

# CS131 Week 7

## Week 7 Lecture 1

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Prolog (finishing up)  
Scope("")  
Storage management

Last time:  $\text{+(x) :- x, !, fail.}$   
 $\text{+(_)}$ .

### **negation as failure**

"Anything I can't prove, must be false."

```
pr(cs31, cs131).  
pr(cs31, cs32).  
pr(cs131, cs132).  
...  
~(dance101, cs131).
```

### **Closed Word Assumption (CWA)**

Little tour of logic propositional logic  
"It is cold today." p  
"The 405 is busy." q  
... r

### **tautologies**

- redundant
- $(p \leftrightarrow q) \leftrightarrow (p \rightarrow q \wedge q \rightarrow p)$

### **0 order logic**

Four of logic  
ositional logic  
props.

old today.  
S is busy.

Prolog →

tautologies are redundant  
 $(p \leftrightarrow q) \leftrightarrow (p \rightarrow q \wedge q \rightarrow p)$   
(0-order logic)  
connectives

P	$p \wedge q$	$p \vee q$	$p \leftarrow q$	$p \rightarrow q$
q	$p \wedge q$	$p \vee q$	$p \leftarrow q$	$p \rightarrow q$
;	$p \cdot q$	$p + q$	$p \subset q$	$p \supset q$
	$p;q$	$p;q$	$p:-q$	$p:-q$
	$p,q$	$p q$		
	$p \& q$			

$p$	$q$	$p \wedge q$	$p \vee q$	$\neg p \vee q$	$p \rightarrow q$	$p \wedge q$	$p \leftarrow q$
0	0	0	0	1	1	0	0
0	1	0	1	1	1	0	1
1	0	0	1	1	0	1	1
1	1	1	1	1	1	1	1

### First order logic (predicate calculus)

Propositions have arguments

"Freeway X is busy."                     $p(X) \leftarrow$  notation to show we're using first order logic  
 "It was cold on day Y."                 $q(Y)$

Can't formulate r using p and q in Example below

- not  $p \wedge q$ ,  $p \mid q$ , etc.

Example:

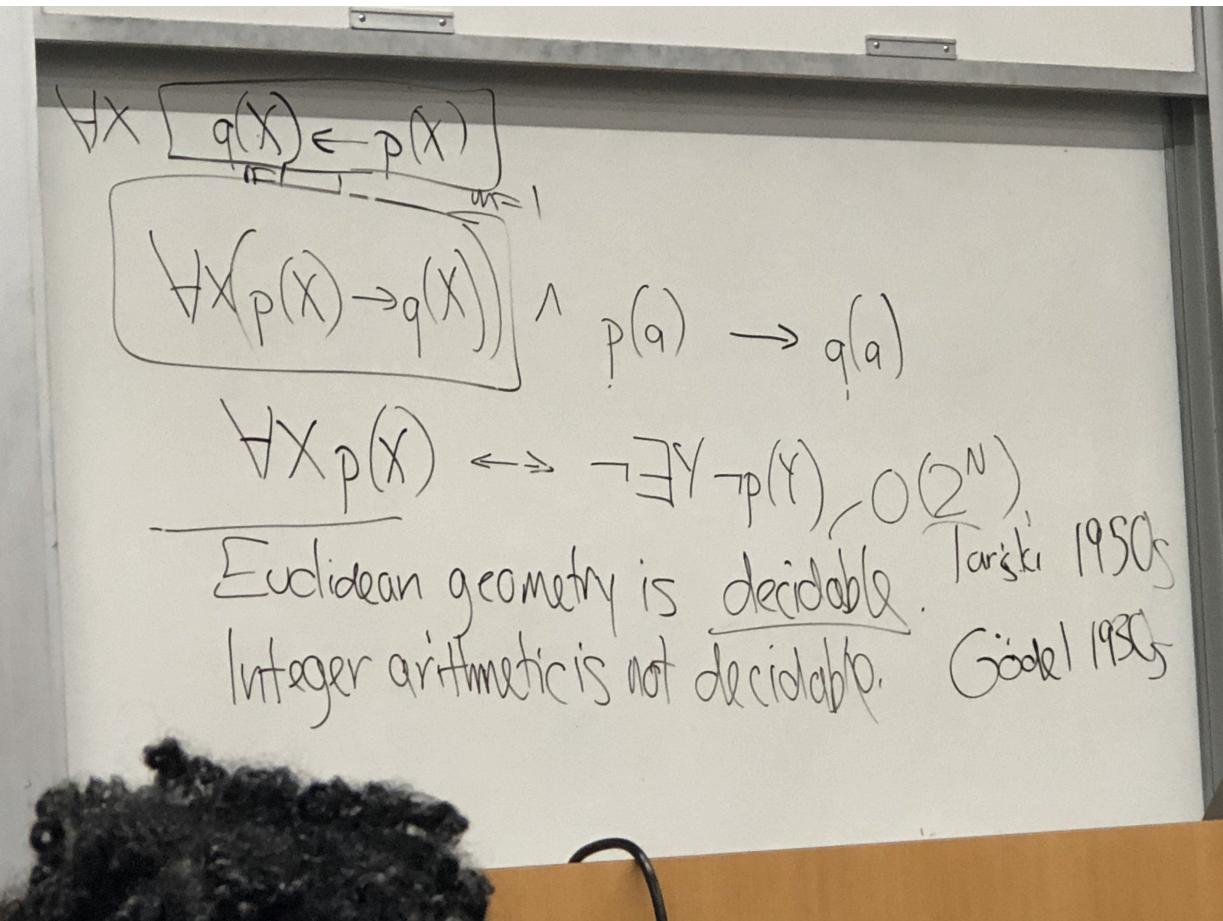
- All men are mortal.                    p
- Socrates is a man.                    q
- Socrates is mortal.                    r

Quantifiers:

"Freeway  $\underline{x}$  is busy."  $p(x)$       q       $\frac{S_1}{S_2}$   
"It was cold on day  $y$ ."  $q(y)$       r       $\frac{S_3}{S_4}$

Quantifiers       $\forall x p(x)$       for all  $P \wedge$   
                         $\exists x p(x)$       there exists

quantifiers



Can always convert logical form into clausal form

**Clausal form:**

- simplified version of predicate calculus
- Any set of predicate calculus statements can be converted to a set of equivalent clauses

Clausal form: Simplified version of predicate calculus.  
 any set of predicate calculus statements can be converted  
 all logical vars to a set of equivalent clauses  
 $\forall B_1 \vee B_2 \vee \dots \vee B_n \leftarrow A_1 \wedge A_2 \wedge \dots \wedge A_m$  ) each is a pred with args

## Approximations

Horn: Simplify by assuming  $n \leq 1$

**Horn clause:** (3 possibilities)

- $n = 1, m = 0$ . Prolog fact.
  - man(socrates)
- $n = 1, m > 0$ . Prolog rule.
  - mortal(X) :- man(X)
- $n = 0$ . Prolog query.
  - ?- mortal(socrates).
  - This is backwards: is same as false  $\leftarrow$  mortal(socrates)
    - Then q = false, p = ?
    - with truth table  $p \rightarrow q$ , p must be true
    - this means true  $\rightarrow$  false... BACKWARDS???
    - equivalent to  $\neg$ mortal(socrates).

## Prolog Interpreter

Works because Prolog interpreter uses proof by contradiction.

- true implies false means contradiction

database of facts

P

q

r

;

,

$\neg z$

query:  
m ?

Assume  
 $\neg m$   
 $\neg p$   
 $\neg q$   
 $\neg r$

$\neg z \rightarrow \text{false}$

then must be true.

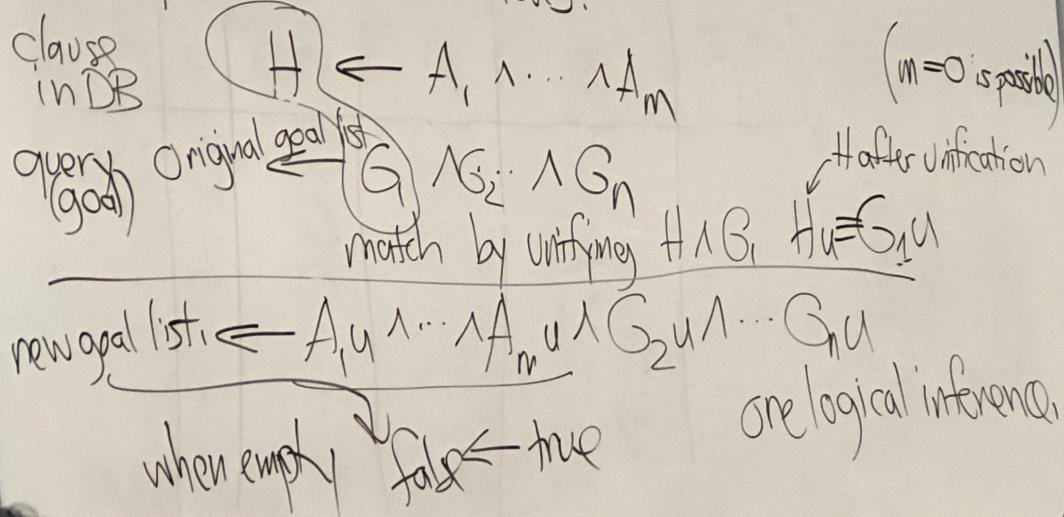
**Resolution Principle:** lets you infer true stmts from true stmts

- simplified for Horn clauses.

clause in DB:  $H \leftarrow A_1 \ \& \dots \ \& \ A_m$       ( $m = 0$  is possible)

query (goal)       $\leftarrow G_1 \ \& \ \dots \ \& \ G_n$

Resolution principle. lets you infer true stuff from true stuff  
 (Simplified for Horn clauses.)



He could ask us how to figure out how the OCaml interpreter works

- slightly simpler: not logic proof by contradiction

## Scope

```
{
    int n = &n == &n;
    int m = n + 1;
    {
        int n = m + 3;
        ...
    }
}
```

```
struct x {
    int v;
    struct x *next;
```

```

}

struct x v = {0, &v};

```

visibility modifiers in Java, visible in

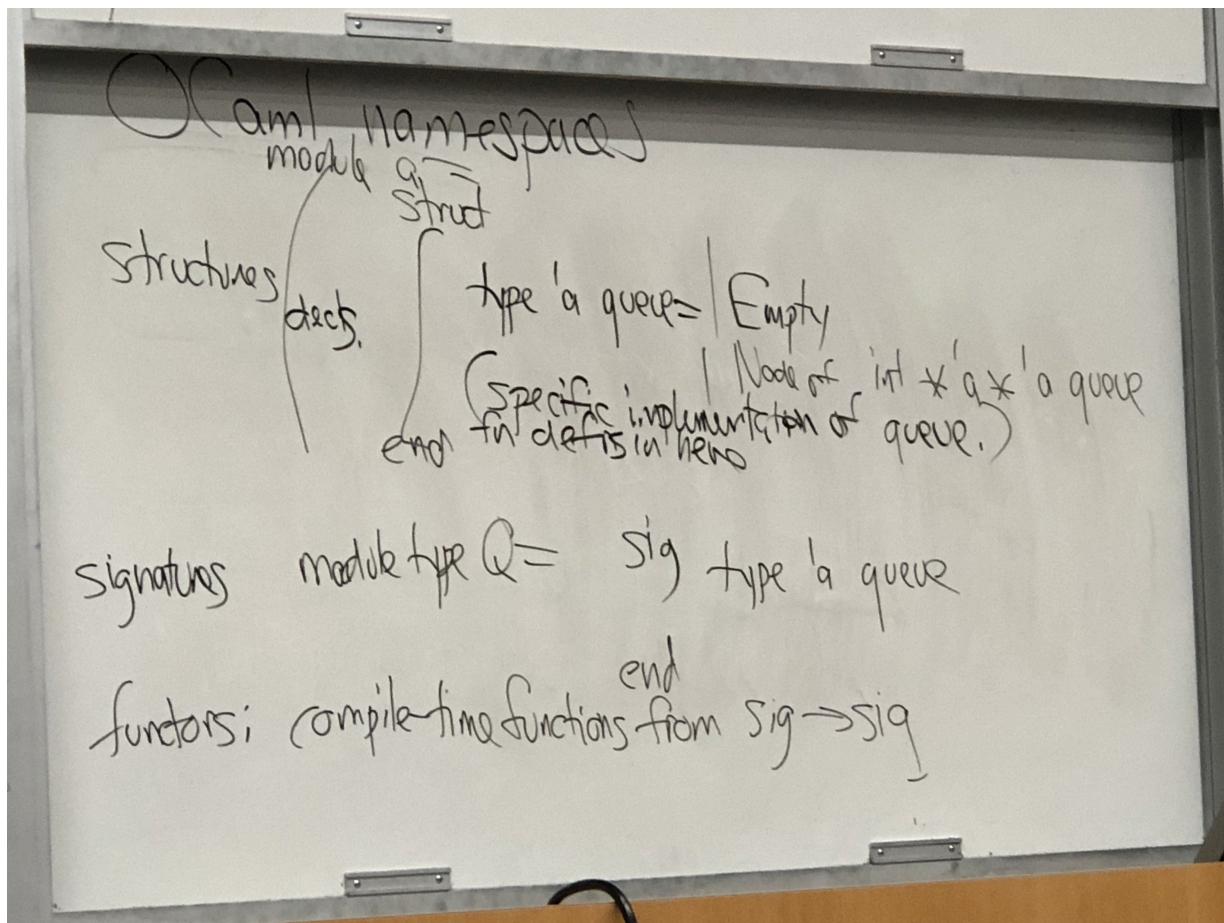
	current class	another class in same package	other subclasses outside package	elsewhere
private	y			
default	y	y		
protected	y	y	y	
public	y	y	y	y

```

class c {
    int n;           // default visibility
}

```

### Ocaml namespaces



**Signature:** like interface

**Structures:** the actual type variable implementing interface

**Functors:** compile time functions from sig —> sig

- more powerful than signature
- generates compile time functions from signatures

## Storage management

warmup. arrays.

All the following need storage:

- string literals
- objects computed dynamically
  - new
  - local vars \
  - stack for recursion
  - pointers to stack locations
  - functions (machine code, closures)
  - VNCZ flags (etc.)
  - function args
  - return addresses
  - buffers for I/O
  - memory manager

## Closures

functions packed in other functions that carry information about the function returned

```
(fun x -> fun y -> x + y) 12  
                  getchar()
```