```
#!/usr/bin/env python3
    # -*- coding: utf-8 -*-
 3
 4
    Example 2.5
 5
    Early Stopping
    Machine Learning for Engineering Problem Solving
 7
     @author: Austin Downey
 8
 9
10
     import IPython as IP
11
     IP.get ipython().run line magic('reset', '-sf')
12
13
     import numpy as np
14
     import matplotlib.pyplot as plt
15
     import sklearn as sk
16
17
18
    plt.close('all')
19
20
    #%% build the data sets
21
22
    # use 6 to help give a smooth curve that makes the case for early stopping
23
    np.random.seed(6)
24
25
    m = 20
26
    X = 6 * np.random.rand(m, 1) - 3
27
    Y = 0.5 * X**2 + X + 2 + np.random.randn(m, 1)
28
29
    # plot the data
30 plt.figure()
31
    plt.grid(True)
32
    plt.scatter(X,Y,color='gray')
33
    plt.xlabel('x')
34
    plt.ylabel('y')
35
36
    X \mod = np.linspace(-3,3,num=1000)
37
    X model = np.expand dims(X model,axis=1)
38
39
     X train, X val, y train, y val = sk.model selection.train test split(X, Y, test size=0.2)
40
41
     #%% perform early stopping
42
43
44
     # prepare the data
45
     poly scaler = sk.pipeline.Pipeline([("poly features", sk.preprocessing.PolynomialFeatures
46
         degree=90, include_bias=False)), ("std_scaler", sk.preprocessing.StandardScaler())])
47
     X_train_poly_scaled = poly_scaler.fit_transform(X_train)
48
     X val poly scaled = poly scaler.fit transform(X val)
49
50
     # set up the model, not that by setting max iter=1 it will only train one epoch
51
    model = sk.linear model.SGDRegressor(max iter=1, tol=0,learning rate="constant"
52
         ,eta0=0.0005,penalty=None,warm start=True)
53
54
55
     # Train the model in a loop to build the data set to investigate the benefit of early
     stopping
56
    val errors = []
57
    train errors = []
58
    for epoch in range(1000):
59
         model.fit(X_train_poly_scaled, y_train.ravel()) # continues where it left off
60
         y val predict = model.predict(X val poly scaled) # Predict the target values
61
         y train predict = model.predict(X train poly scaled) # Predict the target values
62
         val error = sk.metrics.mean squared error(y val, y val predict) # Calculate error
63
         train error = sk.metrics.mean squared error(y train.ravel(), y train predict) #
         Calculate error
64
         val errors.append(val error)
```

```
65
        train_errors.append(train_error)
66
67
   # plot the early learning curves, you may have to plot this a few times to get
# a set of curves that shows strong results
69 plt.figure()
70 plt.grid(True)
71 plt.plot(val_errors, label='validation data')
72 plt.plot(train_errors,'--',label='training data')
73 plt.ylabel('RMSE')
74 plt.xlabel('epoch')
75
    plt.legend()
76
77
78
79
80
81
```