

```

result := {R};
done := false;
compute F+;
while (not done) do
  if (there is a schema Ri in result that is not in BCNF)
    then begin
      let α → β be a nontrivial functional dependency that
        holds on Ri such that α → Ri is not in F+,
        and α ∩ β = ∅;
      result := (result - Ri) ∪ (Ri - β) ∪ (α, β);
    end
  else done := true;

```

To check if a relation R<sub>i</sub> in a decomposition of R is in BCNF,

- Either test R<sub>i</sub> for BCNF with respect to the **restriction** of F to R<sub>i</sub> (that is, all FDs in F<sup>+</sup> that contain only attributes from R<sub>i</sub>)
- or use the original set of dependencies F that hold on R, but with the following test:
  - for every set of attributes α ⊆ R<sub>i</sub>, check that α<sup>+</sup> (the attribute closure of α) either includes no attribute of R<sub>i</sub> - α, or includes all attributes of R<sub>i</sub>.
  - ▶ If the condition is violated by some α → β in F, the dependency α → (α<sup>+</sup> - α) ∩ R<sub>i</sub> can be shown to hold on R<sub>i</sub>, and R<sub>i</sub> violates BCNF.
  - ▶ We use above dependency to decompose R<sub>i</sub>

```

Let Fc be a canonical cover for F;
i := 0;
for each functional dependency α → β in Fc do
  if none of the schemas Rj, 1 ≤ j ≤ i contains α β
    then begin
      i := i + 1;
      Ri := α β
    end
  if none of the schemas Rj, 1 ≤ j ≤ i contains a candidate key for R
    then begin
      i := i + 1;
      Ri := any candidate key for R;
    end
/* Optionally, remove redundant relations */
repeat
  if any schema Rj is contained in another schema Rk
    then /* delete Rj */
      Rj = Rk;
      i = i - 1;
return (R1, R2, ..., Ri)

```

Consider a set F of functional dependencies and the functional dependency α → β in F.

To test if attribute A ∈ α is extraneous in α

1. compute ({α} - A)<sup>+</sup> using the dependencies in F
2. check that ({α} - A)<sup>+</sup> contains β; if it does, A is extraneous in α

To test if attribute A ∈ β is extraneous in β

1. compute α<sup>+</sup> using only the dependencies in F' = (F - {α → β}) ∪ {α → (β - A)},
2. check that α<sup>+</sup> contains A; if it does, A is extraneous in β