

- 5 Suppose  $xH \cap yH \neq \emptyset$ . Then  $\exists z \in xH \cap yH \Rightarrow \exists h_1, h_2 \in H$  such that  $z = xh_1$  and  $z = yh_2$ . Thus,

$$x = zh_1^{-1} = yh_2h_1^{-1} \text{ and } xH = yh_2h_1^{-1}H = y(h_2h_1^{-1}H) = yH$$

Therefore,  $xH = yH$

- 6 Suppose that  $x^{-1}y = h \in H$ . Let  $xk \in xH$  with  $k \in H$ . Then we have,  $xk = (yh^{-1})k = y(h^{-1}k) \in yH$ . Thus,  $xH \subseteq yH$

The proof of  $yH \subseteq xH$  is similar.

Therefore,  $xH = yH$