

CSI3108-01

2015. 09. 21

## Programming HW#3

(Divide-and-Conquer)

Max 40 points

Due on Oct. 2 (Fri) by 5pm

Implement FFT in the textbook for polynomial multiplication using Java. Input to your program is an arbitrary polynomial  $A(x)$  in the coefficient representation.

For evaluation, implement the function FFT in Figure 2.9. Assume that all the coefficients of a polynomial are *integers*.

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**Figure 2.9** The fast Fourier transform

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function FFT( $a, \omega$ )

Input: An array  $a = (a_0, a_1, \dots, a_{n-1})$ , for  $n$  a power of 2

A primitive  $n$ th root of unity,  $\omega$

Output:  $M_n(\omega) a$

if  $\omega = 1$ : return  $a$

$(s_0, s_1, \dots, s_{n/2-1}) = \text{FFT}((a_0, a_2, \dots, a_{n-2}), \omega^2)$

$(s'_0, s'_1, \dots, s'_{n/2-1}) = \text{FFT}((a_1, a_3, \dots, a_{n-1}), \omega^2)$

for  $j = 0$  to  $n/2 - 1$ :

$r_j = s_j + \omega^j s'_j$

$r_{j+n/2} = s_j - \omega^j s'_j$

return  $(r_0, r_1, \dots, r_{n-1})$

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Use the following equation for implementation of  $\omega$ .

$$e^{2\pi i/n} = \cos\left(\frac{2\pi}{n}\right) + i \cdot \sin\left(\frac{2\pi}{n}\right),$$

where  $i = \sqrt{-1}$ , and the circular constant  $\pi$  have to be matched by 3.141592.

## Input

The first line has the number of test cases. From the second line, each test case is given in a single line by ordering coefficients from the constant to the highest degree. Note that [the highest degree of a polynomial is 63](#).

## Output

For each test case, print '#test case number' in the first line. And then print  $n$  values; one value per line in the form of 'real part imaginary part', where  $n$  is the number of points.

## Sample Input

```
20 // the no of test cases = 20
2 1 2 3 // highest deg=2,  $1 + 2x + 3x^2$ 
5 -6 -5 -4 -3 -2 -1 // highest deg=5,  $-6 - 5x - 4x^2 - 3x^3 - 2x^4 - x^5$ 
7 0 1 2 3 4 5 6 7 // example in your text book
...
```

## Sample Output

#1	#3
6.000000 0.000000	28.000000, 0.000000
-2.000000 2.000000	-4.000001 -9.656854
2.000000 0.000000	-4.000000 -4.000000
-2.000000 -2.000000	-4.000001 -1.656854
#2	-4.000000 0.000000
-21.000000 0.000000	-3.999999 1.656854
-4.707108 -8.949747	-4.000000 4.000000
-4.000000 -3.000000	-3.999999 9.656854
-3.292894 -0.949748	#4
-3.000000 0.000000	...
-3.292892 0.949747	
-4.000000 3.000000	
-4.707106 8.949748	