

# Computational Methods in Physics

Electric Fields and potentials

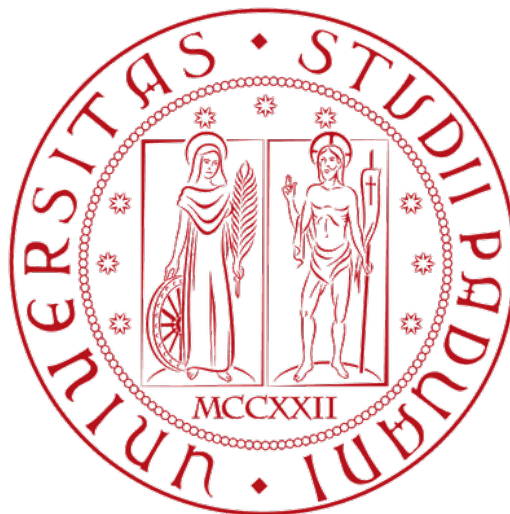
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## 0.1 Introduction

The aim of the program is to simulate electric field and potential in different situations. The options are three (since now): two charges, two conductors, two spheres.

## 0.2 Physics concepts

### 0.2.1 Charges

For a charge  $Q$ , potential and electric fields are basically

$$V = \frac{Q}{4\pi\epsilon_0 \cdot r} \quad E = \frac{Q}{4\pi\epsilon_0 \cdot r^2} \quad (1)$$

where  $\mathbf{r}$  is the distance from the origin of an axis system  $\mathbf{Oxy}$  or  $\mathbf{Oxyz}$ .

Considering that potential and electric field are additive,  $V^{\text{tot}}$  and  $E^{\text{tot}}$  are basically the sum of the ones generated by each charge in the space we are considering.

The plots show what we attend for a configuration where  $Q_1=10$  C,  $Q_2=-10$  C,  $r_1=(1.5,2)$   $r_2=(2,2)$ .

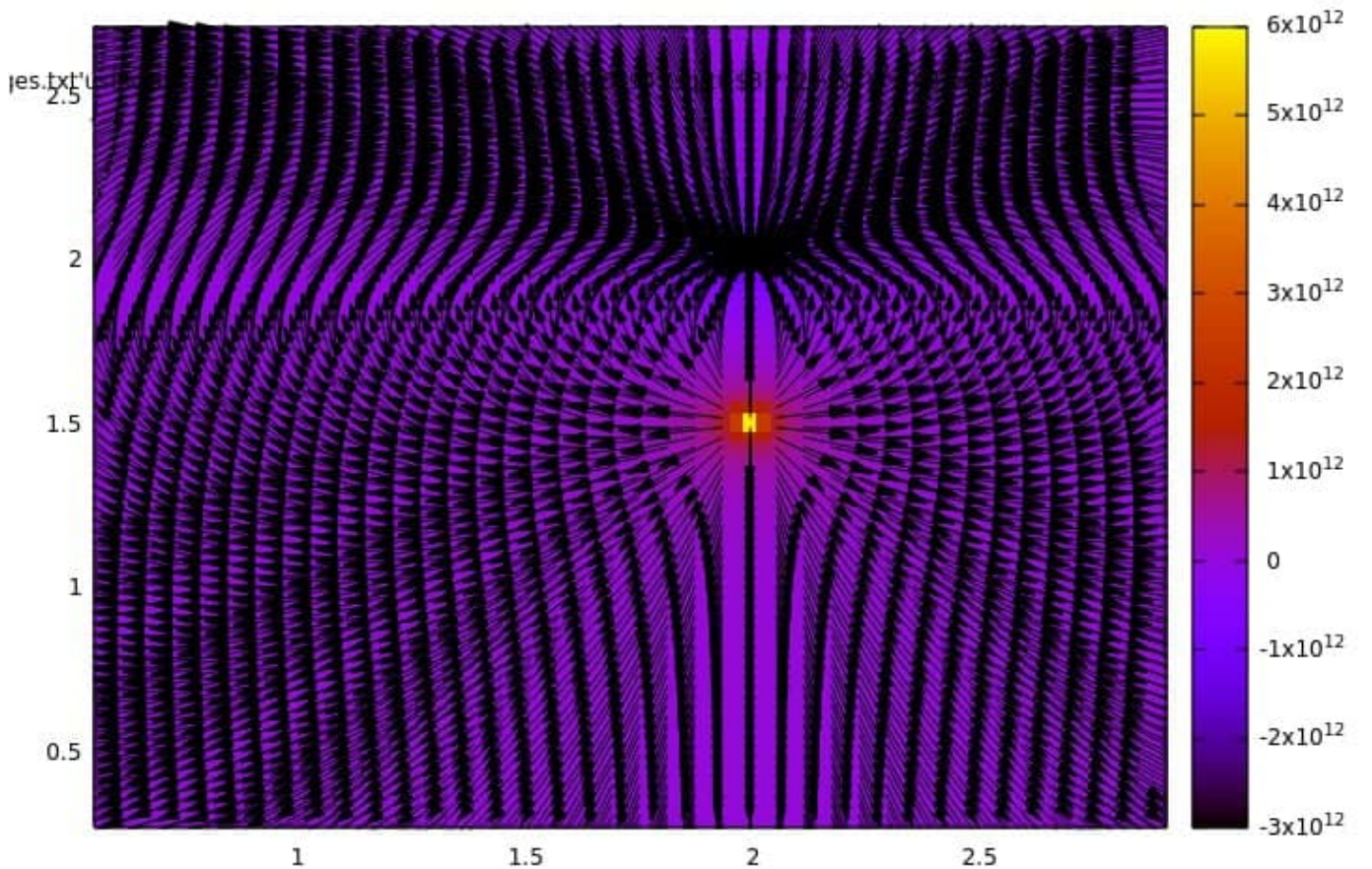


Figure 1: Charges potential and electric field

### 0.2.2 Conductors

For conductors, the situation is similar to the previous one. These objects are characterized by the fact that  $E=0$  inside them.

According to Gauss theorem, for a sphere of radius  $R$  and total charge  $Q$ , we thus obtain

$$E = \begin{cases} \frac{Q}{4\pi\epsilon_0 \cdot r^2} & r \leq R \\ 0 & r > R \end{cases}$$

and, for the potential:

$$V = \begin{cases} \frac{Q}{4\pi\epsilon_0 \cdot R} & r \leq R \\ \frac{Q}{4\pi\epsilon_0 \cdot r^2} & r > R \end{cases}$$

The latter can be demonstrated through the Poisson's theorem, as explained in section [0.2.3].

As for charges, potential and electric field are additive, so the  $E^{\text{tot}}$  and  $V^{\text{tot}}$  are the sum of the contributions of each conductor.

### 0.2.3 Spheres

The situation regarding this case is a little more complicated. According to Poisson's theorem,

$$E = -\nabla V \quad \nabla V = -\frac{\rho}{\epsilon_0} \quad (2)$$

What we have to do, is basically finding a way to compute the potential. Then, by changing its sign and derivating it, we can find the electric field.

In the 2D case, we have to

- create a (x,y) grid;
- set the charge distribution;
- set the border conditions (in my case, border is set to zero);
- after setting a convergence threshold, we use Gauss-Seidel method and compute V.
- by deriving -V, we obtain E=(Ex,Ey).

3D case should be similar, a bit more complicated to program, but similar.

Following these steps, by creating two spheres of centers C1=(4,2) and C2=(7,7), rays r1=1 ua and r2=1 ua, charges  $\rho_1 = 60 \frac{C}{ua^3}$  and  $\rho_2 = -60 \frac{C}{ua^3}$ , we obtain

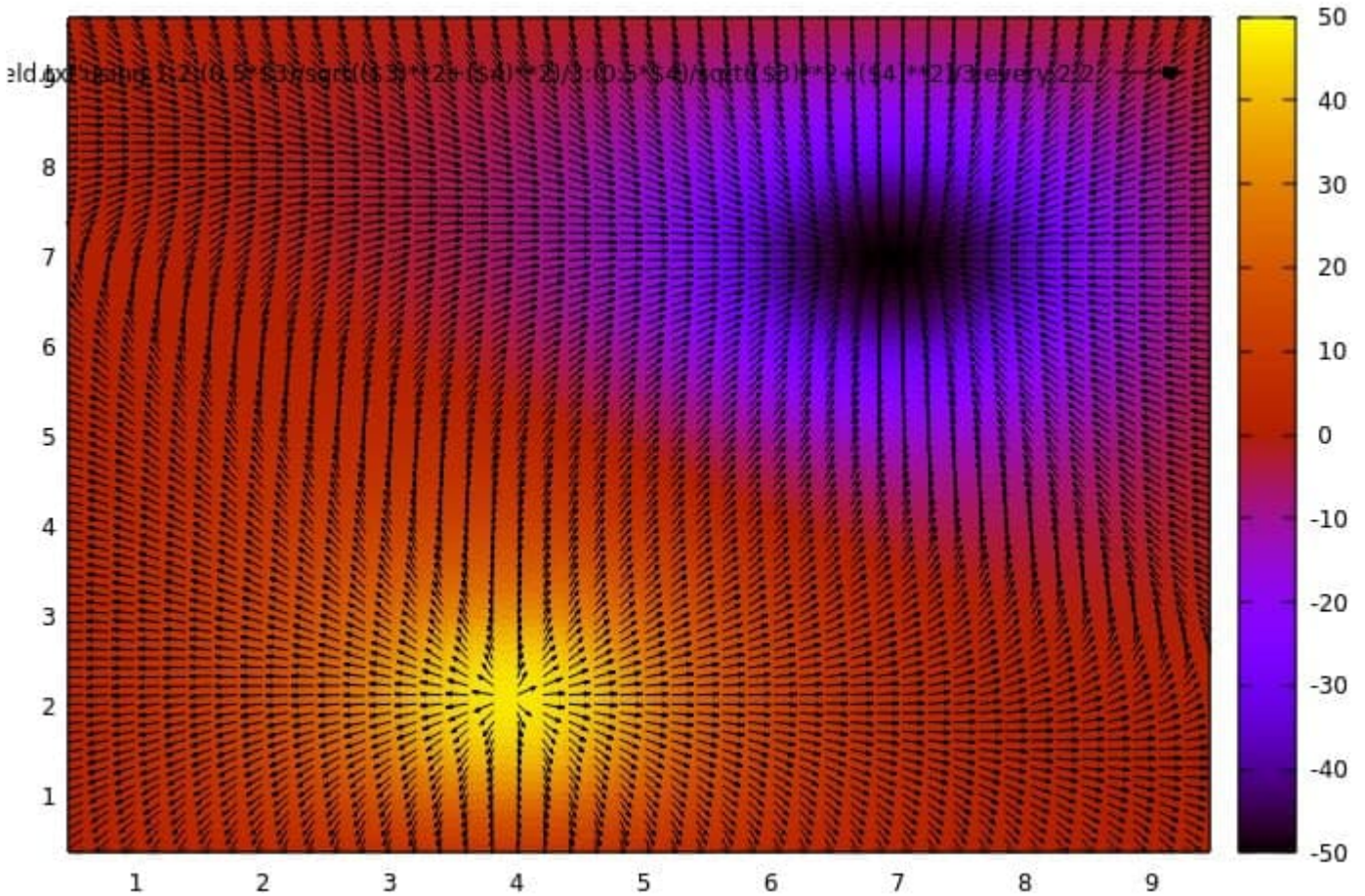


Figure 2: Spheres potential and electric field