



Departamento de  
Ingeniería de la Información  
y las Comunicaciones

UNIVERSIDAD DE  
MURCIA



Computer Sciences Faculty, University of Murcia

# A combination of multi and univariate anomaly detection in urban irrigation systems

EDiS' 2022 : 3rd international conference on Embedded & Distributed Systems

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# Introduction and Motivation

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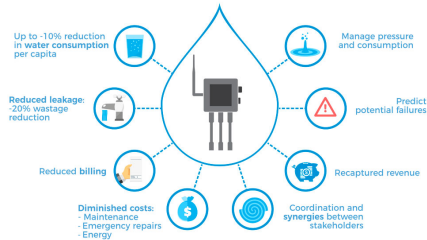
## Water scarcity



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Water scarcity is a global concern that requires a more intelligent way to manage the water network

### BENEFITS OF SMART WATER SOLUTIONS



Automated and intelligent decision support systems that employ data analytic advances to analyze in real-time the anomalies and problems that appear in water usage are needed

Image:

<https://www.libelium.com/libeliumworld/quick-report-smart-water-iot-solutions-to-fight-against-climate-change-and-scarcity/>

# Introduction and Motivation

## Aim



Smart water meters periodically collect measurements of water consumption: multivariate time series

Anomaly detection purposes:

- ▶ Water quality
- ▶ Changes in consumption revealing leaks, device/meter failure, illegal water use, warning situations

Problem: anomalies are rarely annotated → A methodology based on unsupervised methods is needed

## Background and related work



### ► Kind of input data

- A univariate time series  $X = \{x_t\}_{t \in T}$  is an ordered set of real valued observations, where each observation is recorded at a specific time  $t$
- A multivariate time series  $\mathbf{X} = \{\mathbf{x}_t\}_{t \in T}$  is an ordered set of  $k$ -dimensional vectors, each of which is recorded at a specific time  $t$  and consists of  $k$  real-valued observations,  $x_t = (x_{1t}, \dots, x_{kt})$ .

### ► Kind of outlier

- An point outlier  $x_t$  it behaves differently than what it was expected as follows:  $|x_t - \hat{x}_t| > \delta$
- Pattern-wise outliers are a set of consecutive points in time whose joint behaviour is unusual: basic shapelet, seasonality changes and trend alternations

# Background and related work

Related work - anomaly detection in water related scenarios



- ▶ Water usage anomalies in households using DBSCAN and K-means
- ▶ Punctual anomalous water consumption using STL decomposition and Seasonal Hybrid ESD Test
- ▶ Manually spike, jump and drift outliers comparing multivariate and univariate supervised methods

Existent approaches normally chose a strategy that is either multivariate or univariate and therefore, they cannot take advantage of the complex and dynamic behaviour present in water systems



## Methodology and experiments



The water consumption of parks in the city of Murcia, Spain is provided by EMUASA<sup>1</sup>, the Municipal Water and Sanitation Company.

The water meter measurements are present in different granularities (minutely, hourly, daily, and even weekly sometimes). Most water meters have data between the 29th of September, 2017, and 25 of July, 2021.

Challenges:

- ▶ Negative water consumption
- ▶ Change of water meter
- ▶ Different starting and ending days

After cleaning, data was homogenously aggregated every 15 minutes and we count on 283 time series.

The data is huge in volume and dimension → Univariate methods are not feasible → We used a multivariate technique that will tell us for a group of time series, where there has been an anomaly

Methodology:

- ▶ Clustering the parks according to their water consumption,
- ▶ Applying multivariate anomaly detection in each cluster for identifying generally anomalous dates, and
- ▶ Applying univariate anomaly detection for each series in a range close to the previously-detected anomalous dates.

Hierarchical clustering was chosen. Distances - Let  $X_n$  and  $Y_n$  be two time series.

- ▶ Euclidean:

$$d_{L_2}(\mathbf{X}_n, \mathbf{Y}_n) = \left( \sum_{t=1}^n (X_t - Y_t)^2 \right)^{1/2}$$

- ▶ Fréchet:

$$d_F(\mathbf{X}_n, \mathbf{Y}_n) = \min_{r \in M} \left( \max_{i=1, \dots, m} |X_{a_i} - Y_{b_i}| \right)$$

- ▶ DTWARP:

$$d_{DTWARP}(\mathbf{X}_n, \mathbf{Y}_n) = \min_{r \in M} \left( \sum_{i=1, \dots, m} |X_{a_i} - Y_{b_i}| \right)$$

- ▶ Correlation-based:

$$\text{COR}(\mathbf{X}_n, \mathbf{Y}_n) = \frac{\sum_{t=1}^n (X_t - \bar{X}_n) (Y_t - \bar{Y}_n)}{\sqrt{\sum_{t=1}^n (X_t - \bar{X}_n)^2} \sqrt{\sum_{t=1}^n (Y_t - \bar{Y}_n)^2}},$$

where  $M$  is the set of all possible sequences of  $m$  pairs of order-preserving observations and  $\bar{Y}_n$  and  $\bar{X}_n$  are the average of their corresponding series.

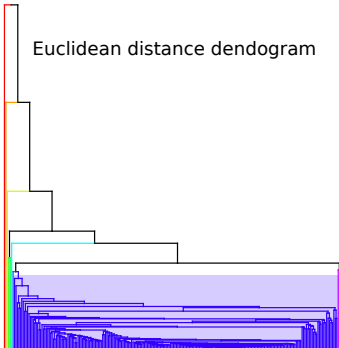
# Methodology and experiments

## Clustering

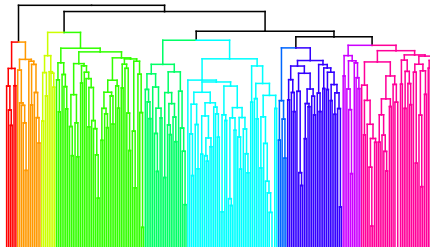


Manual selection of 10 groups. Euclidean  $\sim$  Fréchet and DTW  $\sim$  correlation-based distances

Euclidean distance dendrogram



Correlation distance dendrogram



# Methodology and experiments

## Multivariate Anomaly Detection



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For the multivariate anomaly detection we have used the Vector autoRegression (VAR) model. The formula of the model is as follows:

$$\mathbf{y}_t = \alpha_t + \Phi_1 \mathbf{y}_{t-1} + \dots + \Phi_p \mathbf{y}_{t-p} + \epsilon_t$$

$y_{t-i}$  is the "ith lag" of  $y_t$ .  $\alpha$  is a k-vector of constants serving as the intercept of the model.  $\Phi_i$  is a time-invariant ( $k \times k$ )-matrix and  $\epsilon_t$  is a k-vector of error terms.

As an example the VAR(1) of 3 time series denoted by  $y_{t,1}, y_{t,2}$ , and  $y_{t,3}$  is as follows:

$$y_{t,1} = \alpha_1 + \phi_{11}y_{t-1,1} + \phi_{12}y_{t-1,2} + \phi_{13}y_{t-1,3} + \epsilon_{t,1}$$

$$y_{t,2} = \alpha_2 + \phi_{21}y_{t-1,1} + \phi_{22}y_{t-1,2} + \phi_{23}y_{t-1,3} + \epsilon_{t,2}$$

$$y_{t,3} = \alpha_3 + \phi_{31}y_{t-1,1} + \phi_{32}y_{t-1,2} + \phi_{33}y_{t-1,3} + \epsilon_{t,3}$$

VAR for anomaly detection:

$$SE = \sum_{i=1}^N (y_i - \hat{y}_i)^2,$$

where  $y_i$  are the real values and  $\hat{y}_i$  are the VAR predictions for each observation  $i$ . Then we define a threshold that is:

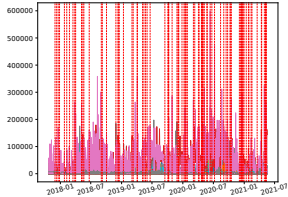
$$threshold = \frac{1}{n} SE + sd(SE),$$

where  $sd$  is the standard deviation. If  $SE \geq threshold \rightarrow \text{ANOMALY}$

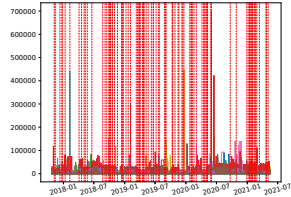
# Methodology and experiments

## VAR

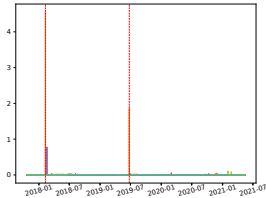
Cluster 3



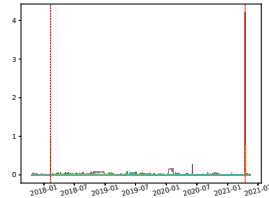
Cluster 4



Cluster 5



Cluster 9





Let  $z_t$  be an ARIMA model, then it is assumed that our series  $y_t$ , which contains  $m$  outliers can be described as:

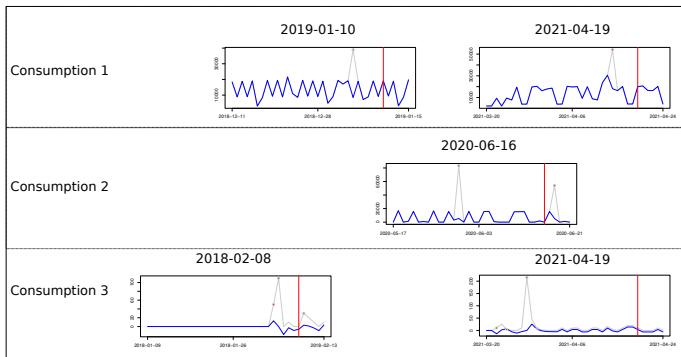
$$y_t = z_t + \sum_{j=1}^m w_j L_j(B) I_{t_j},$$

- ▶ additive outliers
- ▶ level shifts
- ▶ temporary changes
- ▶ innovative outliers
- ▶ seasonal level shift

For further information about how each of the outliers is defined, please check the implementation manual of the R package *tsoutliers* or the original paper "Chen, C., & Liu, L. M. (1993). Joint estimation of model parameters and outlier effects in time series. Journal of the American Statistical Association, 88(421), 284-297"

# Methodology and experiments

## Univariate anomaly detection



## Conclusions

- ▶ We have developed a methodology for unsupervised anomaly detection in IoT deployments
- ▶ We captured general knowledge present in several series through multivariate analysis and then searched for the specific anomalies using univariate analysis
- ▶ Our method is applied for searching anomalies in the irrigation of urban parks, but it is general enough for its use in greater agricultural set-ups



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Questions?

Find this presentation at: [github.com/auroragonzalez/presentations](https://github.com/auroragonzalez/presentations)

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