

Event-Strategy Analytics

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IIIS has about 40 professors and 70 PhD students across ICT, Eng, Sci and Biz and has expertise in AI, Computer Vision, Robotic, Data Analytics, Cybersecurity, **Formal Verification & Analysis**

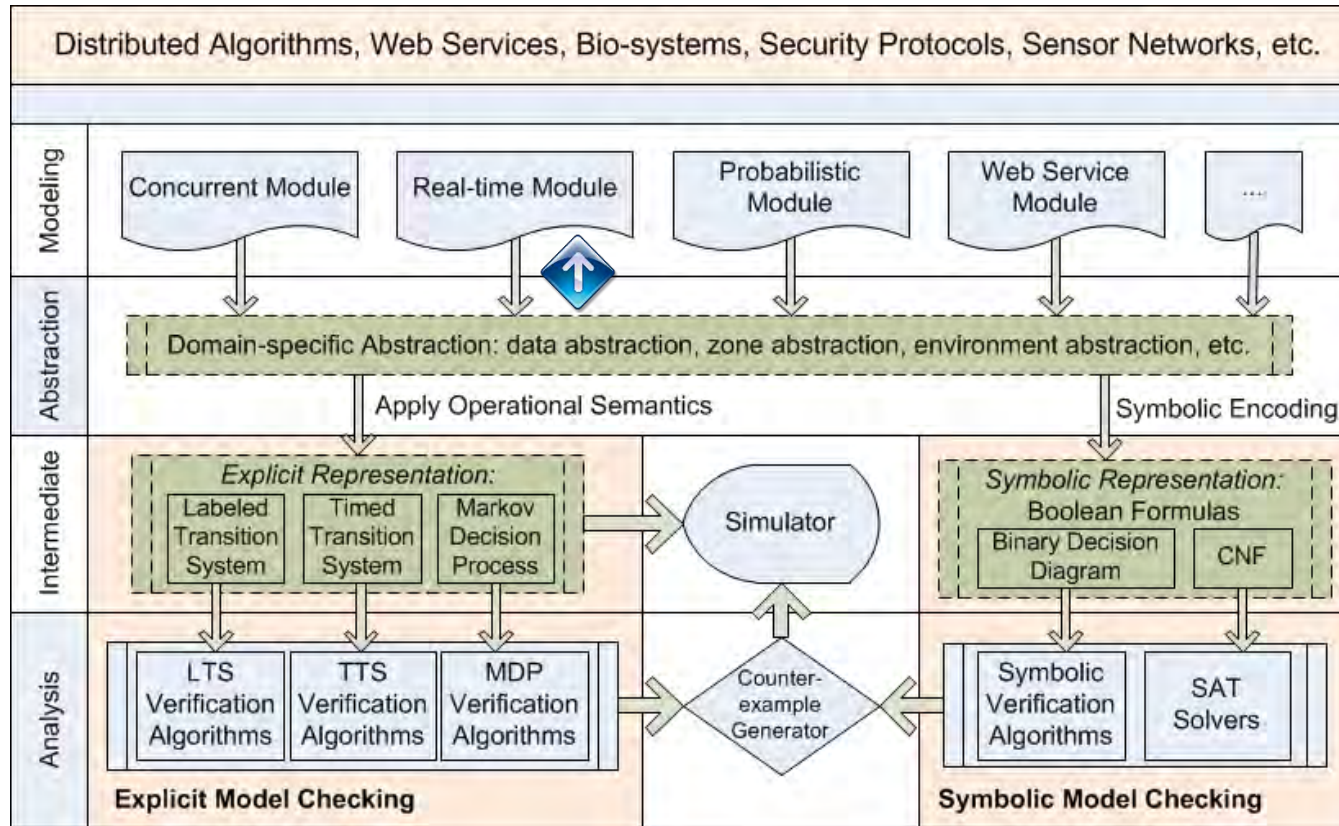
Early Work on Formal Analysis

- 1949 [Alan Turing](#): “Checking Large Routine”
- 1978 [C. A. R. Hoare](#) (1980 Turing Winner). Communicating Sequential Processes: [event based calculus](#) for modelling concurrency and communication.
- 2007 three researchers won ACM Turing Award for inventing model checking, one of them [E. Clarke \(CMU\)](#) has also won Franklin Institute 2014 Bower Award.
 - [successfully applied in industries](#), e.g.,



Past 10 years work on Process Analysis Toolkit (PAT)

(CAV '09'11'13'15, ICSE'08'13,15'16, FM'09'11'12'15, TSE'08'13'15, TOSEM'10'13)



J.Sun, SUTD



Y.Liu, NTU

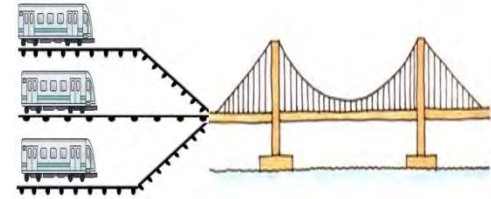


J.S.Dong, NUS

- 1 Million lines of C# code, 15 verification systems, 200+ build in examples, 10 PhDs, 100+ publications
- 3700+ registered users** from **900+ organizations** in **89 countries**, e.g. Microsoft, HP, Sony, Mitsubishi, NTT, Toyota, JAXA ... Commercialised in Japan and thanks to CATS, NII and others

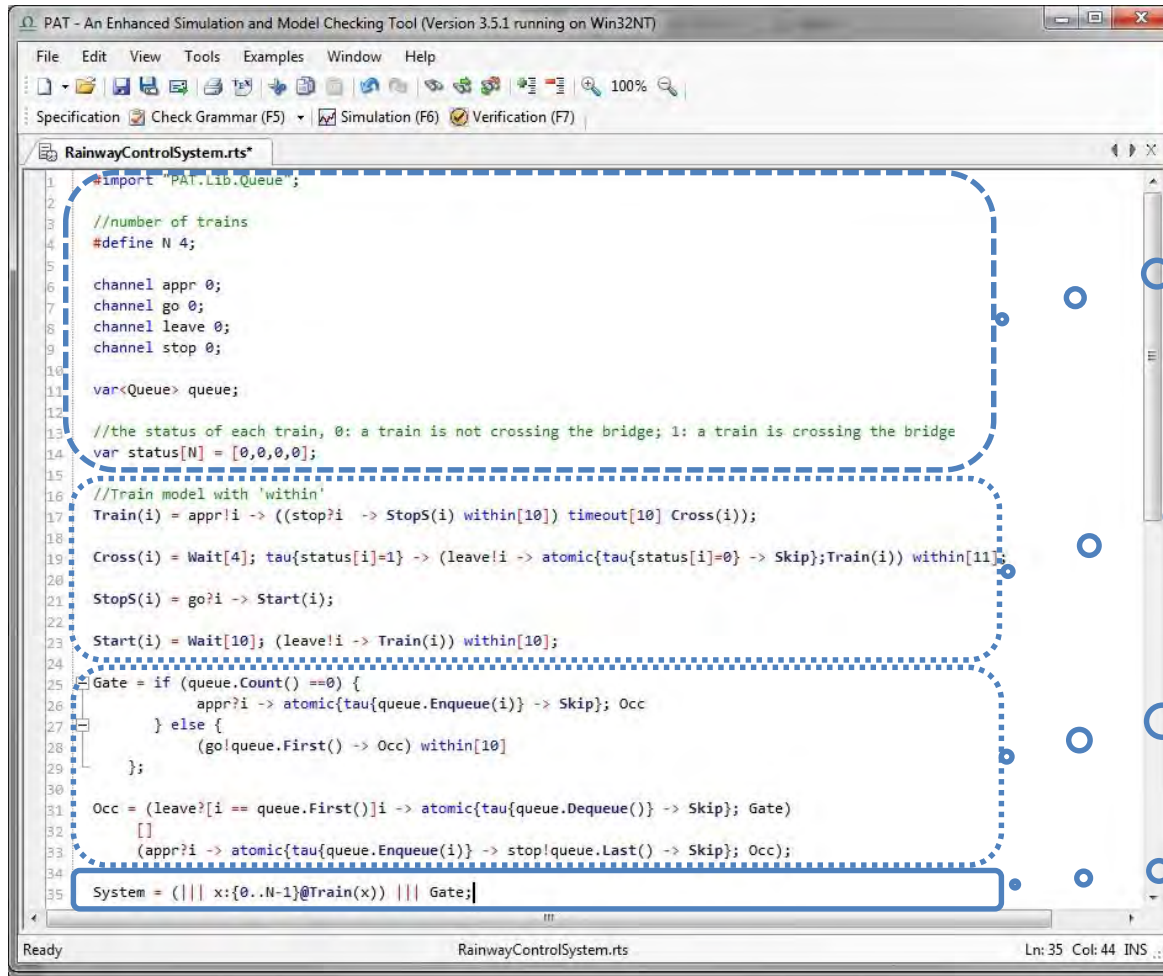


Example: Train Control System



- Problem: to model a railway control system to automatically control trains passing a critical point such as a bridge
 - to use a computer to guide trains from several tracks crossing a single bridge instead of building many bridges
- Safety Property
 - Avoid the situation where more than one train are crossing the bridge at the same time
- How to verify the correctness of such system?
 - Model checking approach and PAT

System Modeling



```
1 #import "PAT.Lib.Queue";
2
3 //number of trains
4 #define N 4;
5
6 channel appr 0;
7 channel go 0;
8 channel leave 0;
9 channel stop 0;
10
11 var<Queue> queue;
12
13 //the status of each train, 0: a train is not crossing the bridge; 1: a train is crossing the bridge
14 var status[N] = [0,0,0,0];
15
16 //Train model with 'within'
17 Train(i) = appr!i -> ((stop?i -> StopS(i) within[10]) timeout[10] Cross(i));
18
19 Cross(i) = Wait[4]; tau{status[i]=1} -> (leave!i -> atomic{tau{status[i]=0} -> Skip};Train(i)) within[11];
20
21 StopS(i) = go?i -> Start(i);
22
23 Start(i) = Wait[10]; (leave!i -> Train(i)) within[10];
24
25 Gate = if (queue.Count() == 0) {
26     appr?i -> atomic{tau{queue.Enqueue(i)} -> Skip}; Occ
27 } else {
28     (go!queue.First() -> Occ) within[10]
29 };
30
31 Occ = (leave?[i == queue.First()]i -> atomic{tau{queue.Dequeue()} -> Skip}; Gate)
32 []
33 (appr?i -> atomic{tau{queue.Enqueue(i)} -> stop!queue.Last() -> Skip}; Occ);
34
35 System = (||| x:{0..N-1}@Train(x)) ||| Gate;
```

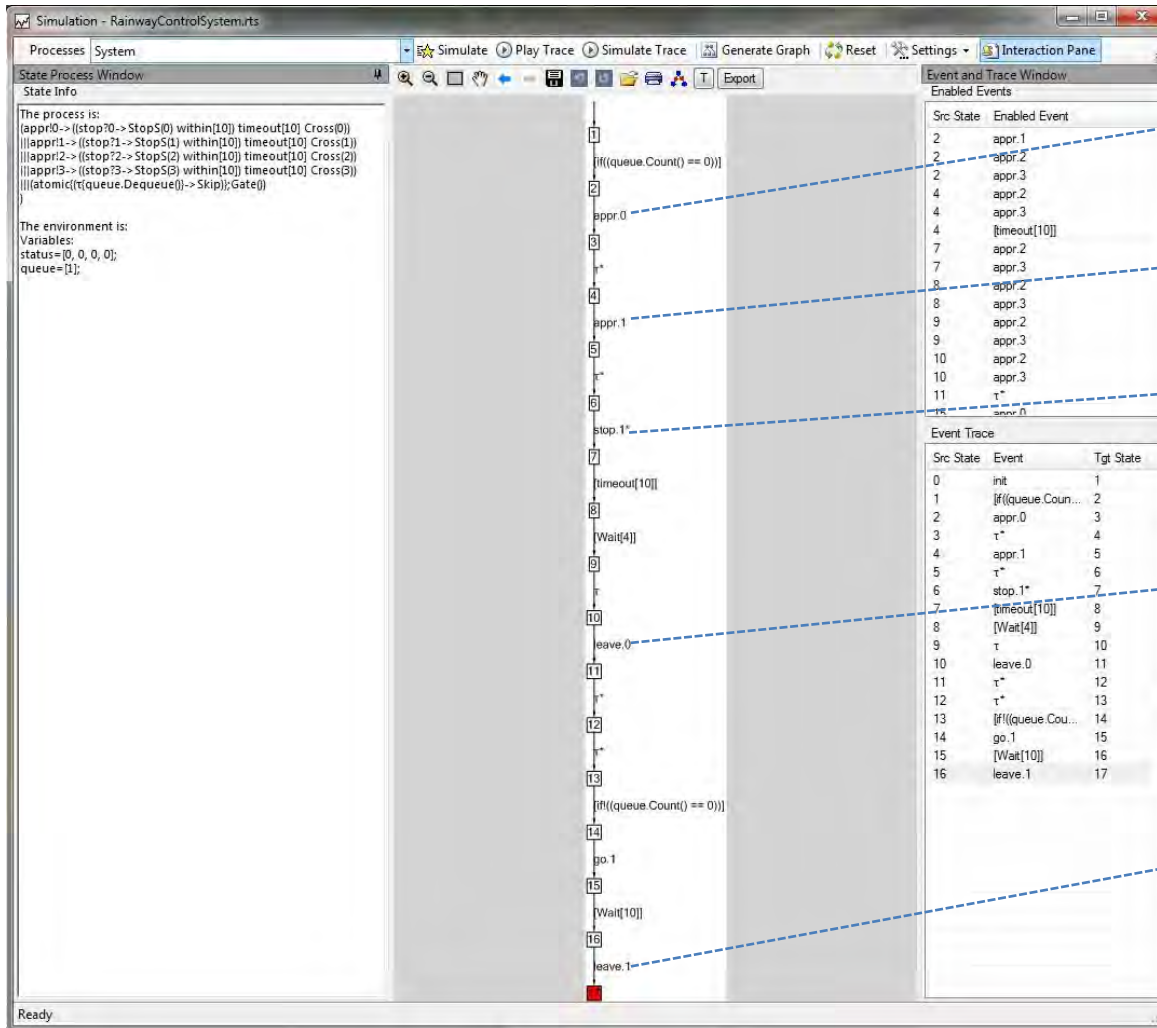
Declaration

Processes for
Train model

Processes for
Controller model

Whole system

Simulation



Train 0 approaches

Train 1 approaches

Train 1 stops

Train 0 crossing the bridge

Train 1 crossing the bridge

Verification

- Safety Property: there can never be more than one train crossing the bridge at the same time

```
#define twoTrainsCrossing ((status[0]==1 && status[1]==1) || (status[0]==1 && status[2]==1)
|| (status[0]==1 && status[3]==1) || (status[1]==1 && status[2]==1)
|| (status[1]==1 && status[3]==1) || (status[2]==1 && status[3]==1));
#assert System reaches twoTrainsCrossing;
```

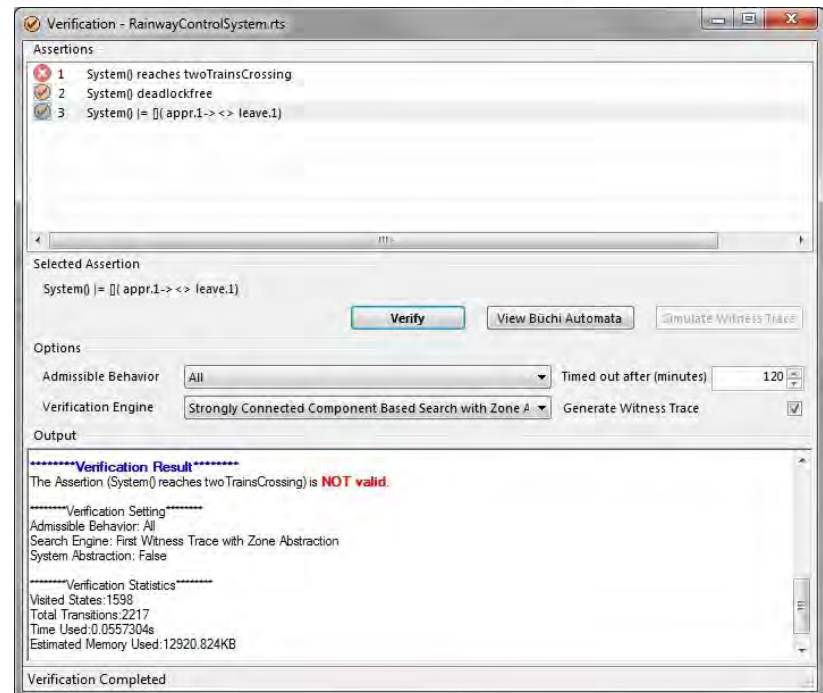
- Other Properties

- Deadlock free

```
#assert System deadlockfree;
```

- Whenever a train approaches the

```
#assert System != [](appr.1 -> <>leave.1);
```



Model Checking for Planning

- *Model Checking as Services for Event Planning, Scheduling, Predication, Decision-Making* [FMSD'14]

Model checking as planning/problem-solving

```
//@@Sliding Game@@
```

```
//The following models the sliding game with the extra 'costs' complexity
```

```
var board[9]:{0..8} = [3,5,6, // 0,1,2 :index  
                        0,2,7, // 3 4 5 :index  
                        8,4,1]; // 6,7,8 :index
```

```
hvar empty:{0..8} = 3; //empty position is a secondary variable, no need to put it in the state space
```

```
var c = 0; // cost utility, e.g. costs 1 for left and right move, 2 for up, 0 for down
```

```
Game() = Left() [] Right() [] Up() [] Down();
```

```
Left() = [empty!=2 && empty!=5 && empty!=8] left // c=c+1  
        {board[empty]=board[empty+1]; board[empty+1]=0; empty=empty+1; c++;} -> Game();
```

```
Right() = [empty!=0 && empty!=3 && empty!=6] right  
         {board[empty]=board[empty-1]; board[empty-1]=0; empty=empty-1; c++;} -> Game();
```

```
Up() = [empty!=6&&empty!=7&&empty!=8] up  
       {board[empty]=board[empty+3]; board[empty+3]=0; empty=empty+3; c=c+2} -> Game();
```

```
Down() = [empty!=0&&empty!=1&&empty!=2] down  
         {board[empty]=board[empty-3]; board[empty-3]=0; empty=empty-3} -> Game();
```

```
#define goal board[0] == 1 && board[1] == 2 && board[2] == 3 &&  
            board[3] == 4 && board[4] == 5 && board[5] == 6 &&  
            board[6] == 7 && board[7] == 8 && board[8] == 0;
```

```
#assert Game() reaches goal with min(c);
```

3	5	6
	2	7
8	4	1

1	2	3
4	5	6
7	8	

The sliding game problem cont'd

8	7	6	8	0	6	8	5	6
0	4	1	5	4	7	7	2	3
2	5	3	2	3	1	4	1	0

(a) Hard1

(b) Hard2

(c) Most1

8	5	4	8	2	1	4	1	7
7	6	3	3	6	4	8	0	3
2	1	0	0	5	7	5	6	2

(d) Most2

(e) Rand1

(f) Rand2

Figure: Initial configurations of *the sliding game problem* instances

Experimental Results

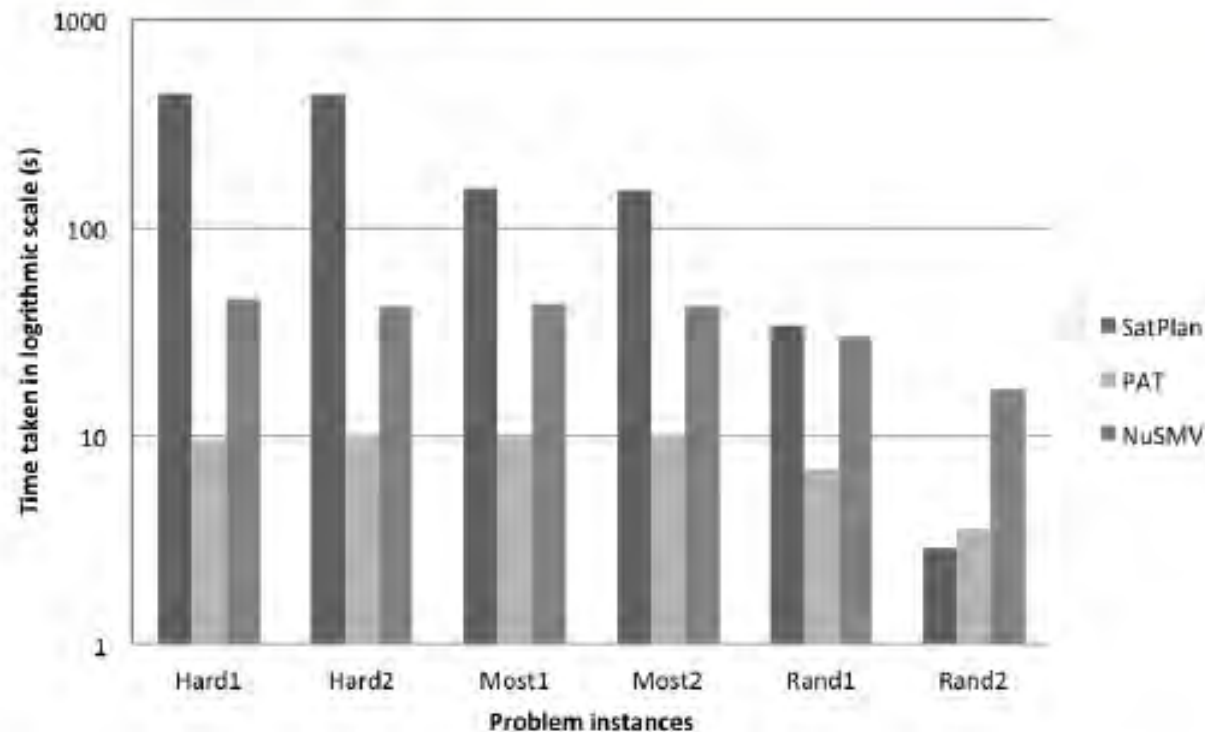
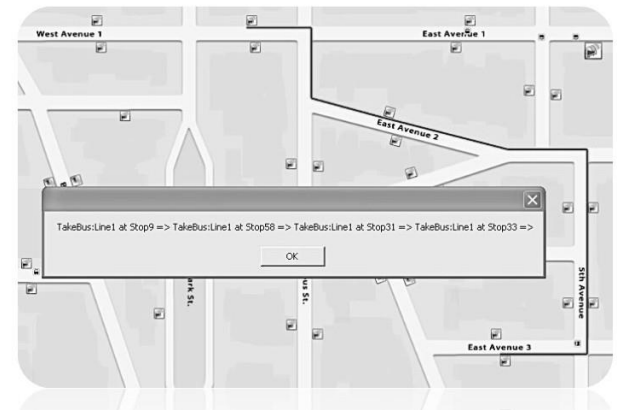


Figure: Execution time comparison of PAT, NuSMV and SatPlan on *the sliding game problem*, shown on a logarithm scale

Model Checking as Planning/Scheduling/Service: Transport4You, an intelligent public transportation manager ICSE 2011 SCORE Competition Project (PAT won FM Award)

- PAT model checker is used not only as a verification tool for the system design but also as a service that computes an optimal travel plan.
- 94 teams from 48 universities in 22 countries started the competition; Two winners (Formal Methods Award and Overall Award) were selected during the conference.

PAT student team won Formal Method Award



Event-Strategy Analytics

- *Proabilistic Model Checking for Predication, Decision-Making*
- *Different from black-box ML based Data Analytics*

Data Analytics is a major IT industry but can lead to **wrong decisions/predications**



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Big data can mean bad analytics, says Harvard professor

by
Linda Tucci
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November 09, 2016

How did the election forecasts get it so wrong?

The [Upshot](#), [FiveThirtyEight](#), [Predictwise](#), etc: their predictions for President varied over the campaign as you'd expect as new data came in, but consistently made Clinton a solid favorite, with a probability of a win topping 70% the day before election day. So what went wrong? As i

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How an algorithm helped global tennis match-fixing investigation

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🕒 27 January 2016 | Tennis


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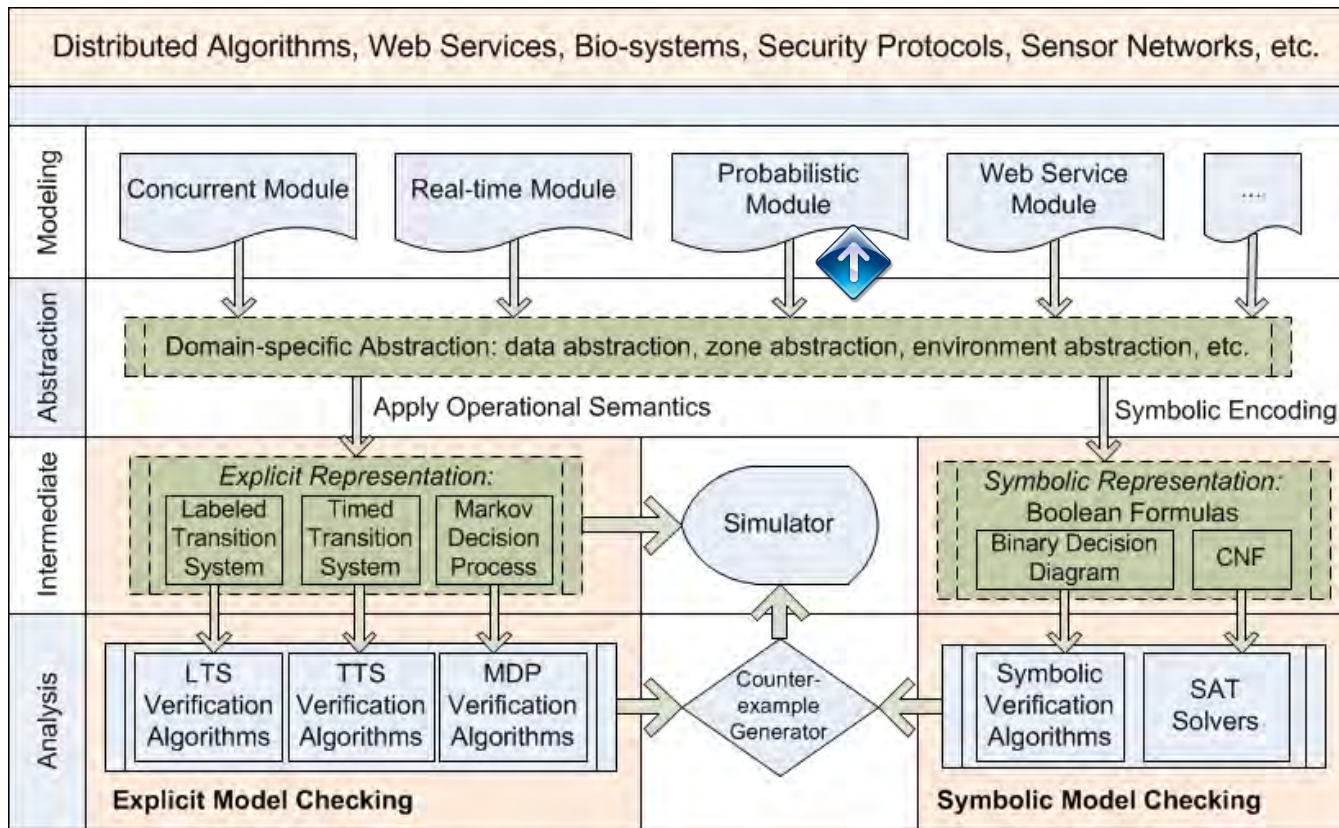
Betting suspended on Australian Open doubles match, players deny fixing

Ravi Ubha, CNN

🕒 Updated 1044 GMT (1844 HKT) January 25, 2016



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Probabilistic Model Checking [CAV'12]

- Syntax
 - Hierarchical concurrent systems with probabilistic choices
- Semantics
 - Markov decision processes
- Given a property, probabilistic model checking returns, instead of true or false
 - the maximum and minimum probability of satisfying the property.

Roger Federer

Rafael Nadal



- 17 Grand Slam
- 302 weeks at #1
- 6 ATP Year End Titles

- 14 Grand Slam
- 141 weeks at #1
- 0 ATP Year End Titles

Before 2017

Roger Federer

Rafael Nadal

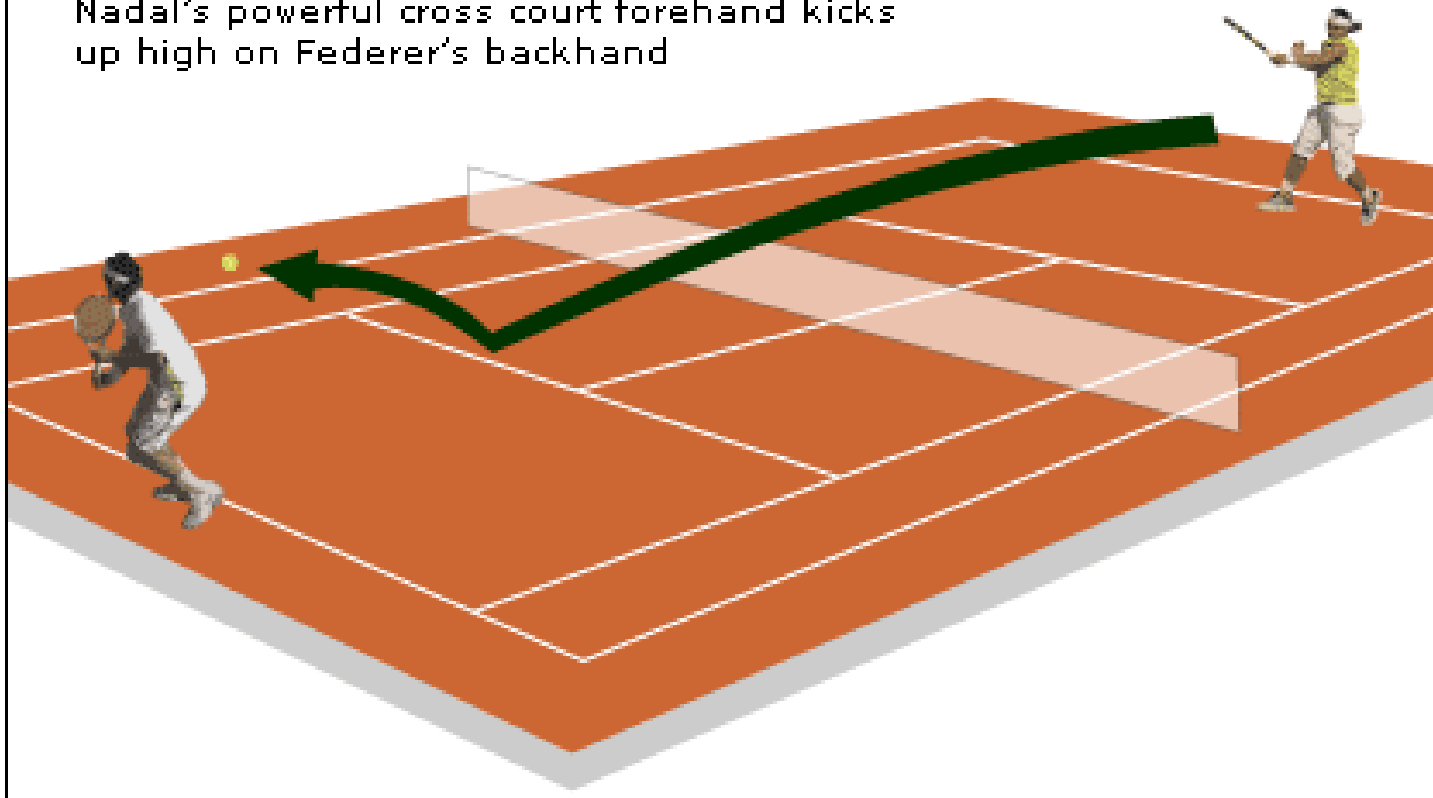


Strategy Analytics

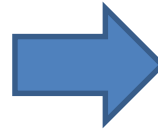
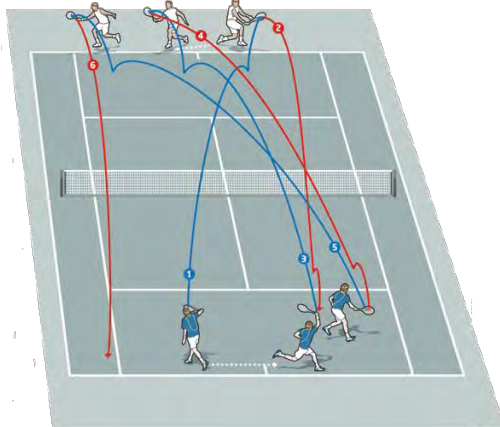
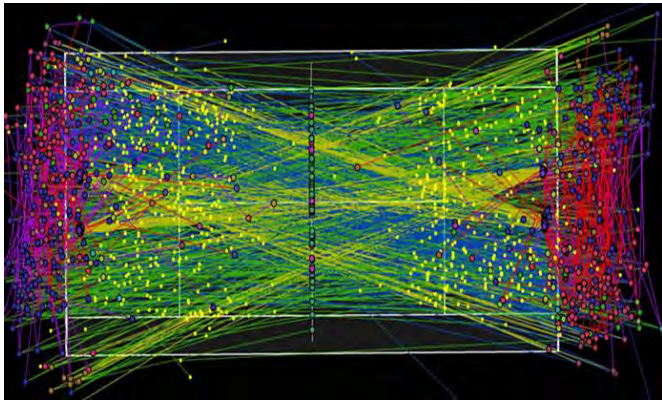
Nadal's strategy

Nadal's most potent weapon

Nadal's powerful cross court forehand kicks up high on Federer's backhand



Model Description



```
//      *****  
//      Player1: Right Handed  
// de_ct  ad_ct  
// -----+-----  
// |      |      |  
// |  1    |  2    |  
// |      |      |  
// |=====|  
// |      |      |  
// |  3    |  4    |  
// |      |      |  
// -----+-----+  
// ad_ct  de_ct  
//      Player2: Right Handed  
//      *****
```

Building a PAT Location based MDP model



```

    Federer
de_ct  ad_ct
-----+----- baseline
|  1  |  2  |
|-----|-----| service line
|  3  |  4  |
|=====| net
|  5  |  6  |
|-----|-----| service line
|  7  |  8  |
-----+----- baseline

```



```

    Nadal
ad_ct  de_ct
"9" represents net error or
hit outside

```

```

enum{f_ad_ct, n_ad_ct, f_de_ct, n_de_ct};
//serve position: ad court or deuce court

```

```

enum{federer, nadal, na};

```

```

var turn = na; //serve turn;
var fscore = 0;
var nscore = 0;
var won = na;
var ball = 9;

```

```

WhoServe1st = []i:{f_de_ct,n_de_ct}@
              TossCoin{turn = i} -> Skip;

```

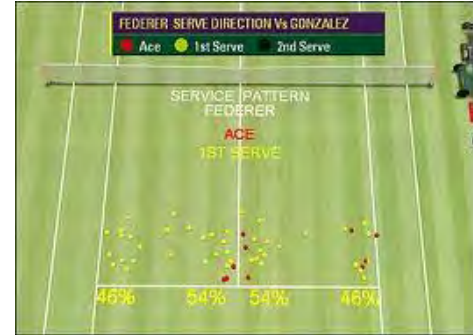
```

TieBreakGame = WhoServe1st;
               (FedererServe [] NadalServe);

```

Probability distribution on Federer Serve

(parameters are based on the last 4 years online data)



```
De_Fed1stServe = pcase {
  23: ServeT_in{ball= 6} -> NadForehandR
  15: ServeT_err{ball=9} -> De_Fed2ndServe
  30: ServeWide_in{ball =6} -> NadBackhandR
  11: ServeWide_err{ball=9} -> De_Fed2ndServe
  14: ServeBody_in{ball=6} -> (NadBackhandR [] NadForehandR)
  7: ServeBody_err{ball=9} -> De_Fed2ndServe};
```

```
De_Fed2ndServe = pcase {
  15: ServeT_in{ball= 6} -> NadForehandR
  3: ServeT_err{ball=9} ->
    Fdoublefault{nscore++; if (nscore == 7) {won = nadal}
    else {if (turn == f_ad_ct){turn = f_de_ct}
    else {turn = n_ad_ct}}}} -> NextPt
  ...
  33: ServeWide_in{ball =6} -> NadBackhandR
  2: ServeWide_err{ball=9} -> ...
  ...
```

```
NextPt = FedererServe [] NadalServe [] ([won != na] GameOver -> Skip);
```

Federer

de_ct	ad_ct
1	2
3	4
5	6
7	8

Nadal

"9" represents hit outside

2014 London RR: Roger Federer vs Andy Murray

Roger Federer d. Andy Murray 6-0 6-1

Use the links below to see dozens of tables displaying detailed data on every aspect of this match. For further context, tour and player averages are visible for most cells when you move your cursor over them. These figures are based on other charted matches, including [265 ATP matches](#), 168 ATP matches on hard, 43 Roger Federer matches (33 on hard), and 18 Andy Murray matches (15 on hard). The more charted matches in the database, the more valuable this project becomes. Please try [charting a match yourself](#).

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Andy Murray: [Serve Breakdown](#) | [Return Breakdown](#) | [Net Points](#) | [Shot Types](#) | [Shot Direction](#)

Full Description !



Server	Sets	Games	Points	
Roger Federer	0-0	0-0	0-0	1st serve down the T, fault (long). 2nd serve to body; backhand return down the middle (very deep); forehand swinging volley down the line (wide), unforced error . (4-shot rally)
Roger Federer	0-0	0-0	0-15	1st serve wide, fault (net). 2nd serve wide; backhand return crosscourt (very deep); backhand down the middle inside-out; backhand crosscourt; forehand inside-in; forehand crosscourt; forehand down the line (net), unforced error .
Roger Federer	0-0	0-0	0-30	1st serve wide, fault (net). 2nd serve to body; backhand return down the middle (very deep); backhand crosscourt; backhand down the middle; forehand crosscourt; forehand down the line; backhand crosscourt; backhand crosscourt; backhand down the middle; forehand crosscourt; backhand crosscourt; backhand slice crosscourt; backhand crosscourt; backhand down the middle; forehand down the middle; backhand crosscourt; backhand down the middle; backhand down the middle; forehand crosscourt; forehand down the line; backhand crosscourt; backhand crosscourt; backhand crosscourt; backhand slice crosscourt; backhand down the line; forehand down the line (net cord); backhand down the line

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Server	Sets	Games	Points
Roger Federer	0-0	0-0	0-15
Roger Federer	0-0	0-0	0-15
Roger Federer	0-0	0-0	0-30



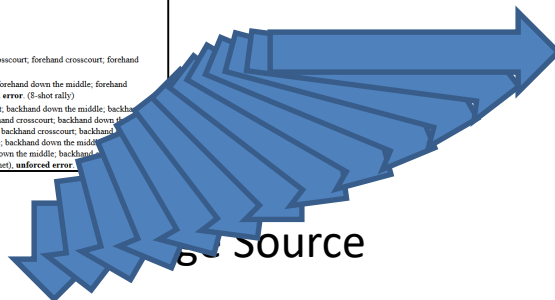
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<script type="text/javascript" src="http://www.minorleaguesplits.com/tennisabstract/jquery.tablesorter.js"></script>
<script language="JavaScript">
```

```
var server = '<table id="reportable" class="tablesorter"><thead><tr><th align="left">SERVE BASICS</th><th align="right">Pts</th><th align="right">Unret--%</th><th align="right">FcdE--%</th><th align="right">=<3W---%</th><th align="right">Wide---%</th><th align="right">RF Total</th><th align="right">36</th><th align="right"><span title="Tour Average: 63%>28 (78%)</span></th><th align="right"><span title="Tour Average: 7%\nHard Average: 8%\nRF Average: 10%\nRF Hard Avg: 10%">0 (0%)</span></th><th align="right"><span title="Tour Average: 3%\nHard Average: 3%\nRF Average: 4%\nRF Hard Avg: 3%">0 (0%)</span></th><th align="right"><span title="Tour Average: 14%\nRF Hard Avg: 14%">3 (8%)</span></th><th align="right"><span title="Tour Average: 34%\nHard Average: 35%\nRF Average: 41%\nRF Hard Avg: 39%">11 (31%)</span></th><th align="right"><span title="Tour Average: 35%\nHard Average: 33%\nRF Average: 39%\nRF Hard Avg: 39%">14 (39%)</span></th><th align="right"><span title="Tour Average: 31%\nHard Average: 36%\nRF Average: 25%\nRF Hard Avg: 26%">14 (39%)</span></th><th align="right"><span title="Tour Average: 71%\nHard Average: 100%">0 (0%)</span></th><th align="right"><span title="Tour Average: 11%\nHard Average: 13%\nRF Average: 16%\nRF Hard Avg: 16%">0 (0%)</span></th><th align="right"><span title="Tour Average: 4%\nHard Average: 5%\nRF Average: 6%\nRF Hard Avg: 5%">0 (0%)</span></th><th align="right"><span title="Tour Average: 18%\nHard Average: 17%">2 (14%)</span></th><th align="right"><span title="Tour Average: 42%\nHard Average: 44%\nRF Average: 53%\nRF Hard Avg: 52%">5 (31%)</span></th><th align="right"><span title="Tour Average: 40%\nHard Average: 40%\nRF Average: 46%\nRF Hard Avg: 46%">6 (43%)</span></th><th align="right"><span title="Tour Average: 37%\nHard Average: 38%\nRF Average: 41%\nRF Hard Avg: 13%">2 (14%)</span></th><th align="right"><span title="Tour Average: 51%\nHard Average: 51%\nRF Average: 57%\nRF Hard Avg: 51%">0 (0%)</span></th><th align="right"><span title="Tour Average: 1%\nHard Average: 1%\nRF Average: 0%\nRF Hard Avg: 0%">0 (0%)</span></th><th align="right"><span title="Tour Average: 6%\nHard Average: 6%\nRF Average: 1%\nRF Hard Avg: 0%">0 (0%)</span></th><th align="right"><span title="Tour Average: 19%\nHard Average: 19%\nRF Average: 22%\nRF Hard Avg: 21%">6 (27%)</span></th><th align="right"><span title="Tour Average: 54%\nHard Average: 56%\nRF Average: 22%\nRF Hard Avg: 28%\nRF Hard Avg: 27%">5 (23%)</span></th><th align="right"><span title="Tour Average: 21%\nHard Average: 21%\nRF Average: 26%\nRF Hard Avg: 25%">5 (23%)</span></th></tr></thead></table>
```

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[illegible]

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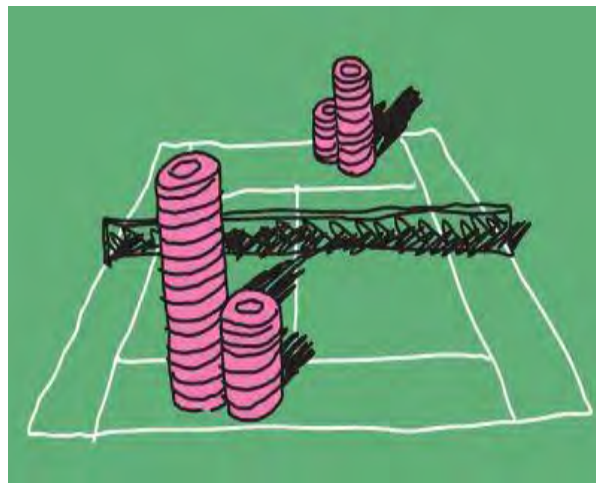
```
var server = '<table id="reportable" class="tablesorter"><thead><tr><th align="left">SERVE BASICS</th><th align="right">Pts</th><th align="right">Unret--%</th><th align="right">FcdE--%</th><th align="right">=<3W---%</th><th align="right">Wide---%</th><th align="right">RF Total</th><th align="right">36</th><th align="right"><span title="Tour Average: 63%>28 (78%)</span></th><th align="right"><span title="Tour Average: 7%\nHard Average: 8%\nRF Average: 10%\nRF Hard Avg: 10%">0</span></th><th align="right"><span title="Tour Average: 3%\nHard Average: 3%\nRF Average: 4%\nRF Hard Avg: 3%">0 (0%)</span></th><th align="right"><span title="Tour Average: 14%\nRF Hard Avg: 14%">3 (8%)</span></th><th align="right"><span title="Tour Average: 34%\nHard Average: 35%\nRF Average: 41%\nRF Hard Avg: 39%">11 (31%)</span></th><th align="right"><span title="Tour Average: 35%\nHard Average: 33%\nRF Average: 39%\nRF Hard Avg: 39%">14 (39%)</span></th><th align="right"><span title="Tour Average: 31%\nHard Average: 36%\nRF Average: 25%\nRF Hard Avg: 26%">14 (39%)</span></th><th align="right"><span title="Tour Average: 71%\nHard Average: 100%">0 (0%)</span></th><th align="right"><span title="Tour Average: 11%\nHard Average: 13%\nRF Average: 16%\nRF Hard Avg: 16%">0 (0%)</span></th><th align="right"><span title="Tour Average: 4%\nHard Average: 5%\nRF Average: 6%\nRF Hard Avg: 5%">0 (0%)</span></th><th align="right"><span title="Tour Average: 18%\nHard Average: 17%">2 (14%)</span></th><th align="right"><span title="Tour Average: 42%\nHard Average: 44%\nRF Average: 53%\nRF Hard Avg: 52%">5 (31%)</span></th><th align="right"><span title="Tour Average: 40%\nHard Average: 40%\nRF Average: 46%\nRF Hard Avg: 46%">6 (43%)</span></th><th align="right"><span title="Tour Average: 37%\nHard Average: 38%\nRF Average: 41%\nRF Hard Avg: 41%">2 (14%)</span></th><th align="right"><span title="Tour Average: 51%\nHard Average: 51%\nRF Average: 57%\nRF Hard Avg: 57%">0 (0%)</span></th><th align="right"><span title="Tour Average: 1%\nHard Average: 1%\nRF Average: 0%\nRF Hard Avg: 0%">0 (0%)</span></th><th align="right"><span title="Tour Average: 6%\nHard Average: 6%\nRF Average: 11%\nRF Hard Avg: 11%">0 (0%)</span></th><th align="right"><span title="Tour Average: 19%\nHard Average: 19%\nRF Average: 22%\nRF Hard Avg: 21%">6 (27%)</span></th><th align="right"><span title="Tour Average: 54%\nHard Average: 56%\nRF Average: 62%\nRF Hard Avg: 28%\nRF Hard Avg: 27%">5 (23%)</span></th><th align="right"><span title="Tour Average: 21%\nHard Average: 21%\nRF Average: 26%\nRF Hard Avg: 25%">5 (23%)</span></th></tr></thead></table>
```



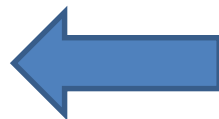

Great Analytics



Correct Prediction



Bet on Market



Profit !!!

Location	Date	WinnerName	LoserName	WinnerOdd	Loserodd	ModelChoice	Winnings
Doha	12/31/2013	Nadal R.	Rosol L.	1.04	11.03	Rosol L.	-100
Melbourne	1/18/2014	Nadal R.	Montils G.	1.11	6.73	Montils G.	-100
Melbourne	1/20/2014	Nadal R.	Nishikori K.	1.03	12.42	Nishikori K.	-100
Melbourne	1/21/2014	Wawrinka S.	Djokovic N.	7.54	1.09	Wawrinka S.	654
Melbourne	1/22/2014	Nadal R.	Dimitrov G.	1.1	7.05	Dimitrov G.	-100
Melbourne	1/22/2014	Federer R.	Murray A.	1.71	2.15	Federer R.	71
Melbourne	1/24/2014	Nadal R.	Federer R.	1.62	2.32	Federer R.	-100
Melbourne	1/26/2014	Wawrinka S.	Nadal R.	5.19	1.17	Wawrinka S.	419
Dubai	2/28/2014	Federer R.	Djokovic N.	4.17	1.22	Federer R.	317
Dubai	3/1/2014	Federer R.	Berdych T.	1.67	2.19	Federer R.	67
Indian Wells	3/16/2014	Djokovic N.	Federer R.	1.55	2.43	Federer R.	-100
Miami	3/25/2014	Federer R.	Gasquet R.	1.12	6.18	Gasquet R.	-100
Miami	3/26/2014	Djokovic N.	Murray A.	1.28	3.62	Murray A.	-100
Miami	3/28/2014	Nadal R.	Berdych T.	1.22	4.22	Berdych T.	-100
Miami	3/30/2014	Djokovic N.	Nadal R.	1.69	2.18	Nadal R.	-100
Monte Carlo	4/18/2014	Ferrer D.	Nadal R.	7.33	1.09	Ferrer D.	633
Monte Carlo	4/19/2014	Federer R.	Djokovic N.	3.35	1.32	Federer R.	235
Monte Carlo	4/20/2014	Wawrinka S.	Federer R.	2.24	1.65	Wawrinka S.	124
Rome	5/18/2014	Djokovic N.	Nadal R.	2.13	1.71	Djokovic N.	113
Paris	5/28/2014	Federer R.	Schwartzman D.	1.01	17.01	Schwartzman D.	-100
Paris	6/4/2014	Nadal R.	Ferrer D.	1.17	5.11	Ferrer D.	-100
Paris	6/6/2014	Nadal R.	Murray A.	1.13	6.13	Nadal R.	13
Paris	6/8/2014	Nadal R.	Djokovic N.	1.68	2.23	Djokovic N.	-100
Halle	6/14/2014	Federer R.	Nishikori K.	1.48	2.62	Nishikori K.	-100
London	6/26/2014	Nadal R.	Rosol L.	1.08	7.77	Rosol L.	-100
London	7/6/2014	Djokovic N.	Federer R.	1.63	2.31	Federer R.	-100
Cincinnati	8/16/2014	Federer R.	Murray A.	1.85	1.92	Federer R.	85
Cincinnati	8/17/2014	Federer R.	Raonic M.	1.43	2.82	Raonic M.	-100
New York	9/4/2014	Djokovic N.	Murray A.	1.25	3.96	Murray A.	-100
Beijing	10/4/2014	Djokovic N.	Murray A.	1.33	3.28	Murray A.	-100
Shanghai	10/11/2014	Federer R.	Djokovic N.	3.24	1.34	Federer R.	224
Paris	10/31/2014	Raonic M.	Federer R.	3.72	1.27	Raonic M.	272
Paris	10/31/2014	Djokovic N.	Murray A.	1.35	3.19	Murray A.	-100
London	11/11/2014	Federer R.	Nishikori K.	1.44	2.76	Nishikori K.	-100
London	11/12/2014	Djokovic N.	Wawrinka S.	1.15	5.37	Wawrinka S.	-100
London	11/13/2014	Federer R.	Murray A.	1.44	2.77	Murray A.	-100
London	11/16/2014	Djokovic N.	Federer R.	1.27	3.79	Federer R.	-100

2014 betting simulation: $827/3700 = 22.35\%$

Analysis

Ply1_ad_stroke

TieBreakGame reaches player1Win with prob

BH_Crosscourt
BH_Downline
FH_InsideOut
FH_InsideIn
FH_Error
BH_Error

BH_Crosscourt
BH_Downline
FH_InsideOut
FH_InsideIn
FH_Error
BH_Error

D:\FYP\propabilititis tennis\PAT342\PAT3.Console.exe

Console

Result

Analysis complete

pMin

pMax

pAvg

Plot Graph

BH_Downline

34

BH_Error

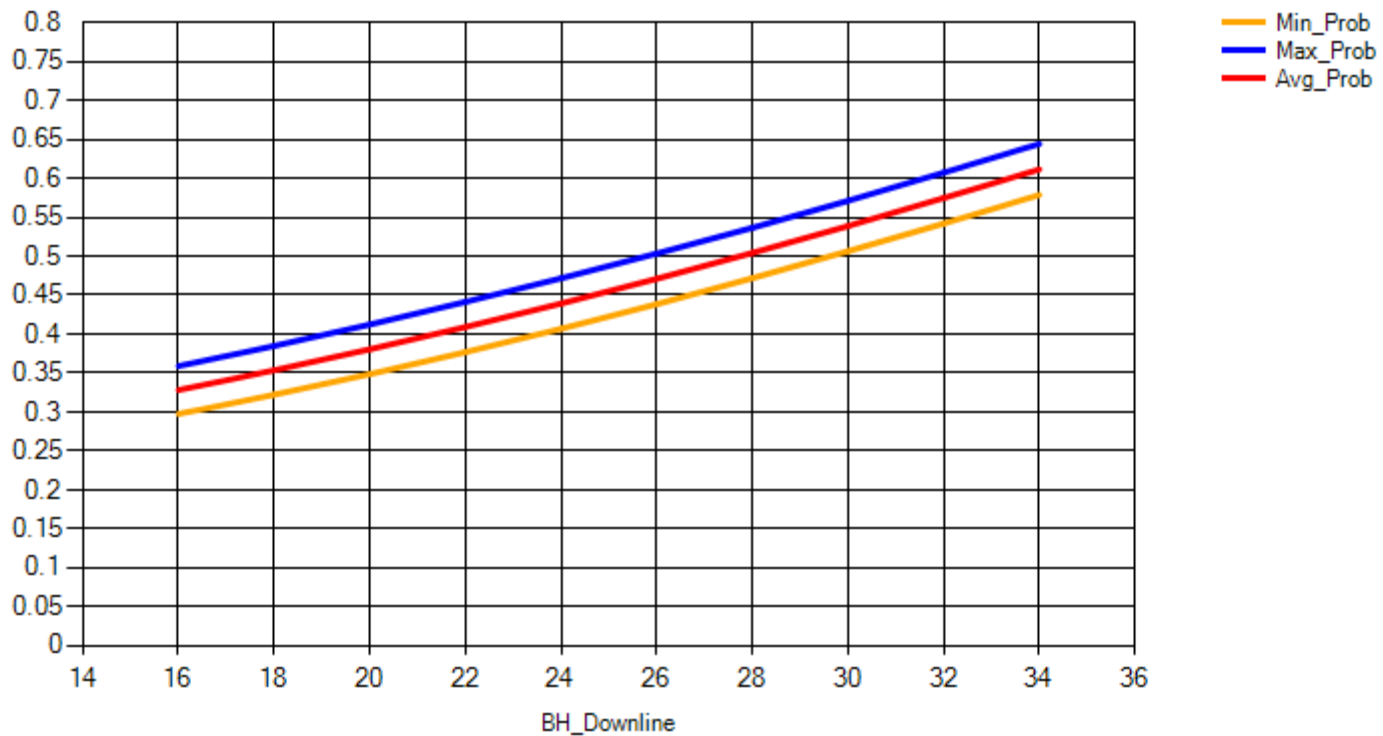
0

Min 16

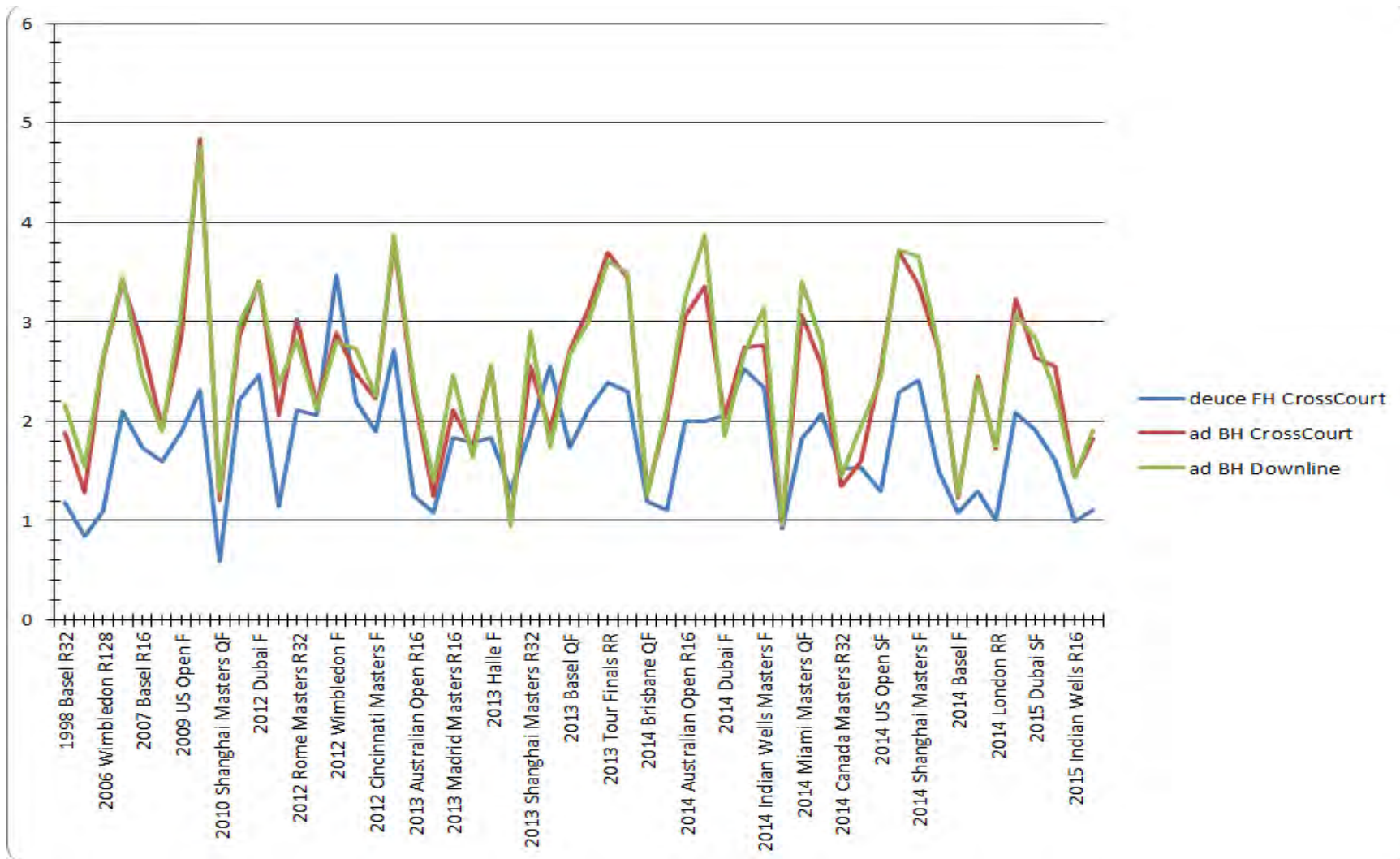
Max 34

Step

2



Finding the best action to improve: vs Right-handed players



Combine Real-Time and Probability



Passing me without
stopping!



Given the C# Program of a lift algorithm

```
C# Library Editor and Compiler
New Library New DataType Open C# Code Save Release
16 public class LiftControl : ExpressionValue
17 {
18     //-1; for not assigned; i for assigned to i-lift;
19     int[] ExternalRequestsUp;
20     int[] ExternalRequestsDown;
21     //0; for not pressed, 1 for pressed
22     int[][] InternalRequests;
23     //0 for stopped at ground level; ready to go up.
24     int[] LiftStatus;
25
26     public LiftControl()
27     {
28         ExternalRequestsUp = new int[2];
29         ExternalRequestsDown = new int[2];
30         InternalRequests = new int[2][];
31         InternalRequests[0] = new int[2];
32         InternalRequests[1] = new int[2];
33         LiftStatus = new int[2];
34     }
35
36     public LiftControl(int levels, int lifts)
37     {
38         ExternalRequestsUp = new int[levels];
39         ExternalRequestsDown = new int[levels]; ;
40
41         for (int i = 0; i < levels; i++)
42         {
43             ExternalRequestsUp[i] = -1;
44             ExternalRequestsDown[i] = -1;
45         }
46         ;
47         InternalRequests = new int[lifts][];
48         LiftStatus = new int[lifts];
```

```
C# Library Editor and Compiler
New Library New DataType Open C# Code Save Release Build DLL
273
274 public int PassBy (int lift, int level, int up)
275 {
276     //if (isToOpenDoor(lift, level) == 0)
277     //{
278         if (up > 0)
279         {
280             if (ExternalRequestsUp[level] != lift && ExternalRequestsUp[level] >= 0)
281             {
282                 return 1;
283             }
284         }
285         else
286         {
287             if (ExternalRequestsDown[level] >= 0 && ExternalRequestsDown[level] == lift)
288             {
289                 return 1;
290             }
291         }
292     //}
293
294     return 0;
295 }
296
297 public void AddInternalRequest(int lift, int level)
298 {
299     InternalRequests[lift][level] = 1;
300 }
301
302 public int UpdateLiftStatus(int lift, int level, int direction)
303 {
304     LiftStatus[lift] = LiftStatus[lift] + 1;
305
306     return PassBy(lift, level, direction);
307 }
```

PAT checking the C# program with time+probability

```
#import "PAT.Lib.Lift";
#define NoOfFloors 2;
#define NoOfLifts 2;
var<LiftControl> ctrl = new LiftControl(NoOfFloors,NoOfLifts);
var passby = 0;

aSystem = (||| x:{0..NoOfLifts-1} @ Lift(x, 0, 1)) ||| Requests();

Requests() = Request();Request();
Request() = pcase {
    1 : extreq.0.1{ctrl.AssignExternalRequest(0,1)} -> Skip
    1 : intreq.0.0.1{ctrl.AddInternalRequest(0,0)} -> Skip
    1 : intreq.1.0.1{ctrl.AddInternalRequest(1,0)} -> Skip
    1 : extreq.1.0{ctrl.AssignExternalRequest(1,0)} -> Skip
    1 : intreq.0.1.1{ctrl.AddInternalRequest(0,1)} -> Skip
    1 : intreq.1.1.1{ctrl.AddInternalRequest(1,1)} -> Skip
} within[1];

Lift(i, level, direction) = case {
    ctrl.isToOpenDoor(i, level) == 1 : (serve.level.direction{ctrl.ClearRequests(i, level, direction)}
                                         -> Lift(i, level, direction))
    ctrl.KeepMoving(i, level, direction) == 1 : (reach.level+direction.direction
                                                  {passby = ctrl.UpdateLiftStatus(i, level, direction)}
                                                  -> Lift(i, level+direction, direction))
    ctrl.HasAssignment(i) == 1 : changedirection.i{ctrl.ChangeDirection(i)}
                                   -> Lift(i, level, -1*direction)
    default : idle.i -> Lift(i, level, direction)
} within[2];

#define goal passby == 1;
#define assert aSystem reaches goal with prob;
```

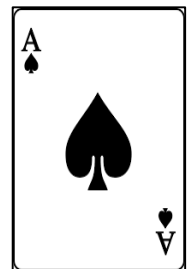
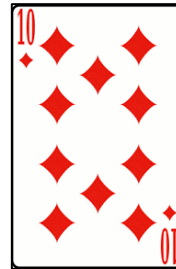
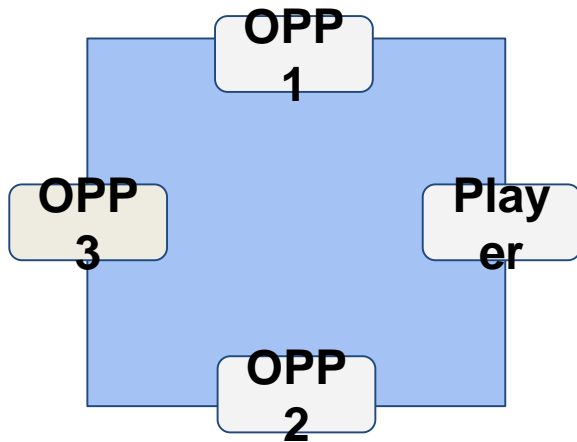
Probabilistic Model Checking + Learning

4-Player Kuhn Poker

- Simplified Poker Game
- Probabilistic in Nature
- Requires Opponent Learning

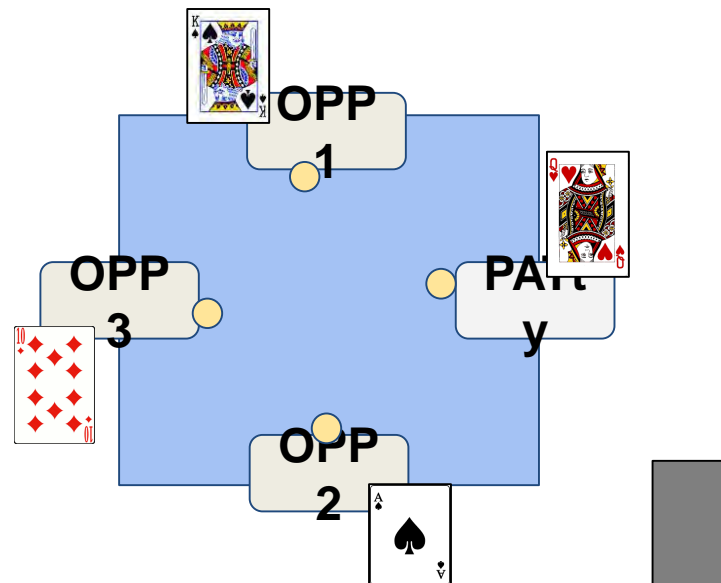
4-Player Kuhn Poker: Rules

- 4 Players
- 5 Cards
 - TEN (lowest value) to ACE (highest value)



4-Player Kuhn Poker: Rules

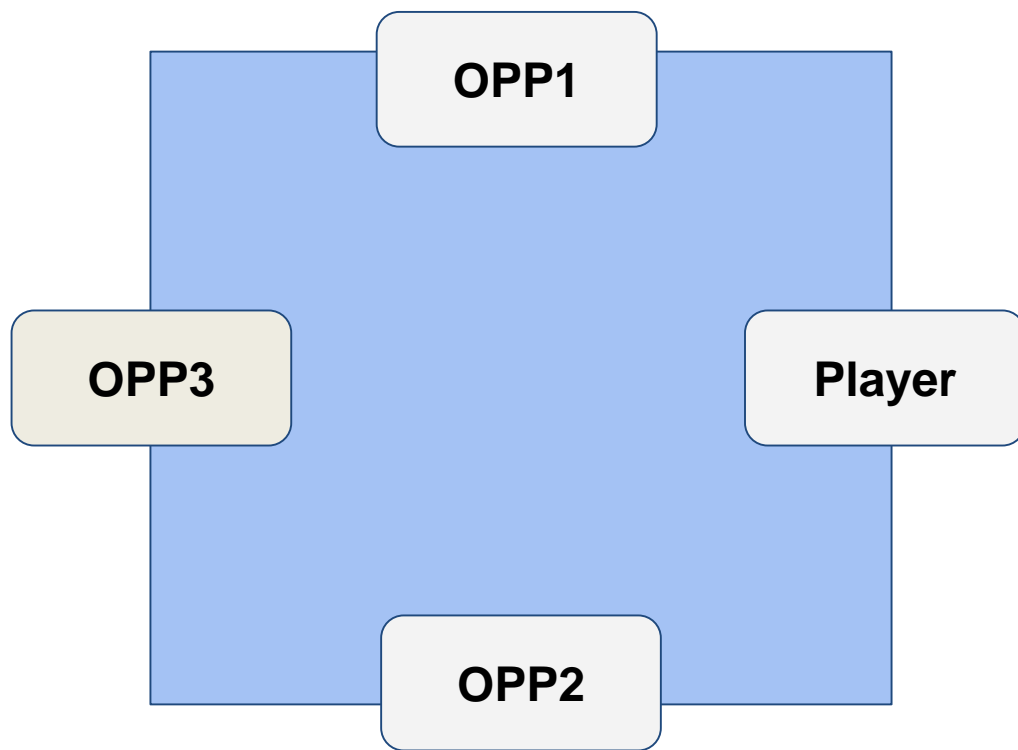
- Each hand
 - every player puts a chip down
 - each player is dealt a card
 - each player can choose to bet or not bet during their turn



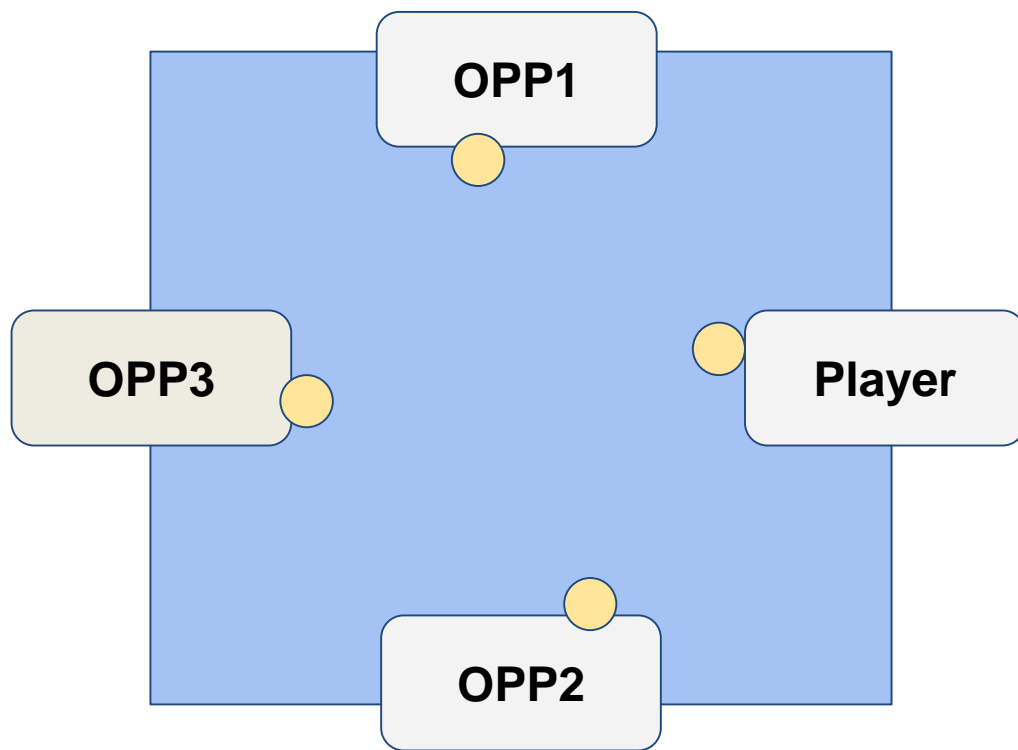
4-Player Kuhn Poker: Rules

- Game ends when:
 - All players don't Bet
 - Some player has Bet, and all players have responded to the Bet
- Player who bets with highest card wins

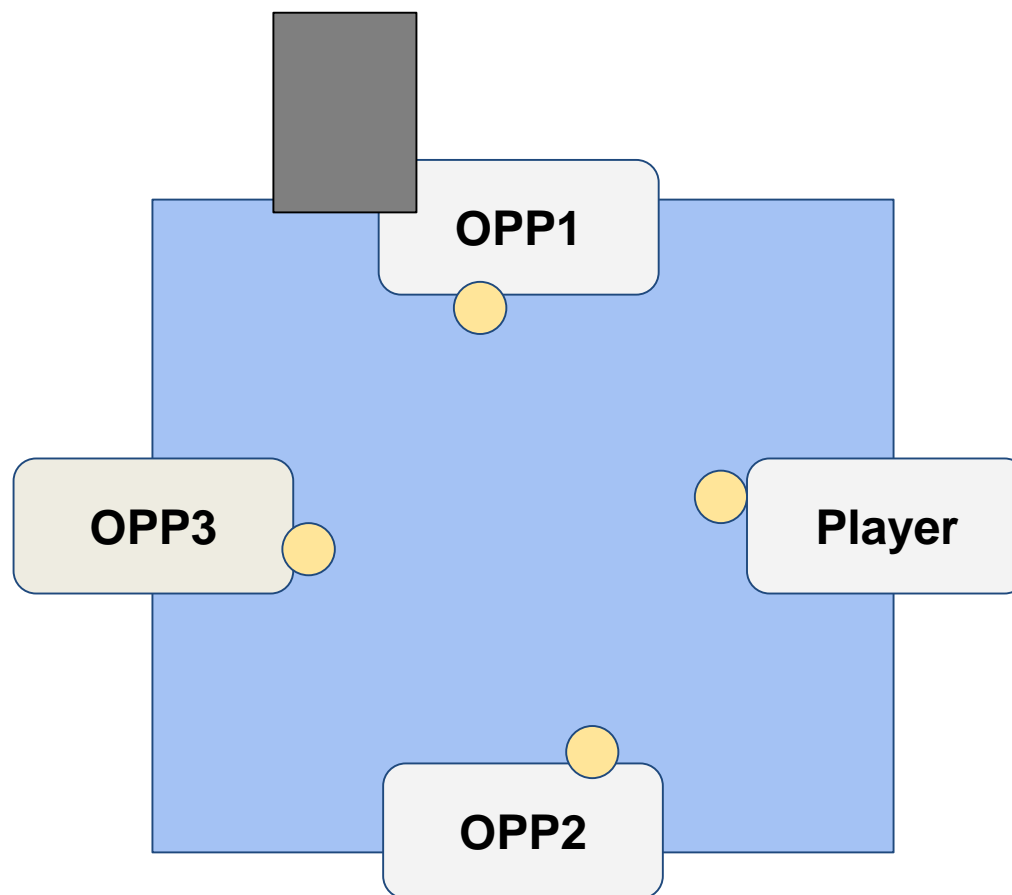
4-Player Kuhn Poker: Example



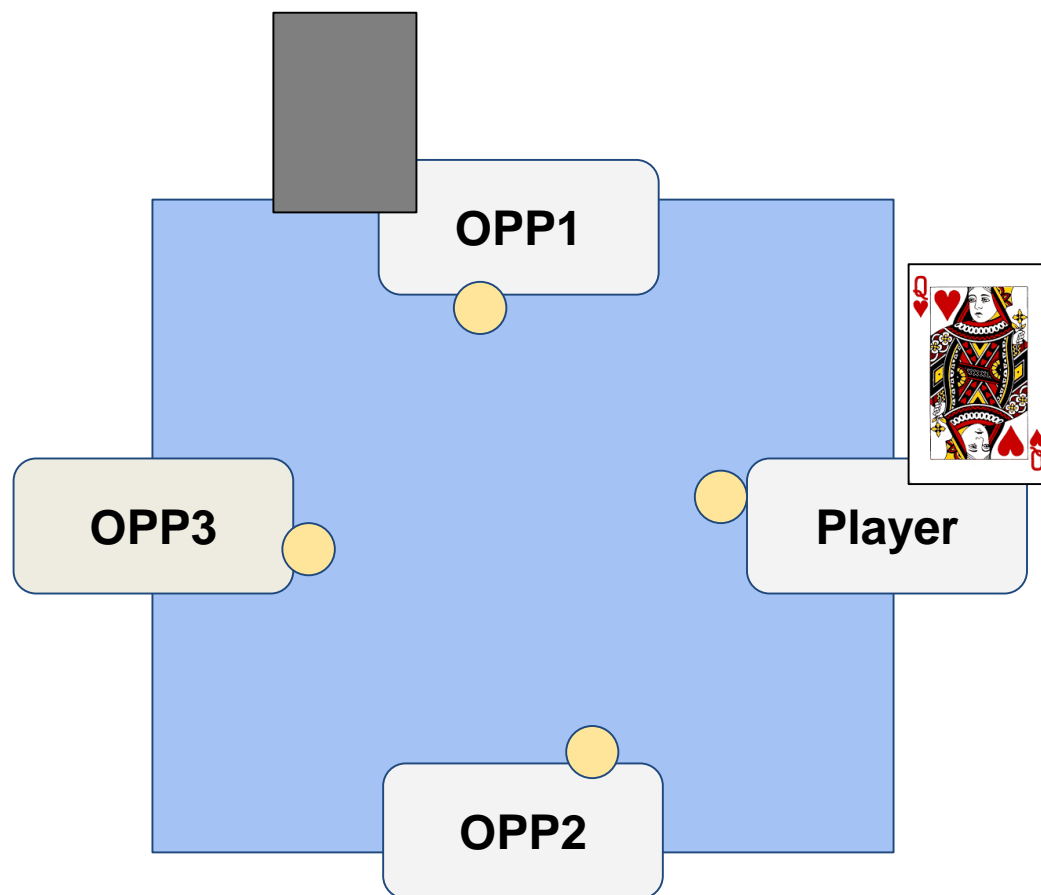
4-Player Kuhn Poker: Example



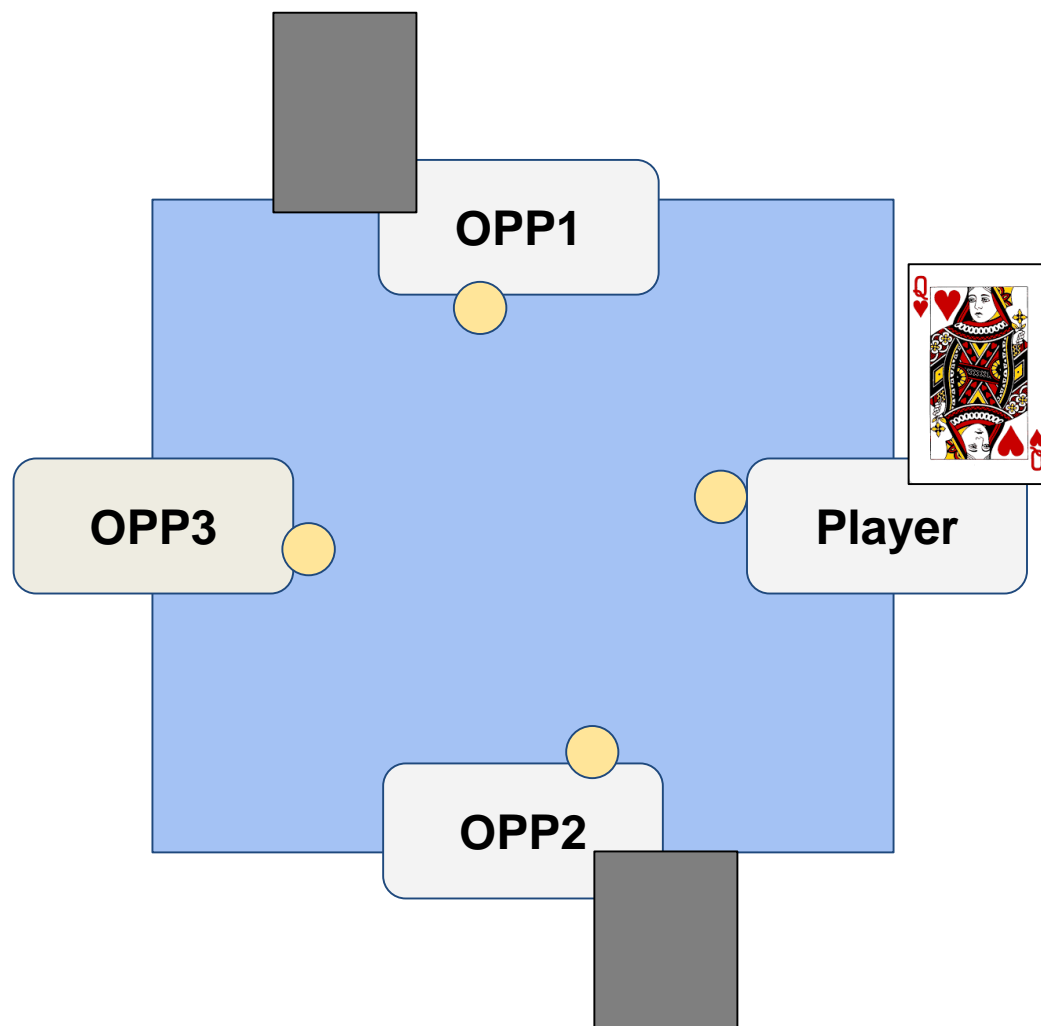
4-Player Kuhn Poker: Example



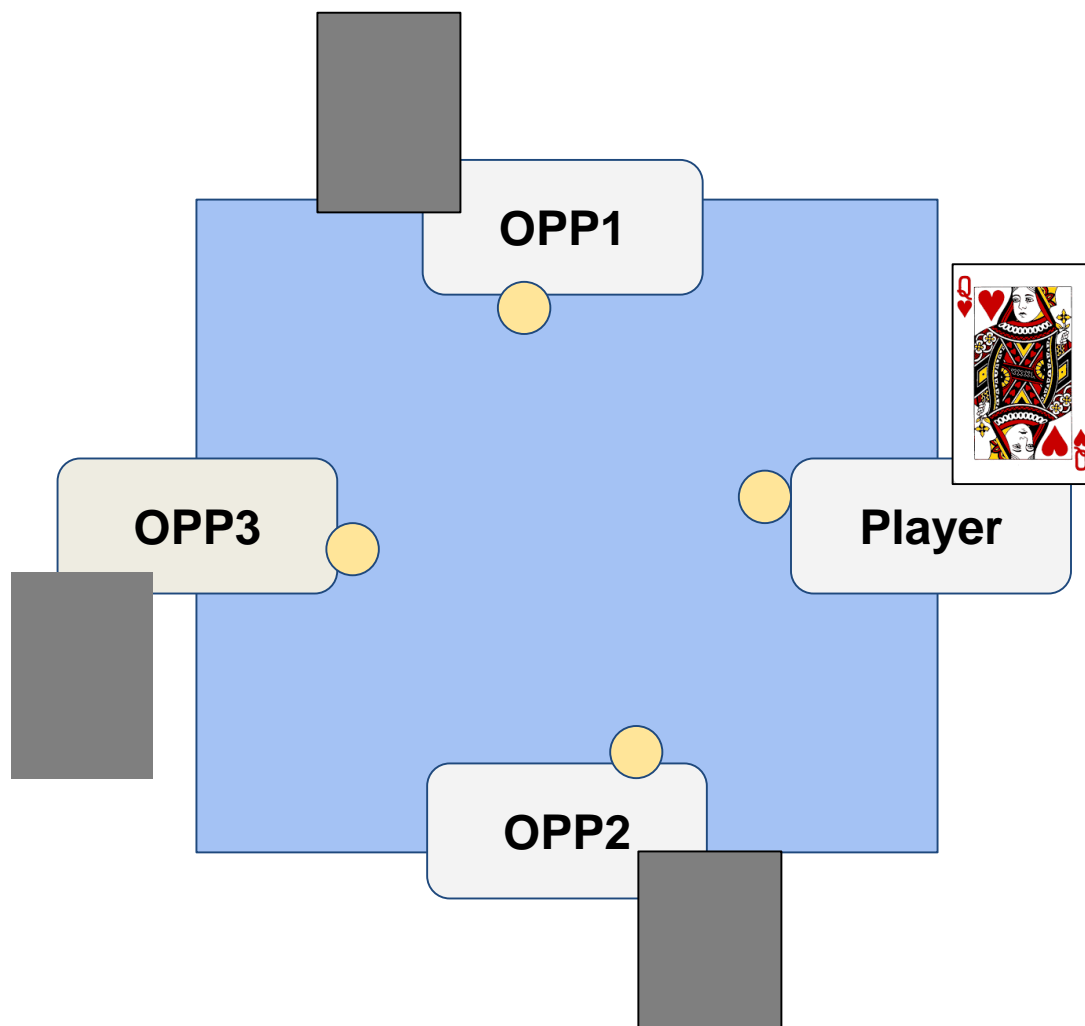
4-Player Kuhn Poker: Example



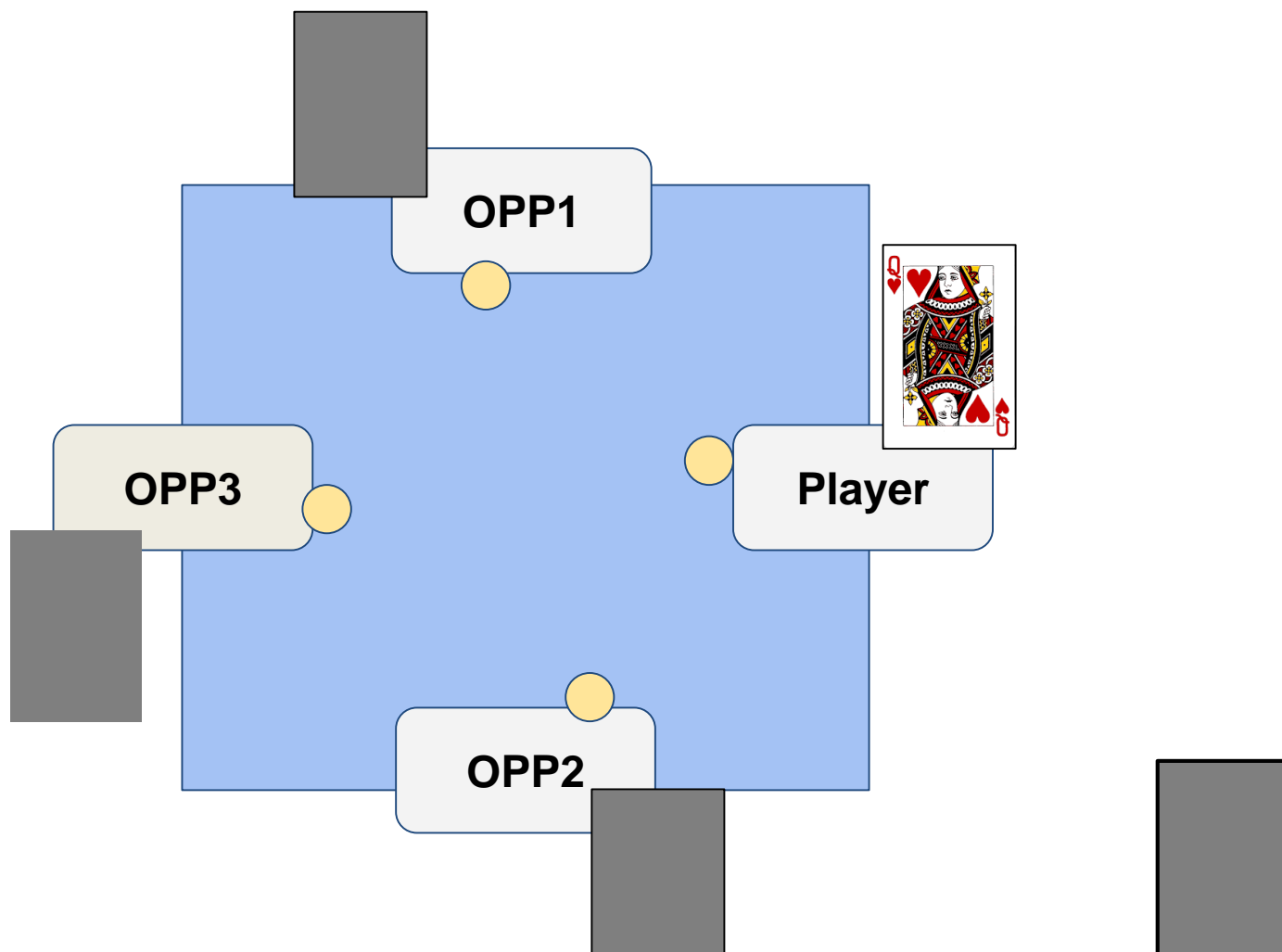
4-Player Kuhn Poker: Example



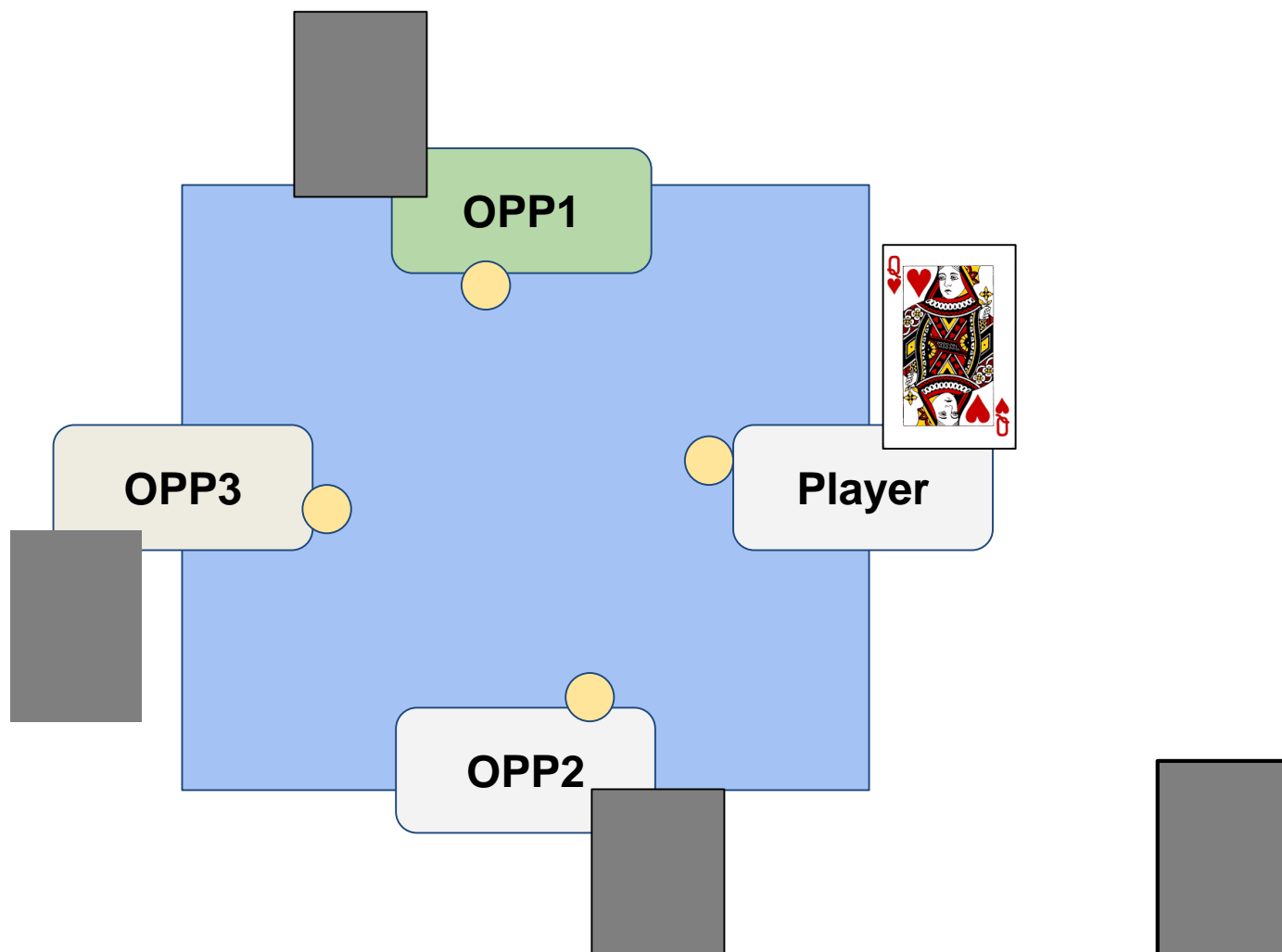
4-Player Kuhn Poker: Example



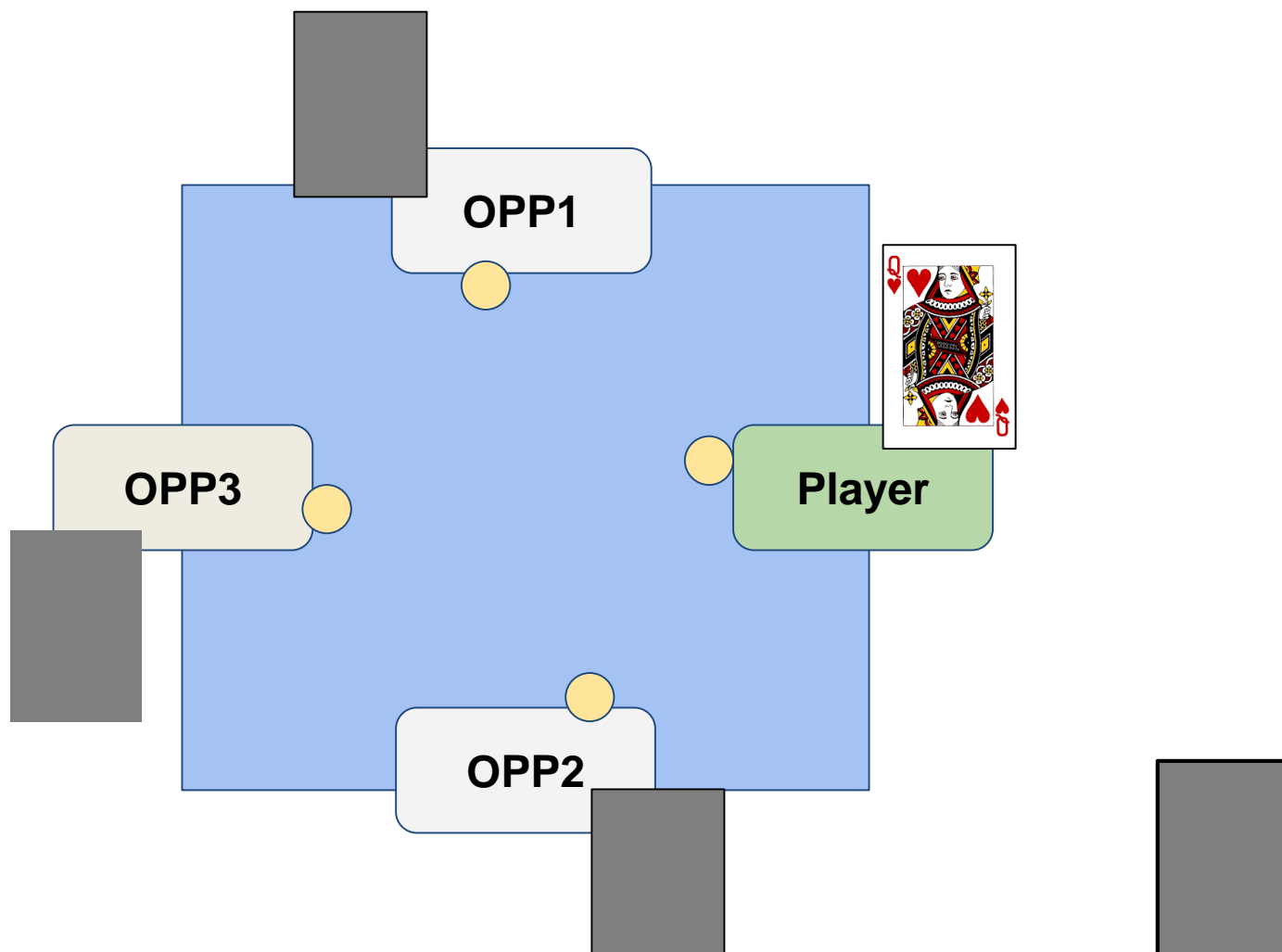
4-Player Kuhn Poker: Example



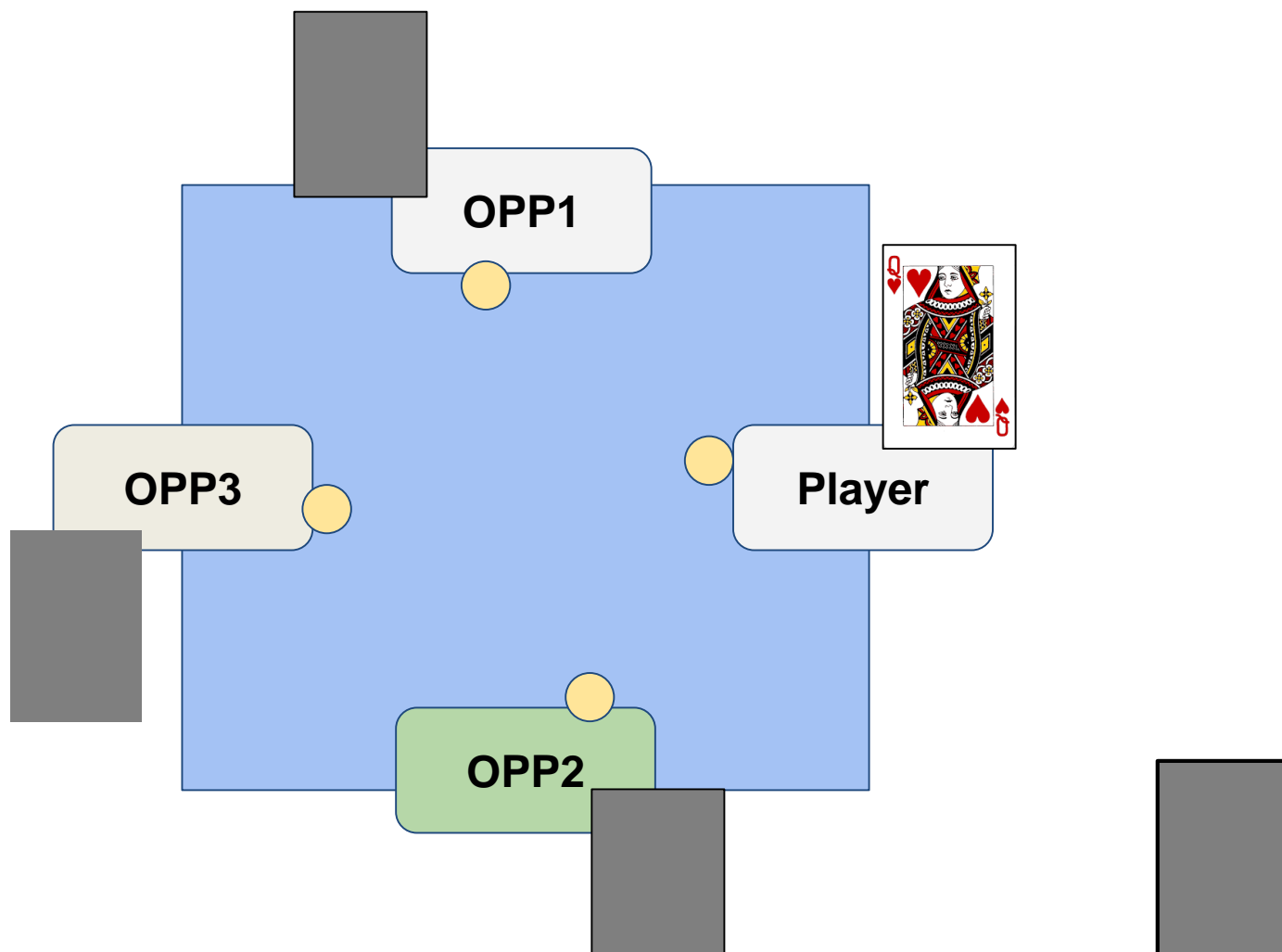
4-Player Kuhn Poker: Example



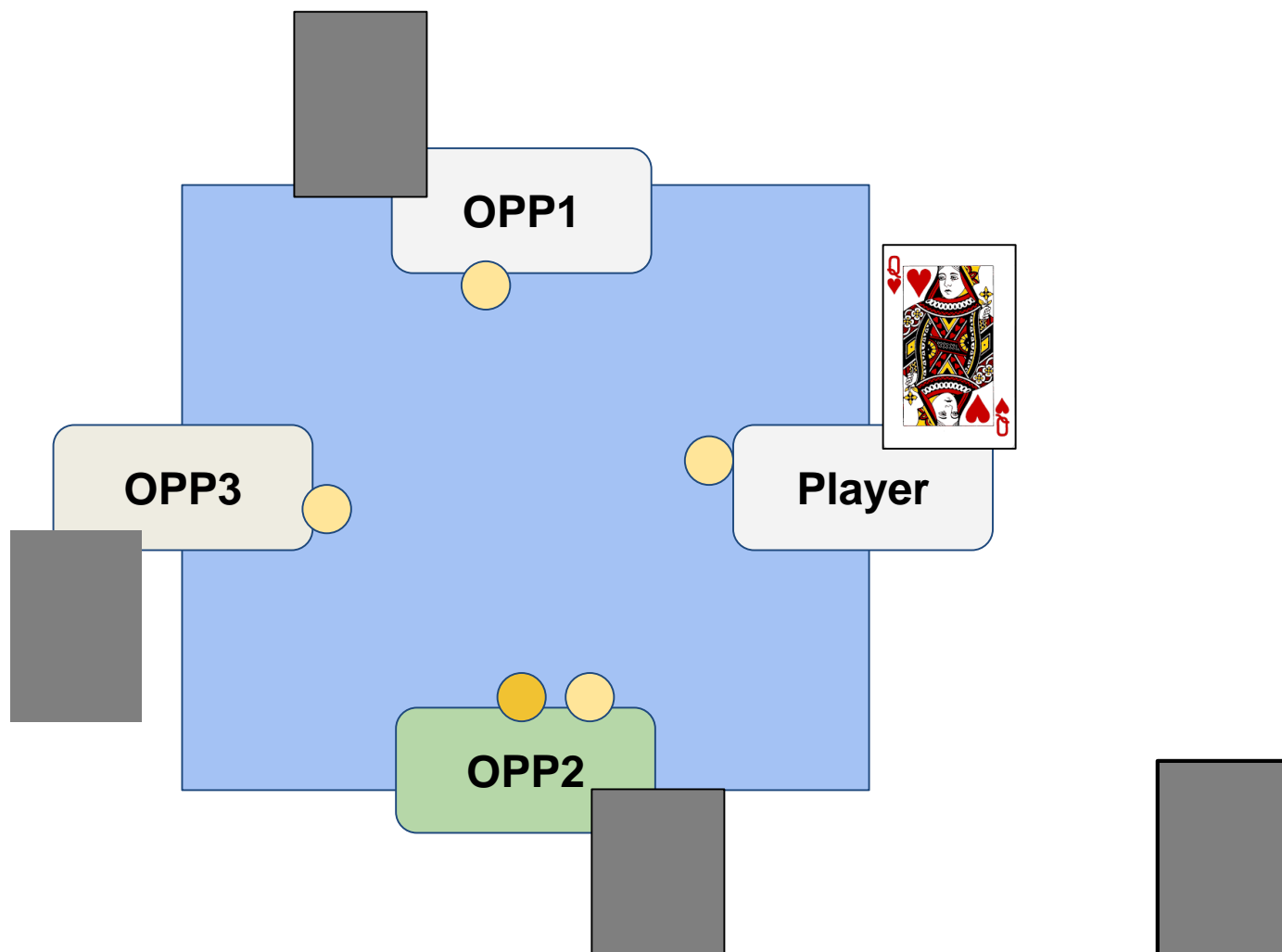
4-Player Kuhn Poker: Example



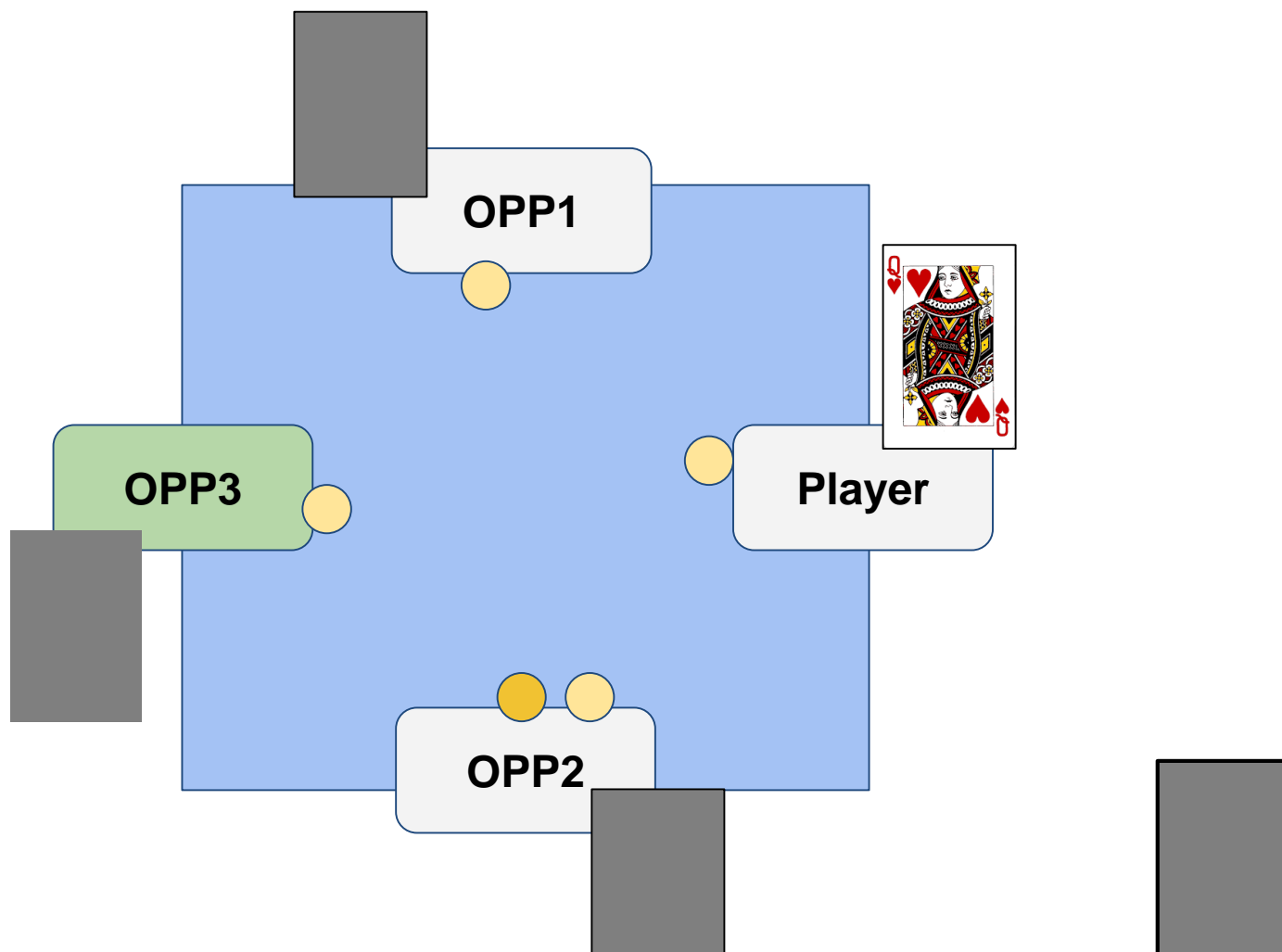
4-Player Kuhn Poker: Example



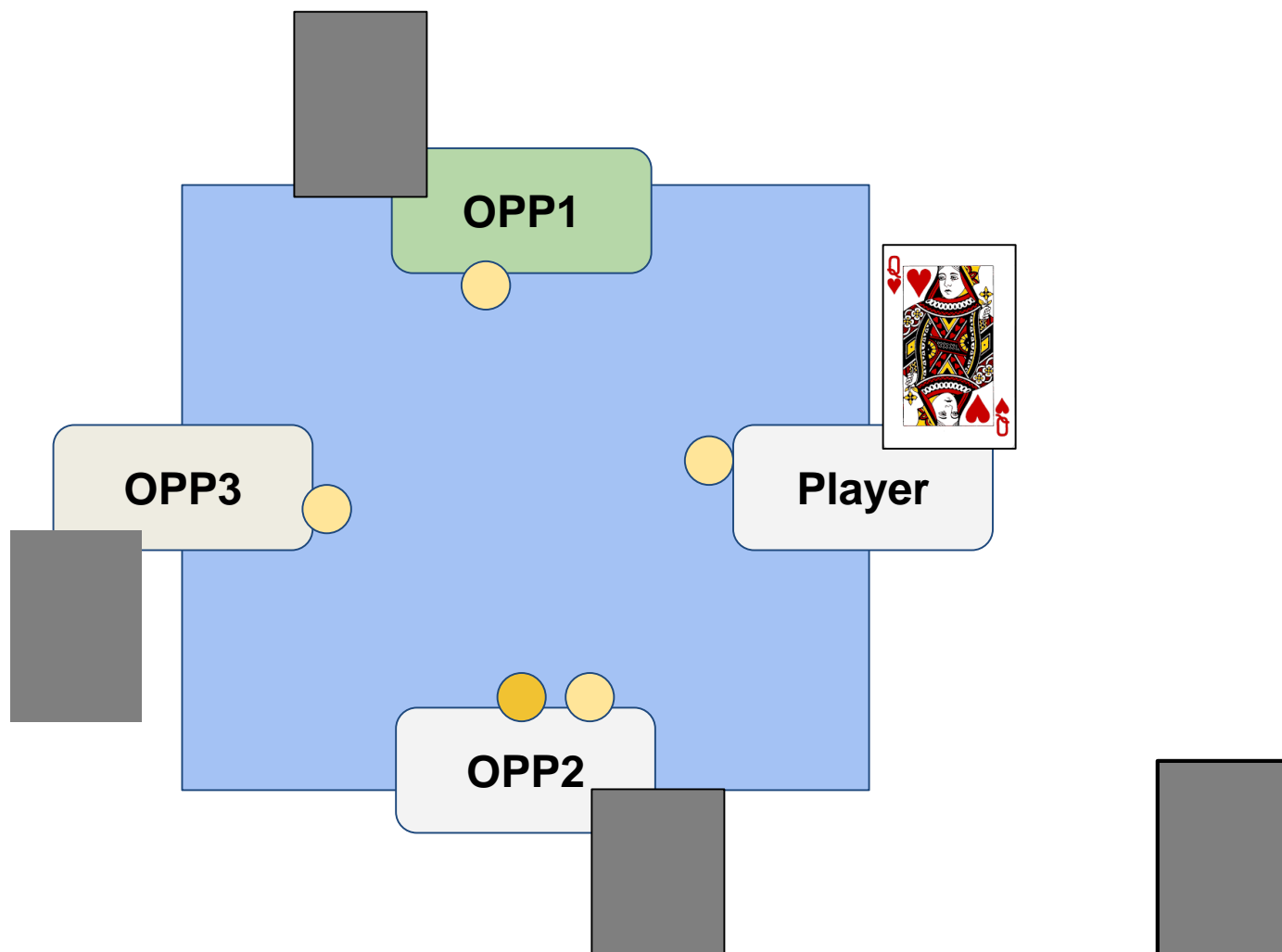
4-Player Kuhn Poker: Example



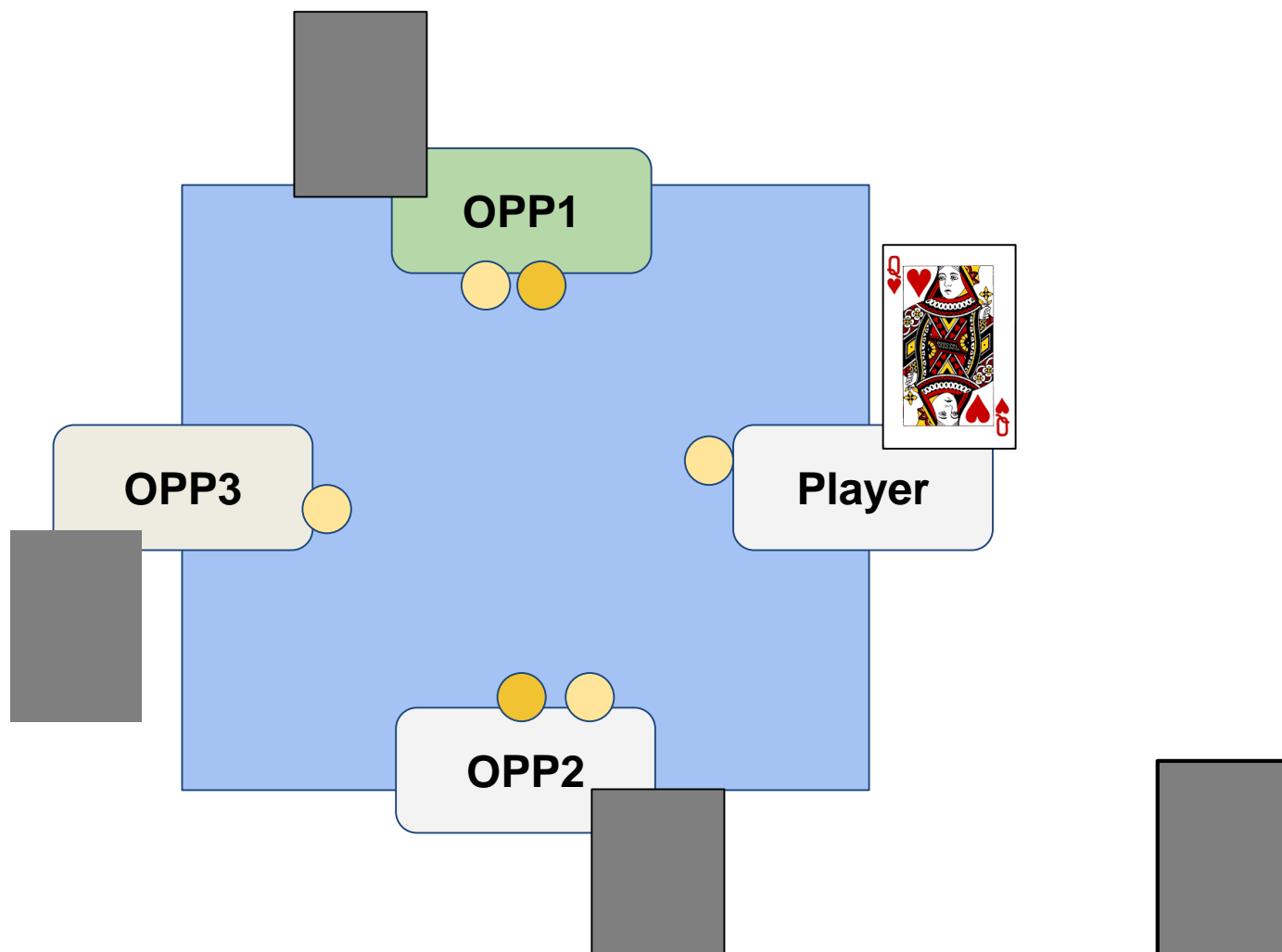
4-Player Kuhn Poker: Example



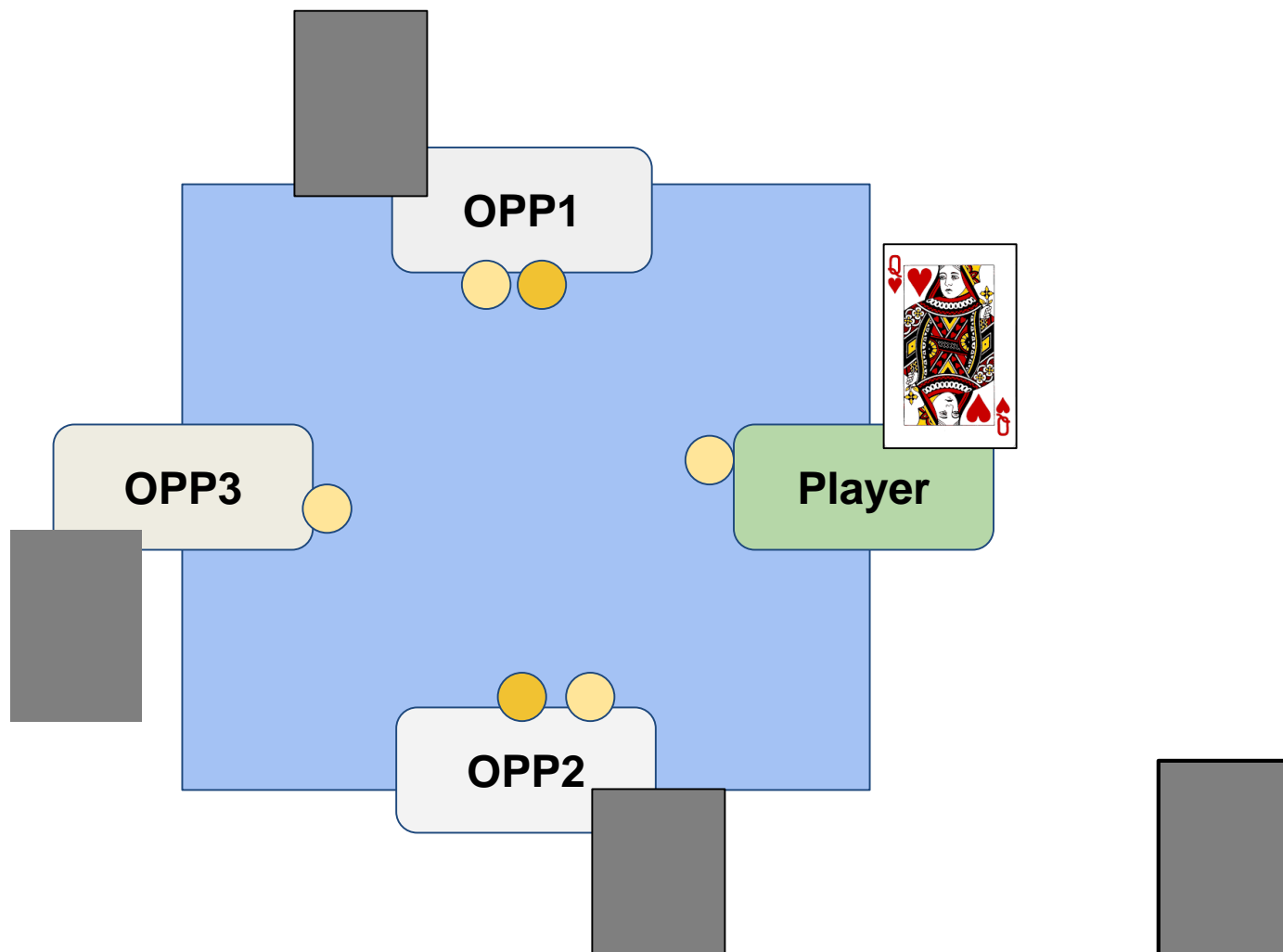
4-Player Kuhn Poker: Example



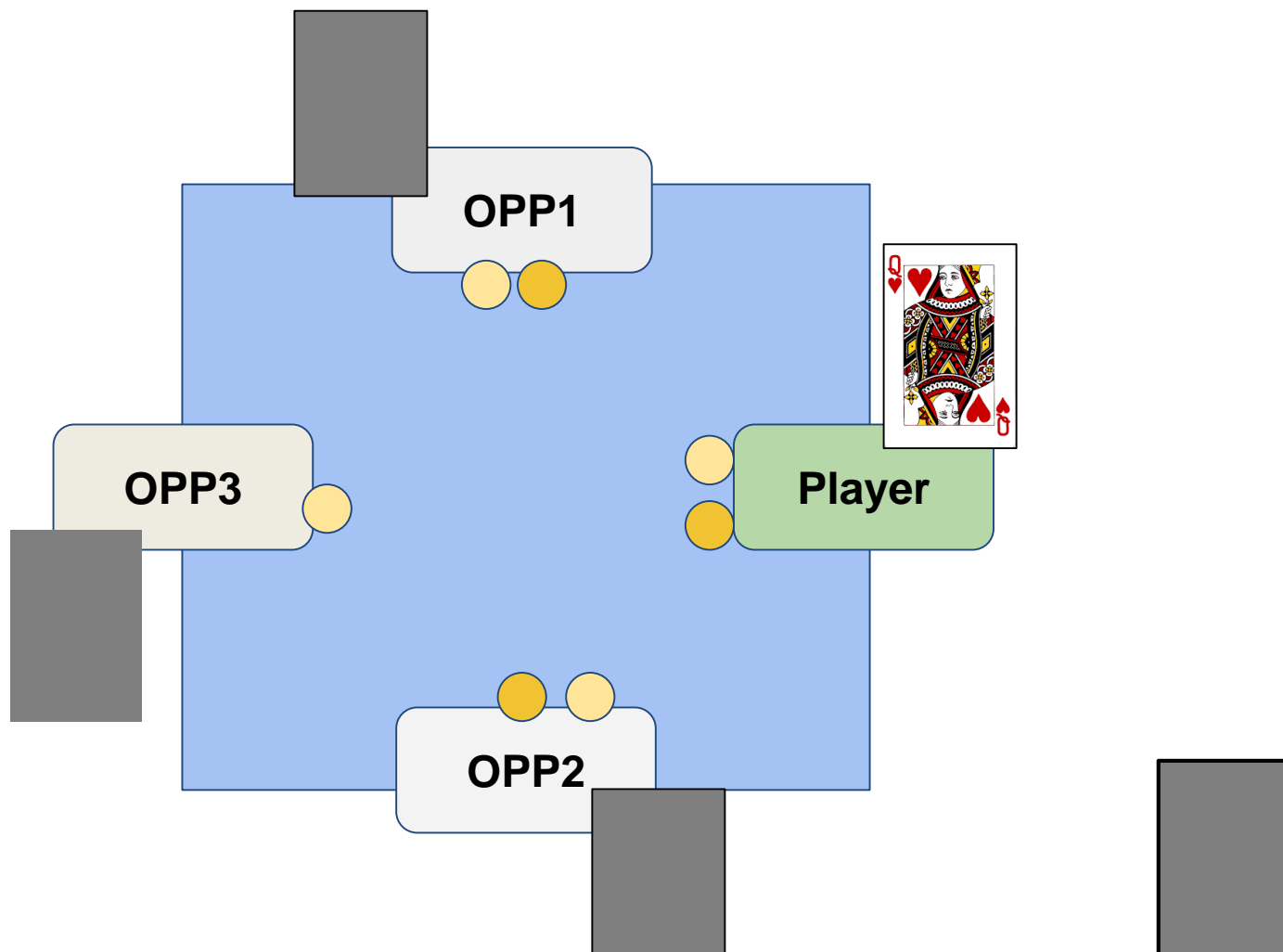
4-Player Kuhn Poker: Example



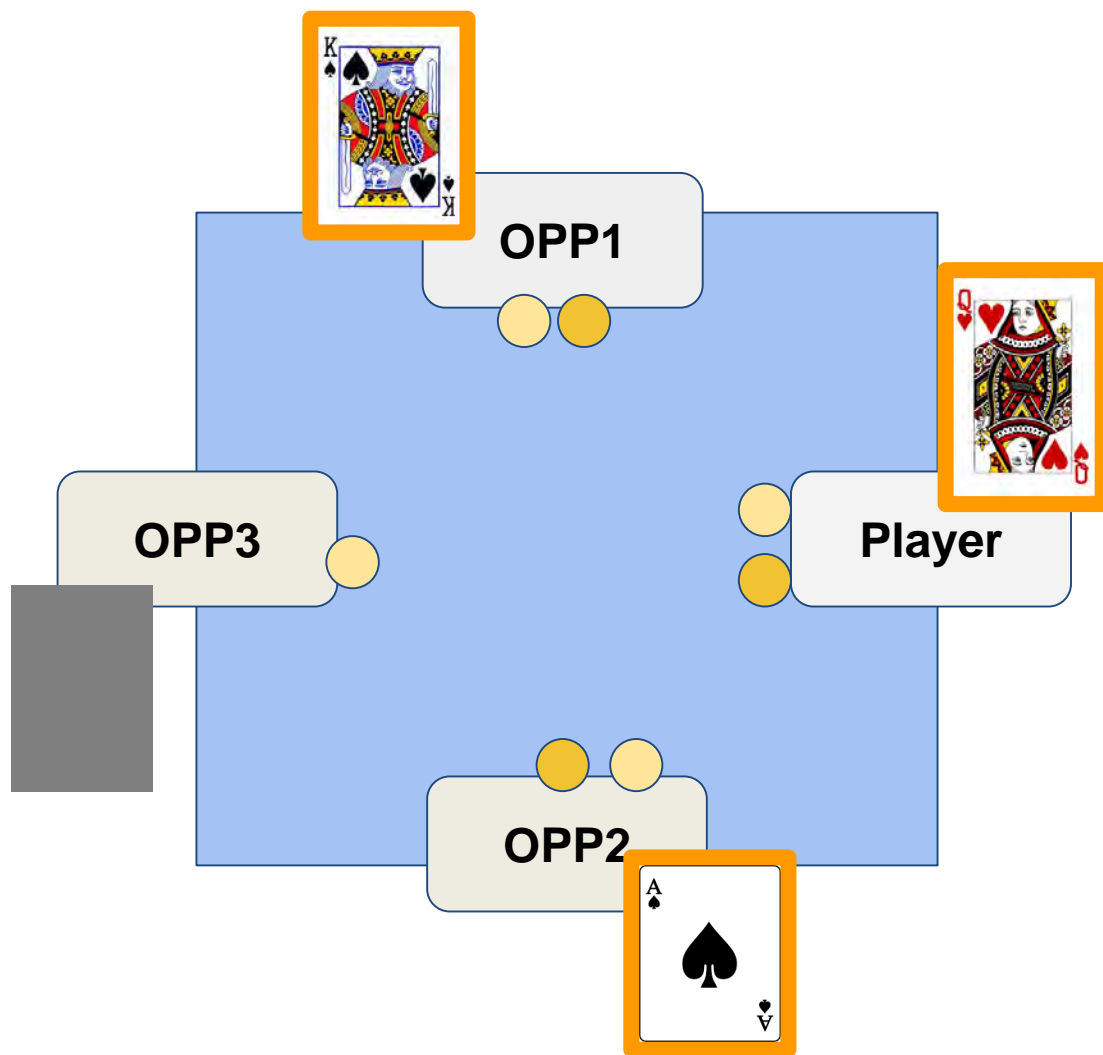
4-Player Kuhn Poker: Example



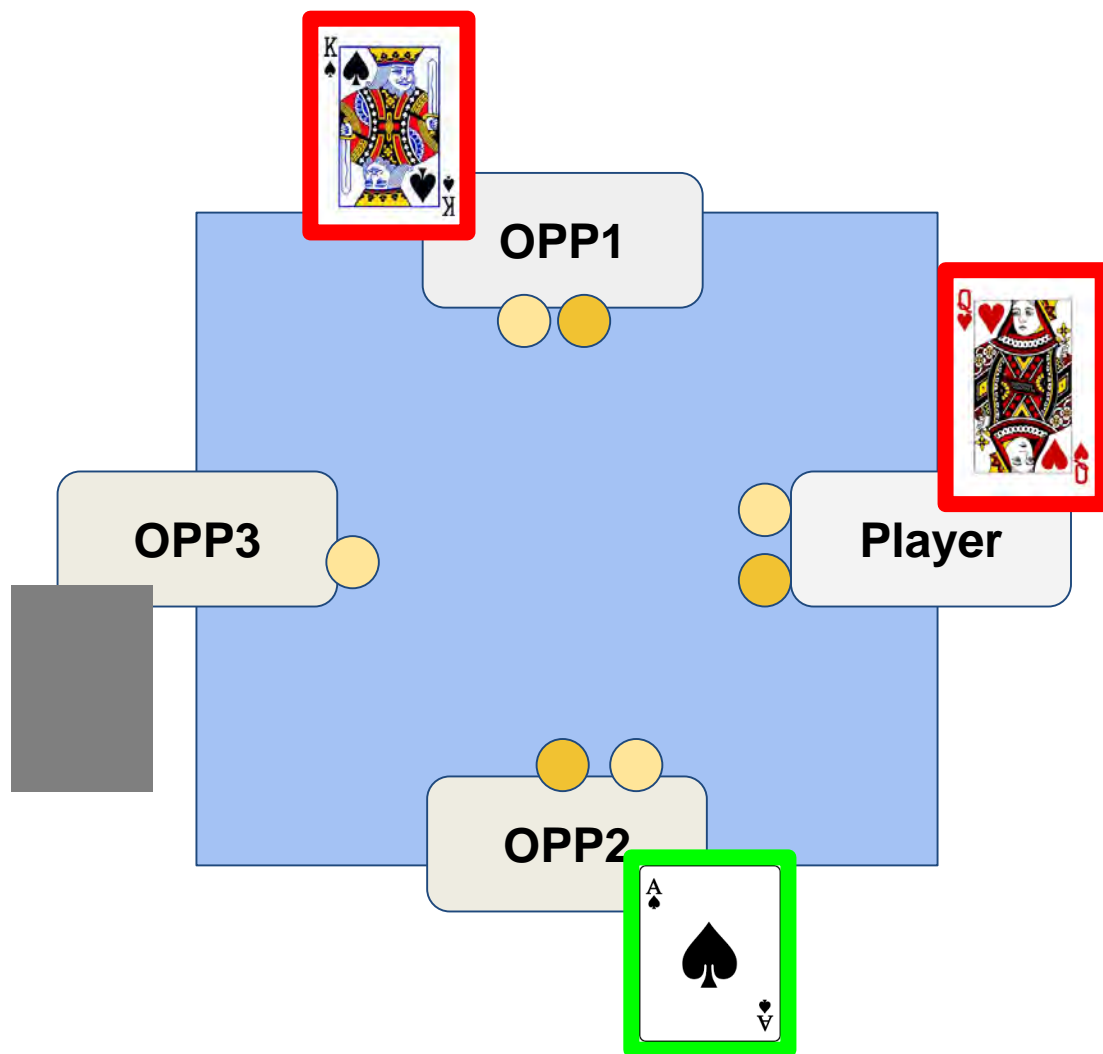
4-Player Kuhn Poker: Example



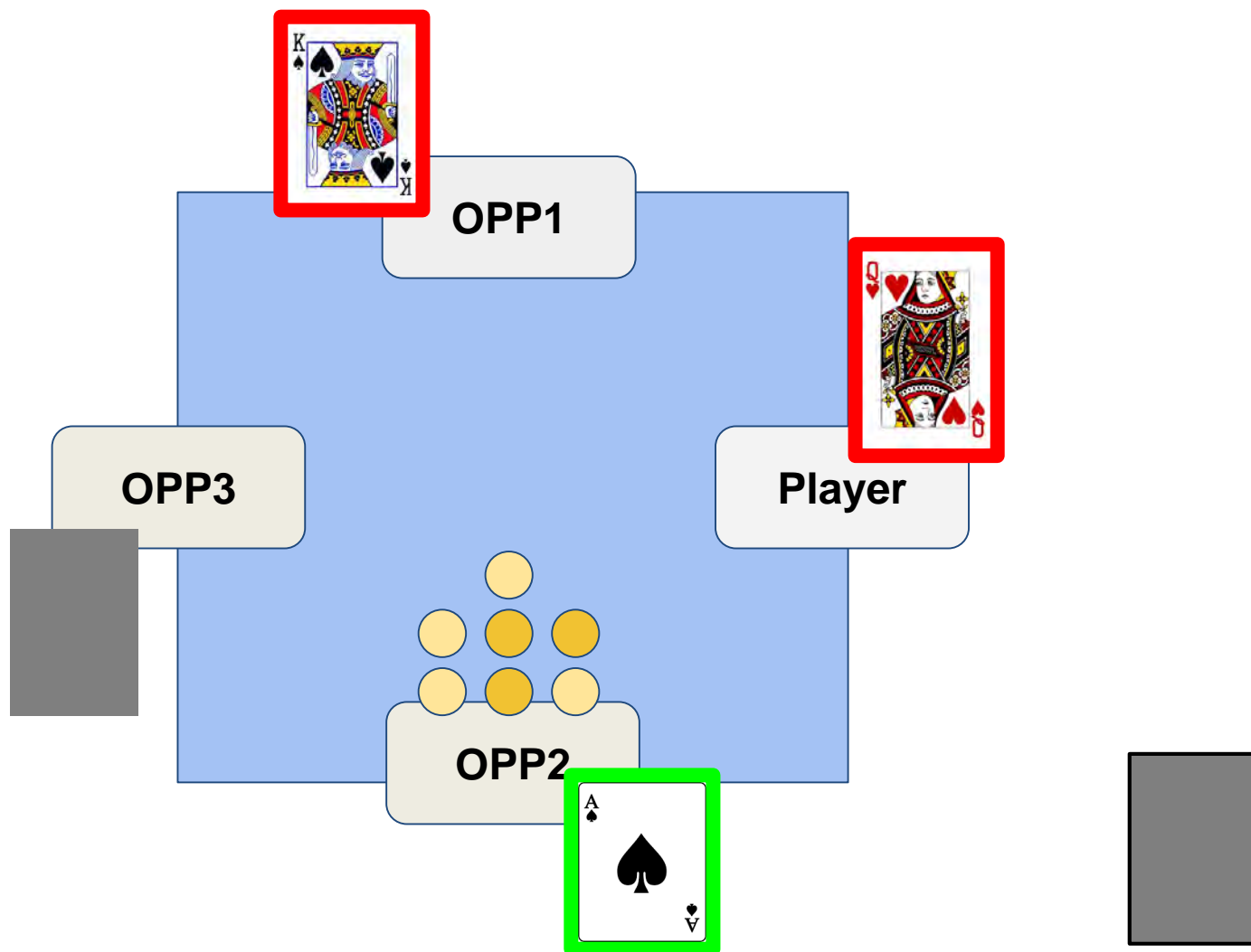
4-Player Kuhn Poker: Example



4-Player Kuhn Poker: Example

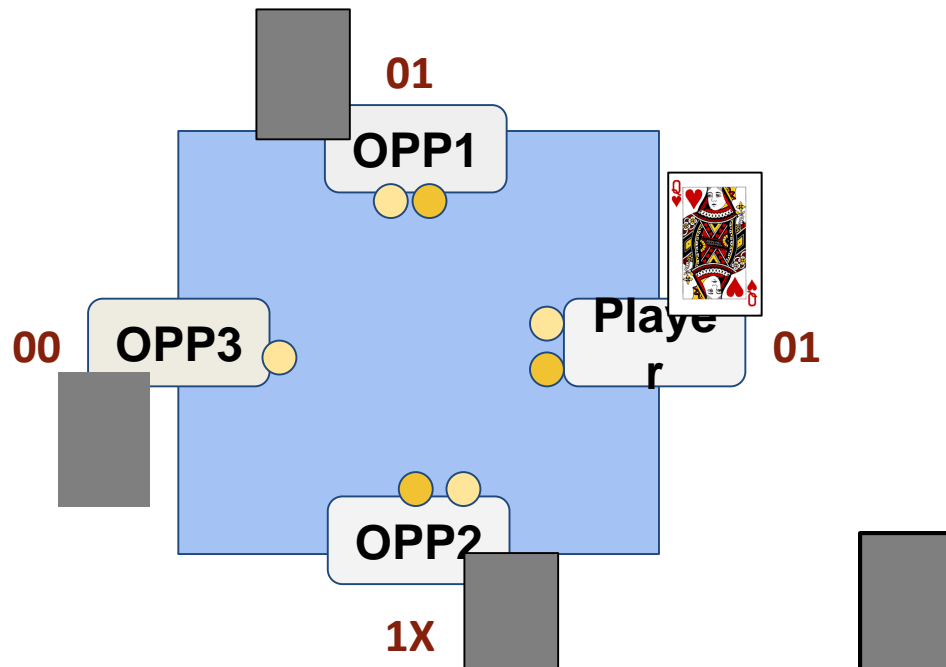


4-Player Kuhn Poker: Example

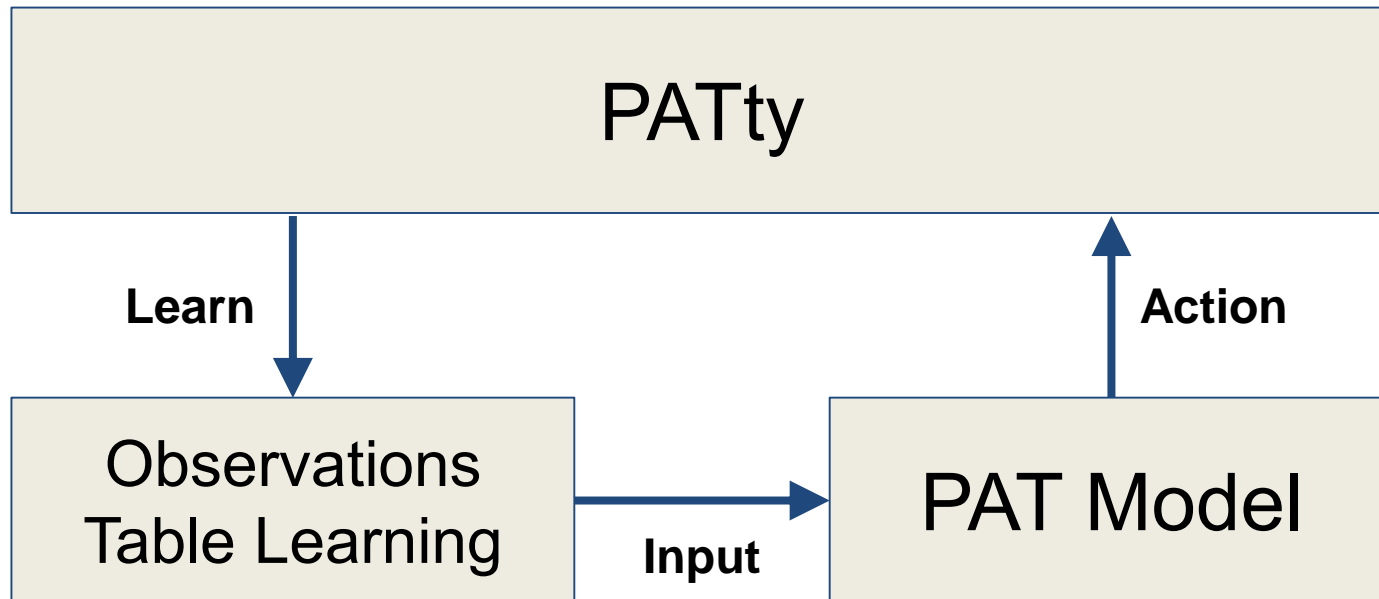


4-Player Kuhn Poker: Playing Method

- There are only 3 ways players play in
 - **00** - Do not bet on both first and second turns
 - **01** - Do not bet on first turn, but bet on second turn
 - **1X** - Bet on first turn, and will not have second turn



4-Player Kuhn Poker: Implementation



4-Player Kuhn Poker: Experimentation

Different configurations

X-Bluffer-Conservative-Bluffer (X-BCB)

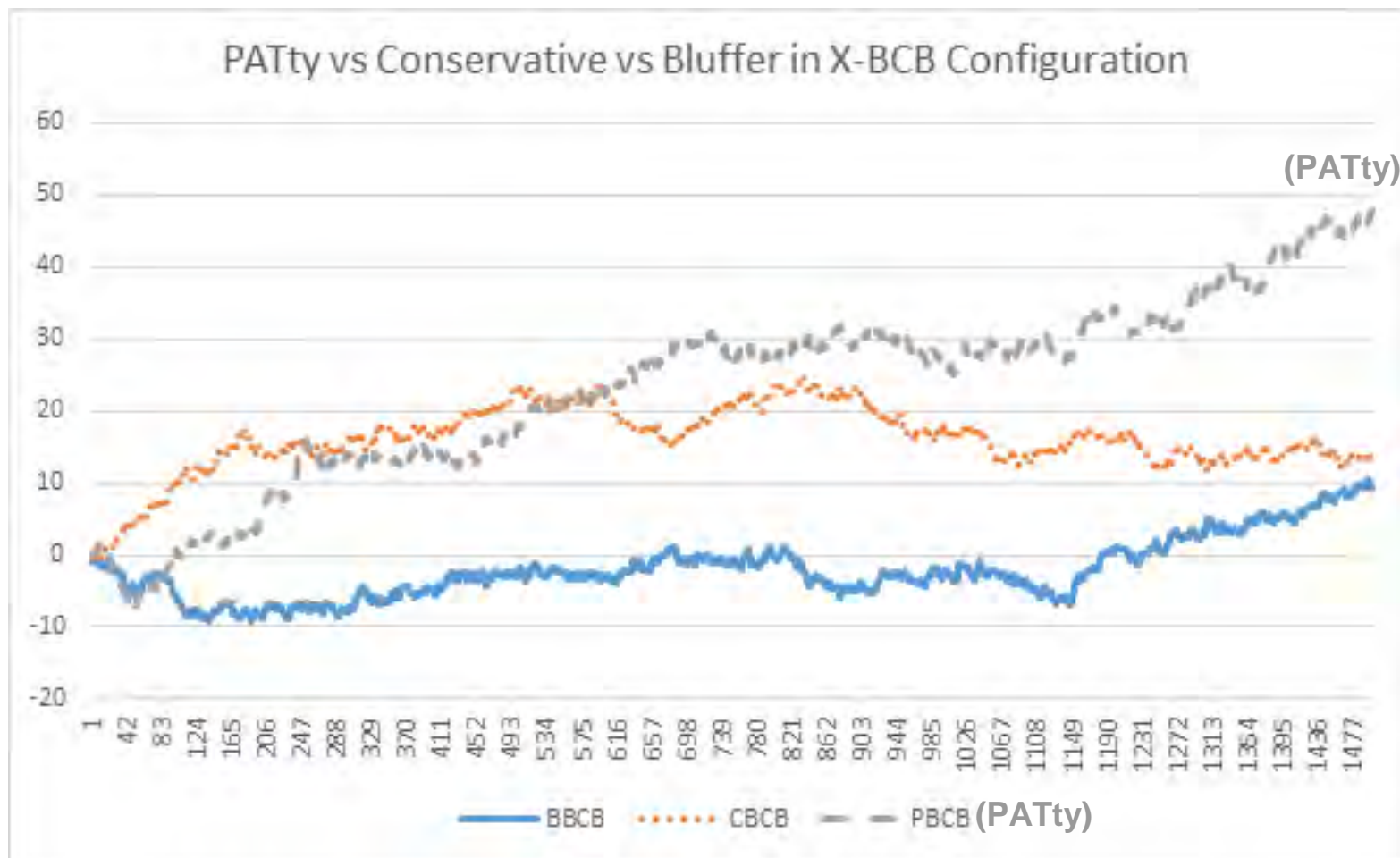
X-Conservative-Bluffer-Conservative (X-CBC)

Where X can be either PATty, Bluffer or Conservative

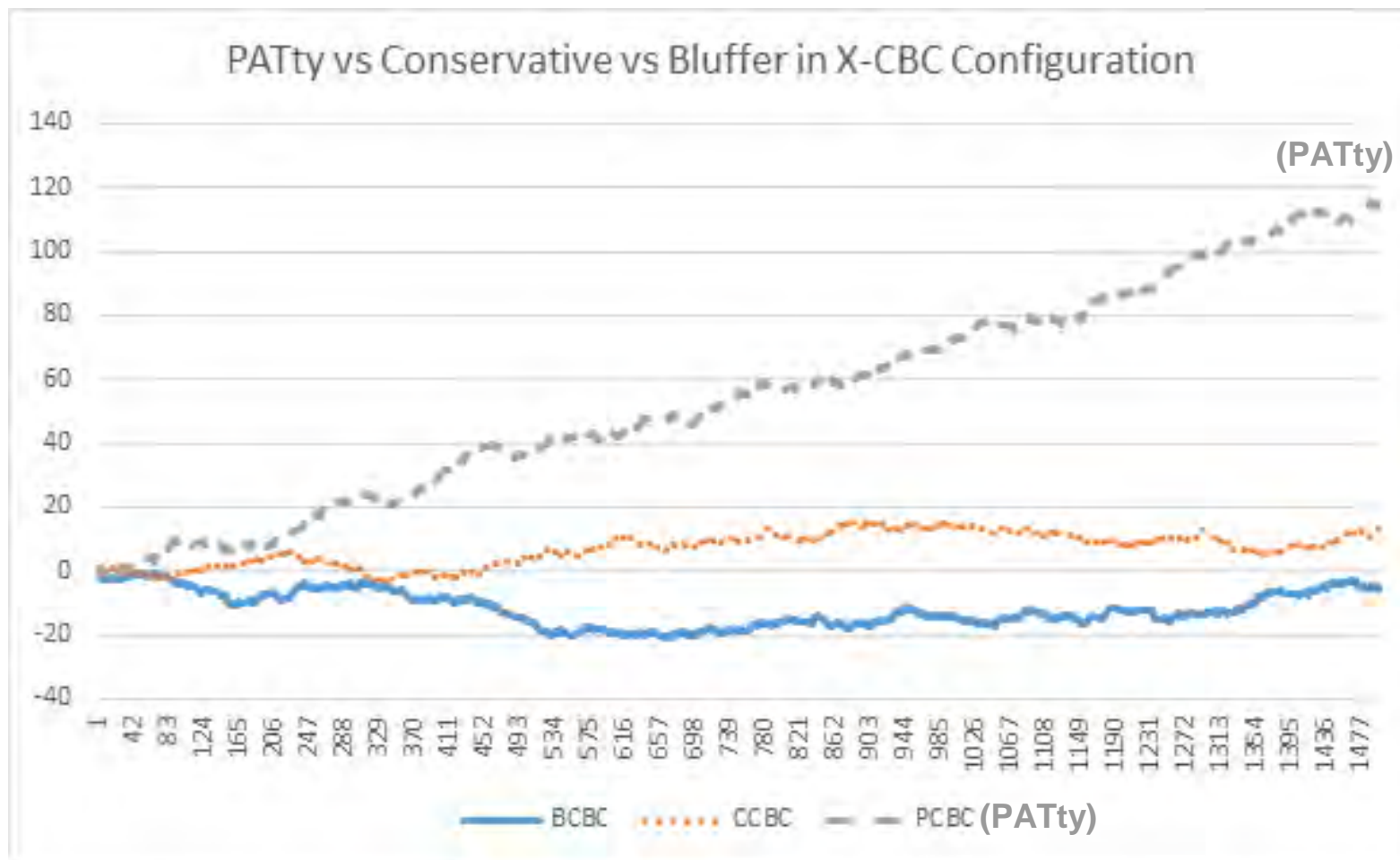
30 games each

1500 hands per game

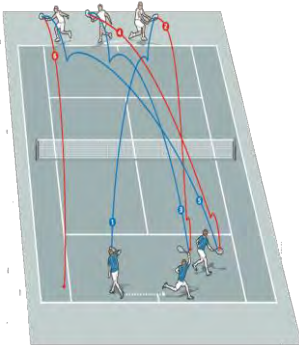
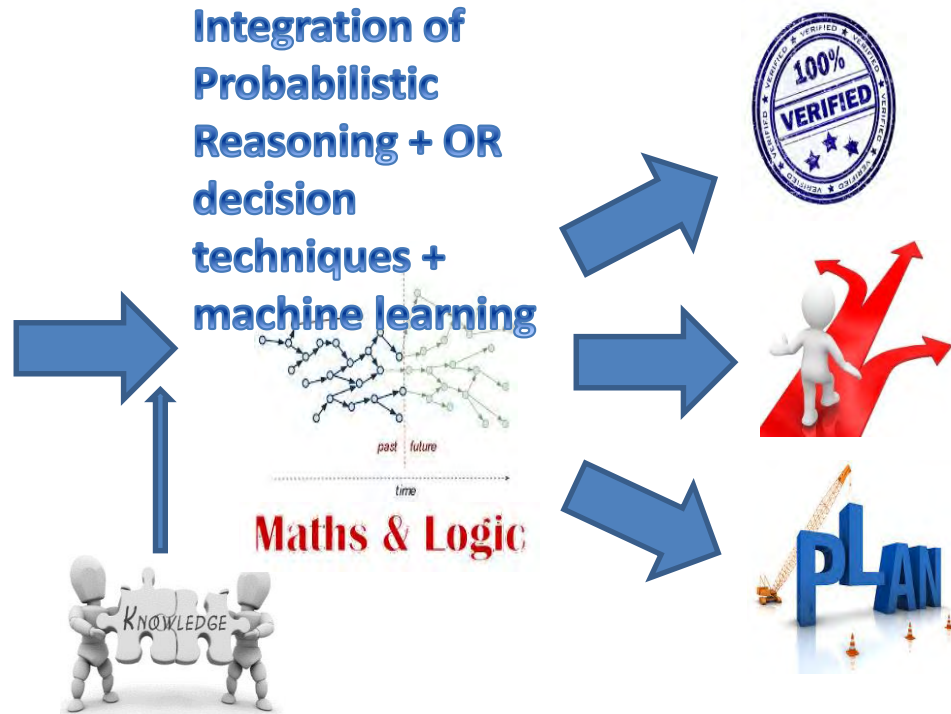
4-Player Kuhn Poker: Findings



4-Player Kuhn Poker: Findings



Event/Strategy Analytics



Event Analytics in current/new projects

- Singapore-UK joint cyber security project on smart grid security and privacy
 - With Andrew Martin (Oxford) and Bai Guangdong (SIT)
- Securify: A Compositional Approach of Building Security Verified System (\$6M)
 - With Liu Yang (NTU), Sun Jun (SUTD), Chin Weingan (NUS) etc
- Trustworthy systems from untrusted Components (\$6M)
 - With Abhik, Prateek (NUS) etc
- Singtel-NUS Cyber Security joint lab (\$43M).
 - With David Rosenblum, Liang Zhenkai (NUS), etc
- Blockchain verification using timed and game-theory based reasoning
 - With Muthu (Griffith), Jun, Yang, Guangdong etc

We are hiring and looking for new collaborators

Thank You!

Some related and background papers

- J. S Dong, L. Shi, and L. V. Khanh, **Sports Analytics Using Probabilistic Reasoning**, ICECCS 2015.
- J. Sun, Y. Liu, J. S. Dong, E. Andre. **Modeling and Verifying Hierarchical Real-time Systems using Stateful Timed CSP**. The ACM Transactions on Software Engineering and Methodology (TOSEM). 2014
- Y. Liu, W. Chen, Y. A. Liu, J. Sun, S. Zhang and J. S. Dong. **Verifying Linearizability via Optimized Refinement Checking**. IEEE Transactions on Software Engineering (TSE), 2013
- Y. Liu, J. Sun and J. S. Dong. **PAT 3: An Extensible Architecture for Building Multi-domain Model Checkers**. The 22nd annual International Symposium on Software Reliability Engineering (ISSRE 2011), Hiroshima, Japan, Nov 29 - Dec 2, 2011.
- J. Sun, Y. Liu, S. Song and J. S. Dong. **PRTS: An Approach for Model Checking Probabilistic Real-time Hierarchical Systems**. ICFEM'11, pages 147-162, Durham, UK, October 25-28, 2011.
- S. Zhang, J. Sun, J. Pang, Y. Liu and J. S. Dong. **On Combining State Space Reductions with Global Fairness Assumptions**. FM'11, pages 432 - 447, Lero, Limerick, Ireland, June 20 - 24, 2011.
- Y. Liu, J. Sun and J. S. Dong. **Analyzing Hierarchical Complex Real-time Systems**. *FSE '10*, Santa Fe, New Mexico, USA, 7-11 November 2010.
- C. Chen, J. S. Dong, J. Sun and A. Martin. **A Verification System for Interval-based Specification Languages**, ACM Transactions on Software Engineering and Methodology, Volume 19(4), pages 1 - 36, ACM. 2010
- C. Chen, J. S. Dong and J. Sun. **A Formal Framework for Modeling and Validating Simulink Diagrams**. Formal Aspects of Computing. 21(5), pages 451-483, Springer. Oct, 2009.
- J. Sun, Y. Liu, J. S. Dong and J. Pang. **PAT: Towards Flexible Verification under Fairness**. CAV '09, Grenoble, France, June 2009.
- J. S. Dong, P. Hao, S. C. Qin, J. Sun and Y. Wang, **Timed Automata Patterns**. IEEE Transactions on Software Engineering, vol. 34(6), pp 844-859, 2008.
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