

Data driven modelling for energy consumption prediction on smart buildings

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Abstract—Many efforts from several organisations are focused on increasing energy efficiency. This is on the interest of everybody, from individuals to governments, since energy efficiency yields to economical savings, to reduce greenhouse gas emissions and to alleviate energy poverty. Buildings are one of the largest consumers of primary energy and its efficiency is an important goal for the achievement of the mentioned goals.

Currently, the new paradigm of the Internet of Things allow us to count on vast amounts of data that can be used for knowledge extraction of all kinds, one can expect that energy prediction will not be an exception.

This new paradigm that brings large amounts of data, and the advantages on machine learning, have motivated us to test the hypothesis of this paper. This hypothesis supports that prior information that one can find on the physics of the building heat transfer, is now redundant due to the completeness of the data from the system.

We propose a machine learning approach and a grey-box model approach to test this hypothesis, the first blind to the physics of the problem, and the second heavily influenced by it. The energy consumption prediction models were created with the two approaches. The method has been designed to be used on a project in which the evaluation of energy efficiency interventions is tested. However, the model at this stage was designed to estimate the energy consumption in normal operation state i.e. if the system would not have been altered by any energy efficiency intervention.

Our black-box method, which is based on a combination of statistical, machine learning models and on a time series structuring of the data, shows better prediction accuracy than the so-called grey-box methods that include basic physical equations. This proves for this case that the hypothesis of this paper can be rejected i.e. also in this field a data driven approach outperforms more informed methods.

Keywords—data-driven models, black-box models, grey-box models, smart buildings, data analytics

I. INTRODUCTION

Energy consumption of buildings in developed countries comprises 20-40% of their total energy use and it is above industry and transport in EU and US [1], [2].

In order to mitigate climate change, the reduction of energy use together with the use of non-fossil energy sources such as solar and wind is crucial. On the other hand, reducing energy consumption on buildings has to be done always maintaining the necessary levels so as to keep comfort for buildings users and to lower their costs to not increase fuel-poverty. Seems like the new sensorisation of buildings might be opening the door for solving these issues.

When it comes to energy savings, energy management should be the process of monitoring, controlling, and conserving energy during buildings' normal use. The prediction of energy use in buildings is a powerful piece of information, that is fundamental in concerns such micro-grids, energy storage, demands analysis or energy feedback. Novel energy feedback systems involve the following steps:

- Metering and collecting energy consumption data,
- Proposing ways of saving energy by analysing the data and putting them into practice, and
- Tracking the consumption in order to quantify the gains due to the proposed activity.

The series of methods and processes used to face the third step, that is to assess the performance of energy efficiency interventions by quantifying the gains on efficiency are commonly noted as Evaluation, Measurement, and Verification (EM&V).

The energy consumption evaluation compared to prior intervention scenarios is currently developing and simple regression models, such the ones proposed in the ASHRAEs Guideline [3], might not be enough at this moment. Several researchers are focusing on the development of EM&V methods with a less naive perspectives [4].

Regression models need to be typically adjusted in an *ad hoc* manner in order to capture non-linear behavior, which arises from complex (physical) multi-variate interactions between ambient conditions, occupancy, building operating conditions and so forth [5].

Regression has always been the standard approach to modelling the relationship between one outcome variable and several input variables, and it can be seen both from a white-box and a black-box point of view. That means, we could use regression for analytical purposes, where a scenario is understood through physics or for data-driven purposes where a scenario is modeled using data alone.

In recent years, a new phenomenon is affecting the building sector, and this is the proliferation of smart meters and in home displays, and the trend seems to be on the rise considering that the European Commission has established that 16 Member States will proceed with large-scale roll-out of smart meters by 2020 or earlier [6]. This together with the new developments on Energy Data Infrastructure (such as [7], [8]) has formed the perfect growing soil for the creation among other technologies of advanced energy feedback strategies for the reduction of energy use in buildings and for the education of building occupants/users [9]. The correct prediction of consumptions is crucial for the functioning of those.

Thanks to that, the generation of data about our surrounding environment and ourselves is explosively growing in terms of *velocity*, *variety* and *volume*. This implies that there is more value hidden in the data than it has never been before and that as the datasets are generally too large for classical methods (with indicators such as p-value) to have meaning. Now, predictive data-driven modelling uses other ways to fit a model such as machine learning, and these approaches are fastly taking over in many disciplines.

Our proposal for energy consumption is to take a machine learning approach, where black-box models are used in order to predict energy consumption, reducing the cost compared to traditional white box processes which require a level of building engineering expertise that limits scalability. This has also been compared with a grey-box approach, that lays between the previous two.

II. RELATED WORK

Building thermodynamics is a complex nonlinear phenomenon, which is strongly influenced by weather conditions, building operating modes, and occupant schedules.

Three general categories of building energy forecasting models have been reported in the literature which include white-box (physics-based), black-box (data-driven), and grey-box (combination of physics based and data-driven) modelling approaches [10].

A. White-box models

Building structure, systems and equipments need to be considered for this kind of models together with weather and other boundary conditions. The first are usually obtained from design plans, manufacture catalogues or visual inspection.

There exist a wealth of mature white box simulation engines that through the combination of mathematical equations, simulate the building and calculate its energy consumption. Well-known engines such as EnergyPlus [11] and TRNSYS [12] have been widely used to analyse energy consumption and determine building control and operation schemes among others [13].

Even though these elaborate simulation tools are effective and accurate, they require detailed information and input parameters. These parameters, however, are in most cases difficult to obtain, and sometimes not available.

B. Black-box models

Black-box models are also known as solely data-driven models. In this case, statistical models are directly applied to capture the relationship between building energy consumption and the inputs such as operation and weather data. This type of models need baseline measurements over a certain period of time.

Regression can be used as a data-driven model. But this method is highly more interpretable than machine learning approaches. Machine learning systems figure out how to solve problems with minimal human guidance and once a machine learning algorithm is trained, it can be difficult to understand why it gives a particular response to a set of inputs. The adaptability of the machine learning models through a self-tuning process (which is different from mathematical models such as regression models) makes accurate decisions without outside expert intervention which comes out useful when unusual perturbations, disturbances, and/or changes in building background conditions may occur.

Several data-based modelling techniques have been used for EM&V, including multiple linear regression [14]. In the case of machine learning techniques such as neural networks, support vector machines and their combination [15], Gaussian Process modelling [5], and fuzzy logic models [16] are some examples. In such studies, the way of relating energy consumption and the input variables is instantaneous. That means, the energy consumption is only related to current indicators such as the temperature, humidity and others at a given timestamp.

C. Grey-box models

Grey-box models use simplified physical descriptions to simulate the behaviour of building energy systems, and with them identify important parameters and characteristics using statistical analysis [17].

Data-driven modelling based on grey-box models have been used for many years. As early of 1951 Burnard demonstrated for the first time that resistor-capacitor (RC) networks can represent the thermodynamics of buildings accurately [18]. Since then, RC-networks have been used to represent the thermodynamics of buildings. In the early years of building dynamic simulation, this was one of the few

ways of representing the thermodynamics of buildings, but even today, programs such as EnergyPlus, include thermal networks on their codes [17] .

In addition to building simulation, grey-box modelling of buildings using RC-networks have been used for the last two decades for Model Predictive Control (MC). MC has been used to govern heating and cooling systems of normally large buildings in a way in which the controller can anticipate to the needs of the building via the previous estimation of its thermodynamic features (these normally translated into response times and conductivity of the thermal envelope) [19].

This has motivated the investigation of ideal model topologies and methodologies for these models to ensure that they represent accurately the responses of buildings [20]. But also, other works are now focusing on how those methods can be used for the characterisation of their thermal envelope [21].

In cases where limited amounts of data are available and the information about the building architecture is partially known, grey models are suitable alternatives for the prediction of energy consumption [22].

III. METHODOLOGY

In this section we introduce both a black-box model and use a grey-box model in order to estimate the energy consumption of a building.

A. Inputs

Energy forecasting studies that use machine learning are usually intended to predict consumption **a priori** in order to manage and store the suitable amount of energy, taking into consideration the market prizes and also the necessities of the buildings. However, our approach is different in the sense that our goal is to quantify the energy savings relative to a baseline period due to certain experiment related to efficiency improvement.

This translates into a difference on the inputs that are available for the prediction. In other scenarios, data concerning energy consumption in previous hours and days is largely useful because it is evidently highly correlated with the later consumption [23]. However, we should not use such data because in case of using this algorithm on a building in which an intervention for energy reduction has taken place the consumption is likely to be altered by the experiment.

On the other side, in other scenarios environmental data is not available yet (it is the future) and predictions have to be used. When applying prediction for EM&V, environmental and occupation variables are usually available and it is not necessary to predict them. The most commonly used weather information is outdoor dry-bulb air temperature and solar irradiance, but in our case temperature was seen to be sufficient.

B. Proposed models

Our interest lies on weekly quantification of the energy use. However, daily dynamics are useful since there exist patterns that can be found depending on the day of the week. Our model predicts daily energy consumption and then compute the metrics on an aggregated manner so that the global quantification is done weekly.

Using this data, we then tested three approaches:

1) *Black-box*: Daily aggregate consumption is used as output and we try to capture the relationship between daily average temperature and the consumption by relating the time series composed by temperature hourly means and the daily consumption.

After this, we used several machine learning models in order to asses which one is the best one for our scenarios. The models are generated following the next steps [24]:

- Clean and transform the data: selecting predictive variables such as temperature and day type, deleting outliers
- Aggregate: compute daily consumption, create the time series with the input variables and represent the series in a lower dimension. That is, apply hourly average or other representation and feature selection methods in order to serve as inputs of our models.
- Divide the dataset into train (75 %) and test (25 %)
- Validation method: 10-fold cross validation and 5 repetitions over the training data set in order to find the hyperparameters of each machine learning algorithm
- Evaluate: apply the algorithm to the test dataset in order to obtain the metric for the model fitting

To our knowledge, our method differs from existing methods in the way which the data is introduced. We are relating the input as a time series with a single output. This has been previously done in scenarios in which consumption could be used as a predictor [25], that means, where the energy consumption is not altered by any intervention and the goal is simply to make a prediction of the energy a priori, with storage and production intentions. However, this is not possible for EM&V, as it is our case, resulting on a novel application of the method.

We have avoided the use of change-point models adding novelty to our approach. In a vast amount of energy efficiency literature, change-point models are used to determine the outdoor air temperatures at which the building transitions from heating to the dead-band and from the dead-band to cooling (like in [26]). However, we cover such effect by using the time series of the daily means of the temperature.

2) *Grey-box*: To make use of this models the set of outputs and inputs have to be defined together with the topology of the system. The most common mathematical representation of lumped parameter models is the state-space representation. The general form for time-invariant models can be written as shown on Eq. 1

$$\begin{cases} x'(t) = Ax(t) + Bu(t) \\ y(t) = Cx(t) + Du(t) \end{cases} \quad (1)$$

where x is a vector with the states of the model, in our case the temperatures, A is a characteristic matrix of the model, B defines the effect of the inputs in the model, and u are the inputs, in our case the outside temperature and electric gains. In this formulation, y represents the variables that are measured, in our case electricity. C is the identity matrix; and D is zero in all cases for this work. Using this formulation, every time that a solution had to be evaluated the Octave built in function **lsim** was used.

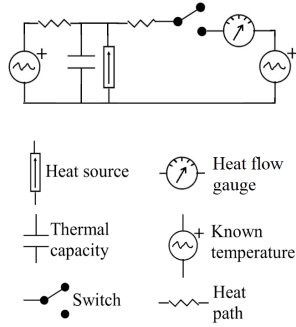


Figure 1: Dual-mode RC network

The conditioning system is governed in our case by a thermostat with a timer that turns it on and off. For this reason one need to consider that the RC-network that represents the building needs to change topologies depending on the operation (on or off). We have considered a dual-mode RC-network as the one shown in Fig. 1 and previously introduced by Ramallo-González on [4].

C. Black-box baseline models

Our proposed black-box models are compared with two baseline approaches that are documented in the literature. The first one is a regression-based electricity load model and the second one is a purely machine learning model that uses the inputs uniquely at the same timestamp than the output.

1) *Time-of-week-and-temperature (TWT)*: This algorithm was introduced in [27]. We have chosen it because of its high accuracy, low complexity and low computational cost when compared with the results of other state-of-the-art works methods used through a wide number of buildings [28].

In this work the predicted load is a sum of two terms: a “time of week effect” that allows each time of the week to have a different predicted load from the others, and a piecewise-continuous effect of temperature.

The central point of this algorithm is the creation of several coefficients that will be estimated using multiple ordinary least square regression. There will be a coefficient for every “time of the week”. A time of the week is a

unique instant of a week (Monday 1AM, Monday 2AM, ad so on). For example, there will be $24 \times 5 = 120$ (24 hours and 5 working days) coefficients in the case of hourly predictions or $4 \times 24 \times 5 = 480$ in the case of 15 minutes prediction. In addition, also some coefficients related to the temperature need to be calculated. Basically, the range of outside temperature data is cut into 6 levels and each of those has an assigned coefficient.

2) *Gaussian*: A Gaussian process (GP) modelling framework determineing energy savings and uncertainty levels in measurement and verification (EM&V) practice is presented in [5]. In this work they compare a black-box approach to the regular linear regression techniques that are widely explored on the literature and they state that GP models can capture complex nonlinear and multivariable interactions as well as multiresolution trends of energy behaviour thanks to the Bayesian approach under which they are developed.

D. Model Accuracy Metrics

To assess model accuracy, this work uses two metrics: the mean absolute percentage of error (MAPE) and the coefficient of variation of the root mean squared error (CVRMSE). The MAPE metric has been used in a wide number of electricity prediction studies [29], [30]. It expresses the average absolute error as a percentage and is calculated as it follows:

$$MAPE = \frac{1}{n} \sum_{i=1}^n \left| \frac{y_i - \bar{y}_i}{y_i} \right| \times 100,$$

where y_i is the real consumption, \bar{y}_i is the predicted consumption and n is the number of observations.

Also the CVRMSE has often been used in energy prediction studies [31] and will be used also here. It evaluates how much error varies with respect to the actual consumption mean and is calculated as it follows:

$$CVRMSE = \frac{\sqrt{\frac{1}{n-1} \sum_{i=1}^n (y_i - \bar{y}_i)^2}}{\bar{y}} \times 100,$$

E. Savings Metrics

To determine energy savings and uncertainty levels from energy efficiency measures, the IPMVP [13] and ASHRAE's Guideline 14 [2] provide three methods. The one that is suitable for our approach is whole-building metering, since it compares the total energy demand or cost during pre-experiment and post-experiments periods.

The predictive baseline models' output is the metered pre-experiment energy use $energy_{pre}$ and uses the so called predictors environmental conditions inputs $inputs_{pre}$ as inputs of the model. The error in reported savings is proportional to the error in the baseline model forecasts.

IV. USE CASE

The reference building in which the proposed procedure has been carried out to generate accurate building models is the Chemistry Faculty of the University of Murcia, which is a building used as a pilot for the H2020 project ENTROPY¹.

The data that is used in order to build and train our baseline corresponds to 1 year worth of data, from February 2016 to February 2017.

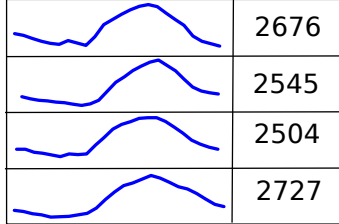


Figure 2: Daily temperature time series input and consumption output. Numbers in Watts hour

A. Black-box approach

Our black-box methodology is highly versatile with respect to the input data i.e., it allows the addition of variables with minimal effort. We started them method on a constructive way by relating the 24 temperature values of each day with the energy consumption of the building (see Fig. 2).

Having introduced the daily temperature time series, we considered that the addition of a categorical variable indicating season was irrelevant. The subject building has several features that are typical of educational buildings: the load on weekends is substantially lower than the load on weekdays and there are also differences among week days (mainly Fridays). In those terms, we used analysis of variance (ANOVA) in order to determine whether there exist differences between the consumption of the different days of the week ($p\text{-value} = 0.001 < 0.05$). In a **post-hoc** test, the conclusion is that we can consider that Fridays have a different behaviour than the rest of the days of the week, this could be due to lower occupation. With this knowledge, we considered necessary to add a dichotomus variable that indicates the kind of day of the week. Weekends and holidays consumption is estimated with the mean of the previous weekends and holidays.

The algorithms that we found relevant to use within our black-box methodology are: Support Vector Regression (SVR), Regression Forest (RF) and Extreme Gradient Boosting (XGB).

SVR works in a similar fashion to Support Vector Machines (SVM). Whereas SVM is a classification technique, SVR fits the optimal curve out of which the training data do not deviate more than a small number ϵ . More specifically,

during classification the samples that are close to the margin are penalised even if they are correctly classified, whereas in the regression method an acceptable deviation margin of the samples from the prediction curve is set. The free parameter of this model is C , the penalty parameter of the error term. C is the weight of how much samples inside the margin contribute to the overall error.

Regression Forest is a type of ensemble learning method, where a group of weak models combine to form a more powerful model. In Regression Forest multiple regression trees are grown. In order to predict a new observation, each tree gives its own prediction and then the average of the output of each one is taken. The algorithm works growing a tree from each random with replacement samples taken from the training. For each node, m_{try} variables are selected at random out of the number of inputs. The best split on these m_{try} is used to split the node. The hyperparameter of Regression Forest that we will search for is the number of random variables that are taken into account on every split: m_{try} .

XGB is built on the principles of gradient boosting and designed for speed and performance (from where it comes the term “extreme”). Gradient Boosted Regression is a technique that generates a prediction through an ensemble of weak prediction models, decision trees in our case. The concept is to sequentially build the model by fitting a weak prediction model on the weighted training data set, where the higher weights are assigned on samples that were previously difficult to predict.

The free parameters that are adjusted in this model are the maximum depth limit of number of nodes in the tree, the minimum number of samples required to split an internal node and the learning rate by which the contribution of each tree is shrunk.

For the sake of comparison, we are using also the Gaussian Process for modelling the instantaneous consumption prediction using the current input values (mean daily temperature for daily consumption or mean hourly temperature for hourly consumption).

B. Grey-box approach

In the case of our grey-box methodology, a topology was selected that could represent the building adequately.

Once the system was defined, an optimisation algorithm was used to find the values that minimise the RMSE (10 minutes intervals) of the simulated power consumption. To ensure that the data was used adequately, the total electricity consumption was separated onto an un-seasonal component and a seasonal one. The un-seasonal component was used as electric loads and the seasonal component was considered as the heating and cooling load. The building is equipped with a boiler and radiators network that contribute to some of the heating loads. To take into account this effect, the preliminary estimation was done using the summer period. From that, the

¹<http://entropy-project.eu/>

heating portion that is given by radiators was extracted. This ratio was used in the consecutive calculations.

The optimisation method to find the parameters of the model was the simplex. method. The termination criteria was to get a change on the solution smaller than 0.01 in all parameters.

C. Results

The prediction metrics are summarised on Table I. The first three methods: SVR, RF, XGB belong to the group of black-box models and are blind to the physics of the problem. Also we have the TWT the GP and the Grey-box model the later with information about the physical phenomenon on the model topology. As it can be seen, they return the best results compared to the Gaussian method, that is applied in a more traditional way, that is relating the instantaneous consumption measurement with the instantaneous inputs measurements and also with our grey-box model approach.

Between the three black-box methods, Random Forest is the one that stands out getting a CVRMSE of 9 and 5 % and a MAPE of 6, 4.5 % for the daily and weekly predictions respectively. We have plotted the prediction vs the real daily consumption in Fig. 3 and weekly in Fig. 4 .

Table I: Metrics

		Models					
		SVR	RF	XGB	TWT	Gauss	Grey
Daily	CVRMSE	12.4	9	11	14.9	17.45	33.57
	MAPE	7.2	6	7.3	12.3	15.01	43.02
Weekly	CVRMSE	6.4	5	6.2	11.1	16.3	19.53
	MAPE	5.2	4.5	5.5	9.4	12.3	15.48

V. DISCUSSION

As previously mentioned, this paper aims to evaluate if the fact that the RC-networks on the grey-box inverse modelling contains basic information about the physical system (i.e. how the thermodynamics of the building should be) deliver any advantage for energy consumption prediction of a smart building for measurement and verification purposes. To this aim, they were compared to our proposed state-of-the-art black-box method in which no prior high level information about the system is included (i.e. they are blind to the physics of the problem) and that combines statistical analysis and machine learning techniques.

We have shown that using the daily temperature time series we are able to capture the behaviour of the people better than if instantaneous values are used for predicting consumption (Gaussian) or if we use a barrage of coefficients in linear regression for modelling each small part of the day (TWT).

This result could in some aspect have been anticipated, energy consumption is a phenomenon heavily dominated by human behaviour. The physics of the building can capture

the response of passive elements such as walls and windows, but behavioural patterns are out of their scope.

A drawback of the baseline data-driven models is that they neglect the correlation between timestamps. TWT creates artificial features in order to model each moment independently. We understand the input data as time series and we are considering in an indirect way all the interactions that building and temperature experience towards consumption. Also, the application of regression techniques have to be preceded by the assessment of the assumptions that have to be fulfilled: normality, little multicollinearity, no auto correlation and homocedasticity. However, a black-box models does not need such assumptions.

That way, we have created a methodology where the combination of time series and current state variables is possible and provides a wide variety of techniques related to time series that can be used to improve the results of the analysis.

VI. CONCLUSIONS AND FUTURE WORK

After applying all the baseline models, grey-box approach and black-box approach we have seen that black-box models overcome the rest.

It is foreseen, a future research avenue consists on the application of the same models to several buildings that share some characteristics. That is, they belong to the same environment: different faculties of a university (where students and professors behave similarly among buildings), several houses of a neighbourhood or different commercial buildings of the same city.

Reducing the total time required for EM&V is key to scaling the deployment of energy efficiency projects in general, and reducing overall costs [32]. That is why a transfer learning approach has to be considered in future studies in order to reduce the quantity of data that needs to be collected for creating a reasonable building model.

Also, a wider study on the way of introducing the time series to the algorithms should be done. That means, applying time series segmentation and representation techniques for finding more representative ways of introducing the data. Or also considering feature selection techniques.

Overall, we believe that the work reported on this paper has explored yet another discipline in which data-driven methods are overweighting traditional methods based on the physics. The results once more demonstrate, that data science can provide an as good or better answer than physically informed approaches.

ACKNOWLEDGEMENTS

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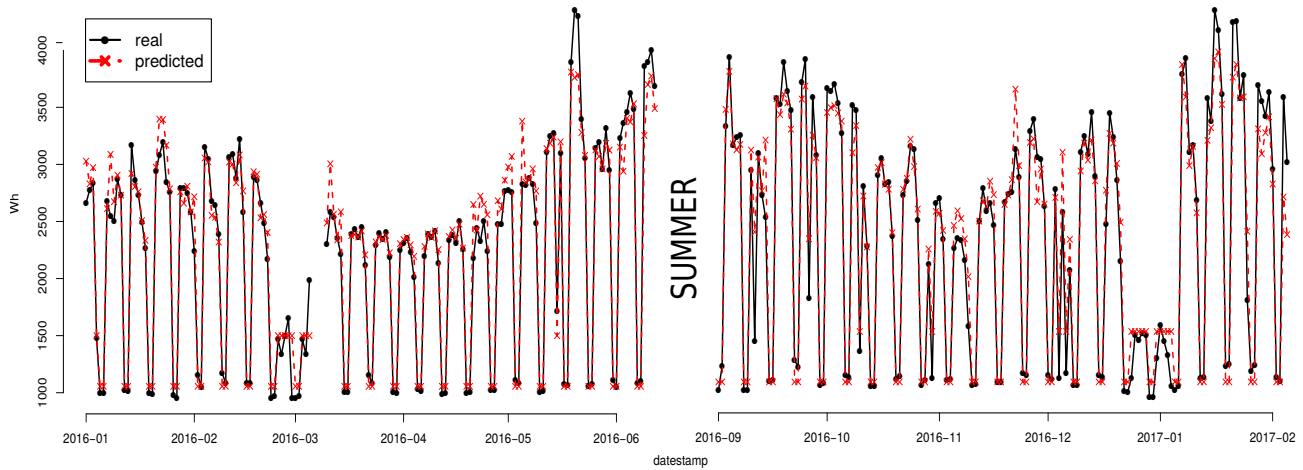


Figure 3: Daily predictions using RF and real consumption

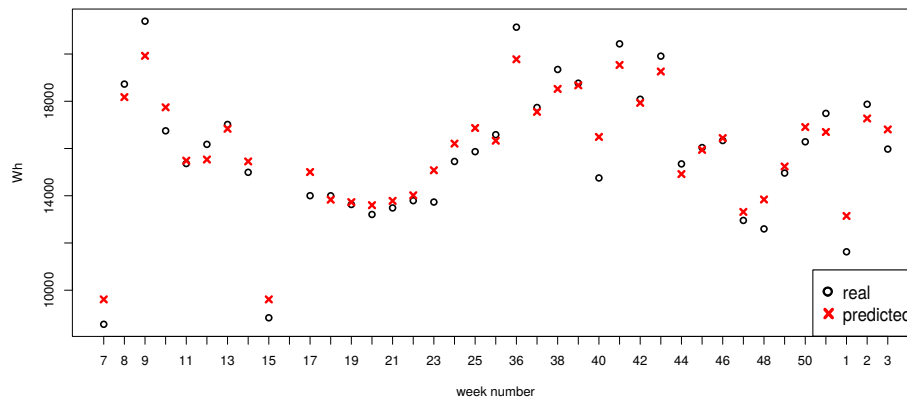


Figure 4: Weekly predictions using RF and real consumption

REFERENCES

- [1] L. Pérez-Lombard, J. Ortiz, and C. Pout, "A review on buildings energy consumption information," *Energy and buildings*, vol. 40, no. 3, pp. 394–398, 2008.
- [2] "Monthly energy review," *U.S. Energy Information Administration*, September, 2017.
- [3] A. S. Committee *et al.*, "Ashrae guideline 14, measurement of energy and demand savings. atlanta.," 2002.
- [4] A. P. Ramallo-González, M. Brown, and D. A. Coley, "Identifying the ideal topology of simple models to represent dwellings."
- [5] Y. Heo and V. M. Zavala, "Gaussian process modeling for measurement and verification of building energy savings," *Energy and Buildings*, vol. 53, pp. 7–18, 2012.
- [6] EC, "Benchmarking smart metering deployment in the eu-27 with a focus on electricity," *Report from the Commission*, 2014.
- [7] F. Terroso-Saenz, A. González-Vidal, A. P. Ramallo-González, and A. F. Skarmeta, "An open iot platform for the management and analysis of energy data," *Future Generation Computer Systems*, 2017.
- [8] E. Fotopoulou, A. Zafeiropoulos, F. Terroso-Sáenz, U. Şimşek, A. González-Vidal, G. Tsiolis, P. Gouvas, P. Liapis, A. Fensel, and A. Skarmeta, "Providing personalized energy management and awareness services for energy efficiency in smart buildings," *Sensors*, vol. 17, no. 9, p. 2054, 2017.
- [9] N. Mogles, I. Walker, A. P. Ramallo-González, S. Lee, J. and Natarajan, J. Padget, E. Gabe-Thomas, T. Lovett, S. Ren, G. and Hyniewska, E. O'Neill, R. Hourizi, and D. Coley, "How smart do smart meters need to be?" *Building and Environment*, no. 125, pp. 439–450, 2017.
- [10] X. Li and J. Wen, "Review of building energy modeling for control and operation," *Renewable and Sustainable Energy Reviews*, vol. 37, pp. 517–537, 2014.
- [11] D. B. Crawley, L. K. Lawrie, F. C. Winkelmann, W. F. Buhl, Y. J. Huang, C. O. Pedersen, R. K. Strand, R. J. Liesen, D. E. Fisher, M. J. Witte *et al.*, "Energyplus: creating a new-generation building energy simulation program," *Energy and buildings*, vol. 33, no. 4, pp. 319–331, 2001.
- [12] "Thermal energy system specialists," <http://www.trnsys.com>, accessed: 2017-09-30.

- [13] D. B. Crawley, J. W. Hand, M. Kummert, and B. T. Griffith, "Contrasting the capabilities of building energy performance simulation programs," *Building and environment*, vol. 43, no. 4, pp. 661–673, 2008.
- [14] M. Braun, H. Altan, and S. Beck, "Using regression analysis to predict the future energy consumption of a supermarket in the uk," *Applied Energy*, vol. 130, pp. 305–313, 2014.
- [15] A. Ahmad, M. Hassan, M. Abdullah, H. Rahman, F. Hussin, H. Abdullah, and R. Saidur, "A review on applications of ann and svm for building electrical energy consumption forecasting," *Renewable and Sustainable Energy Reviews*, vol. 33, pp. 102–109, 2014.
- [16] L. Ciabattoni, M. Grisostomi, G. Ippoliti, and S. Longhi, "Fuzzy logic home energy consumption modeling for residential photovoltaic plant sizing in the new italian scenario," *Energy*, vol. 74, pp. 359–367, 2014.
- [17] A. F. Handbook, "American society of heating, refrigerating and air-conditioning engineers," *Inc.: Atlanta, GA, USA*, 2017.
- [18] G. Burnand, "The study of the thermal behaviour of structures by electrical analogy," *British Journal of Applied Physics*, vol. 3, no. 2, p. 50, 1952.
- [19] D. Coley and J. Penman, "Second order system identification in the thermal response of real buildings. paper ii: recursive formulation for on-line building energy management and control," *Building and Environment*, vol. 27, no. 3, pp. 269–277, 1992.
- [20] P. Bacher and H. Madsen, "Identifying suitable models for the heat dynamics of buildings," *Energy and Buildings*, vol. 43, no. 7, pp. 1511–1522, 2011.
- [21] A. P. Ramallo-González, M. Brown, E. Gabe-Thomas, T. Lovett, and D. A. Coley, "The reliability of inverse modelling for the wide scale characterization of the thermal properties of buildings," *Journal of Building Performance Simulation*, pp. 1–19, 2017.
- [22] C. Hamzacebi and H. A. Es, "Forecasting the annual electricity consumption of turkey using an optimized grey model," *Energy*, vol. 70, pp. 165–171, 2014.
- [23] S. Aman, M. Frincu, C. Charalampos, U. Noor, Y. Simmhan, and V. Prasanna, "Empirical comparison of prediction methods for electricity consumption forecasting," *University of Southern California, Tech. Rep*, pp. 14–942, 2014.
- [24] A. González-Vidal, V. Moreno-Cano, F. Terroso-Sáenz, and A. F. Skarmeta, "Towards energy efficiency smart buildings models based on intelligent data analytics," *Procedia Computer Science*, vol. 83, pp. 994–999, 2016.
- [25] Z. Ruijin, P. Yiqun, H. Zhizhong, and W. Qiuqian, "Building energy use prediction using time series analysis," in *Service-Oriented Computing and Applications (SOCA), 2013 IEEE 6th International Conference on*. IEEE, 2013, pp. 309–313.
- [26] J. K. Kissock, T. A. Reddy, and D. E. Claridge, "Ambient-temperature regression analysis for estimating retrofit savings in commercial buildings," *Journal of Solar Energy Engineering*, vol. 120, no. 3, pp. 168–176, 1998.
- [27] J. L. Mathieu, P. N. Price, S. Kiliccote, and M. A. Piette, "Quantifying changes in building electricity use, with application to demand response," *IEEE Transactions on Smart Grid*, vol. 2, no. 3, pp. 507–518, 2011.
- [28] J. Granderson, S. Touzani, C. Custodio, M. D. Sohn, D. Jump, and S. Fernandes, "Accuracy of automated measurement and verification (m&v) techniques for energy savings in commercial buildings," *Applied Energy*, vol. 173, pp. 296–308, 2016.
- [29] C. Fan, F. Xiao, and S. Wang, "Development of prediction models for next-day building energy consumption and peak power demand using data mining techniques," *Applied Energy*, vol. 127, pp. 1–10, 2014.
- [30] R. E. Edwards, J. New, and L. E. Parker, "Predicting future hourly residential electrical consumption: A machine learning case study," *Energy and Buildings*, vol. 49, pp. 591–603, 2012.
- [31] F. L. Quilumba, W.-J. Lee, H. Huang, D. Y. Wang, and R. L. Szabados, "Using smart meter data to improve the accuracy of intraday load forecasting considering customer behavior similarities," *IEEE Transactions on Smart Grid*, vol. 6, no. 2, pp. 911–918, 2015.
- [32] J. Granderson, P. N. Price, D. Jump, N. Addy, and M. D. Sohn, "Automated measurement and verification: Performance of public domain whole-building electric baseline models," *Applied Energy*, vol. 144, pp. 106–113, 2015.