## mean of x mean of y
    14.81584 11.48134
##
##
##
##
## t.test(Speed[hour == 1 ], Speed[hour == 19 ])
##
##
##
   Welch Two Sample t-test
##
```

```
## data: x and y
## t = 84.433, df = 92229, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
## 2.714830 2.843867
## sample estimates:
## mean of x mean of y
##
   14.81584 12.03649
##
##
##
## t.test(Speed[hour == 1], Speed[hour == 20])
##
##
##
   Welch Two Sample t-test
##
## data: x and y
## t = 61.876, df = 97980, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
  2.017778 2.149790
## sample estimates:
## mean of x mean of y
   14.81584 12.73205
##
##
##
##
## t.test(Speed[hour == 1 ], Speed[hour == 21 ])
##
##
##
   Welch Two Sample t-test
##
## data: x and y
## t = 36.11, df = 102860, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to \theta
## 95 percent confidence interval:
## 1.174273 1.309066
## sample estimates:
## mean of x mean of y
##
   14.81584 13.57417
##
##
##
## t.test(Speed[hour == 1], Speed[hour == 22])
##
##
   Welch Two Sample t-test
##
##
## data: x and y
## t = 21.99, df = 106940, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to \theta
## 95 percent confidence interval:
## 0.7011587 0.8383809
## sample estimates:
```

```
## mean of x mean of y
##
   14.81584 14.04607
##
##
##
##
  t.test(Speed[hour == 1], Speed[hour == 23])
##
##
##
   Welch Two Sample t-test
##
## data: x and y
## t = 13.665, df = 110020, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to \theta
## 95 percent confidence interval:
## 0.4173976 0.5571858
## sample estimates:
## mean of x mean of y
   14.81584 14.32855
##
##
##
##
## t.test(Speed[hour == 2 ], Speed[hour == 3 ])
##
##
##
   Welch Two Sample t-test
##
## data: x and y
## t = -7.5176, df = 65456, p-value = 5.649e-14
## alternative hypothesis: true difference in means is not equal to \theta
## 95 percent confidence interval:
   -0.4818624 -0.2825612
## sample estimates:
## mean of x mean of y
   14.99760 15.37981
##
##
##
##
  t.test(Speed[hour == 2], Speed[hour == 4])
##
##
##
##
   Welch Two Sample t-test
##
## data: x and y
## t = -20.534, df = 48093, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to \theta
## 95 percent confidence interval:
  -1.322589 -1.092098
## sample estimates:
## mean of x mean of y
##
   14.99760 16.20494
##
##
##
## t.test(Speed[hour == 2], Speed[hour == 5])
```

```
##
##
##
   Welch Two Sample t-test
##
## data: x and y
## t = -38.869, df = 24088, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to \theta
## 95 percent confidence interval:
   -3.127702 -2.827401
##
## sample estimates:
## mean of x mean of y
   14.99760 17.97515
##
##
##
##
## t.test(Speed[hour == 2], Speed[hour == 6])
##
##
##
   Welch Two Sample t-test
##
## data: x and y
## t = -31.798, df = 39295, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
##
   -2.100640 -1.856712
## sample estimates:
## mean of x mean of y
   14.99760 16.97628
##
##
##
##
## t.test(Speed[hour == 2 ], Speed[hour == 7 ])
##
##
##
   Welch Two Sample t-test
##
## data: x and y
## t = 32.5, df = 82683, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
##
   1.437968 1.622539
## sample estimates:
## mean of x mean of y
##
   14.99760 13.46735
##
##
##
## t.test(Speed[hour == 2 ], Speed[hour == 8 ])
##
##
   Welch Two Sample t-test
##
##
## data: x and y
## t = 65.297, df = 87557, p-value < 2.2e-16
```

```
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
   2.643811 2.807439
## sample estimates:
## mean of x mean of y
##
   14.99760 12.27198
##
##
##
  t.test(Speed[hour == 2], Speed[hour == 9])
##
##
##
##
   Welch Two Sample t-test
##
## data: x and y
## t = 58.822, df = 88571, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
## 2.372802 2.536378
## sample estimates:
## mean of x mean of y
##
   14.99760 12.54301
##
##
##
## t.test(Speed[hour == 2], Speed[hour == 10])
##
##
##
   Welch Two Sample t-test
##
## data: x and y
## t = 59.781, df = 86860, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to \theta
## 95 percent confidence interval:
##
   2.411000 2.574455
## sample estimates:
## mean of x mean of y
##
   14.99760 12.50487
##
##
##
  t.test(Speed[hour == 2], Speed[hour == 11])
##
##
##
##
   Welch Two Sample t-test
##
## data: x and y
## t = 66.796, df = 86283, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
## 2.696907 2.859961
## sample estimates:
## mean of x mean of y
   14.99760 12.21917
##
```

```
##
##
##
## t.test(Speed[hour == 2], Speed[hour == 12])
##
##
   Welch Two Sample t-test
##
##
## data: x and y
## t = 70.477, df = 84521, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to \theta
## 95 percent confidence interval:
  2.807913 2.968559
## sample estimates:
## mean of x mean of y
   14.99760 12.10937
##
##
##
##
  t.test(Speed[hour == 2], Speed[hour == 13])
##
##
##
##
   Welch Two Sample t-test
##
## data: x and y
## t = 72.427, df = 84574, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to \theta
## 95 percent confidence interval:
## 2.890926 3.051745
## sample estimates:
## mean of x mean of y
##
   14.99760 12.02627
##
##
##
## t.test(Speed[hour == 2], Speed[hour == 14])
##
##
##
   Welch Two Sample t-test
##
## data: x and y
## t = 88.729, df = 78274, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
##
   3.392594 3.545863
## sample estimates:
## mean of x mean of y
   14.99760 11.52837
##
##
##
##
## t.test(Speed[hour == 2], Speed[hour == 15])
##
##
```

```
Welch Two Sample t-test
##
##
## data: x and y
## t = 101.83, df = 71898, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
## 3.771247 3.919275
## sample estimates:
## mean of x mean of y
   14.99760 11.15234
##
##
##
##
## t.test(Speed[hour == 2], Speed[hour == 16])
##
##
   Welch Two Sample t-test
##
##
## data: x and y
## t = 109.37, df = 69198, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
   3.999319 4.145274
## sample estimates:
## mean of x mean of y
##
     14.9976
              10.9253
##
##
##
## t.test(Speed[hour == 2], Speed[hour == 17])
##
##
   Welch Two Sample t-test
##
##
## data: x and y
## t = 113.27, df = 63310, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to \theta
## 95 percent confidence interval:
## 4.027545 4.169384
## sample estimates:
## mean of x mean of y
   14.99760 10.89914
##
##
##
##
## t.test(Speed[hour == 2], Speed[hour == 18])
##
##
##
   Welch Two Sample t-test
##
## data: x and y
## t = 97.596, df = 62559, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to \theta
## 95 percent confidence interval:
```

```
## 3.445642 3.586875
## sample estimates:
## mean of x mean of y
   14.99760 11.48134
##
##
##
## t.test(Speed[hour == 2], Speed[hour == 19])
##
##
   Welch Two Sample t-test
##
##
## data: x and y
## t = 81.393, df = 64672, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to \theta
## 95 percent confidence interval:
  2.889805 3.032417
## sample estimates:
## mean of x mean of y
##
   14.99760 12.03649
##
##
##
## t.test(Speed[hour == 2], Speed[hour == 20])
##
##
##
   Welch Two Sample t-test
##
## data: x and y
## t = 61.118, df = 68699, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
## 2.192893 2.338201
## sample estimates:
## mean of x mean of y
   14.99760 12.73205
##
##
##
##
## t.test(Speed[hour == 2], Speed[hour == 21])
##
##
##
   Welch Two Sample t-test
##
## data: x and y
## t = 37.743, df = 72389, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
  1.349513 1.497352
## sample estimates:
## mean of x mean of y
##
   14.99760 13.57417
##
##
```

```
##
## t.test(Speed[hour == 2], Speed[hour == 22])
##
##
##
    Welch Two Sample t-test
##
## data: x and y
## t = 24.857, df = 75615, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to \theta
## 95 percent confidence interval:
## 0.8765035 1.0265615
## sample estimates:
## mean of x mean of y
   14.99760 14.04607
##
##
##
##
## t.test(Speed[hour == 2], Speed[hour == 23])
##
##
   Welch Two Sample t-test
##
##
## data: x and y
## t = 17.208, df = 78645, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to \boldsymbol{\theta}
## 95 percent confidence interval:
## 0.5928504 0.7452585
## sample estimates:
## mean of x mean of y
##
   14.99760 14.32855
##
##
##
## t.test(Speed[hour == 3], Speed[hour == 4])
##
##
##
   Welch Two Sample t-test
##
## data: x and y
## t = -13.102, df = 52763, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
   -0.9485680 -0.7016953
##
## sample estimates:
## mean of x mean of y
    15.37981 16.20494
##
##
##
##
## t.test(Speed[hour == 3 ], Speed[hour == 5 ])
##
##
##
   Welch Two Sample t-test
##
```

```
## data: x and y
## t = -32.5, df = 27493, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
  -2.751864 -2.438815
## sample estimates:
## mean of x mean of y
##
   15.37981 17.97515
##
##
##
## t.test(Speed[hour == 3], Speed[hour == 6])
##
##
##
   Welch Two Sample t-test
##
## data: x and y
## t = -24.12, df = 44515, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
   -1.726195 -1.466733
## sample estimates:
## mean of x mean of y
   15.37981 16.97628
##
##
##
##
## t.test(Speed[hour == 3], Speed[hour == 7])
##
##
##
   Welch Two Sample t-test
##
## data: x and y
## t = 36.63, df = 68137, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to \theta
## 95 percent confidence interval:
## 1.810134 2.014797
## sample estimates:
## mean of x mean of y
##
   15.37981 13.46735
##
##
##
## t.test(Speed[hour == 3], Speed[hour == 8])
##
##
   Welch Two Sample t-test
##
##
## data: x and y
## t = 65.5, df = 60137, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to \theta
## 95 percent confidence interval:
  3.014839 3.200835
## sample estimates:
```

```
## mean of x mean of y
##
   15.37981 12.27198
##
##
##
##
  t.test(Speed[hour == 3], Speed[hour == 9])
##
##
##
   Welch Two Sample t-test
##
## data: x and y
## t = 59.802, df = 60394, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to \theta
## 95 percent confidence interval:
## 2.743826 2.929778
## sample estimates:
## mean of x mean of y
   15.37981 12.54301
##
##
##
##
## t.test(Speed[hour == 3], Speed[hour == 10])
##
##
##
   Welch Two Sample t-test
##
## data: x and y
## t = 60.641, df = 59847, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to \theta
## 95 percent confidence interval:
   2.782017 2.967861
## sample estimates:
## mean of x mean of y
   15.37981 12.50487
##
##
##
##
  t.test(Speed[hour == 3], Speed[hour == 11])
##
##
##
##
   Welch Two Sample t-test
##
## data: x and y
## t = 66.794, df = 59472, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to \theta
## 95 percent confidence interval:
## 3.067900 3.253392
## sample estimates:
## mean of x mean of y
##
   15.37981 12.21917
##
##
##
## t.test(Speed[hour == 3], Speed[hour == 12])
```

```
##
##
##
   Welch Two Sample t-test
##
## data: x and y
## t = 69.911, df = 57714, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
   3.178758 3.362137
##
## sample estimates:
## mean of x mean of y
   15.37981 12.10937
##
##
##
##
## t.test(Speed[hour == 3], Speed[hour == 13])
##
##
##
   Welch Two Sample t-test
##
## data: x and y
## t = 71.628, df = 57819, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
##
  3.261782 3.445312
## sample estimates:
## mean of x mean of y
   15.37981 12.02627
##
##
##
##
## t.test(Speed[hour == 3], Speed[hour == 14])
##
##
##
   Welch Two Sample t-test
##
## data: x and y
## t = 85.321, df = 52251, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
##
   3.762965 3.939917
## sample estimates:
## mean of x mean of y
   15.37981 11.52837
##
##
##
##
## t.test(Speed[hour == 3], Speed[hour == 15])
##
##
   Welch Two Sample t-test
##
##
## data: x and y
## t = 96.106, df = 48066, p-value < 2.2e-16
```

```
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
   4.141256 4.313689
## sample estimates:
## mean of x mean of y
##
   15.37981 11.15234
##
##
##
  t.test(Speed[hour == 3], Speed[hour == 16])
##
##
##
##
   Welch Two Sample t-test
##
## data: x and y
## t = 102.32, df = 46419, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
## 4.369181 4.539836
## sample estimates:
## mean of x mean of y
##
   15.37981 10.92530
##
##
##
## t.test(Speed[hour == 3], Speed[hour == 17])
##
##
##
   Welch Two Sample t-test
##
## data: x and y
## t = 105.08, df = 43109, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to \theta
## 95 percent confidence interval:
##
  4.397102 4.564251
## sample estimates:
## mean of x mean of y
##
   15.37981 10.89914
##
##
##
  t.test(Speed[hour == 3], Speed[hour == 18])
##
##
##
##
   Welch Two Sample t-test
##
## data: x and y
## t = 91.71, df = 42659, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
## 3.815153 3.981788
## sample estimates:
## mean of x mean of y
   15.37981 11.48134
##
```

```
##
##
##
## t.test(Speed[hour == 3], Speed[hour == 19])
##
##
   Welch Two Sample t-test
##
##
## data: x and y
## t = 78.102, df = 43783, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to \theta
## 95 percent confidence interval:
  3.259420 3.427226
## sample estimates:
## mean of x mean of y
   15.37981 12.03649
##
##
##
##
  t.test(Speed[hour == 3], Speed[hour == 20])
##
##
##
##
   Welch Two Sample t-test
##
## data: x and y
## t = 61.017, df = 45994, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to \theta
## 95 percent confidence interval:
## 2.562707 2.732811
## sample estimates:
## mean of x mean of y
##
   15.37981 12.73205
##
##
##
## t.test(Speed[hour == 3], Speed[hour == 21])
##
##
##
   Welch Two Sample t-test
##
## data: x and y
## t = 41.088, df = 48093, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
##
   1.719509 1.891779
## sample estimates:
## mean of x mean of y
   15.37981 13.57417
##
##
##
##
## t.test(Speed[hour == 3], Speed[hour == 22])
##
##
```

```
Welch Two Sample t-test
##
##
## data: x and y
## t = 30.017, df = 49969, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
## 1.246655 1.420833
## sample estimates:
## mean of x mean of y
   15.37981 14.04607
##
##
##
##
## t.test(Speed[hour == 3 ], Speed[hour == 23 ])
##
##
   Welch Two Sample t-test
##
##
## data: x and y
## t = 23.387, df = 51901, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
## 0.9631628 1.1393697
## sample estimates:
## mean of x mean of y
##
   15.37981 14.32855
##
##
##
## t.test(Speed[hour == 4 ], Speed[hour == 5 ])
##
##
   Welch Two Sample t-test
##
##
## data: x and y
## t = -20.791, df = 32328, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to \theta
## 95 percent confidence interval:
   -1.937094 -1.603322
## sample estimates:
## mean of x mean of y
   16.20494 17.97515
##
##
##
##
## t.test(Speed[hour == 4 ], Speed[hour == 6 ])
##
##
##
   Welch Two Sample t-test
##
## data: x and y
## t = -10.642, df = 47778, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to \theta
## 95 percent confidence interval:
```

```
## -0.9133933 -0.6292715
## sample estimates:
## mean of x mean of y
   16.20494 16.97628
##
##
##
## t.test(Speed[hour == 4 ], Speed[hour == 7 ])
##
##
   Welch Two Sample t-test
##
##
## data: x and y
## t = 45.638, df = 50674, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to \theta
## 95 percent confidence interval:
  2.620026 2.855168
## sample estimates:
## mean of x mean of y
##
   16.20494 13.46735
##
##
##
## t.test(Speed[hour == 4 ], Speed[hour == 8 ])
##
##
##
   Welch Two Sample t-test
##
## data: x and y
## t = 70.371, df = 42288, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
## 3.823424 4.042513
## sample estimates:
## mean of x mean of y
   16.20494 12.27198
##
##
##
##
## t.test(Speed[hour == 4 ], Speed[hour == 9 ])
##
##
##
   Welch Two Sample t-test
##
## data: x and y
## t = 65.532, df = 42339, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
  3.552408 3.771459
## sample estimates:
## mean of x mean of y
##
   16.20494 12.54301
##
##
```

```
##
## t.test(Speed[hour == 4], Speed[hour == 10])
##
##
##
    Welch Two Sample t-test
##
## data: x and y
## t = 66.243, df = 42164, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to \theta
## 95 percent confidence interval:
## 3.590591 3.809551
## sample estimates:
## mean of x mean of y
   16.20494 12.50487
##
##
##
##
## t.test(Speed[hour == 4], Speed[hour == 11])
##
##
   Welch Two Sample t-test
##
##
## data: x and y
## t = 71.455, df = 41955, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to \boldsymbol{\theta}
## 95 percent confidence interval:
## 3.876447 4.095108
## sample estimates:
## mean of x mean of y
   16.20494 12.21917
##
##
##
##
## t.test(Speed[hour == 4], Speed[hour == 12])
##
##
   Welch Two Sample t-test
##
##
## data: x and y
## t = 74.029, df = 40832, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
## 3.987144 4.204015
## sample estimates:
## mean of x mean of y
    16.20494 12.10937
##
##
##
##
## t.test(Speed[hour == 4 ], Speed[hour == 13 ])
##
##
##
   Welch Two Sample t-test
##
```

```
## data: x and y
## t = 75.487, df = 40907, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
## 4.070179 4.287178
## sample estimates:
## mean of x mean of y
##
   16.20494 12.02627
##
##
##
## t.test(Speed[hour == 4], Speed[hour == 14])
##
##
##
   Welch Two Sample t-test
##
## data: x and y
## t = 86.693, df = 37484, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
## 4.570840 4.782305
## sample estimates:
## mean of x mean of y
   16.20494 11.52837
##
##
##
##
## t.test(Speed[hour == 4 ], Speed[hour == 15 ])
##
##
##
   Welch Two Sample t-test
##
## data: x and y
## t = 95.362, df = 35128, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to \theta
## 95 percent confidence interval:
## 4.948755 5.156453
## sample estimates:
## mean of x mean of y
##
   16.20494 11.15234
##
##
##
## t.test(Speed[hour == 4], Speed[hour == 16])
##
##
   Welch Two Sample t-test
##
##
## data: x and y
## t = 100.36, df = 34220, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
  5.176527 5.382753
## sample estimates:
```

```
## mean of x mean of y
##
   16.20494 10.92530
##
##
##
##
  t.test(Speed[hour == 4 ], Speed[hour == 17 ])
##
##
##
   Welch Two Sample t-test
##
## data: x and y
## t = 102.29, df = 32441, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to \theta
## 95 percent confidence interval:
## 5.204141 5.407475
## sample estimates:
## mean of x mean of y
   16.20494 10.89914
##
##
##
##
## t.test(Speed[hour == 4], Speed[hour == 18])
##
##
##
   Welch Two Sample t-test
##
## data: x and y
## t = 91.256, df = 32193, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to \theta
## 95 percent confidence interval:
  4.622146 4.825057
## sample estimates:
## mean of x mean of y
   16.20494 11.48134
##
##
##
##
  t.test(Speed[hour == 4], Speed[hour == 19])
##
##
##
##
   Welch Two Sample t-test
##
## data: x and y
## t = 80.151, df = 32786, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to \theta
## 95 percent confidence interval:
## 4.066518 4.270391
## sample estimates:
## mean of x mean of y
##
   16.20494 12.03649
##
##
##
## t.test(Speed[hour == 4 ], Speed[hour == 20 ])
```

```
##
##
##
   Welch Two Sample t-test
##
## data: x and y
## t = 66.162, df = 33962, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
   3.370006 3.575775
##
## sample estimates:
## mean of x mean of y
   16.20494 12.73205
##
##
##
##
## t.test(Speed[hour == 4], Speed[hour == 21])
##
##
##
   Welch Two Sample t-test
##
## data: x and y
## t = 49.685, df = 35090, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
##
   2.526994 2.734557
## sample estimates:
## mean of x mean of y
   16.20494 13.57417
##
##
##
##
## t.test(Speed[hour == 4 ], Speed[hour == 22 ])
##
##
##
   Welch Two Sample t-test
##
## data: x and y
## t = 40.464, df = 36102, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
##
   2.054301 2.263451
## sample estimates:
## mean of x mean of y
##
   16.20494 14.04607
##
##
##
## t.test(Speed[hour == 4], Speed[hour == 23])
##
##
   Welch Two Sample t-test
##
##
## data: x and y
## t = 34.887, df = 37176, p-value < 2.2e-16
```

```
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
   1.770977 1.981819
## sample estimates:
## mean of x mean of y
##
   16.20494 14.32855
##
##
##
  t.test(Speed[hour == 5], Speed[hour == 6])
##
##
##
##
   Welch Two Sample t-test
##
## data: x and y
## t = 11.41, df = 33400, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to \theta
## 95 percent confidence interval:
## 0.8272815 1.1704694
## sample estimates:
## mean of x mean of y
   17.97515 16.97628
##
##
##
##
## t.test(Speed[hour == 5], Speed[hour == 7])
##
##
##
   Welch Two Sample t-test
##
## data: x and y
## t = 58.151, df = 25136, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to \theta
## 95 percent confidence interval:
##
  4.355862 4.659748
## sample estimates:
## mean of x mean of y
##
   17.97515 13.46735
##
##
##
  t.test(Speed[hour == 5], Speed[hour == 8])
##
##
##
##
   Welch Two Sample t-test
##
## data: x and y
## t = 76.66, df = 21697, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
## 5.557355 5.848997
## sample estimates:
## mean of x mean of y
   17.97515 12.27198
##
```

```
##
##
##
## t.test(Speed[hour == 5], Speed[hour == 9])
##
##
   Welch Two Sample t-test
##
##
## data: x and y
## t = 73.024, df = 21695, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to \theta
## 95 percent confidence interval:
  5.286335 5.577948
## sample estimates:
## mean of x mean of y
   17.97515 12.54301
##
##
##
##
## t.test(Speed[hour == 5], Speed[hour == 10])
##
##
##
   Welch Two Sample t-test
##
## data: x and y
## t = 73.554, df = 21666, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to \theta
## 95 percent confidence interval:
## 5.324507 5.616051
## sample estimates:
## mean of x mean of y
##
   17.97515 12.50487
##
##
##
## t.test(Speed[hour == 5], Speed[hour == 11])
##
##
##
   Welch Two Sample t-test
##
## data: x and y
## t = 77.455, df = 21601, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
##
   5.610325 5.901646
## sample estimates:
## mean of x mean of y
   17.97515 12.21917
##
##
##
##
## t.test(Speed[hour == 5], Speed[hour == 12])
##
##
```

```
Welch Two Sample t-test
##
##
## data: x and y
## t = 79.298, df = 21226, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
   5.720797 6.010777
##
## sample estimates:
## mean of x mean of y
   17.97515 12.10937
##
##
##
##
## t.test(Speed[hour == 5], Speed[hour == 13])
##
##
   Welch Two Sample t-test
##
##
## data: x and y
## t = 80.395, df = 21252, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
  5.803849 6.093924
## sample estimates:
## mean of x mean of y
##
   17.97515 12.02627
##
##
##
## t.test(Speed[hour == 5], Speed[hour == 14])
##
##
   Welch Two Sample t-test
##
##
## data: x and y
## t = 88.378, df = 20123, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to \theta
## 95 percent confidence interval:
## 6.303801 6.589760
## sample estimates:
## mean of x mean of y
   17.97515 11.52837
##
##
##
##
## t.test(Speed[hour == 5], Speed[hour == 15])
##
##
##
   Welch Two Sample t-test
##
## data: x and y
## t = 94.449, df = 19375, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to \theta
## 95 percent confidence interval:
```

```
## 6.681220 6.964405
## sample estimates:
## mean of x mean of y
   17.97515 11.15234
##
##
##
## t.test(Speed[hour == 5], Speed[hour == 16])
##
##
   Welch Two Sample t-test
##
##
## data: x and y
## t = 97.965, df = 19088, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to \theta
## 95 percent confidence interval:
## 6.908795 7.190901
## sample estimates:
## mean of x mean of y
##
   17.97515 10.92530
##
##
##
## t.test(Speed[hour == 5 ], Speed[hour == 17 ])
##
##
##
   Welch Two Sample t-test
##
## data: x and y
## t = 99.069, df = 18533, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
## 6.936016 7.216016
## sample estimates:
## mean of x mean of y
   17.97515 10.89914
##
##
##
##
## t.test(Speed[hour == 5], Speed[hour == 18])
##
##
##
   Welch Two Sample t-test
##
## data: x and y
## t = 91.017, df = 18454, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
## 6.353963 6.633656
## sample estimates:
## mean of x mean of y
##
   17.97515 11.48134
##
##
```

```
##
## t.test(Speed[hour == 5], Speed[hour == 19])
##
##
##
   Welch Two Sample t-test
##
## data: x and y
## t = 83.029, df = 18637, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to \theta
## 95 percent confidence interval:
## 5.798466 6.078858
## sample estimates:
## mean of x mean of y
   17.97515 12.03649
##
##
##
##
## t.test(Speed[hour == 5], Speed[hour == 20])
##
##
   Welch Two Sample t-test
##
##
## data: x and y
## t = 72.945, df = 19002, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
## 5.102212 5.383985
## sample estimates:
## mean of x mean of y
##
   17.97515 12.73205
##
##
##
## t.test(Speed[hour == 5], Speed[hour == 21])
##
##
   Welch Two Sample t-test
##
##
## data: x and y
## t = 60.945, df = 19352, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
## 4.259440 4.542527
## sample estimates:
## mean of x mean of y
   17.97515 13.57417
##
##
##
##
## t.test(Speed[hour == 5], Speed[hour == 22])
##
##
##
   Welch Two Sample t-test
##
```

```
## data: x and y
## t = 54.187, df = 19667, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
## 3.786958 4.071209
## sample estimates:
## mean of x mean of y
##
   17.97515 14.04607
##
##
##
## t.test(Speed[hour == 5], Speed[hour == 23])
##
##
##
   Welch Two Sample t-test
##
## data: x and y
## t = 50.071, df = 20005, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
  3.503856 3.789355
## sample estimates:
## mean of x mean of y
   17.97515 14.32855
##
##
##
##
## t.test(Speed[hour == 6 ], Speed[hour == 7 ])
##
##
##
   Welch Two Sample t-test
##
## data: x and y
## t = 55.391, df = 41450, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to \theta
## 95 percent confidence interval:
## 3.384765 3.633093
## sample estimates:
## mean of x mean of y
##
   16.97628 13.46735
##
##
##
## t.test(Speed[hour == 6 ], Speed[hour == 8 ])
##
##
   Welch Two Sample t-test
##
##
## data: x and y
## t = 79.084, df = 34421, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
  4.587709 4.820893
## sample estimates:
```

```
## mean of x mean of y
   16.97628 12.27198
##
##
##
##
##
  t.test(Speed[hour == 6], Speed[hour == 9])
##
##
##
   Welch Two Sample t-test
##
## data: x and y
## t = 74.539, df = 34441, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to \theta
## 95 percent confidence interval:
## 4.316692 4.549840
## sample estimates:
## mean of x mean of y
   16.97628 12.54301
##
##
##
##
## t.test(Speed[hour == 6], Speed[hour == 10])
##
##
##
   Welch Two Sample t-test
##
## data: x and y
## t = 75.208, df = 34337, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to \theta
## 95 percent confidence interval:
  4.354872 4.587935
## sample estimates:
## mean of x mean of y
   16.97628 12.50487
##
##
##
##
  t.test(Speed[hour == 6], Speed[hour == 11])
##
##
##
##
   Welch Two Sample t-test
##
## data: x and y
## t = 80.11, df = 34182, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to \theta
## 95 percent confidence interval:
## 4.640719 4.873501
## sample estimates:
## mean of x mean of y
##
   16.97628 12.21917
##
##
##
## t.test(Speed[hour == 6], Speed[hour == 12])
```

```
##
##
##
   Welch Two Sample t-test
##
## data: x and y
## t = 82.555, df = 33327, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
   4.751361 4.982463
##
## sample estimates:
## mean of x mean of y
   16.97628 12.10937
##
##
##
##
## t.test(Speed[hour == 6], Speed[hour == 13])
##
##
##
   Welch Two Sample t-test
##
## data: x and y
## t = 83.921, df = 33385, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
##
  4.834400 5.065622
## sample estimates:
## mean of x mean of y
   16.97628 12.02627
##
##
##
##
## t.test(Speed[hour == 6], Speed[hour == 14])
##
##
##
   Welch Two Sample t-test
##
## data: x and y
## t = 94.482, df = 30798, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
##
   5.334887 5.560923
## sample estimates:
## mean of x mean of y
##
   16.97628 11.52837
##
##
##
## t.test(Speed[hour == 6], Speed[hour == 15])
##
##
   Welch Two Sample t-test
##
##
## data: x and y
## t = 102.6, df = 29051, p-value < 2.2e-16
```

```
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
   5.712679 5.935195
## sample estimates:
## mean of x mean of y
##
   16.97628 11.15234
##
##
##
  t.test(Speed[hour == 6 ], Speed[hour == 16 ])
##
##
##
##
   Welch Two Sample t-test
##
## data: x and y
## t = 107.26, df = 28380, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to \theta
## 95 percent confidence interval:
## 5.940401 6.161543
## sample estimates:
## mean of x mean of y
##
   16.97628 10.92530
##
##
##
## t.test(Speed[hour == 6 ], Speed[hour == 17 ])
##
##
##
   Welch Two Sample t-test
##
## data: x and y
## t = 109.06, df = 27075, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to \theta
## 95 percent confidence interval:
##
   5.967917 6.186364
## sample estimates:
## mean of x mean of y
##
   16.97628 10.89914
##
##
##
  t.test(Speed[hour == 6 ], Speed[hour == 18 ])
##
##
##
##
   Welch Two Sample t-test
##
## data: x and y
## t = 98.786, df = 26891, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
## 5.385907 5.603962
## sample estimates:
## mean of x mean of y
   16.97628 11.48134
##
```

```
##
##
##
## t.test(Speed[hour == 6], Speed[hour == 19])
##
##
    Welch Two Sample t-test
##
##
## data: x and y
## t = 88.442, df = 27324, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to \theta
## 95 percent confidence interval:
   4.830312 5.049262
## sample estimates:
## mean of x mean of y
   16.97628 12.03649
##
##
##
##
## t.test(Speed[hour == 6], Speed[hour == 20])
##
##
##
    Welch Two Sample t-test
##
## data: x and y
## t = 75.381, df = 28185, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to \boldsymbol{\theta}
## 95 percent confidence interval:
## 4.133865 4.354581
## sample estimates:
## mean of x mean of y
##
    16.97628 12.73205
##
##
##
## t.test(Speed[hour == 6], Speed[hour == 21])
##
##
##
   Welch Two Sample t-test
##
## data: x and y
## t = 59.969, df = 29012, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
##
   3.290913 3.513303
## sample estimates:
## mean of x mean of y
    16.97628 13.57417
##
##
##
##
## t.test(Speed[hour == 6], Speed[hour == 22])
##
##
```

```
Welch Two Sample t-test
##
##
## data: x and y
## t = 51.309, df = 29756, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
  2.818273 3.042144
##
## sample estimates:
## mean of x mean of y
   16.97628 14.04607
##
##
##
##
## t.test(Speed[hour == 6 ], Speed[hour == 23 ])
##
##
   Welch Two Sample t-test
##
##
## data: x and y
## t = 46.038, df = 30550, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
   2.535004 2.760457
## sample estimates:
## mean of x mean of y
##
   16.97628 14.32855
##
##
##
## t.test(Speed[hour == 7], Speed[hour == 8])
##
##
   Welch Two Sample t-test
##
##
## data: x and y
## t = 27.545, df = 85176, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to \theta
## 95 percent confidence interval:
## 1.110313 1.280430
## sample estimates:
## mean of x mean of y
   13.46735 12.27198
##
##
##
##
## t.test(Speed[hour == 7 ], Speed[hour == 9 ])
##
##
##
   Welch Two Sample t-test
##
## data: x and y
## t = 21.305, df = 85986, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to \theta
## 95 percent confidence interval:
```

```
## 0.8393022 1.0093708
## sample estimates:
## mean of x mean of y
   13.46735 12.54301
##
##
##
## t.test(Speed[hour == 7 ], Speed[hour == 10 ])
##
##
   Welch Two Sample t-test
##
##
## data: x and y
## t = 22.2, df = 84579, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to \theta
## 95 percent confidence interval:
## 0.8774985 1.0474495
## sample estimates:
## mean of x mean of y
##
   13.46735 12.50487
##
##
##
## t.test(Speed[hour == 7 ], Speed[hour == 11 ])
##
##
##
   Welch Two Sample t-test
##
## data: x and y
## t = 28.855, df = 84034, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
## 1.163398 1.332964
## sample estimates:
## mean of x mean of y
   13.46735 12.21917
##
##
##
##
## t.test(Speed[hour == 7 ], Speed[hour == 12 ])
##
##
##
   Welch Two Sample t-test
##
## data: x and y
## t = 31.828, df = 82149, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
  1.274357 1.441608
## sample estimates:
## mean of x mean of y
##
   13.46735 12.10937
##
##
```

```
##
## t.test(Speed[hour == 7], Speed[hour == 13])
##
##
##
    Welch Two Sample t-test
##
## data: x and y
## t = 33.742, df = 82225, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to \theta
## 95 percent confidence interval:
## 1.357373 1.524790
## sample estimates:
## mean of x mean of y
   13.46735 12.02627
##
##
##
##
## t.test(Speed[hour == 7], Speed[hour == 14])
##
##
    Welch Two Sample t-test
##
##
## data: x and y
## t = 47.452, df = 75704, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to \boldsymbol{\theta}
## 95 percent confidence interval:
## 1.858886 2.019065
## sample estimates:
## mean of x mean of y
##
   13.46735 11.52837
##
##
##
## t.test(Speed[hour == 7], Speed[hour == 15])
##
##
   Welch Two Sample t-test
##
##
## data: x and y
## t = 58.483, df = 69652, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
## 2.237421 2.392593
## sample estimates:
## mean of x mean of y
    13.46735 11.15234
##
##
##
##
## t.test(Speed[hour == 7], Speed[hour == 16])
##
##
##
   Welch Two Sample t-test
##
```

```
## data: x and y
## t = 65.047, df = 67138, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
## 2.465446 2.618640
## sample estimates:
## mean of x mean of y
##
   13.46735 10.92530
##
##
##
## t.test(Speed[hour == 7 ], Speed[hour == 17 ])
##
##
##
   Welch Two Sample t-test
##
## data: x and y
## t = 67.44, df = 61775, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
## 2.493572 2.642850
## sample estimates:
## mean of x mean of y
   13.46735 10.89914
##
##
##
##
## t.test(Speed[hour == 7 ], Speed[hour == 18 ])
##
##
##
   Welch Two Sample t-test
##
## data: x and y
## t = 52.354, df = 61079, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to \theta
## 95 percent confidence interval:
## 1.911653 2.060356
## sample estimates:
## mean of x mean of y
##
   13.46735 11.48134
##
##
##
## t.test(Speed[hour == 7], Speed[hour == 19])
##
##
   Welch Two Sample t-test
##
##
## data: x and y
## t = 37.39, df = 62978, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to \theta
## 95 percent confidence interval:
  1.355851 1.505864
## sample estimates:
```

```
## mean of x mean of y
   13.46735 12.03649
##
##
##
##
##
  t.test(Speed[hour == 7], Speed[hour == 20])
##
##
##
   Welch Two Sample t-test
##
## data: x and y
## t = 18.891, df = 66623, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to \theta
## 95 percent confidence interval:
## 0.6590035 0.8115832
## sample estimates:
## mean of x mean of y
   13.46735 12.73205
##
##
##
##
## t.test(Speed[hour == 7 ], Speed[hour == 21 ])
##
##
##
   Welch Two Sample t-test
##
## data: x and y
## t = -2.7017, df = 69993, p-value = 0.006901
## alternative hypothesis: true difference in means is not equal to \theta
## 95 percent confidence interval:
   -0.18431703 -0.02932543
## sample estimates:
## mean of x mean of y
   13.46735 13.57417
##
##
##
##
  t.test(Speed[hour == 7], Speed[hour == 22])
##
##
##
##
   Welch Two Sample t-test
##
## data: x and y
## t = -14.44, df = 72958, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to \theta
## 95 percent confidence interval:
  -0.6572757 -0.5001664
## sample estimates:
## mean of x mean of y
##
   13.46735 14.04607
##
##
##
## t.test(Speed[hour == 7 ], Speed[hour == 23 ])
```

```
##
##
##
   Welch Two Sample t-test
##
## data: x and y
## t = -21.185, df = 75811, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
   -0.9408768 -0.7815214
##
## sample estimates:
## mean of x mean of y
   13.46735 14.32855
##
##
##
##
## t.test(Speed[hour == 8], Speed[hour == 9])
##
##
##
   Welch Two Sample t-test
##
## data: x and y
## t = -7.2239, df = 120580, p-value = 5.081e-13
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
##
   -0.3445717 -0.1974980
## sample estimates:
## mean of x mean of y
   12.27198 12.54301
##
##
##
##
## t.test(Speed[hour == 8], Speed[hour == 10])
##
##
##
   Welch Two Sample t-test
##
## data: x and y
## t = -6.2132, df = 116110, p-value = 5.21e-10
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
##
   -0.3063662 -0.1594284
## sample estimates:
## mean of x mean of y
##
   12.27198 12.50487
##
##
##
## t.test(Speed[hour == 8], Speed[hour == 11])
##
##
   Welch Two Sample t-test
##
##
## data: x and y
## t = 1.4131, df = 115450, p-value = 0.1576
```

```
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
   -0.0204369 0.1260554
## sample estimates:
## mean of x mean of y
##
   12.27198 12.21917
##
##
##
  t.test(Speed[hour == 8], Speed[hour == 12])
##
##
##
##
   Welch Two Sample t-test
##
## data: x and y
## t = 4.4325, df = 116320, p-value = 9.321e-06
## alternative hypothesis: true difference in means is not equal to \theta
## 95 percent confidence interval:
## 0.09070756 0.23451462
## sample estimates:
## mean of x mean of y
##
   12.27198 12.10937
##
##
##
## t.test(Speed[hour == 8], Speed[hour == 13])
##
##
   Welch Two Sample t-test
##
##
## data: x and y
## t = 6.6887, df = 116040, p-value = 2.261e-11
## alternative hypothesis: true difference in means is not equal to \theta
## 95 percent confidence interval:
##
  0.1737102 0.3177103
## sample estimates:
## mean of x mean of y
##
   12.27198 12.02627
##
##
##
  t.test(Speed[hour == 8], Speed[hour == 14])
##
##
##
##
   Welch Two Sample t-test
##
## data: x and y
## t = 21.51, df = 118460, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
## 0.6758459 0.8113621
## sample estimates:
## mean of x mean of y
   12.27198 11.52837
##
```

```
##
##
##
## t.test(Speed[hour == 8 ], Speed[hour == 15 ])
##
##
   Welch Two Sample t-test
##
##
## data: x and y
## t = 33.876, df = 113840, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to \theta
## 95 percent confidence interval:
  1.054857 1.184415
## sample estimates:
## mean of x mean of y
   12.27198 11.15234
##
##
##
##
  t.test(Speed[hour == 8], Speed[hour == 16])
##
##
##
##
   Welch Two Sample t-test
##
## data: x and y
## t = 41.506, df = 111110, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to \theta
## 95 percent confidence interval:
## 1.283079 1.410264
## sample estimates:
## mean of x mean of y
##
   12.27198 10.92530
##
##
##
## t.test(Speed[hour == 8], Speed[hour == 17])
##
##
##
   Welch Two Sample t-test
##
## data: x and y
## t = 43.952, df = 102630, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
##
   1.311620 1.434059
## sample estimates:
## mean of x mean of y
   12.27198 10.89914
##
##
##
##
## t.test(Speed[hour == 8 ], Speed[hour == 18 ])
##
##
```

```
Welch Two Sample t-test
##
##
## data: x and y
## t = 25.459, df = 101840, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
## 0.7297653 0.8515018
## sample estimates:
## mean of x mean of y
   12.27198 11.48134
##
##
##
##
## t.test(Speed[hour == 8], Speed[hour == 19])
##
##
   Welch Two Sample t-test
##
##
## data: x and y
## t = 7.4845, df = 105530, p-value = 7.235e-14
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
## 0.1738191 0.2971531
## sample estimates:
## mean of x mean of y
   12.27198 12.03649
##
##
##
##
## t.test(Speed[hour == 8 ], Speed[hour == 20 ])
##
##
   Welch Two Sample t-test
##
##
## data: x and y
## t = -14.263, df = 111800, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to \theta
## 95 percent confidence interval:
   -0.5232994 -0.3968565
## sample estimates:
## mean of x mean of y
   12.27198 12.73205
##
##
##
##
## t.test(Speed[hour == 8], Speed[hour == 21])
##
##
##
   Welch Two Sample t-test
##
## data: x and y
## t = -39.465, df = 116810, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to \theta
## 95 percent confidence interval:
```

```
## -1.366864 -1.237521
## sample estimates:
## mean of x mean of y
   12.27198 13.57417
##
##
##
## t.test(Speed[hour == 8], Speed[hour == 22])
##
##
   Welch Two Sample t-test
##
##
## data: x and y
## t = -52.735, df = 120870, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to \theta
## 95 percent confidence interval:
  -1.840029 -1.708156
## sample estimates:
## mean of x mean of y
##
   12.27198 14.04607
##
##
##
## t.test(Speed[hour == 8 ], Speed[hour == 23 ])
##
##
##
   Welch Two Sample t-test
##
## data: x and y
## t = -59.92, df = 123300, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
## -2.123841 -1.989300
## sample estimates:
## mean of x mean of y
   12.27198 14.32855
##
##
##
##
## t.test(Speed[hour == 9], Speed[hour == 10])
##
##
##
   Welch Two Sample t-test
##
## data: x and y
## t = 1.0178, df = 119000, p-value = 0.3088
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
   -0.03530319 0.11157831
## sample estimates:
## mean of x mean of y
   12.54301 12.50487
##
##
##
```

```
##
## t.test(Speed[hour == 9], Speed[hour == 11])
##
##
##
   Welch Two Sample t-test
##
## data: x and y
## t = 8.669, df = 118350, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to \theta
## 95 percent confidence interval:
## 0.2506262 0.3970620
## sample estimates:
## mean of x mean of y
   12.54301 12.21917
##
##
##
##
## t.test(Speed[hour == 9], Speed[hour == 12])
##
##
   Welch Two Sample t-test
##
##
## data: x and y
## t = 11.825, df = 119510, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to \theta
## 95 percent confidence interval:
## 0.3617712 0.5055207
## sample estimates:
## mean of x mean of y
   12.54301 12.10937
##
##
##
##
## t.test(Speed[hour == 9], Speed[hour == 13])
##
##
##
   Welch Two Sample t-test
##
## data: x and y
## t = 14.072, df = 119190, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
## 0.4447738 0.5887164
## sample estimates:
## mean of x mean of y
   12.54301 12.02627
##
##
##
##
## t.test(Speed[hour == 9], Speed[hour == 14])
##
##
##
   Welch Two Sample t-test
##
```

```
## data: x and y
## t = 29.363, df = 122720, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
## 0.9469113 1.0823664
## sample estimates:
## mean of x mean of y
##
   12.54301 11.52837
##
##
##
## t.test(Speed[hour == 9], Speed[hour == 15])
##
##
##
   Welch Two Sample t-test
##
## data: x and y
## t = 42.097, df = 118590, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
## 1.325923 1.455418
## sample estimates:
## mean of x mean of y
   12.54301 11.15234
##
##
##
##
## t.test(Speed[hour == 9], Speed[hour == 16])
##
##
##
   Welch Two Sample t-test
##
## data: x and y
## t = 49.885, df = 116000, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to \theta
## 95 percent confidence interval:
## 1.554147 1.681266
## sample estimates:
## mean of x mean of y
##
   12.54301 10.92530
##
##
##
## t.test(Speed[hour == 9], Speed[hour == 17])
##
##
   Welch Two Sample t-test
##
##
## data: x and y
## t = 52.659, df = 107500, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
  1.582689 1.705060
## sample estimates:
```

```
## mean of x mean of y
   12.54301 10.89914
##
##
##
##
##
  t.test(Speed[hour == 9 ], Speed[hour == 18 ])
##
##
##
   Welch Two Sample t-test
##
## data: x and y
## t = 34.205, df = 106750, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to \theta
## 95 percent confidence interval:
## 1.000834 1.122503
## sample estimates:
## mean of x mean of y
   12.54301 11.48134
##
##
##
##
## t.test(Speed[hour == 9 ], Speed[hour == 19 ])
##
##
##
   Welch Two Sample t-test
##
## data: x and y
## t = 16.108, df = 110530, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to \theta
## 95 percent confidence interval:
  0.4448875 0.5681544
## sample estimates:
## mean of x mean of y
   12.54301 12.03649
##
##
##
##
  t.test(Speed[hour == 9], Speed[hour == 20])
##
##
##
##
   Welch Two Sample t-test
##
## data: x and y
## t = -5.8637, df = 116870, p-value = 4.538e-09
## alternative hypothesis: true difference in means is not equal to \theta
## 95 percent confidence interval:
  -0.2522318 -0.1258544
## sample estimates:
## mean of x mean of y
##
   12.54301 12.73205
##
##
##
## t.test(Speed[hour == 9], Speed[hour == 21])
```

```
##
##
##
   Welch Two Sample t-test
##
## data: x and y
## t = -31.266, df = 121860, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to \theta
## 95 percent confidence interval:
   -1.0957973 -0.9665181
##
## sample estimates:
## mean of x mean of y
   12.54301 13.57417
##
##
##
##
## t.test(Speed[hour == 9], Speed[hour == 22])
##
##
##
   Welch Two Sample t-test
##
## data: x and y
## t = -44.7, df = 125850, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
   -1.568963 -1.437152
##
## sample estimates:
## mean of x mean of y
   12.54301 14.04607
##
##
##
##
## t.test(Speed[hour == 9], Speed[hour == 23])
##
##
##
   Welch Two Sample t-test
##
## data: x and y
## t = -52.047, df = 128080, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
##
   -1.852776 -1.718295
## sample estimates:
## mean of x mean of y
   12.54301 14.32855
##
##
##
##
## t.test(Speed[hour == 10 ], Speed[hour == 11 ])
##
##
   Welch Two Sample t-test
##
##
## data: x and y
## t = 7.6553, df = 113960, p-value = 1.944e-14
```

```
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
   0.2125569 0.3588562
## sample estimates:
## mean of x mean of y
   12.50487 12.21917
##
##
##
##
  t.test(Speed[hour == 10 ], Speed[hour == 12 ])
##
##
##
##
   Welch Two Sample t-test
##
## data: x and y
## t = 10.796, df = 114730, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to \theta
## 95 percent confidence interval:
## 0.3237032 0.4673136
## sample estimates:
## mean of x mean of y
   12.50487 12.10937
##
##
##
##
## t.test(Speed[hour == 10 ], Speed[hour == 13 ])
##
##
   Welch Two Sample t-test
##
##
## data: x and y
## t = 13.046, df = 114450, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to \theta
## 95 percent confidence interval:
##
  0.4067057 0.5505094
## sample estimates:
## mean of x mean of y
##
   12.50487 12.02627
##
##
##
  t.test(Speed[hour == 10 ], Speed[hour == 14 ])
##
##
##
##
   Welch Two Sample t-test
##
## data: x and y
## t = 28.29, df = 116470, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
## 0.9088475 1.0441550
## sample estimates:
## mean of x mean of y
   12.50487 11.52837
##
```

```
##
##
##
## t.test(Speed[hour == 10 ], Speed[hour == 15 ])
##
##
   Welch Two Sample t-test
##
##
## data: x and y
## t = 40.992, df = 111690, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to \theta
## 95 percent confidence interval:
   1.287863 1.417203
## sample estimates:
## mean of x mean of y
   12.50487 11.15234
##
##
##
##
  t.test(Speed[hour == 10 ], Speed[hour == 16 ])
##
##
##
##
   Welch Two Sample t-test
##
## data: x and y
## t = 48.769, df = 108910, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to \theta
## 95 percent confidence interval:
## 1.516088 1.643050
## sample estimates:
## mean of x mean of y
##
   12.50487 10.92530
##
##
##
## t.test(Speed[hour == 10 ], Speed[hour == 17 ])
##
##
##
   Welch Two Sample t-test
##
## data: x and y
## t = 51.506, df = 100440, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
##
   1.544633 1.666841
## sample estimates:
## mean of x mean of y
   12.50487 10.89914
##
##
##
##
## t.test(Speed[hour == 10 ], Speed[hour == 18 ])
##
##
```

```
Welch Two Sample t-test
##
##
## data: x and y
## t = 33.021, df = 99640, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
## 0.9627788 1.0842829
## sample estimates:
## mean of x mean of y
   12.50487 11.48134
##
##
##
##
## t.test(Speed[hour == 10 ], Speed[hour == 19 ])
##
##
   Welch Two Sample t-test
##
##
## data: x and y
## t = 14.915, df = 103290, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
## 0.4068310 0.5299357
## sample estimates:
## mean of x mean of y
##
   12.50487 12.03649
##
##
##
## t.test(Speed[hour == 10 ], Speed[hour == 20 ])
##
##
   Welch Two Sample t-test
##
##
## data: x and y
## t = -7.0555, df = 109530, p-value = 1.73e-12
## alternative hypothesis: true difference in means is not equal to \theta
## 95 percent confidence interval:
   -0.2902903 -0.1640711
## sample estimates:
## mean of x mean of y
   12.50487 12.73205
##
##
##
##
## t.test(Speed[hour == 10 ], Speed[hour == 21 ])
##
##
##
   Welch Two Sample t-test
##
## data: x and y
## t = -32.462, df = 114550, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to \theta
## 95 percent confidence interval:
```

```
## -1.133858 -1.004733
## sample estimates:
## mean of x mean of y
   12.50487 13.57417
##
##
##
## t.test(Speed[hour == 10 ], Speed[hour == 22 ])
##
##
   Welch Two Sample t-test
##
##
## data: x and y
## t = -45.887, df = 118620, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to \theta
## 95 percent confidence interval:
  -1.607025 -1.475366
## sample estimates:
## mean of x mean of y
##
   12.50487 14.04607
##
##
##
## t.test(Speed[hour == 10 ], Speed[hour == 23 ])
##
##
##
   Welch Two Sample t-test
##
## data: x and y
## t = -53.217, df = 121130, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
## -1.890839 -1.756507
## sample estimates:
## mean of x mean of y
   12.50487 14.32855
##
##
##
##
## t.test(Speed[hour == 11 ], Speed[hour == 12 ])
##
##
##
   Welch Two Sample t-test
##
## data: x and y
## t = 3.0067, df = 114070, p-value = 0.002642
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
## 0.03822453 0.18137909
## sample estimates:
## mean of x mean of y
##
   12.21917 12.10937
##
##
```

```
##
## t.test(Speed[hour == 11 ], Speed[hour == 13 ])
##
##
##
   Welch Two Sample t-test
##
## data: x and y
## t = 5.275, df = 113790, p-value = 1.33e-07
## alternative hypothesis: true difference in means is not equal to \theta
## 95 percent confidence interval:
## 0.1212268 0.2645753
## sample estimates:
## mean of x mean of y
   12.21917 12.02627
##
##
##
##
## t.test(Speed[hour == 11 ], Speed[hour == 14 ])
##
##
   Welch Two Sample t-test
##
##
## data: x and y
## t = 20.085, df = 115850, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to \theta
## 95 percent confidence interval:
## 0.6233829 0.7582065
## sample estimates:
## mean of x mean of y
##
   12.21917 11.52837
##
##
##
## t.test(Speed[hour == 11 ], Speed[hour == 15 ])
##
##
   Welch Two Sample t-test
##
##
## data: x and y
## t = 32.46, df = 111090, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
## 1.002410 1.131244
## sample estimates:
## mean of x mean of y
   12.21917 11.15234
##
##
##
##
## t.test(Speed[hour == 11 ], Speed[hour == 16 ])
##
##
##
   Welch Two Sample t-test
##
```

```
## data: x and y
## t = 40.111, df = 108320, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
## 1.230639 1.357086
## sample estimates:
## mean of x mean of y
##
   12.21917 10.92530
##
##
##
## t.test(Speed[hour == 11 ], Speed[hour == 17 ])
##
##
##
   Welch Two Sample t-test
##
## data: x and y
## t = 42.528, df = 99851, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
## 1.259194 1.380867
## sample estimates:
## mean of x mean of y
   12.21917 10.89914
##
##
##
##
## t.test(Speed[hour == 11 ], Speed[hour == 18 ])
##
##
##
   Welch Two Sample t-test
##
## data: x and y
## t = 23.91, df = 99049, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to \theta
## 95 percent confidence interval:
## 0.6773418 0.7983068
## sample estimates:
## mean of x mean of y
##
   12.21917 11.48134
##
##
##
## t.test(Speed[hour == 11 ], Speed[hour == 19 ])
##
##
   Welch Two Sample t-test
##
##
## data: x and y
## t = 5.8422, df = 102710, p-value = 5.168e-09
## alternative hypothesis: true difference in means is not equal to \theta
## 95 percent confidence interval:
## 0.1213905 0.2439631
## sample estimates:
```

```
## mean of x mean of y
   12.21917 12.03649
##
##
##
##
   t.test(Speed[hour == 11 ], Speed[hour == 20 ])
##
##
##
##
    Welch Two Sample t-test
##
## data: x and y
## t = -15.994, df = 108950, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to \theta
## 95 percent confidence interval:
## -0.5757374 -0.4500371
## sample estimates:
## mean of x mean of y
   12.21917 12.73205
##
##
##
##
## t.test(Speed[hour == 11 ], Speed[hour == 21 ])
##
##
##
   Welch Two Sample t-test
##
## data: x and y
## t = -41.297, df = 113970, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to \theta
## 95 percent confidence interval:
   -1.419311 -1.290693
## sample estimates:
## mean of x mean of y
   12.21917 13.57417
##
##
##
##
   t.test(Speed[hour == 11 ], Speed[hour == 22 ])
##
##
##
##
    Welch Two Sample t-test
##
## data: x and y
## t = -54.6, df = 118040, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to \theta
## 95 percent confidence interval:
## -1.892482 -1.761321
## sample estimates:
## mean of x mean of y
##
   12.21917 14.04607
##
##
##
## t.test(Speed[hour == 11 ], Speed[hour == 23 ])
```

```
##
##
##
   Welch Two Sample t-test
##
## data: x and y
## t = -61.779, df = 120530, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to \theta
## 95 percent confidence interval:
   -2.176302 -2.042458
##
## sample estimates:
## mean of x mean of y
   12.21917 14.32855
##
##
##
##
## t.test(Speed[hour == 12 ], Speed[hour == 13 ])
##
##
##
   Welch Two Sample t-test
##
## data: x and y
## t = 2.3168, df = 115010, p-value = 0.02052
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
## 0.01279761 0.15340079
## sample estimates:
## mean of x mean of y
   12.10937 12.02627
##
##
##
##
## t.test(Speed[hour == 12 ], Speed[hour == 14 ])
##
##
##
   Welch Two Sample t-test
##
## data: x and y
## t = 17.267, df = 119190, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
## 0.5150425 0.6469433
## sample estimates:
## mean of x mean of y
   12.10937 11.52837
##
##
##
##
## t.test(Speed[hour == 12 ], Speed[hour == 15 ])
##
##
   Welch Two Sample t-test
##
##
## data: x and y
## t = 29.828, df = 115450, p-value < 2.2e-16
```

```
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
   0.8941387 1.0199110
## sample estimates:
## mean of x mean of y
##
   12.10937 11.15234
##
##
##
  t.test(Speed[hour == 12], Speed[hour == 16])
##
##
##
##
   Welch Two Sample t-test
##
## data: x and y
## t = 37.636, df = 112980, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
## 1.122398 1.245723
## sample estimates:
## mean of x mean of y
##
   12.10937 10.92530
##
##
##
## t.test(Speed[hour == 12 ], Speed[hour == 17 ])
##
##
   Welch Two Sample t-test
##
##
## data: x and y
## t = 40.059, df = 104490, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to \theta
## 95 percent confidence interval:
##
  1.151016 1.269441
## sample estimates:
## mean of x mean of y
##
   12.10937 10.89914
##
##
##
  t.test(Speed[hour == 12], Speed[hour == 18])
##
##
##
##
   Welch Two Sample t-test
##
## data: x and y
## t = 20.916, df = 103780, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
## 0.5691731 0.6868718
## sample estimates:
## mean of x mean of y
   12.10937 11.48134
##
```

```
##
##
##
## t.test(Speed[hour == 12 ], Speed[hour == 19 ])
##
##
   Welch Two Sample t-test
##
##
## data: x and y
## t = 2.3935, df = 107630, p-value = 0.01669
## alternative hypothesis: true difference in means is not equal to \theta
## 95 percent confidence interval:
  0.01319987 0.13255015
## sample estimates:
## mean of x mean of y
   12.10937 12.03649
##
##
##
##
## t.test(Speed[hour == 12 ], Speed[hour == 20 ])
##
##
##
   Welch Two Sample t-test
##
## data: x and y
## t = -19.916, df = 114020, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to \theta
## 95 percent confidence interval:
   -0.6839692 -0.5614089
## sample estimates:
## mean of x mean of y
##
   12.10937 12.73205
##
##
##
## t.test(Speed[hour == 12 ], Speed[hour == 21 ])
##
##
##
   Welch Two Sample t-test
##
## data: x and y
## t = -45.735, df = 118970, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
##
   -1.527579 -1.402028
## sample estimates:
## mean of x mean of y
   12.10937 13.57417
##
##
##
##
## t.test(Speed[hour == 12 ], Speed[hour == 22 ])
##
##
```

```
Welch Two Sample t-test
##
##
## data: x and y
## t = -59.239, df = 122900, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
   -2.000781 -1.872626
##
## sample estimates:
## mean of x mean of y
   12.10937 14.04607
##
##
##
##
## t.test(Speed[hour == 12 ], Speed[hour == 23 ])
##
##
   Welch Two Sample t-test
##
##
## data: x and y
## t = -66.456, df = 124940, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
   -2.284631 -2.153732
## sample estimates:
## mean of x mean of y
##
   12.10937 14.32855
##
##
##
## t.test(Speed[hour == 13], Speed[hour == 14])
##
##
   Welch Two Sample t-test
##
##
## data: x and y
## t = 14.773, df = 118600, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to \theta
## 95 percent confidence interval:
## 0.4318380 0.5639494
## sample estimates:
## mean of x mean of y
   12.02627 11.52837
##
##
##
##
## t.test(Speed[hour == 13 ], Speed[hour == 15 ])
##
##
##
   Welch Two Sample t-test
##
## data: x and y
## t = 27.19, df = 114720, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to \theta
## 95 percent confidence interval:
```

```
## 0.8109291 0.9369222
## sample estimates:
## mean of x mean of y
   12.02627 11.15234
##
##
##
## t.test(Speed[hour == 13 ], Speed[hour == 16 ])
##
##
   Welch Two Sample t-test
##
##
## data: x and y
## t = 34.931, df = 112220, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to \theta
## 95 percent confidence interval:
## 1.039186 1.162737
## sample estimates:
## mean of x mean of y
##
   12.02627 10.92530
##
##
##
## t.test(Speed[hour == 13 ], Speed[hour == 17 ])
##
##
##
   Welch Two Sample t-test
##
## data: x and y
## t = 37.235, df = 103720, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
## 1.067799 1.186459
## sample estimates:
## mean of x mean of y
   12.02627 10.89914
##
##
##
##
## t.test(Speed[hour == 13], Speed[hour == 18])
##
##
##
   Welch Two Sample t-test
##
## data: x and y
## t = 18.112, df = 103000, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
## 0.4859560 0.6038905
## sample estimates:
## mean of x mean of y
##
   12.02627 11.48134
##
##
```

```
##
## t.test(Speed[hour == 13 ], Speed[hour == 19 ])
##
##
##
   Welch Two Sample t-test
##
## data: x and y
## t = -0.33515, df = 106830, p-value = 0.7375
## alternative hypothesis: true difference in means is not equal to \theta
## 95 percent confidence interval:
   -0.07001560 0.04956723
##
## sample estimates:
## mean of x mean of y
   12.02627 12.03649
##
##
##
##
## t.test(Speed[hour == 13 ], Speed[hour == 20 ])
##
##
   Welch Two Sample t-test
##
##
## data: x and y
## t = -22.532, df = 113210, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to \theta
## 95 percent confidence interval:
   -0.7671816 -0.6443949
##
## sample estimates:
## mean of x mean of y
##
   12.02627 12.73205
##
##
##
## t.test(Speed[hour == 13 ], Speed[hour == 21 ])
##
##
   Welch Two Sample t-test
##
##
## data: x and y
## t = -48.244, df = 118170, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
   -1.610789 -1.485017
##
## sample estimates:
## mean of x mean of y
   12.02627 13.57417
##
##
##
##
## t.test(Speed[hour == 13 ], Speed[hour == 22 ])
##
##
##
   Welch Two Sample t-test
##
```

```
## data: x and y
## t = -61.677, df = 122120, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
## -2.083989 -1.955617
## sample estimates:
## mean of x mean of y
##
   12.02627 14.04607
##
##
##
## t.test(Speed[hour == 13], Speed[hour == 23])
##
##
##
   Welch Two Sample t-test
##
## data: x and y
## t = -68.833, df = 124210, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to \theta
## 95 percent confidence interval:
   -2.367836 -2.236725
## sample estimates:
## mean of x mean of y
   12.02627 14.32855
##
##
##
##
## t.test(Speed[hour == 14 ], Speed[hour == 15 ])
##
##
##
   Welch Two Sample t-test
##
## data: x and y
## t = 12.685, df = 136280, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to \theta
## 95 percent confidence interval:
## 0.3179312 0.4341328
## sample estimates:
## mean of x mean of y
##
   11.52837 11.15234
##
##
##
## t.test(Speed[hour == 14 ], Speed[hour == 16 ])
##
##
   Welch Two Sample t-test
##
##
## data: x and y
## t = 20.819, df = 136510, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
## 0.5462936 0.6598418
## sample estimates:
```

```
## mean of x mean of y
   11.52837 10.92530
##
##
##
##
##
  t.test(Speed[hour == 14 ], Speed[hour == 17 ])
##
##
##
   Welch Two Sample t-test
##
## data: x and y
## t = 22.795, df = 130230, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to \theta
## 95 percent confidence interval:
## 0.5751323 0.6833391
## sample estimates:
## mean of x mean of y
   11.52837 10.89914
##
##
##
##
## t.test(Speed[hour == 14 ], Speed[hour == 18 ])
##
##
##
   Welch Two Sample t-test
##
## data: x and y
## t = 1.7163, df = 130560, p-value = 0.0861
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
   -0.006675832 0.100734992
## sample estimates:
## mean of x mean of y
   11.52837 11.48134
##
##
##
##
  t.test(Speed[hour == 14], Speed[hour == 19])
##
##
##
##
   Welch Two Sample t-test
##
## data: x and y
## t = -18.237, df = 134800, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to \theta
## 95 percent confidence interval:
   -0.5627269 -0.4535088
## sample estimates:
## mean of x mean of y
##
   11.52837 12.03649
##
##
##
## t.test(Speed[hour == 14], Speed[hour == 20])
```

```
##
##
##
   Welch Two Sample t-test
##
## data: x and y
## t = -41.86, df = 140460, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to \theta
## 95 percent confidence interval:
   -1.260040 -1.147323
##
## sample estimates:
## mean of x mean of y
   11.52837 12.73205
##
##
##
##
## t.test(Speed[hour == 14 ], Speed[hour == 21 ])
##
##
##
   Welch Two Sample t-test
##
## data: x and y
## t = -69.156, df = 143640, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
##
   -2.103777 -1.987816
## sample estimates:
## mean of x mean of y
   11.52837 13.57417
##
##
##
##
## t.test(Speed[hour == 14 ], Speed[hour == 22 ])
##
##
##
   Welch Two Sample t-test
##
## data: x and y
## t = -83.091, df = 145800, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
##
   -2.577085 -2.458308
## sample estimates:
## mean of x mean of y
   11.52837 14.04607
##
##
##
##
## t.test(Speed[hour == 14 ], Speed[hour == 23 ])
##
##
   Welch Two Sample t-test
##
##
## data: x and y
## t = -90.17, df = 144440, p-value < 2.2e-16
```

```
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
   -2.861041 -2.739308
## sample estimates:
## mean of x mean of y
##
   11.52837 14.32855
##
##
##
  t.test(Speed[hour == 15], Speed[hour == 16])
##
##
##
##
   Welch Two Sample t-test
##
## data: x and y
## t = 8.3669, df = 151360, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
## 0.1738520 0.2802195
## sample estimates:
## mean of x mean of y
##
   11.15234 10.92530
##
##
##
## t.test(Speed[hour == 15 ], Speed[hour == 17 ])
##
##
##
   Welch Two Sample t-test
##
## data: x and y
## t = 9.8618, df = 150740, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to \theta
## 95 percent confidence interval:
##
  0.2028809 0.3035265
## sample estimates:
## mean of x mean of y
##
   11.15234 10.89914
##
##
##
  t.test(Speed[hour == 15 ], Speed[hour == 18 ])
##
##
##
##
   Welch Two Sample t-test
##
## data: x and y
## t = -12.924, df = 153160, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
## -0.3788970 -0.2791077
## sample estimates:
## mean of x mean of y
   11.15234 11.48134
##
```

```
##
##
##
## t.test(Speed[hour == 15], Speed[hour == 19])
##
##
   Welch Two Sample t-test
##
##
## data: x and y
## t = -34.068, df = 156700, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to \theta
## 95 percent confidence interval:
   -0.9350159 -0.8332838
## sample estimates:
## mean of x mean of y
   11.15234 12.03649
##
##
##
##
  t.test(Speed[hour == 15], Speed[hour == 20])
##
##
##
##
   Welch Two Sample t-test
##
## data: x and y
## t = -58.707, df = 159270, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to \theta
## 95 percent confidence interval:
   -1.632454 -1.526974
## sample estimates:
## mean of x mean of y
##
   11.15234 12.73205
##
##
##
## t.test(Speed[hour == 15 ], Speed[hour == 21 ])
##
##
##
   Welch Two Sample t-test
##
## data: x and y
## t = -87.144, df = 158820, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
##
   -2.476298 -2.367359
## sample estimates:
## mean of x mean of y
   11.15234 13.57417
##
##
##
##
## t.test(Speed[hour == 15], Speed[hour == 22])
##
##
```

```
Welch Two Sample t-test
##
##
## data: x and y
## t = -101.34, df = 158060, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
   -2.949694 -2.837762
##
## sample estimates:
## mean of x mean of y
   11.15234 14.04607
##
##
##
##
## t.test(Speed[hour == 15], Speed[hour == 23])
##
##
   Welch Two Sample t-test
##
##
## data: x and y
## t = -108.21, df = 152650, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
   -3.233738 -3.118675
## sample estimates:
## mean of x mean of y
   11.15234 14.32855
##
##
##
##
## t.test(Speed[hour == 16], Speed[hour == 17])
##
##
   Welch Two Sample t-test
##
##
## data: x and y
## t = 1.0513, df = 161660, p-value = 0.2931
## alternative hypothesis: true difference in means is not equal to \theta
## 95 percent confidence interval:
   -0.02261708 0.07495301
## sample estimates:
## mean of x mean of y
   10.92530 10.89914
##
##
##
##
## t.test(Speed[hour == 16 ], Speed[hour == 18 ])
##
##
##
   Welch Two Sample t-test
##
## data: x and y
## t = -22.543, df = 165710, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to \theta
## 95 percent confidence interval:
```

```
## -0.6043814 -0.5076948
## sample estimates:
## mean of x mean of y
   10.92530 11.48134
##
##
##
## t.test(Speed[hour == 16], Speed[hour == 19])
##
##
   Welch Two Sample t-test
##
##
## data: x and y
## t = -44.136, df = 168360, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to \theta
## 95 percent confidence interval:
  -1.160531 -1.061840
## sample estimates:
## mean of x mean of y
##
   10.92530 12.03649
##
##
##
## t.test(Speed[hour == 16 ], Speed[hour == 20 ])
##
##
##
   Welch Two Sample t-test
##
## data: x and y
## t = -69.063, df = 168300, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
## -1.858024 -1.755475
## sample estimates:
## mean of x mean of y
   10.92530 12.73205
##
##
##
##
## t.test(Speed[hour == 16], Speed[hour == 21])
##
##
##
   Welch Two Sample t-test
##
## data: x and y
## t = -97.86, df = 165310, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
   -2.701917 -2.595812
## sample estimates:
## mean of x mean of y
##
   10.92530 13.57417
##
##
```

```
##
## t.test(Speed[hour == 16 ], Speed[hour == 22 ])
##
##
##
   Welch Two Sample t-test
##
## data: x and y
## t = -112.05, df = 162730, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to \theta
## 95 percent confidence interval:
   -3.175352 -3.066177
## sample estimates:
## mean of x mean of y
   10.92530 14.04607
##
##
##
##
## t.test(Speed[hour == 16 ], Speed[hour == 23 ])
##
##
   Welch Two Sample t-test
##
##
## data: x and y
## t = -118.71, df = 155140, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to \theta
## 95 percent confidence interval:
   -3.459434 -3.347050
##
## sample estimates:
## mean of x mean of y
##
   10.92530 14.32855
##
##
##
## t.test(Speed[hour == 17 ], Speed[hour == 18 ])
##
##
   Welch Two Sample t-test
##
##
## data: x and y
## t = -25.259, df = 183950, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
   -0.6273829 -0.5370293
##
## sample estimates:
## mean of x mean of y
   10.89914 11.48134
##
##
##
##
## t.test(Speed[hour == 17 ], Speed[hour == 19 ])
##
##
##
   Welch Two Sample t-test
##
```

```
## data: x and y
## t = -48.201, df = 183720, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
   -1.183601 -1.091106
## sample estimates:
## mean of x mean of y
##
   10.89914 12.03649
##
##
##
## t.test(Speed[hour == 17 ], Speed[hour == 20 ])
##
##
##
   Welch Two Sample t-test
##
## data: x and y
## t = -74.377, df = 176980, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to \theta
## 95 percent confidence interval:
   -1.881218 -1.784617
## sample estimates:
## mean of x mean of y
   10.89914 12.73205
##
##
##
##
## t.test(Speed[hour == 17 ], Speed[hour == 21 ])
##
##
##
    Welch Two Sample t-test
##
## data: x and y
## t = -104.48, df = 168660, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to \theta
## 95 percent confidence interval:
## -2.725216 -2.624848
## sample estimates:
## mean of x mean of y
##
   10.89914 13.57417
##
##
##
## t.test(Speed[hour == 17 ], Speed[hour == 22 ])
##
##
   Welch Two Sample t-test
##
##
## data: x and y
## t = -119.06, df = 162760, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to \theta
## 95 percent confidence interval:
   -3.198736 -3.095128
## sample estimates:
```

```
## mean of x mean of y
   10.89914 14.04607
##
##
##
##
##
  t.test(Speed[hour == 17 ], Speed[hour == 23 ])
##
##
##
   Welch Two Sample t-test
##
## data: x and y
## t = -125.66, df = 151770, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to \theta
## 95 percent confidence interval:
## -3.482902 -3.375918
## sample estimates:
## mean of x mean of y
   10.89914 14.32855
##
##
##
##
## t.test(Speed[hour == 18], Speed[hour == 19])
##
##
##
   Welch Two Sample t-test
##
## data: x and y
## t = -23.767, df = 192480, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to \theta
## 95 percent confidence interval:
   -0.6009286 -0.5093663
## sample estimates:
## mean of x mean of y
   11.48134 12.03649
##
##
##
##
  t.test(Speed[hour == 18], Speed[hour == 20])
##
##
##
##
   Welch Two Sample t-test
##
## data: x and y
## t = -51.225, df = 182880, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to \theta
## 95 percent confidence interval:
## -1.298566 -1.202857
## sample estimates:
## mean of x mean of y
##
   11.48134 12.73205
##
##
##
## t.test(Speed[hour == 18 ], Speed[hour == 21 ])
```

```
##
##
##
   Welch Two Sample t-test
##
## data: x and y
## t = -82.442, df = 172490, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to \theta
## 95 percent confidence interval:
   -2.142581 -2.043072
##
## sample estimates:
## mean of x mean of y
   11.48134 13.57417
##
##
##
##
## t.test(Speed[hour == 18 ], Speed[hour == 22 ])
##
##
##
   Welch Two Sample t-test
##
## data: x and y
## t = -97.82, df = 165360, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
##
   -2.616114 -2.513338
## sample estimates:
## mean of x mean of y
   11.48134 14.04607
##
##
##
##
## t.test(Speed[hour == 18 ], Speed[hour == 23 ])
##
##
##
   Welch Two Sample t-test
##
## data: x and y
## t = -105.11, df = 153150, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
##
   -2.900293 -2.794115
## sample estimates:
## mean of x mean of y
   11.48134 14.32855
##
##
##
##
## t.test(Speed[hour == 19], Speed[hour == 20])
##
##
   Welch Two Sample t-test
##
##
## data: x and y
## t = -27.898, df = 184350, p-value < 2.2e-16
```

```
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
   -0.7444305 -0.6466976
## sample estimates:
## mean of x mean of y
##
   12.03649 12.73205
##
##
##
  t.test(Speed[hour == 19], Speed[hour == 21])
##
##
##
##
   Welch Two Sample t-test
##
## data: x and y
## t = -59.41, df = 175270, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
## -1.588407 -1.486950
## sample estimates:
## mean of x mean of y
   12.03649 13.57417
##
##
##
##
## t.test(Speed[hour == 19], Speed[hour == 22])
##
##
##
   Welch Two Sample t-test
##
## data: x and y
## t = -75.264, df = 168820, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to \theta
## 95 percent confidence interval:
##
   -2.061911 -1.957246
## sample estimates:
## mean of x mean of y
##
   12.03649 14.04607
##
##
##
  t.test(Speed[hour == 19], Speed[hour == 23])
##
##
##
##
   Welch Two Sample t-test
##
## data: x and y
## t = -83.187, df = 157140, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
## -2.346060 -2.238053
## sample estimates:
## mean of x mean of y
   12.03649 14.32855
##
```

```
##
##
##
## t.test(Speed[hour == 20 ], Speed[hour == 21 ])
##
##
   Welch Two Sample t-test
##
##
## data: x and y
## t = -31.374, df = 175520, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to \theta
## 95 percent confidence interval:
   -0.8947219 -0.7895072
## sample estimates:
## mean of x mean of y
   12.73205 13.57417
##
##
##
##
## t.test(Speed[hour == 20 ], Speed[hour == 22 ])
##
##
##
   Welch Two Sample t-test
##
## data: x and y
## t = -47.557, df = 171060, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to \theta
## 95 percent confidence interval:
   -1.368170 -1.259859
## sample estimates:
## mean of x mean of y
##
   12.73205 14.04607
##
##
##
## t.test(Speed[hour == 20 ], Speed[hour == 23 ])
##
##
##
   Welch Two Sample t-test
##
## data: x and y
## t = -56.105, df = 161310, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
##
   -1.652264 -1.540721
## sample estimates:
## mean of x mean of y
   12.73205 14.32855
##
##
##
##
## t.test(Speed[hour == 21 ], Speed[hour == 22 ])
##
##
```

```
##
   Welch Two Sample t-test
##
## data: x and y
## t = -16.563, df = 170190, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
   -0.5277411 -0.4160586
##
## sample estimates:
## mean of x mean of y
   13.57417 14.04607
##
##
##
##
##
  t.test(Speed[hour == 21 ], Speed[hour == 23 ])
##
##
   Welch Two Sample t-test
##
##
## data: x and y
## t = -25.754, df = 162550, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
##
   -0.8117883 -0.6969674
## sample estimates:
## mean of x mean of y
   13.57417 14.32855
##
##
##
##
## t.test(Speed[hour == 22], Speed[hour == 23])
##
##
   Welch Two Sample t-test
##
##
## data: x and y
## t = -9.4107, df = 163050, p-value < 2.2e-16
## alternative hypothesis: true difference in means is not equal to \theta
## 95 percent confidence interval:
   -0.3413100 -0.2236461
## sample estimates:
## mean of x mean of y
   14.04607 14.32855
```

The p-value of the ANOVA test is very small and close to 0. Thus, the null hypothesis is rejected - the average trip speeds are not same for all hours.

A 2-sample t-test, with significance value set at 0.05, is performed on all the hours, to check if the means are same between any two hours, the results of p-value is given below:

- Hours 8:00 AM and 11:00 AM, 9:00 AM and 10:00 AM have the same mean p-value is greater than significance value
 - peak hour traffic would be nearly same, people start leaving for office around 7:00 AM and reach around 11:00 AM causing the average to be approximately same between 8:00 AM and 11:00 AM.

Thus, the average speed is same.

- Hours 1:00 PM and 7:00 PM, 2:00 PM and 6:00 PM have the same mean p-value is greater than significance value
 - mid-day traffic and just after office hours traffic would be nearly same as roads would be cleared from morning rush hour (between 7 to 11 AM and evening rush hour 4-5 PM). Thus, the average speed is same.
- Hours 4:00 PM and 5:00 PM have the same mean p-value is greater than significance value
 - evening peak hour traffic would be nearly same, people start leaving from office around 4:00 PM causing the average speed to be approximately same
- For the remaining combination of hours, p-value is close to 0 and so they don't have the same means.

My hypothesis for average speed variation (based on the boxplot) is below:

- average speed is increasing continuously from mid-night, 00:00 AM to 5:00 AM, as majority of the people would be home, and the roads would be empty
- average speed dropped at 7:00 AM and continuous nearly the same during the morning peak hours, 7:00 AM to 11:00 AM, as people would be rushing to office
- average speed is fluctuating during mid-day, 10:00 AM to 5:00 PM, schools would close, people will be running errands randomly and would start leaving office
- average speed is increasing slowly after evening peak hours, 6:00 PM to 11:00 PM, as people would have reached home