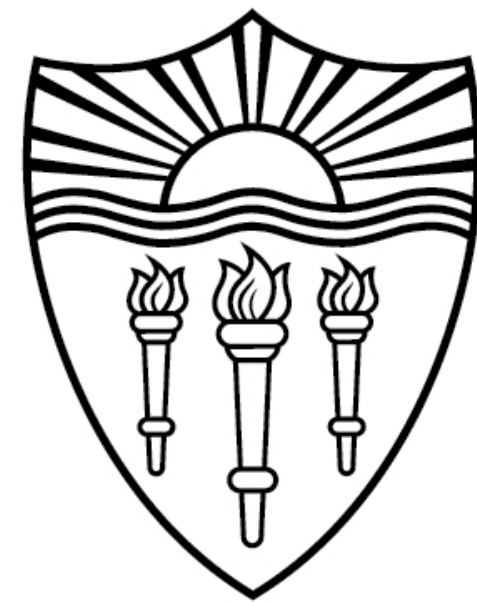


CSCI 544: Applied Natural Language Processing

Sequence Labeling-I

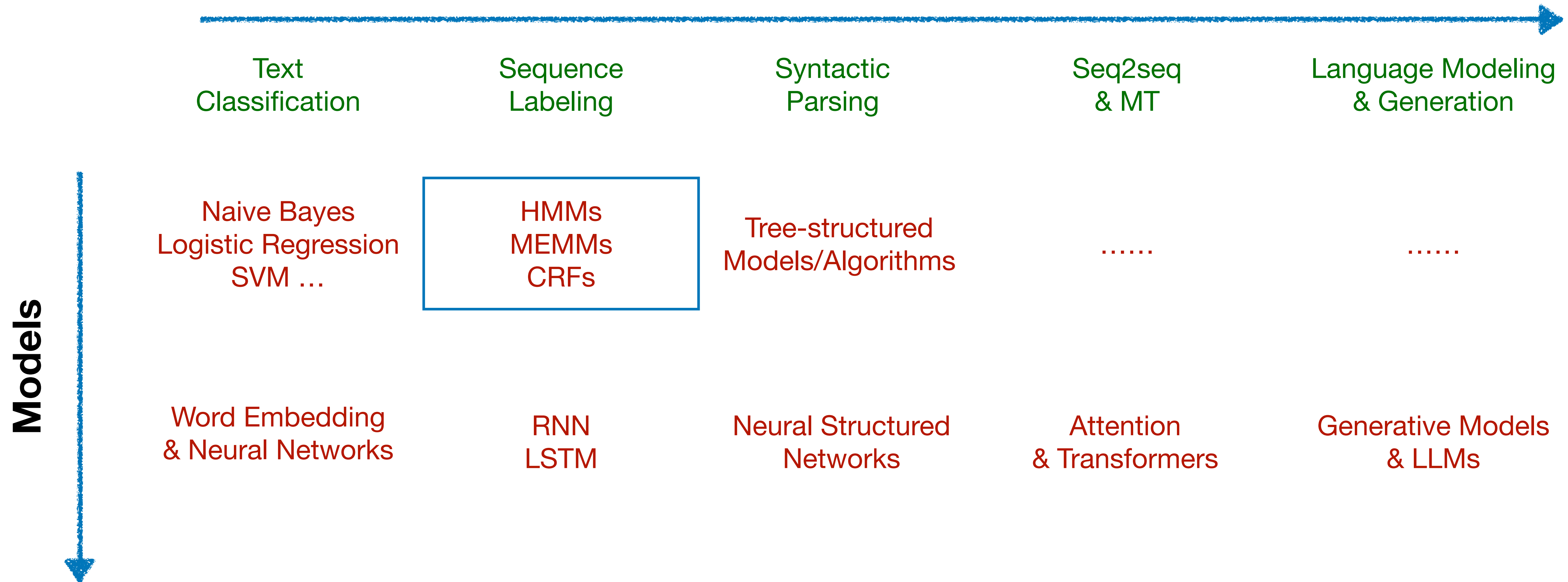
Xuezhe Ma (Max)



USC University of
Southern California

Course Organization

NLP Tasks



Overview

- **The Sequence Labeling Problem**
 - General Structured Prediction Tasks
 - Part-of-speech Tagging: A case study
 - Generative Models vs. Discriminative Models
- **Hidden Markov Model (HMM)**
 - Basic definitions
 - Parameter estimation
 - The Viterbi algorithm
- **Log-Linear Models**
 - Maximum Entropy Markov Models (MEMMs)
 - Conditional Random Fields (CRFs)

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Structured Prediction

What is Structured Prediction

- Unstructured Prediction
 - Output Y consists of a **single component**



X



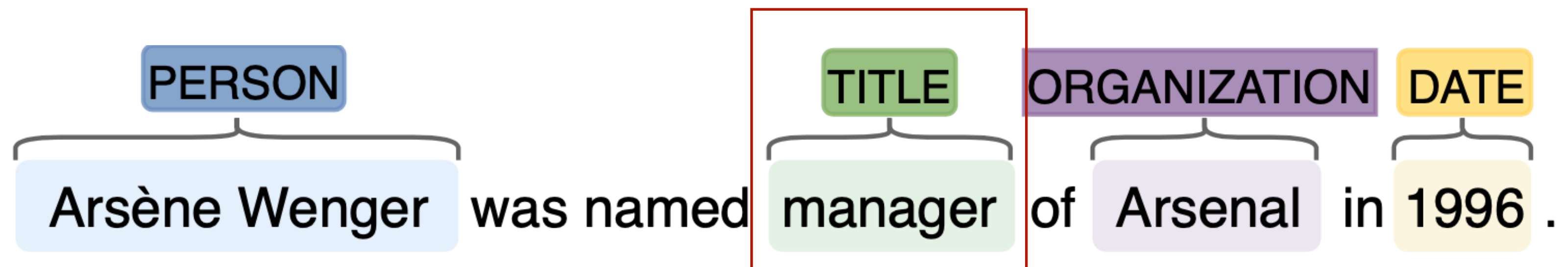
{**Cat**, Dog, Finch, Owl}

Y

Structured Prediction

- Y consists of **multiple components** $Y = \{y_1, y_2, \dots, y_n\}$

Named Entity Recognition



$$Y_i = \langle \mathbf{manager} \rightarrow \mathbf{Title} \rangle$$

Structured Prediction

- Y consists of **multiple components** $Y = \{y_1, y_2, \dots, y_n\}$

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X



Max is working at USC

↑
 Y_1

↑
 Y_2

↑
 Y_3

↑
 Y_4

↑
 Y_5

Structured Prediction

- Y consists of **multiple components** $Y = \{y_1, y_2, \dots, y_n\}$
- **(Strong) correlations** between output components

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X



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↑
 Y_1

↑
 Y_2

↑
 Y_3

↑
 Y_4

↑
 Y_5

Structured Prediction

- Y consists of **multiple components** $Y = \{y_1, y_2, \dots, y_n\}$
- **(Strong) correlations** between output components
- **Exponential** output space
 - Decoding: $y^* = \operatorname{argmax}_{y \in \mathcal{Y}} p(y | x)$

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X



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↑
 Y_1

↑
 Y_2

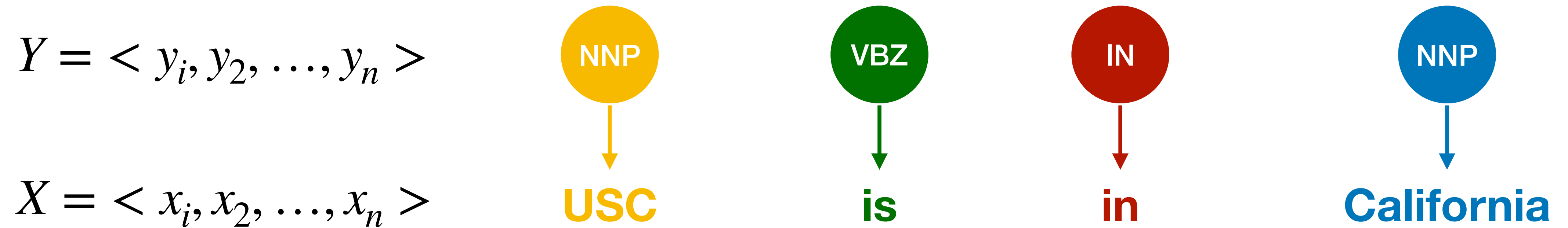
↑
 Y_3

↑
 Y_4

↑
 Y_5

What is Sequence Labeling?

A type of structured prediction tasks



Assigning each token of X , e.g. x_i a corresponding label y_i

Why Sequence Labeling?

Part-of-Speech Tagging

PRP VBD DT NN IN DT NN
I saw a girl with a telescope

Named Entity Recognition

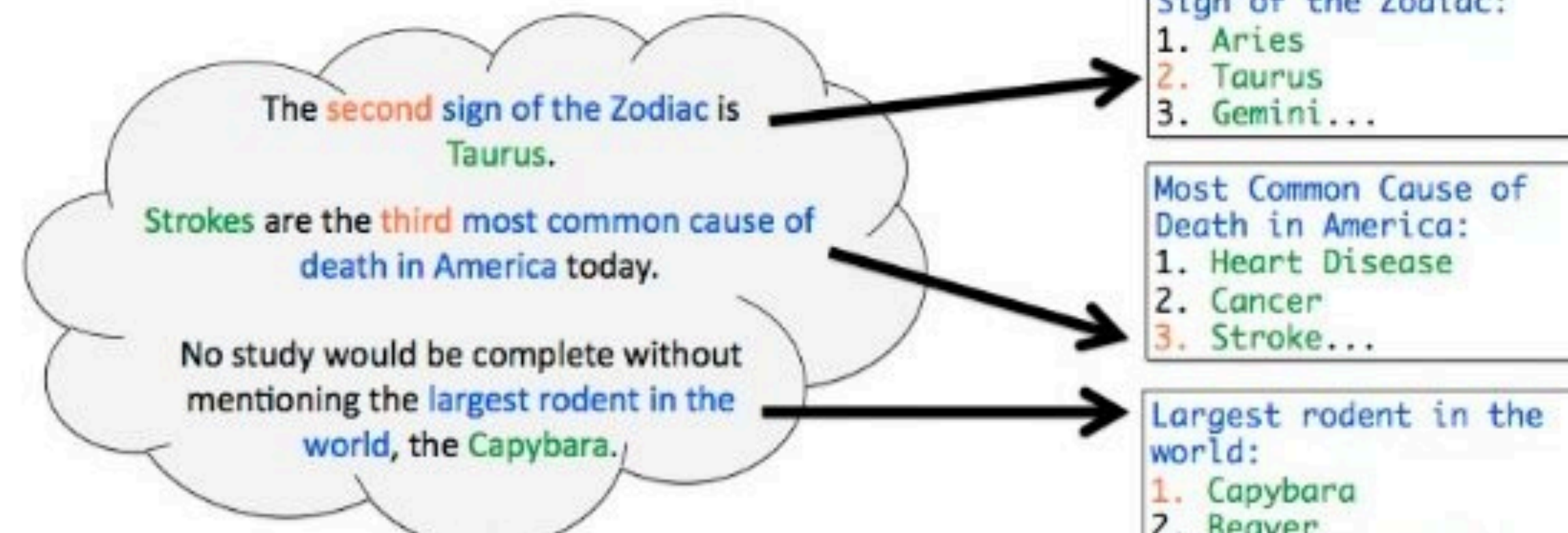
PERSON TITLE ORGANIZATION DATE
Arsène Wenger was named manager of Arsenal in 1996 .

Information Extraction

Unstructured Web Text

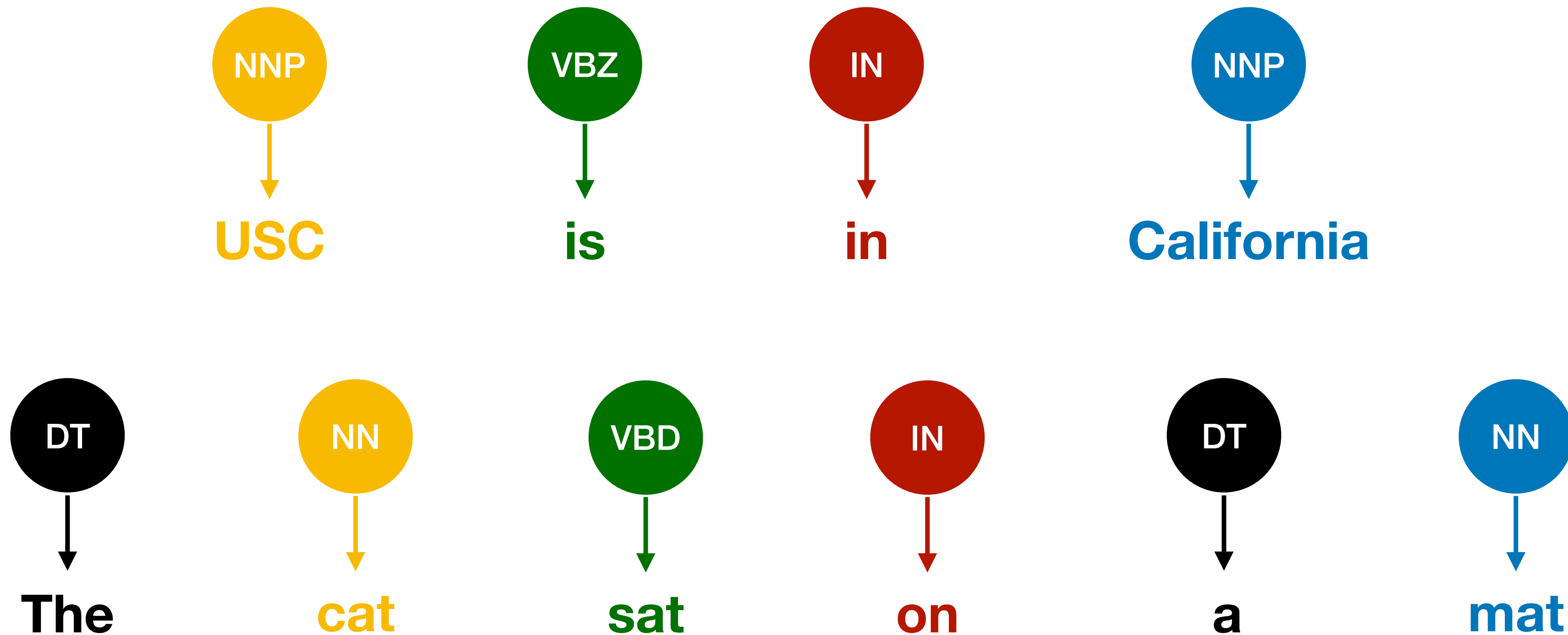


Structured Sequences



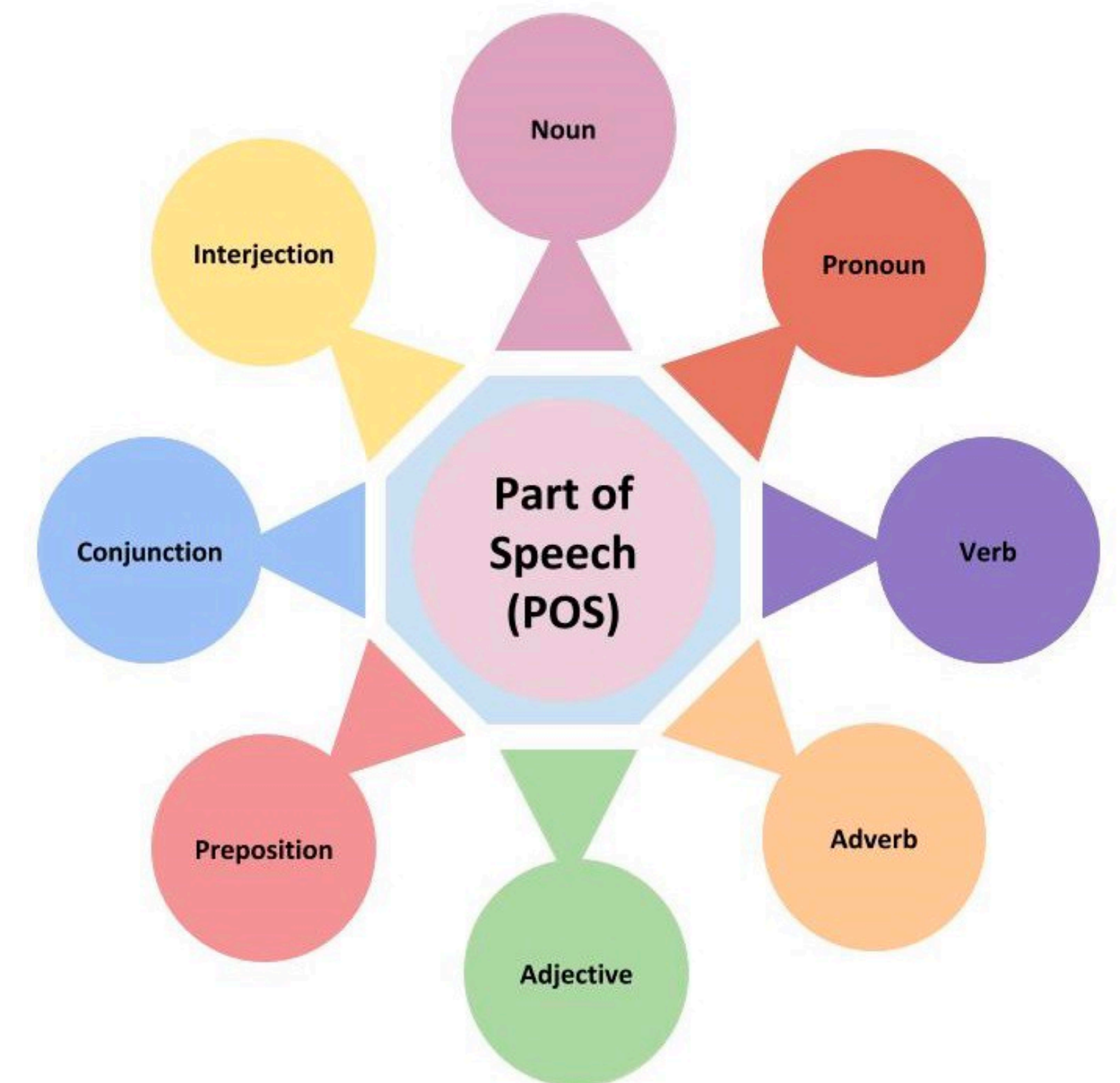
What are Part-of-Speech (POS) Tags

- Word classes or syntactic categories
- Reveal useful information about the syntactic role of a word (and its neighbors!)



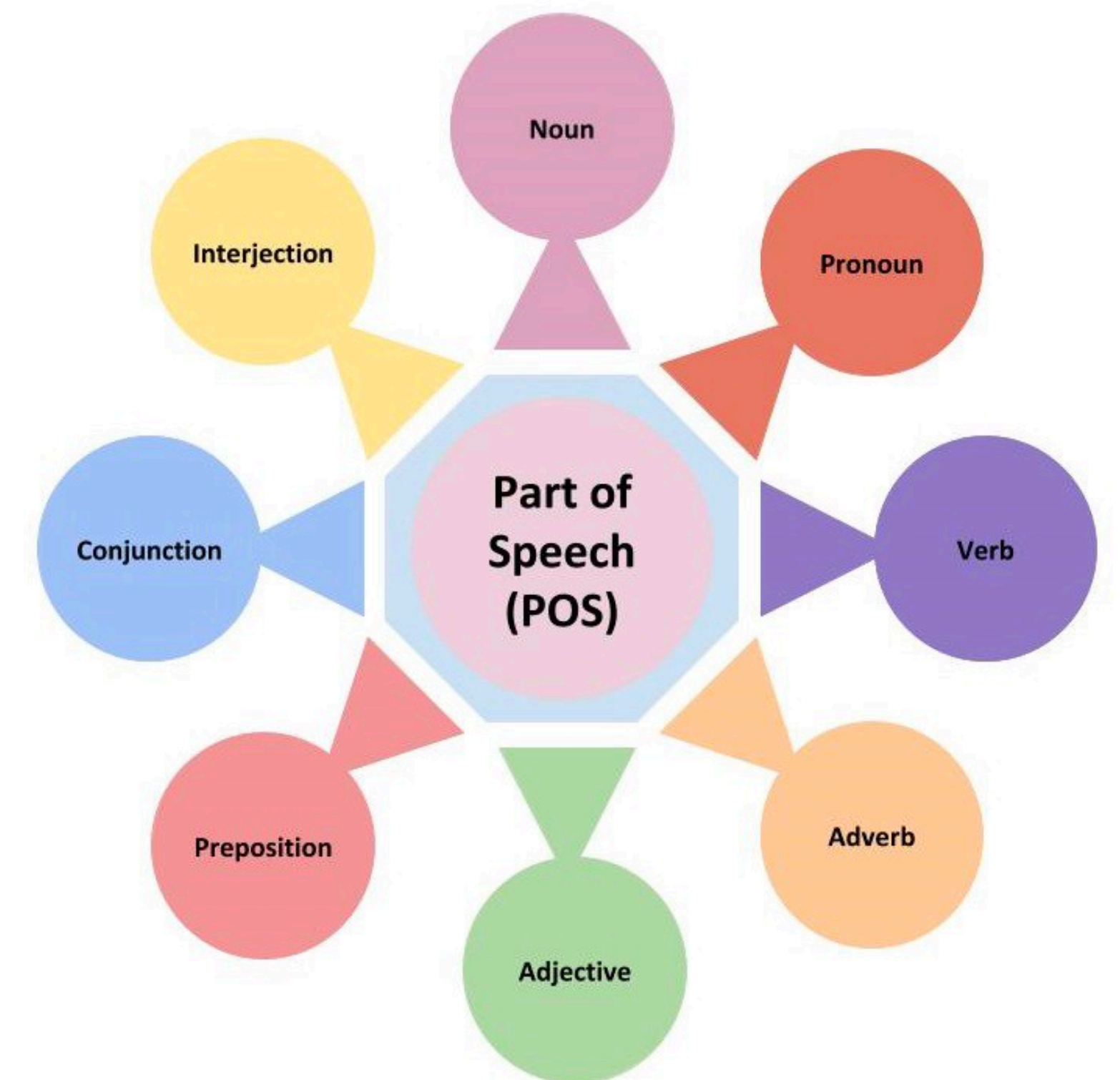
Part of Speech

- Different words have different syntactic functions
- Can be roughly divided into two classes
 - **Closed class:** fixed membership, function words
 - e.g. prepositions (in, on, of), determiners (a, the)
 - **Open class:** New words get added frequently
 - e.g. nouns (Twitter, Facebook), verbs (google), adjectives and adverbs.



Part of Speech

- How many part of speech tags do you think English has?
 - A. < 10
 - B. 10 - 30
 - C. 30 - 50
 - D. > 50



Penn Tree Bank Tagset

Tag	Description	Example	Tag	Description	Example	Tag	Description	Example
CC	coordinating conjunction	<i>and, but, or</i>	PDT	predeterminer	<i>all, both</i>	VBP	verb non-3sg present	<i>eat</i>
CD	cardinal number	<i>one, two</i>	POS	possessive ending	<i>'s</i>	VBZ	verb 3sg pres	<i>eats</i>
DT	determiner	<i>a, the</i>	PRP	personal pronoun	<i>I, you, he</i>	WDT	wh-determ.	<i>which, that</i>
EX	existential 'there'	<i>there</i>	PRP\$	possess. pronoun	<i>your, one's</i>	WP	wh-pronoun	<i>what, who</i>
FW	foreign word	<i>mea culpa</i>	RB	adverb	<i>quickly</i>	WP\$	wh-possess.	<i>whose</i>
IN	preposition/ subordin-conj	<i>of, in, by</i>	RBR	comparative adverb	<i>faster</i>	WRB	wh-adverb	<i>how, where</i>
JJ	adjective	<i>yellow</i>	RBS	superlatv. adverb	<i>fastest</i>	\$	dollar sign	<i>\$</i>
JJR	comparative adj	<i>bigger</i>	RP	particle	<i>up, off</i>	#	pound sign	<i>#</i>
JJS	superlative adj	<i>wildest</i>	SYM	symbol	<i>+, %, &</i>	“	left quote	<i>‘ or “</i>
LS	list item marker	<i>1, 2, One</i>	TO	“to”	<i>to</i>	”	right quote	<i>’ or ”</i>
MD	modal	<i>can, should</i>	UH	interjection	<i>ah, oops</i>	(left paren	<i>[, (, {, <</i>
NN	sing or mass noun	<i>llama</i>	VB	verb base form	<i>eat</i>)	right paren	<i>],), }, ></i>
NNS	noun, plural	<i>llamas</i>	VBD	verb past tense	<i>ate</i>	,	comma	<i>,</i>
NNP	proper noun, sing.	<i>IBM</i>	VBG	verb gerund	<i>eating</i>	.	sent-end punc	<i>. ! ?</i>
NNPS	proper noun, plu.	<i>Carolinas</i>	VBN	verb past part.	<i>eaten</i>	:	sent-mid punc	<i>: ; ... - -</i>

45 tags!
(Marcus et al., 1993)

The Task of Part of Speech Tagging

- Tag each word with its part of speech
- Disambiguation task: each word might have different senses/functions

- The/DT **back/ADJ** door/NN

- On/IN my/PRP\$ **back/NN**

- Win/VB the/DT voters/NNS **back/RP**

←
←
← Same word, different tags

Types:		WSJ		Brown	
Unambiguous	(1 tag)	44,432	(86%)	45,799	(85%)
Ambiguous	(2+ tags)	7,025	(14%)	8,050	(15%)
Tokens:					
Unambiguous	(1 tag)	577,421	(45%)	384,349	(33%)
Ambiguous	(2+ tags)	711,780	(55%)	786,646	(67%)

A Simple Baseline

- Many words might be easy to disambiguate
- **Most Frequent Class**: Assign each token (word) to the class it occurred most in the training data. (e.g. student/NN)
 - Entirely discarding contextual information
- How accurate do you think this baseline would be at tagging words?
 - A. < 50%
 - B. 50% - 75%
 - C. 75% - 90%
 - D. > 90%

Accurately tags **92.34%** of word tokens on Wall Street Journal (WSJ)

POS Tagging **Not** Solved!

- State of the art: $\sim 97\%$
- Sentence level accuracies
 - Average length of English sentence ~ 14 words
 - $0.92^{14} = 31\%$ vs. $0.97^{14} = 65\%$
- Highly relying on domain information
 - Training data and testing data must be from the same domain
 - $< 70\%$ on data from social media

Some Observations

- The function (or POS) of a word depends on its context
 - The/DT **back/ADJ** door/NN
 - On/IN my/PRP\$ **back/NN**
 - Win/VB the/DT voters/NNS **back/RP**
- Certain POS combinations are extremely unlikely
 - **<JJ, DT>** (“good the”) or **<DT, IN>** (“the in”)
- Better to make predictions on entire sentences instead of individual words

Sequence Labeling Models!

Generative Models vs Discriminative Models

Generative vs Discriminative: Revisit

- **Generative Models**
 - Modeling the joint distribution: $P(X, S)$
- **Discriminative Models**
 - Modeling $P(S | X)$ directly

Generative

Classification

Naive Bayes: $P(s)P(x | s)$

Sequence Labeling

HMM:

$$P(s_1, \dots, s_n)P(x_1, \dots, x_n | s_1, \dots, s_n)$$

Discriminative

Logistic Regression: $P(s | x)$

MEMM/CRF:

$$P(s_1, \dots, s_n | x_1, \dots, x_n)$$

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Hidden Markov Models

Markov Sequences

- ▶ Consider a sequence of random variables X_1, X_2, \dots, X_m where m is the length of the sequence
- ▶ Each variable X_i can take any value in $\{1, 2, \dots, k\}$
- ▶ How do we model the joint distribution

$$P(X_1 = x_1, X_2 = x_2, \dots, X_m = x_m)$$

?

The Markov Assumption

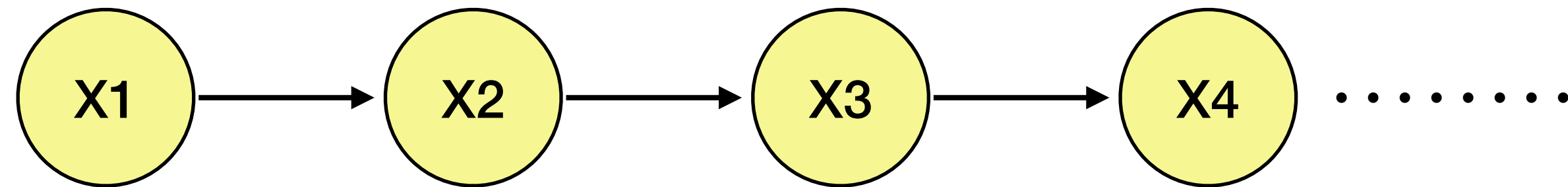
$$\begin{aligned} & P(X_1 = x_1, X_2 = x_2, \dots, X_m = x_m) \\ &= P(X_1 = x_1) \prod_{j=2}^m P(X_j = x_j | X_1 = x_1, \dots, X_{j-1} = x_{j-1}) \\ &= P(X_1 = x_1) \prod_{j=2}^m P(X_j = x_j | X_{j-1} = x_{j-1}) \quad \text{Markov assumption} \end{aligned}$$

- ▶ The first equality is exact (by the chain rule).
- ▶ The second equality follows from *the Markov assumption*: for all $j = 2 \dots m$,

$$P(X_j = x_j | X_1 = x_1, \dots, X_{j-1} = x_{j-1}) = P(X_j = x_j | X_{j-1} = x_{j-1})$$

Markov Sequences

- A Generative Model for Sequences



Pick x_1 at random from the distribution $P(X_1)$

Pick x_2 at random from the distribution $P(X_2 | X_1 = x_1)$

Pick x_t at random from the distribution $P(X_t | X_{t-1} = x_{t-1})$

Modeling Pairs of Sequences

- In Sequence Labeling, we need to model pairs of sequences

$S = S_1, S_2, \dots, S_n$



$X = X_1, X_2, \dots, X_n$

USC

is

in

California

Hidden Markov Models (HMMs) allow us to *jointly* reason over X and S

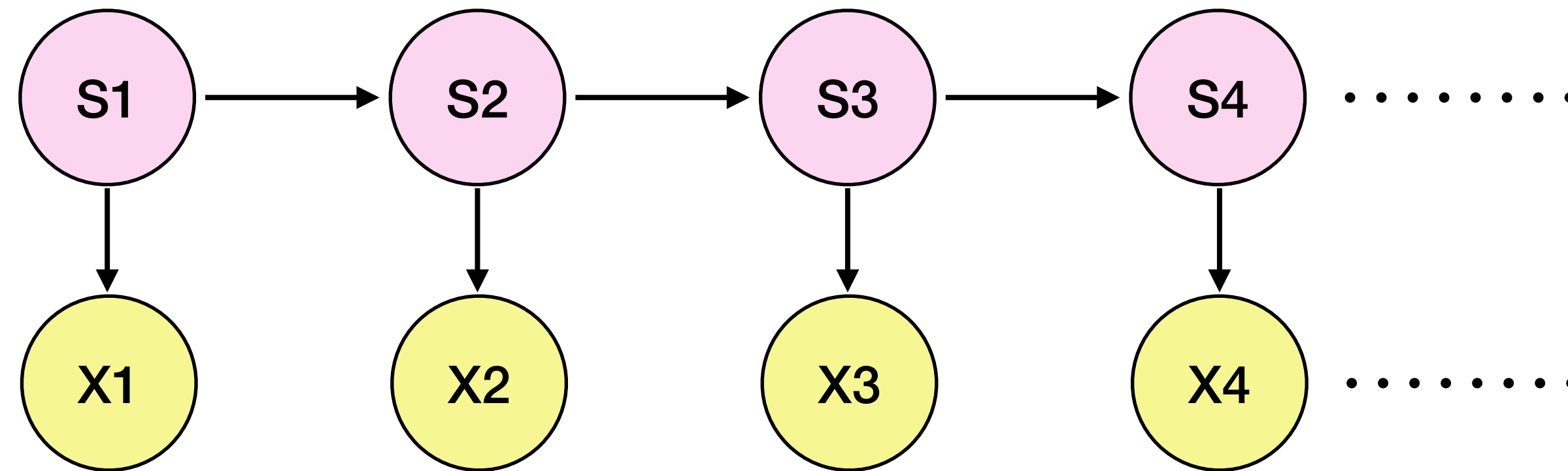
Hidden Markov Models

- ▶ We have two sequences of random variables:
 X_1, X_2, \dots, X_m and S_1, S_2, \dots, S_m
- ▶ Intuitively, each X_i corresponds to an “observation” and each S_i corresponds to an underlying “state” that generated the observation. Assume that each S_i is in $\{1, 2, \dots, k\}$, and each X_i is in $\{1, 2, \dots, o\}$
- ▶ How do we model the joint distribution

$$P(X_1 = x_1, \dots, X_m = x_m, S_1 = s_1, \dots, S_m = s_m)$$

?

The HMM Assumptions



1. Markov Assumption on S

$$P(S_j = s_j | S_{j-1} = s_{j-1}, \dots, S_1 = s_1) = P(S_j = s_j | S_{j-1} = s_{j-1})$$

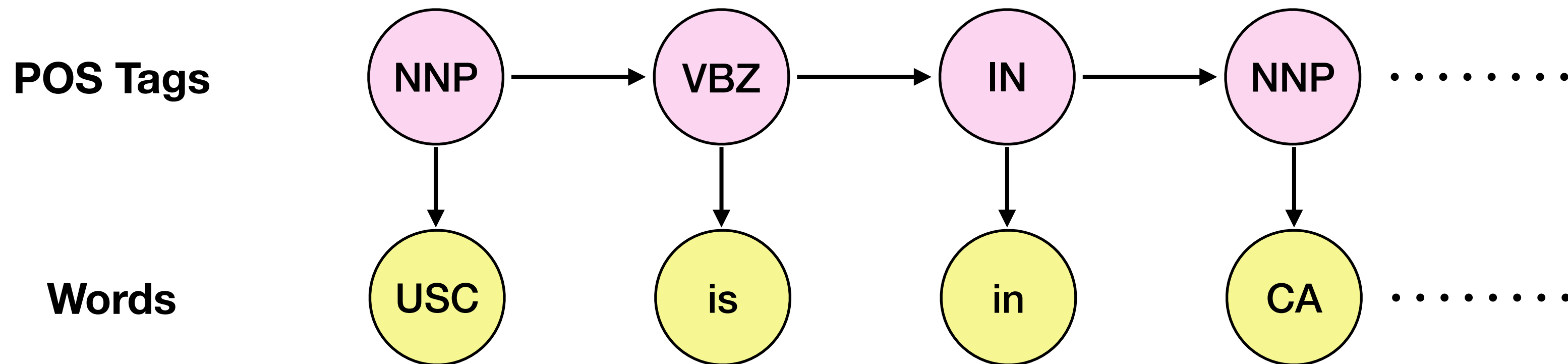
Transition Probabilities

2. Conditional Independence on X given S

$$P(X_1 = x_1, \dots, X_m = x_m | S_1 = s_1, \dots, S_m = s_m) = \prod_{j=1}^m P(X_j = x_j | S_j = s_j)$$

Emission Probabilities

The HMM Assumptions



1. Markov Assumption on S

$$P(S_3 = \text{IN} \mid S_2 = \text{VBZ}, S_1 = \text{NNP}) = P(S_3 = \text{IN} \mid S_2 = \text{VBZ})$$

2. Conditional Independence on X given S

$$P(\text{USC is in CA} \mid \text{NNP VBZ IN NNP}) = P(\text{USC} \mid \text{NNP})P(\text{is} \mid \text{VBZ})P(\text{in} \mid \text{IN})P(\text{CA} \mid \text{NNP})$$

Which assumption do you think is stronger?

Joint Distribution of Sequence Pairs in HMMs

$$P(X_1 = x_1, \dots, X_m = x_m, S_1 = s_1, \dots, S_m = s_m)$$

$$= P(X_1 = x_1, \dots, X_m = x_m \mid S_1 = s_1, \dots, S_m = s_m)$$

Output Independence

$$\times P(S_1 = s_1, \dots, S_m = s_m)$$

Markov Assumption

$$= \prod_{j=1}^m P(X_j = x_j \mid S_j = s_j)$$

How to model $P(X_j = x_j \mid S_j = s_j)$
and $P(S_j = s_j \mid S_{j-1} = s_{j-1})$?

$$\times P(S_1 = s_1) \prod_{j=2}^m P(S_j = s_j \mid S_{j-1} = s_{j-1})$$

Homogeneous HMMs

- In a *homogeneous* HMM, we make an additional assumption:

$$P(S_j = s_j | S_{j-1} = s_{j-1}) = t(s_j | s_{j-1})$$

$$P(X_j = x_j | S_j = s_j) = e(x_j | s_j)$$

- Idea behind this assumption: the transition and emission probabilities do **NOT** depend on the **position** in the Markov chain (do not depend on the index j)

The Model Form for Homogeneous HMMs

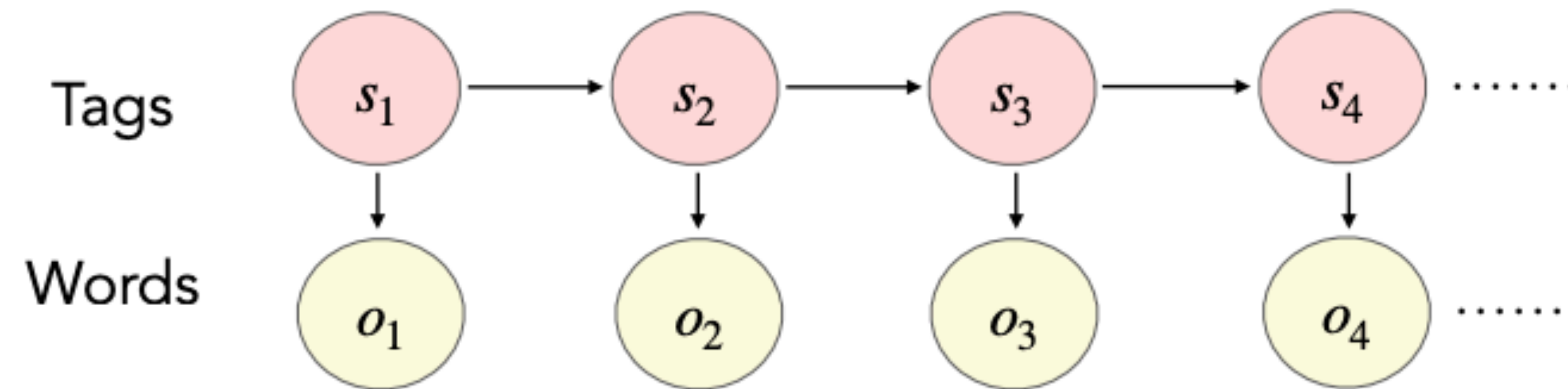
- ▶ The model takes the following form:

$$p(x_1 \dots x_m, s_1 \dots s_m; \underline{\theta}) = t(s_1) \prod_{j=2}^m t(s_j | s_{j-1}) \prod_{j=1}^m e(x_j | s_j)$$

- ▶ Parameters in the model:

1. Initial state parameters $t(s)$ for $s \in \{1, 2, \dots, k\}$
2. Transition parameters $t(s' | s)$ for $s, s' \in \{1, 2, \dots, k\}$
3. Emission parameters $e(x | s)$ for $s \in \{1, 2, \dots, k\}$ and $x \in \{1, 2, \dots, o\}$

Example: Sequence Probability



What is the joint probability $P(\text{the cat, DT NN})$?

- A) $(0.8 * 0.8) * (0.9 * 0.5)$
- B) $(0.2 * 0.8) * (0.9 * 0.5)$
- C) $(0.3 * 0.7) * (0.5 * 0.5)$

Dummy start state

		s_{t+1}	
		DT	NN
s_t	\emptyset	0.8	0.2
	DT	0.2	0.8
	NN	0.3	0.7

		o_t	
		the	cat
s_t	DT	0.9	0.1
	NN	0.5	0.5

Learning a Hidden Markov Model

Parameter Estimation

- Assuming we have fully observed data $\{X_i, S_i\}_{i=1}^N$, e.g. WSJ

Training set:

1 Pierre/**NNP** Vinken/**NNP** ,/, 61/**CD** years/**NNS** old/**JJ** ,/
join/**VB** the/**DT** board/**NN** as/**IN** a/**DT** nonexecutive/**JJ** di
Nov./**NNP** 29/**CD** ./.

2 Mr./**NNP** Vinken/**NNP** is/**VBZ** chairman/**NN** of/**IN** Elsev
N.V./**NNP** ,/, the/**DT** Dutch/**NNP** publishing/**VBG** group/

3 Rudolph/**NNP** Agnew/**NNP** ,/, 55/**CD** years/**NNS** old/**JJ**
chairman/**NN** of/**IN** Consolidated/**NNP** Gold/**NNP** Fields/**N**
./, was/**VBD** named/**VBN** a/**DT** nonexecutive/**JJ** director/
this/**DT** British/**JJ** industrial/**JJ** conglomerate/**NN** ./.

...

38,219 It/**PRP** is/**VBZ** also/**RB** pulling/**VBG** 20/**CD** peopl
of/**IN** Puerto/**NNP** Rico/**NNP** ,/, who/**WP** were/**VBD** help
Hurricane/**NNP** Hugo/**NNP** victims/**NNS** ,/, and/**CC** sendin
them/**PRP** to/**TO** San/**NNP** Francisco/**NNP** instead/**RB** ./

Maximum Likelihood Estimate:

$$\max_{t(\cdot|\cdot), e(\cdot|\cdot)} \prod_{i=1}^N P(X_i, S_i)$$

$$t(s' | s) = \frac{\text{count}(s \rightarrow s')}{\text{count}(s)}$$

$$e(x | s) = \frac{\text{count}(s \rightarrow x)}{\text{count}(s)}$$

Learning Example

1. the/**DT** cat/**NN** sat/**VBD** on/**IN** the/**DT** mat/**NN**
2. Princeton/**NNP** is/**VBZ** in/**IN** New/**NNP** Jersey/**NNP**
3. the/**DT** old/**NN** man/**VB** the/**DT** boats/**NNS**

$$t(\mathbf{NN} \mid \mathbf{DT}) = \frac{3}{4}$$
$$e(\mathbf{cat} \mid \mathbf{NN}) = \frac{1}{3}$$

Maximum Likelihood Estimate:

$$\max_{t(\cdot|\cdot), e(\cdot|\cdot)} \prod_{i=1}^N P(X_i, S_i)$$

$$t(s' \mid s) = \frac{\text{count}(s \rightarrow s')}{\text{count}(s)}$$

$$e(x \mid s) = \frac{\text{count}(s \rightarrow x)}{\text{count}(s)}$$

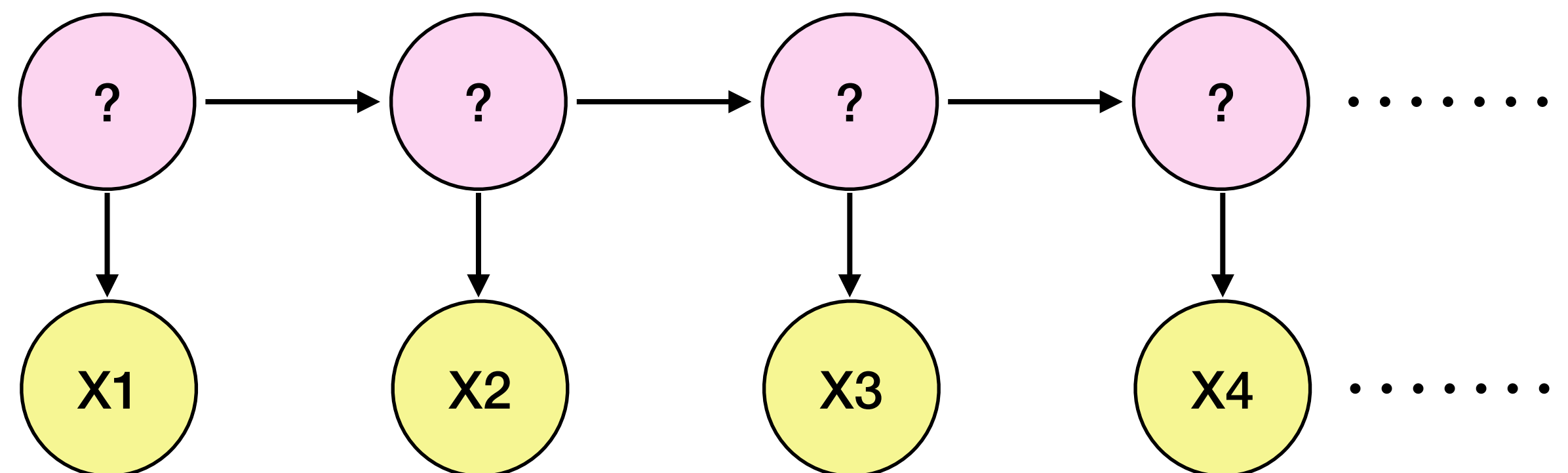
Decoding with HMMs

Decoding with HMMs

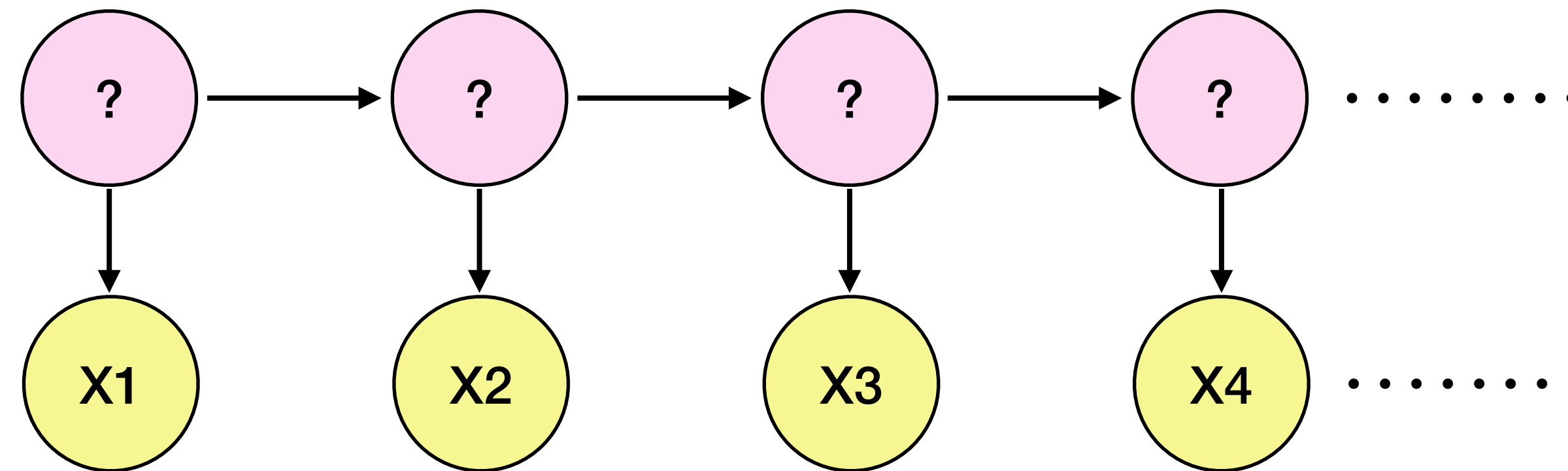
- ▶ Goal: for a given input sequence x_1, \dots, x_m , find

$$\arg \max_{s_1, \dots, s_m} p(x_1 \dots x_m, s_1 \dots s_m; \underline{\theta})$$

- ▶ This is the most likely state sequence $s_1 \dots s_m$ for the given input sequence $x_1 \dots x_m$



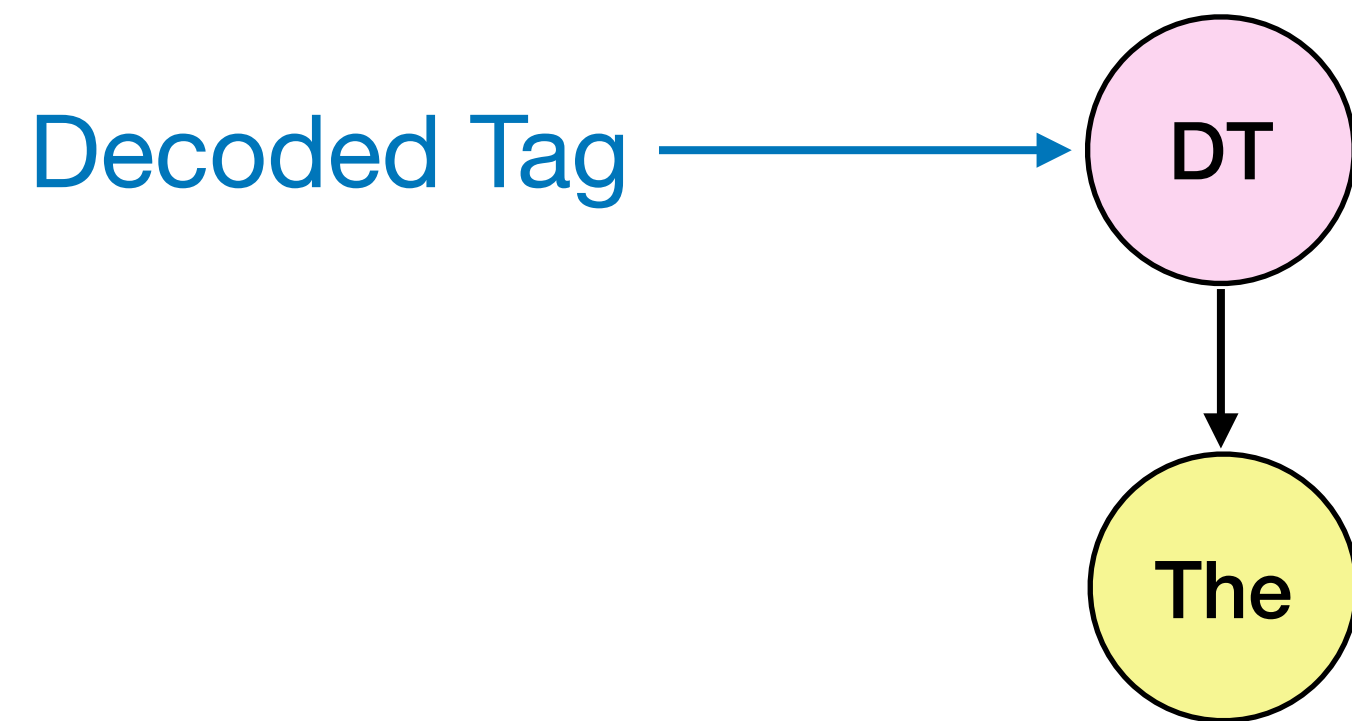
Decoding with HMMs



$$S^* = \arg \max_{s_1, \dots, s_m} p(x_1, \dots, x_m, s_1, \dots, s_m) = t(s_1) \prod_{j=2}^m t(s_j | s_{j-1}) \prod_{j=1}^m e(x_j | s_j)$$

How can we maximize this over all state sequences?

Greedy Decoding

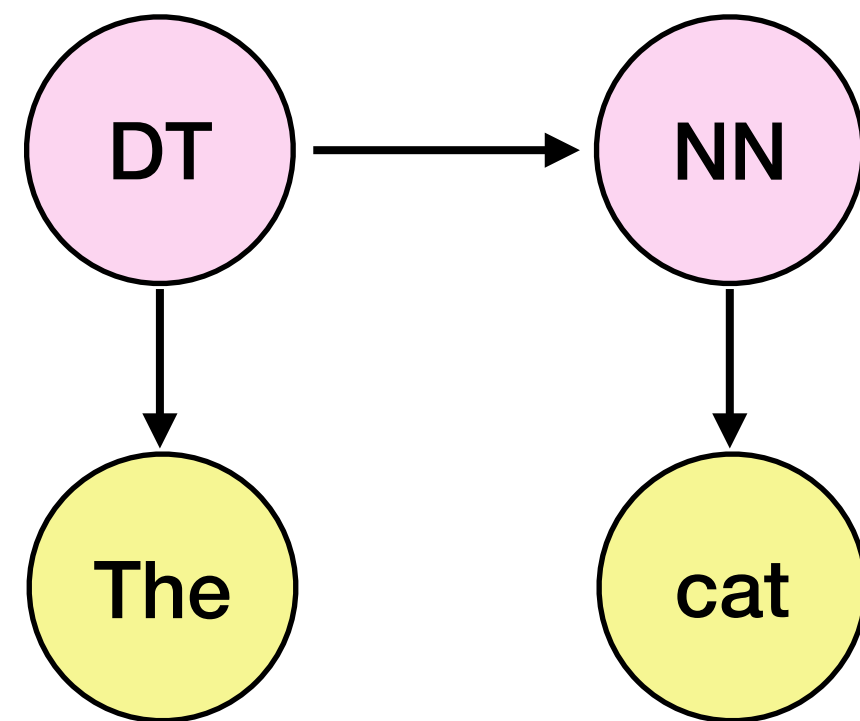


Decode/reveal one state at a time

$$s_1^* = \arg \max_{s_1} t(s_1) e(x_1 | s_1)$$

$$S^* = \arg \max_{s_1, \dots, s_m} p(x_1, \dots, x_m, s_1, \dots, s_m) = t(s_1) \prod_{j=2}^m t(s_j | s_{j-1}) \prod_{j=1}^m e(x_j | s_j)$$

Greedy Decoding

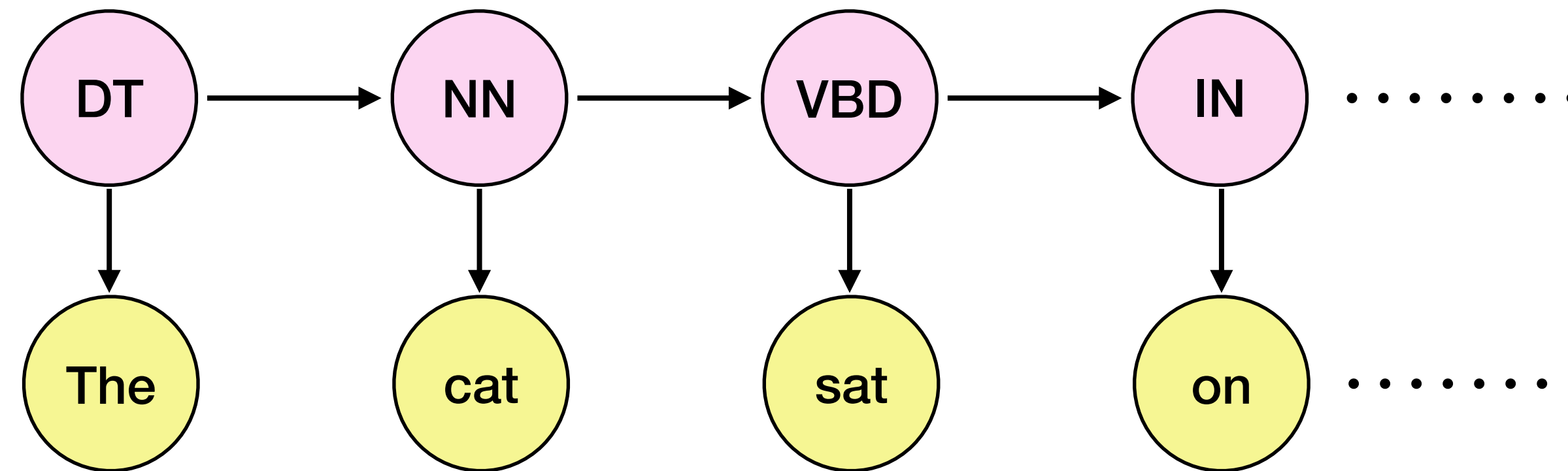


Decode/reveal one state at a time

$$s_2^* = \arg \max_{s_2} t(s_2 | s_1^*) e(x_2 | s_2)$$

$$S^* = \arg \max_{s_1, \dots, s_m} p(x_1, \dots, x_m, s_1, \dots, s_m) = t(s_1) \prod_{j=2}^m t(s_j | s_{j-1}) \prod_{j=1}^m e(x_j | s_j)$$

Greedy Decoding



$$s_j^* = \arg \max_{s_j} t(s_j | s_{j-1}^*) e(x_j | s_j), \quad \forall j$$

- Local decisions
- Not guaranteed to produce the overall optimal sequence

Viterbi Decoding

- ▶ The *Viterbi algorithm* is a dynamic programming algorithm.
Basic data structure:

$$\pi[j, s]$$

will be a table entry that stores the maximum probability for any state sequence ending in state s at position j . More formally: $\pi[1, s] = t(s)e(x_1|s)$, and for $j > 1$,

$$\pi[j, s] = \max_{s_1 \dots s_{j-1}} \left[t(s_1)e(x_1|s_1) \left(\prod_{k=2}^{j-1} t(s_k|s_{k-1})e(x_k|s_k) \right) \boxed{t(s|s_{j-1})e(x_j|s)} \right]$$

Viterbi Decoding

- ▶ Initialization: for $s = 1 \dots k$

$$\pi[1, s] = t(s)e(x_1|s)$$

- ▶ For $j = 2 \dots m$, $s = 1 \dots k$:

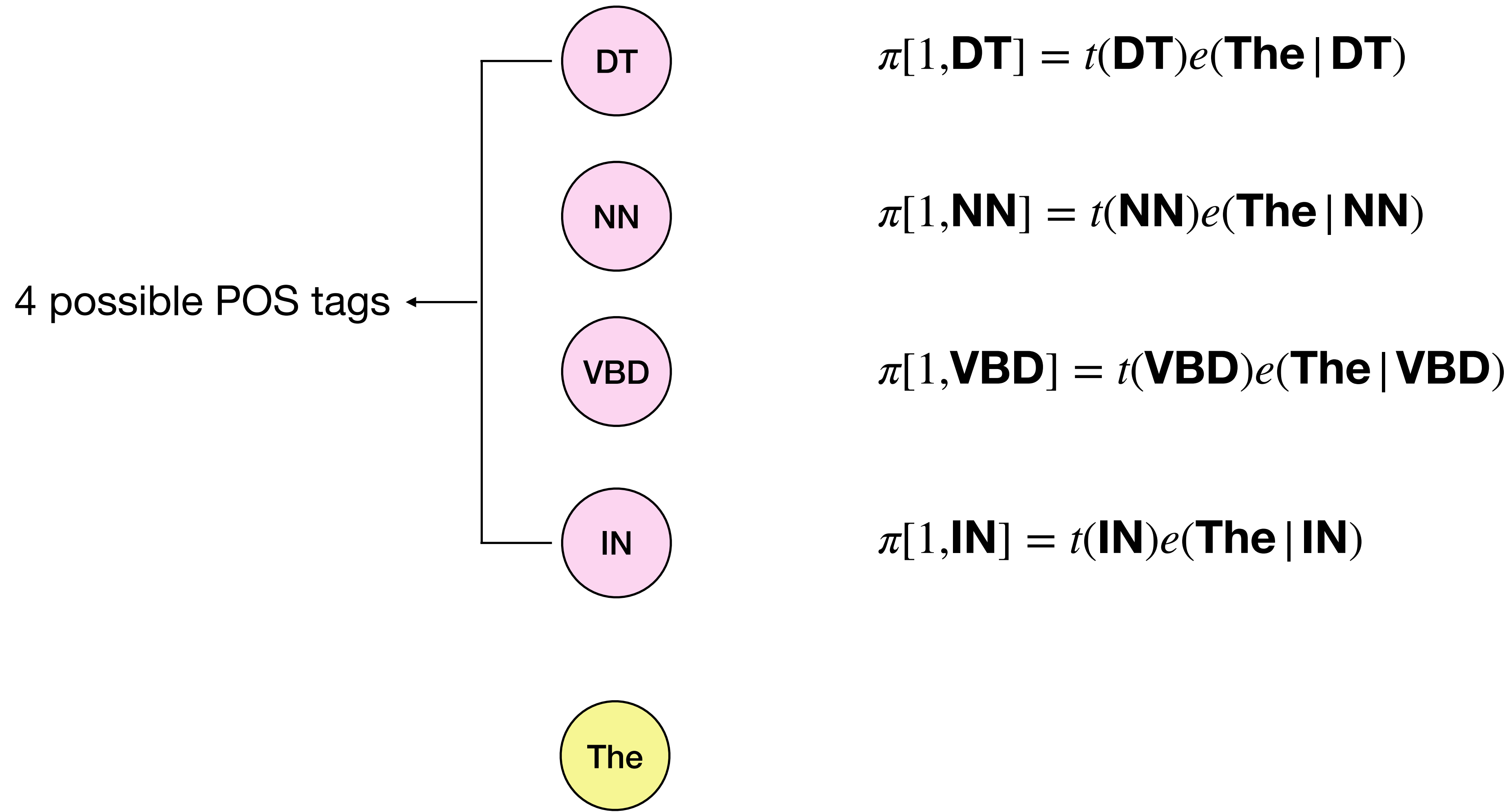
$$\pi[j, s] = \max_{s' \in \{1 \dots k\}} [\pi[j-1, s'] \times t(s|s') \times e(x_j|s)]$$

- ▶ We then have

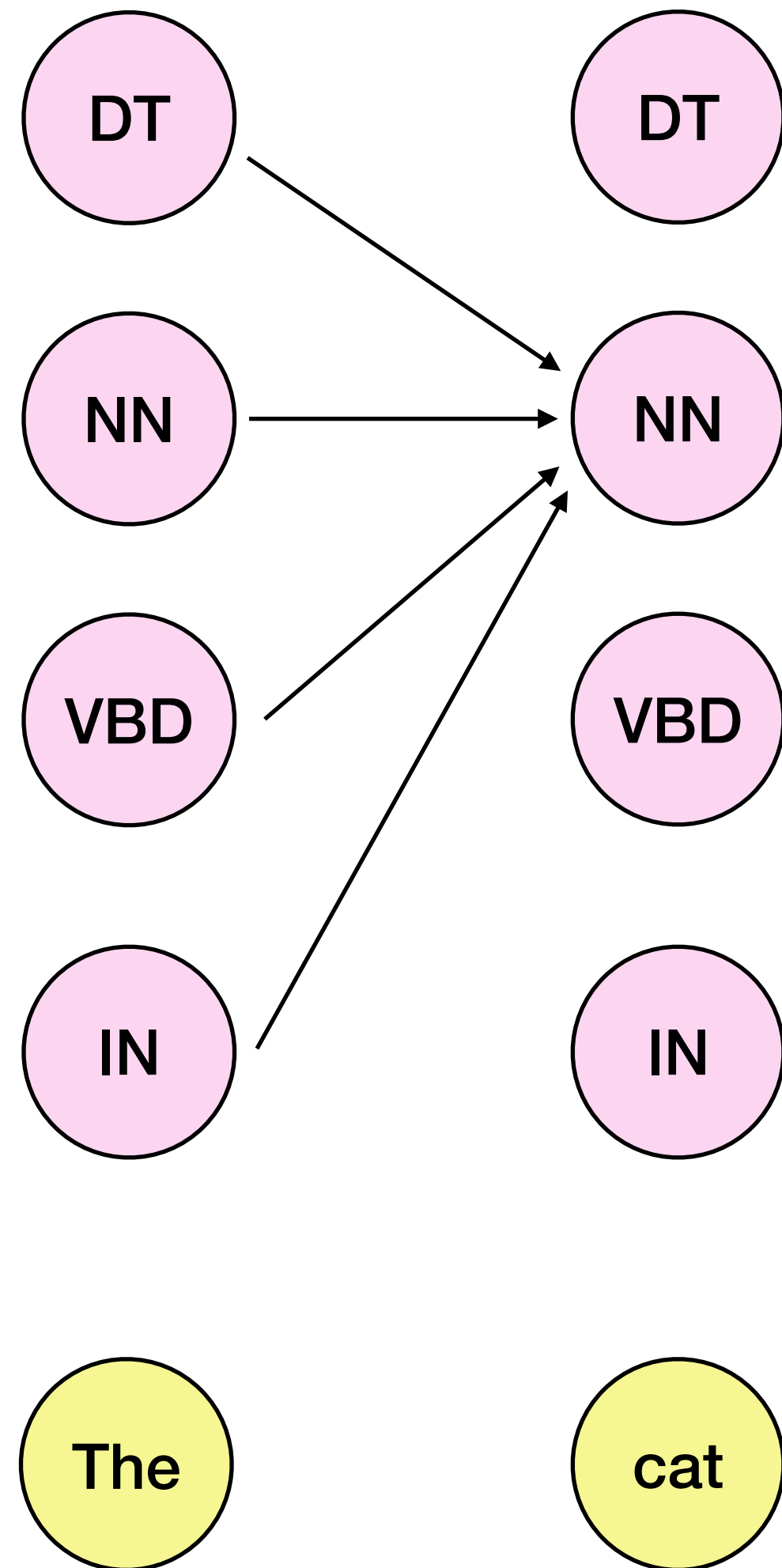
$$\max_{s_1 \dots s_m} p(x_1 \dots x_m, s_1 \dots s_m; \underline{\theta}) = \max_s \pi[m, s]$$

- ▶ The algorithm runs in $O(mk^2)$ time

Viterbi Decoding

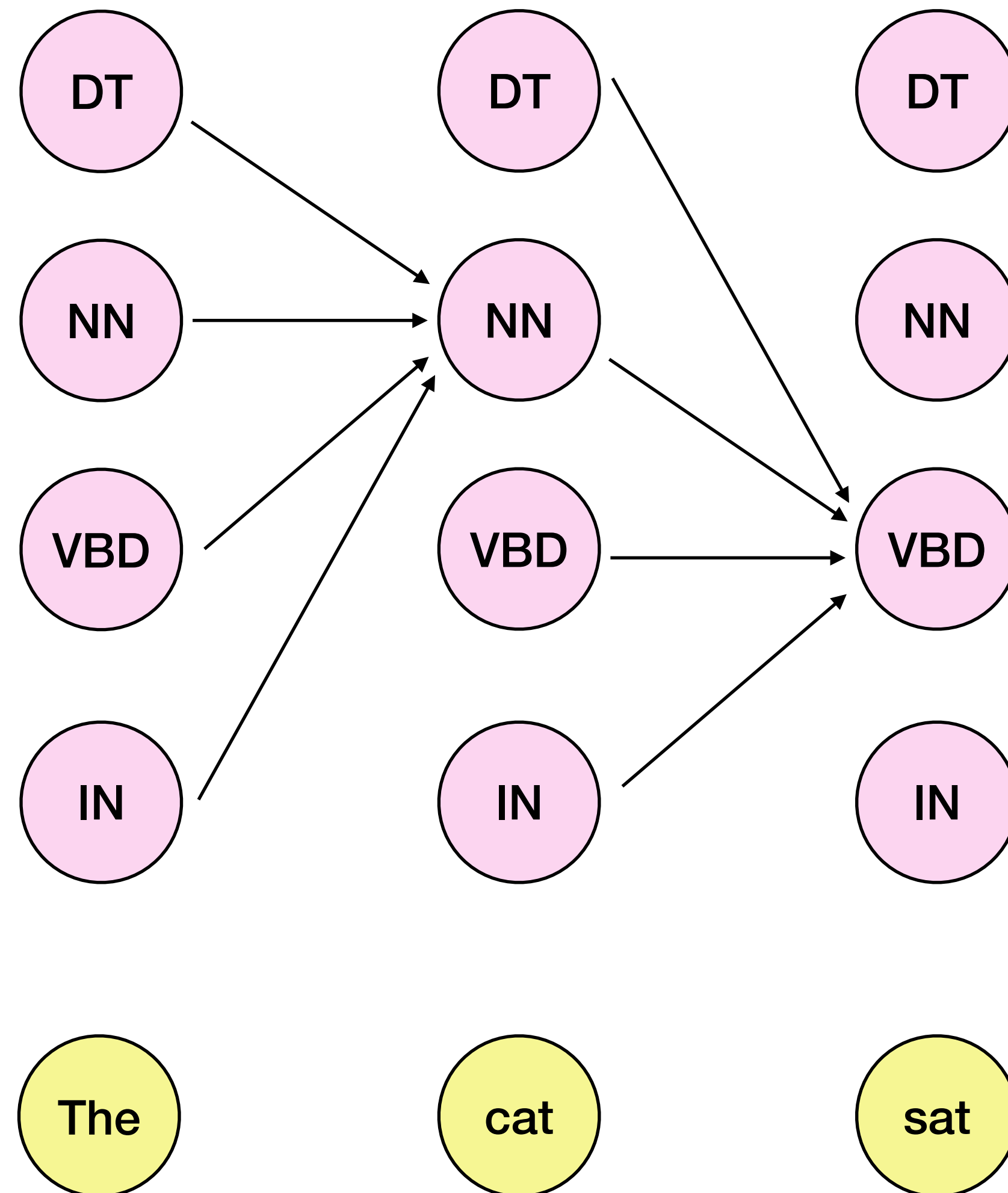


Viterbi Decoding



$$\pi[2, \mathbf{NN}] = \max_{s_1} \boxed{\pi[1, s_1]} t(\mathbf{NN} | s_1) e(\mathbf{cat} | \mathbf{NN})$$

Viterbi Decoding



$$\pi[2, \mathbf{NN}] = \max_{s_1} \pi[1, s_1] t(\mathbf{NN} | s_1) e(\mathbf{cat} | \mathbf{NN})$$

$$\pi[3, \mathbf{VBD}] = \max_{s_2} \pi[2, s_2] t(\mathbf{VBD} | s_2) e(\mathbf{sat} | \mathbf{VBD})$$

Pros and Cons

- **HMMs are simple to train**
 - Just need to compile counts from the training corpus
- **Performs relatively well**
 - > 96% on POS tagging (92.3% of most frequent class)
 - > 90% on Named Entity Recognition
- **Main difficulty is modeling $e(word | tag)$**
 - Words are very complex
 - Unknown words

Overview

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Log-Linear Models

Log-Linear Models

- The General Problem

- ▶ We have some **input domain** \mathcal{X}
- ▶ Have a finite **label set** \mathcal{Y}
- ▶ Aim is to provide a **conditional probability** $p(y \mid x)$ for any x, y where $x \in \mathcal{X}, y \in \mathcal{Y}$

Log-Linear Models

- ▶ We have some input domain \mathcal{X} , and a finite label set \mathcal{Y} . Aim is to provide a conditional probability $p(y \mid x)$ for any $x \in \mathcal{X}$ and $y \in \mathcal{Y}$.
- ▶ A feature is a function $f : \mathcal{X} \times \mathcal{Y} \rightarrow \mathbb{R}$
(Often binary features or indicator functions $f_k : \mathcal{X} \times \mathcal{Y} \rightarrow \{0, 1\}$).
- ▶ Say we have m features f_k for $k = 1 \dots m$
 \Rightarrow A feature vector $f(x, y) \in \mathbb{R}^m$ for any $x \in \mathcal{X}$ and $y \in \mathcal{Y}$.
- ▶ We also have a **parameter vector** $v \in \mathbb{R}^m$
- ▶ We define

$$p(y \mid x; v) = \frac{e^{v \cdot f(x, y)}}{\sum_{y' \in \mathcal{Y}} e^{v \cdot f(x, y')}}$$

Why the name?

$$p(y \mid x; v) = \frac{e^{v \cdot f(x, y)}}{\sum_{y' \in \mathcal{Y}} e^{v \cdot f(x, y')}}$$

$$\log p(y \mid x; v) = \underbrace{v \cdot f(x, y)}_{\text{Linear term}} - \underbrace{\log \sum_{y' \in \mathcal{Y}} e^{v \cdot f(x, y')}}_{\text{Normalization term}}$$

Features in Log-linear Models

$S = S_1, S_2, \dots, S_n$

NNP

VBZ

IN

NNP

$X = X_1, X_2, \dots, X_n$

USC

is

in

California

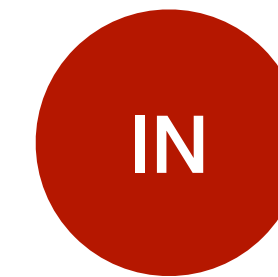
Theoretically, we can use any features in X and S : $f(X, S)$

- The current word: $\langle is \rangle$
- The surrounding words: $\langle USC, is \rangle, \dots$
- The current POS tag: $\langle VBZ \rangle$
- The surrounding tags: $\langle NNP, VBZ \rangle, \dots$
- The current word and tag: $\langle is, VBZ \rangle$

How to design these features into numerical vectors?

Feature Vocabulary

$$S = S_1, S_2, \dots, S_n$$



$$X = X_1, X_2, \dots, X_n$$

USC

is

in

California

Theoretically, we can use any features in X and S : $f(X, S)$

- The current word: **<is>**
- The surrounding words: **<USC, is>**, ...
- The current POS tag: **<VBZ>**
- The surrounding tags: **<NNP, VBZ>**, ...
- The current word and tag: **<is, VBZ>**

Vocab = [is, in, USC, California, ...]

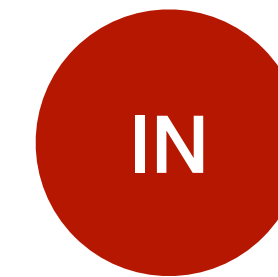
Vocab += [<USC, is>, <is, in>, ...]

Vocab += [NNP, VBZ, IN, ...]

Vocab += [<USC, NNP>, <is, VBZ>, ...]

Feature Sparsity Problem

$$S = S_1, S_2, \dots, S_n$$



$$X = X_1, X_2, \dots, X_n$$

USC

is

in

California

Theoretically, we can use any features in X and S : $f(X, S)$

- The current word: **<is>**
- The surrounding words: **<USC, is>**, ...
- The current POS tag: **<VBZ>**
- The surrounding tags: **<NNP, VBZ>**, ...
- The current word and tag: **<is, VBZ>**

Number of Features

V

V^2

VK

Features vs. Independence

- We need independence assumptions to compute the nominator
- Stronger assumptions lead to less flexible features

$$p(y \mid x; v) = \frac{e^{v \cdot f(x, y)}}{\sum_{y' \in \mathcal{Y}} e^{v \cdot f(x, y')}} \quad \boxed{\phantom{\sum_{y' \in \mathcal{Y}} e^{v \cdot f(x, y')}}}$$

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Independence Assumptions in MEMMs

- Goal: modeling the distribution

$$p(s_1, \dots, s_m \mid x_1, \dots, x_m)$$

- Markov Assumption on S

$$p(s_1, \dots, s_m \mid x_1, \dots, x_m) = \prod_{j=1}^m p(s_j \mid s_1, \dots, s_{j-1}, x_1, \dots, x_m)$$

chain rule (no assumptions)

$$= \prod_{j=1}^m p(s_j \mid s_{j-1}, x_1, \dots, x_m)$$

Markov assumption

Using Log-Linear Models

- We then model each term using a log-linear model:

$$p(s_j | s_{j-1}, x_1, \dots, x_m) = \frac{\exp(v \cdot f(x_1, \dots, x_m, j, s_{j-1}, s_j))}{\sum_{s'_j \in \mathcal{S}} \exp(v \cdot f(x_1, \dots, x_m, j, s_{j-1}, s'_j))}$$

- Here $f(x_1, \dots, x_m, j, s, s')$ is the feature vector:
 - x_1, \dots, x_m is the sequence of words to be tagged
 - j is the position to be tagged (any value from $1, \dots, m$)
 - s is the previous state
 - s' is the current state

Using Log-Linear Models

- We then model each term using a log-linear model:

$$p(s_j | s_{j-1}, x_1, \dots, x_m) = \frac{\exp(v \cdot f(x_1, \dots, x_m, i, s_{j-1}, s_j))}{\sum_{s'_j \in S} \exp(v \cdot f(x_1, \dots, x_m, i, s_{j-1}, s'_j))}$$

Trackable

- Here $f(x_1, \dots, x_m, j, s, s')$ is the feature vector:

- x_1, \dots, x_m is the sequence of words to be tagged
- j is the position to be tagged (any value from $1, \dots, m$)
- s is the previous state
- s' is the current state

The whole sequence of X
Only two successive tags

Features in MEMMs

$$S = S_1, S_2, \dots, S_n$$



$$X = X_1, X_2, \dots, X_n$$

USC

is

in

California

What are the most important features $f(x_1, \dots, x_m, j, s, s')$?

- The current word: **<is>**
- The surrounding words: **<USC, is>**, ...
- The current POS tag: **<VBZ>**
- The previous tag: **<NNP, VBZ>**, ...
- The current word and tag: **<is, VBZ>**
- Prefix or suffix features: **<ing>**
- ...

Decoding with MEMMs: Viterbi Algorithm

- ▶ Goal: for a given input sequence x_1, \dots, x_m , find

$$\arg \max_{s_1, \dots, s_m} p(s_1 \dots s_m | x_1 \dots x_m)$$

- ▶ We can use the *Viterbi* algorithm again (see last lecture on HMMs). Basic data structure:

$$\pi[j, s]$$

will be a table entry that stores the maximum probability for any state sequence ending in state s at position j . More formally:

$$\pi[j, s] = \max_{s_1 \dots s_{j-1}} \left(p(s | s_{j-1}, x_1 \dots x_m) \prod_{k=1}^{j-1} p(s_k | s_{k-1}, x_1 \dots x_m) \right)$$

Decoding with MEMMs: Viterbi Algorithm

- Initialization: for $s \in \mathcal{S}$

$$\pi[1, s] = p(s|s_0, x_1 \dots x_m)$$

where s_0 is a special “initial” state.

- For $j = 2 \dots m, s = 1 \dots k$:

$$\pi[j, s] = \max_{s' \in \mathcal{S}} [\pi[j - 1, s'] \times p(s|s', x_1 \dots x_m)]$$

- We then have

$$\max_{s_1 \dots s_m} p(s_1 \dots s_m | x_1 \dots x_m) = \max_s \pi[m, s]$$

Model Performance

	POS Tagging	NER
HMM	96.4%	75.3
MEMM	96.9%	85.9

HMMs vs. MEMMs

- In MEMMs, each state transition has probability

$$p(s_j | s_{j-1}, x_1, \dots, x_m) = \frac{\exp(v \cdot f(x_1, \dots, x_m, i, s_{j-1}, s_j))}{\sum_{s' \in S} \exp(v \cdot f(x_1, \dots, x_m, i, s_{j-1}, s'_j))}$$

- In HMMs, each state transition has probability

$$p(s_j | s_{j-1})p(x_j | s_j)$$

- Feature vectors f allows much richer representations in MEMMs:
 - Sensitivity to *any* word in the input sequence x_1, \dots, x_m , not just x_j
 - Sensitivity to spelling features (prefixes, suffixes etc.) of current or surrounding words
- Parameter estimation in MEMMs is more expensive than in HMMs (but is still not prohibitive for most tasks)

Can we relax the Markov assumption in MEMMs but keep the same features?

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Conditional Random Fields (CRFs)

- Goal: modeling the distribution

$$p(s_1, \dots, s_m \mid x_1, \dots, x_m)$$

- In MEMMs we had

$$p(s_1, \dots, s_m \mid x_1, \dots, x_m) = \prod_{j=1}^m p(s_j \mid s_1, \dots, s_{j-1}, x_1, \dots, x_m)$$

chain rule (no assumptions)

$$= \prod_{j=1}^m p(s_j \mid s_{j-1}, x_1, \dots, x_m)$$

Markov assumption

- Using log-linear model

$$p(s_j \mid s_{j-1}, x_1, \dots, x_m) = \frac{\exp(v \cdot f(x_1, \dots, x_m, i, s_{j-1}, s_j))}{\sum_{s' \in \mathcal{S}} \exp(v \cdot f(x_1, \dots, x_m, i, s_{j-1}, s'_j))}$$

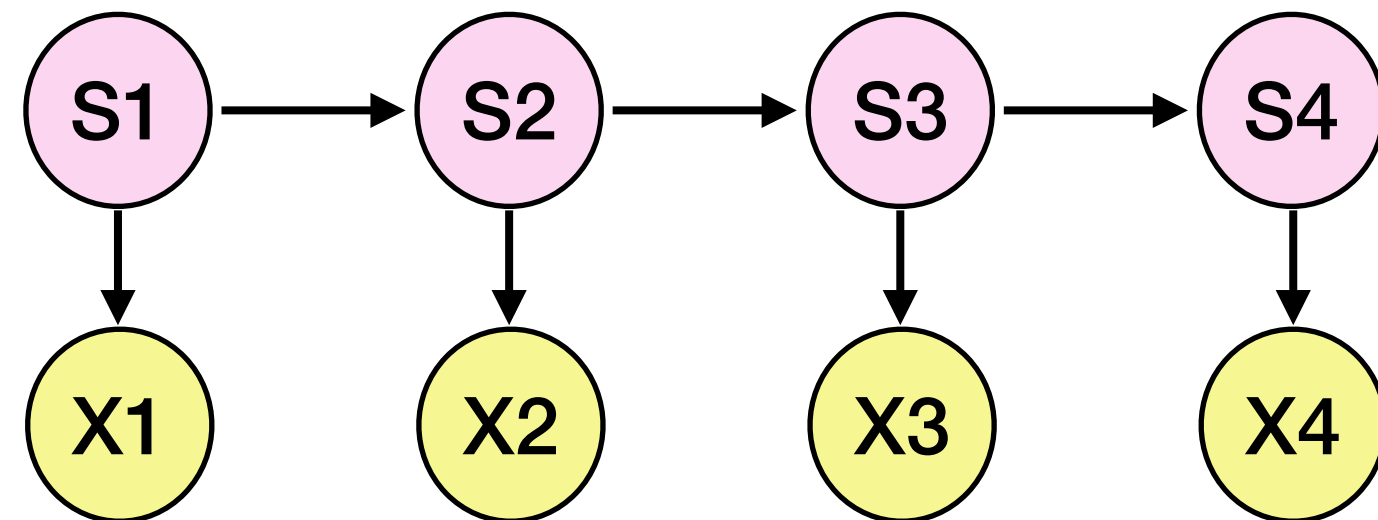
Can we build a *giant* log-linear model?

$$p(s_1, \dots, s_m \mid x_1, \dots, x_m)$$

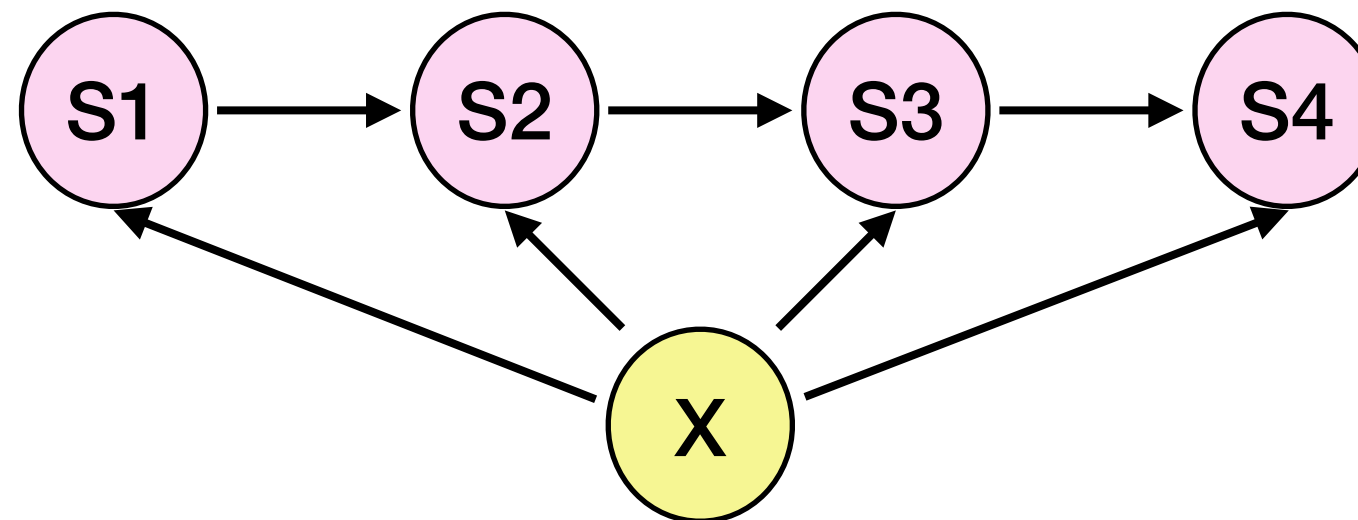
Conditional Random Fields (CRFs)

- Globally Normalized Model

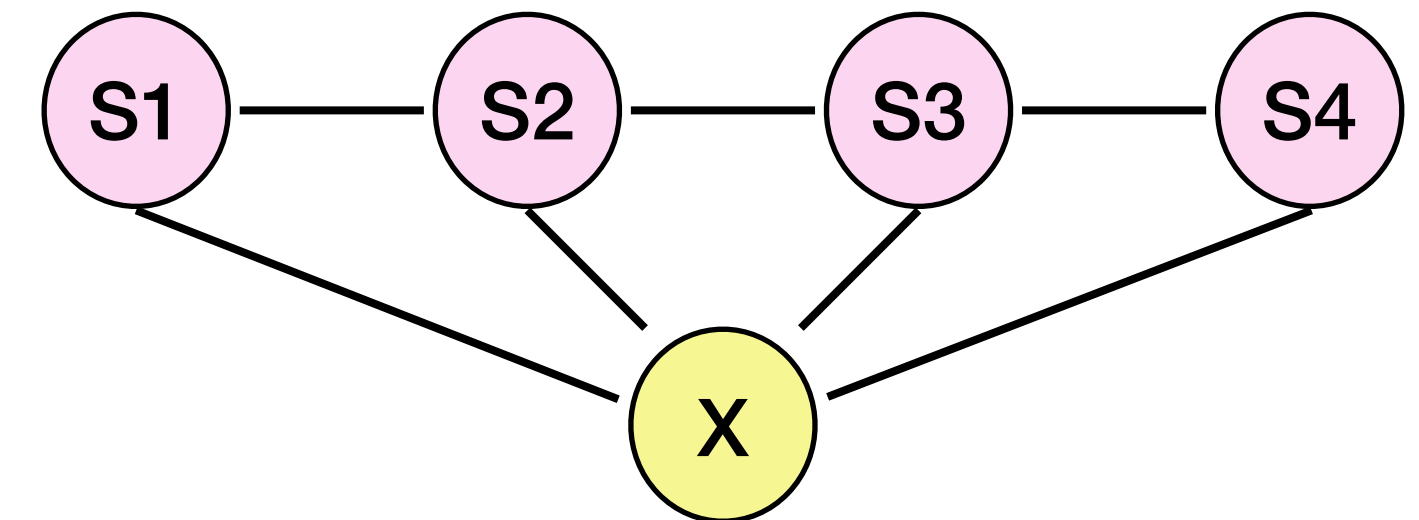
$$p(s_1, \dots, s_m | x_1, \dots, x_m) = \frac{\prod_{j=1}^m \exp(v \cdot f(x_1, \dots, x_m, i, s_{j-1}, s_j))}{\sum_{s'_1, \dots, s'_m \in \mathcal{S}} \prod_{j=1}^m \exp(v \cdot f(x_1, \dots, x_m, i, s'_{j-1}, s'_j))}$$



HMM



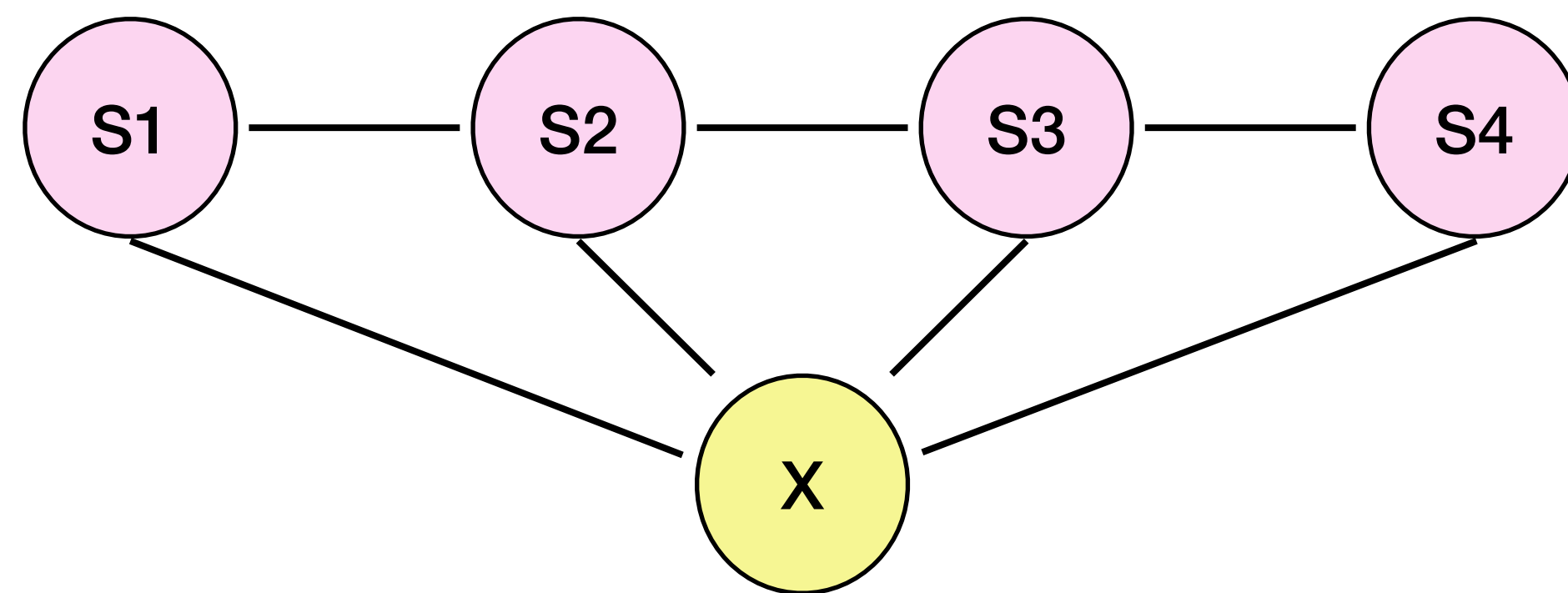
MEMM



CRF

Independence Assumptions in CRFs

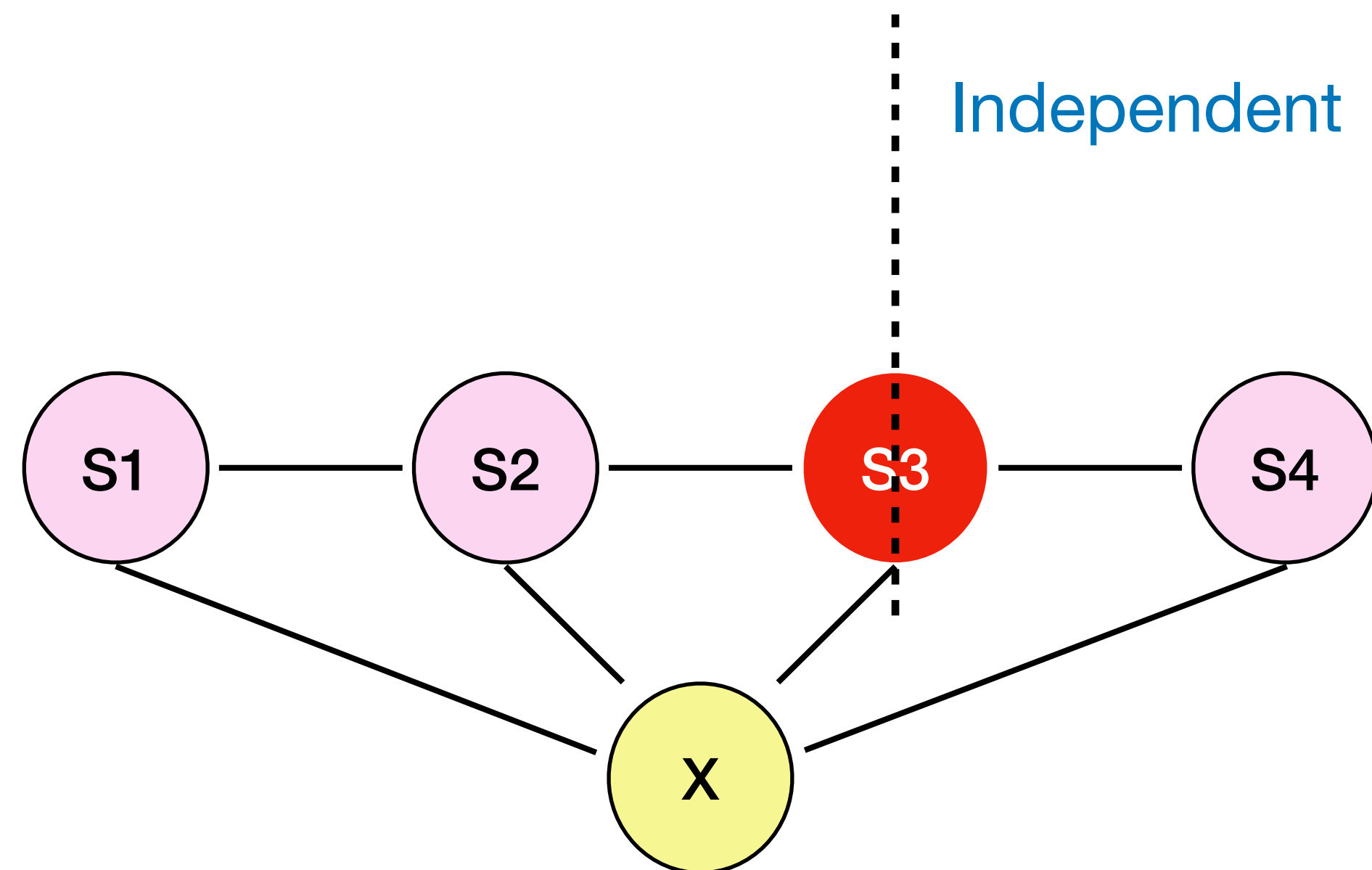
$$p(s_1, \dots, s_m | x_1, \dots, x_m) = \frac{\prod_{j=1}^m \exp(v \cdot f(x_1, \dots, x_m, i, s_{j-1}, s_j))}{\sum_{s'_1, \dots, s'_m \in \mathcal{S}} \prod_{j=1}^m \exp(v \cdot f(x_1, \dots, x_m, i, s'_{j-1}, s'_j))}$$



CRF

Independence Assumptions in CRFs

$$p(s_1, \dots, s_m | x_1, \dots, x_m) = \frac{\prod_{j=1}^m \exp(v \cdot f(x_1, \dots, x_m, i, s_{j-1}, s_j))}{\sum_{s'_1, \dots, s'_m \in \mathcal{S}} \prod_{j=1}^m \exp(v \cdot f(x_1, \dots, x_m, i, s'_{j-1}, s'_j))}$$



CRF

CRF has weaker independence assumption than MEMMs!

Decoding with CRFs

- Viterbi Algorithm still applicable!

$$p(s_1, \dots, s_m | x_1, \dots, x_m) = \frac{\prod_{j=1}^m \exp(v \cdot f(x_1, \dots, x_m, i, s_{j-1}, s_j))}{\sum_{s'_1, \dots, s'_m \in \mathcal{S}} \prod_{j=1}^m \exp(v \cdot f(x_1, \dots, x_m, i, s'_{j-1}, s'_j))}$$

Makes no effects on decoding!

Computation of the Global Nominator

- How to compute the global nominator?
 - Dynamic programming similar to the Viterbi algorithm
 - Replacing the maximum operation in decoding with sum operation

$$p(s_1, \dots, s_m | x_1, \dots, x_m) = \frac{\prod_{j=1}^m \exp(v \cdot f(x_1, \dots, x_m, i, s_{j-1}, s_j))}{\sum_{s'_1, \dots, s'_m \in \mathbb{S}} \prod_{j=1}^m \exp(v \cdot f(x_1, \dots, x_m, i, s'_{j-1}, s'_j))} \quad \text{Partition Function}$$

$$\pi[j, s] = \sum_{s_1, \dots, s_{j-1}} \left[\prod_{k=1}^{j-1} \exp(v \cdot f(x_1, \dots, x_m, k, s_{k-1}, s_k)) \right] \exp(v \cdot f(x_1, \dots, x_m, k, s_{j-1}, s))$$

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Maximum Likelihood Estimation

- **Need to maximize:**

$$\begin{aligned}\max_v L(v) &= \sum_{i=1}^N \log P(S_i | X_i; v) \\ &= \sum_{i=1}^N v \cdot f(X_i, S_i) - \sum_{i=1}^N \log \sum_{s' \in \mathbb{S}} e^{v \cdot f(X_i, S')}\end{aligned}$$

Do we need to manually
derive the gradients?

Back-propagation!

- **Calculating gradients:**

$$\frac{\partial L(v)}{\partial v_k} = \underbrace{\sum_{i=1}^N f_k(X_i, S_i)}_{\text{Empirical counts}} - \underbrace{\sum_{i=1}^N \sum_{S' \in \mathbb{S}} f_k(X_i, S') p(S' | X_i; v)}_{\text{Expected counts}}$$

See Collin's notes for derivations

Model Performance

	POS Tagging	NER
HMM	96.4%	75.3
MEMM	96.9%	85.9
CRF	97.3%	88.7

Reading Materials

- **Notes from Michael Collins:**
 - Sequence Labeling and HMMs
 - EM Algorithm
 - Log-linear Models
 - MEMMs and CRFs