

Policy Evaluation

The Big Picture

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Winter Term 2021

Recap I : Markov Decision Process (MDP)

- ▶ Markov Decision Process is Markov Reward Process + actions
- ▶ Definition of MDP
 - ▶ S is a (finite) set of Markov states $s \in S$
 - ▶ A is a (finite) set of actions $a \in A$
 - ▶ P is dynamics/transition model for each action, that specifies $P(s_{t+1} = s' \mid s_t = s, a_t = a)$
 - ▶ R is a reward function $R(s_t = s, a_t = a) = \mathbb{E}[r_t \mid s_t = s, a_t = a]$
 - ▶ Sometimes R is also defined based on (s) or on (s, a, s')
 - ▶ Discount factor $\gamma \in [0, 1]$
- ▶ MDP is tuple (S, A, P, R, γ)

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↪ Unfortunately, we often do not have access to true MDP models

Recap II

- ▶ Definition of Return G_t (for a MRP)
 - ▶ Discounted sum of rewards from time step t to horizon

$$G_t = r_t + \gamma r_{t+1} + \gamma^2 r_{t+2} + \gamma^3 r_{t+3} + \dots$$

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- ▶ Expected return from starting in state s under policy π

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- ▶ Definition of State-Action Value Function $Q^\pi(s, a)$

- ▶ Expected return from starting in state s , taking action a and then following policy π

$$\begin{aligned} Q^\pi(s, a) &= \mathbb{E}_\pi[G_t \mid s_t = s, a_t = a] \\ &= \mathbb{E}_\pi[r_t + \gamma r_{t+1} + \gamma^2 r_{t+2} + \gamma^3 r_{t+3} + \dots \mid s_t = s, a_t = a] \end{aligned}$$

Goal for this week

- ▶ Assumption: We don't have the exact model of the environment (i.e., model-free), but we can query the environment ("playing roll-outs")
 - ▶ state space and action space are in principle known
 - ▶ we don't know the transition probabilities beforehand
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- ▶ Goal for this week: We want to learn $V^\pi(s)$ or $Q^\pi(s, a)$ (depending on the RL algorithm we want to use) by only querying the unknown MDP