



SCHOOL OF INFORMATION CENTER FOR  
SOCIAL MEDIA RESPONSIBILITY  
UNIVERSITY OF MICHIGAN

# ***Calibrate-Extrapolate:*** **Rethinking Prevalence Estimation with Black Box Classifiers**

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Buffalo, NY, USA

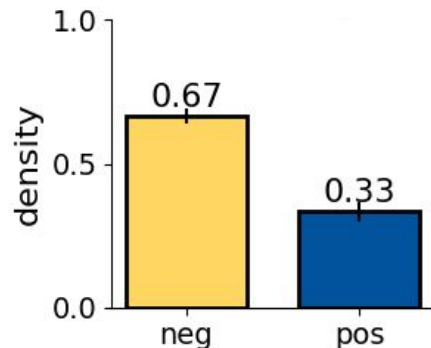
Tutorial: <https://avalanchesiqi.github.io/prevalence-estimation-tutorial/>



*Given an unlabeled dataset, count the frequency of each class in it*

A core task in computational social science, to estimate the fraction of

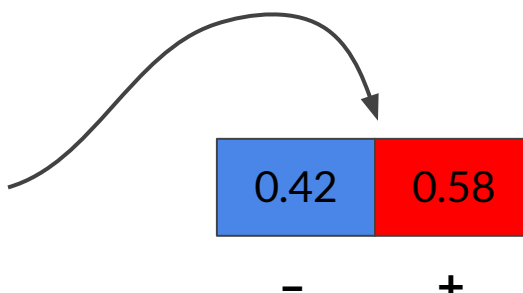
- happy tweets in a day (Dodds et al. 2011)
- automated accounts on Twitter (Yang et al. 2020)
- cross-partisan discussion on YouTube (Wu and Resnick 2021)
- political discussion in non-political subreddits (Rajadesingan et al. 2021)
- anti-social posts on Reddit (Part et al. 2022)
- many many more...



Each item has a set of features **X**, and an unobserved ground truth label **GT**

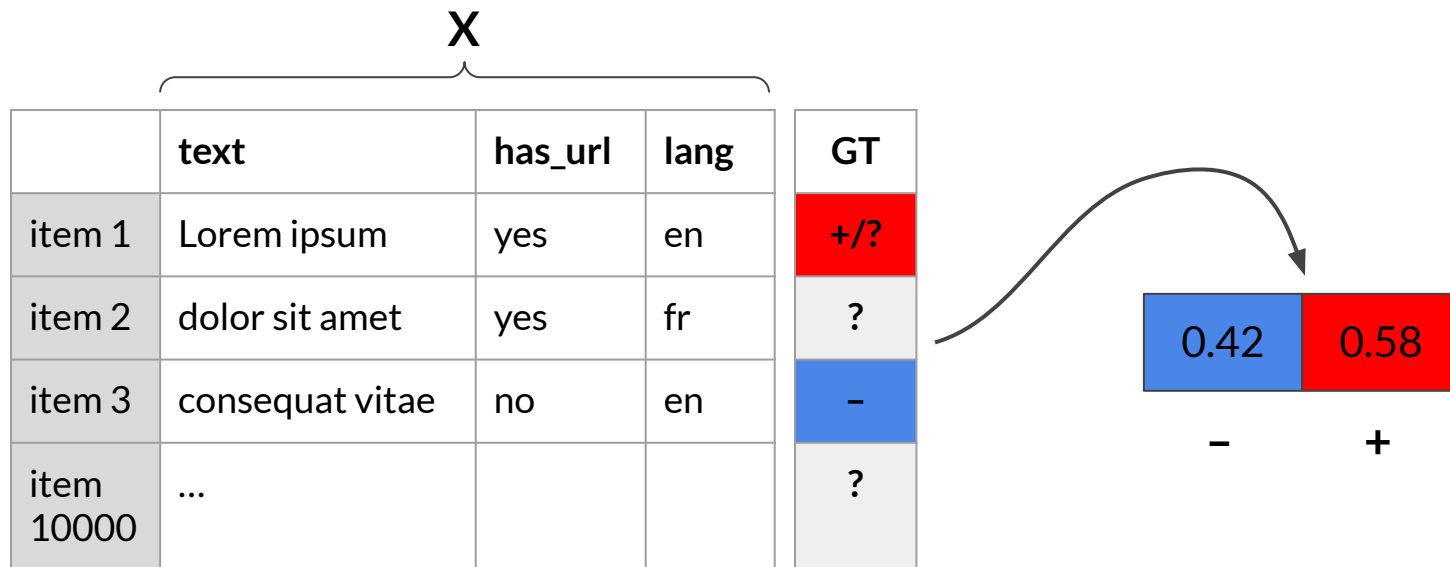
**X**

	text	has_url	lang	GT
item 1	Lorem ipsum	yes	en	+
item 2	dolor sit amet	yes	fr	+
item 3	consequat vitae	no	en	-
item 4	...			-



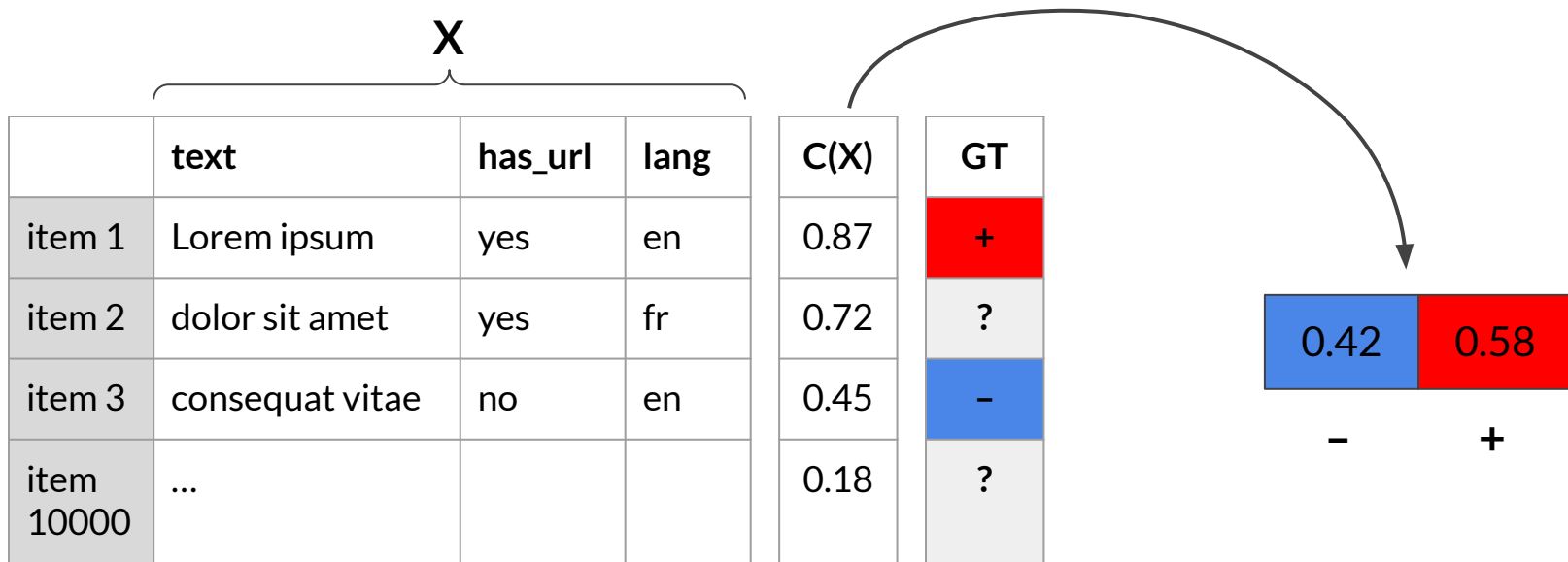
-                      +

- Social media data is often on a large scale
- Ground truth labels are difficult or expensive to obtain
- Obtained GT labels have noise



*classifier:  $X \Rightarrow C(X) \sim GT$ , where  $C(X)$  in  $[0, 1]$*

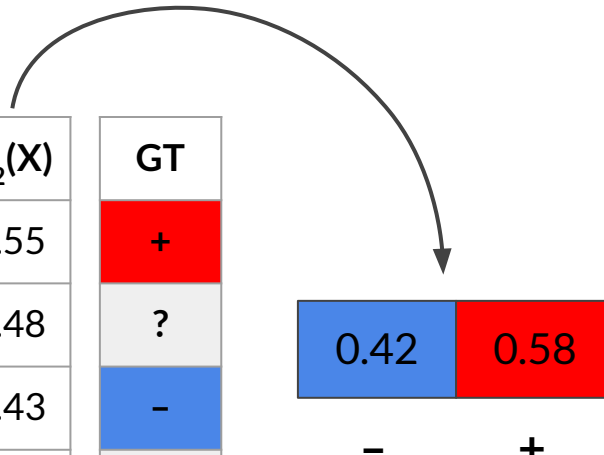
VADER (sentiment), Perspective API (toxicity), ChatGPT (almost everything)...



- What if we have a less accurate classifier?
- $C(X)$  is a confidence score, but not a probability score
- How to make reliable estimates with fewer GT labels?

$X$

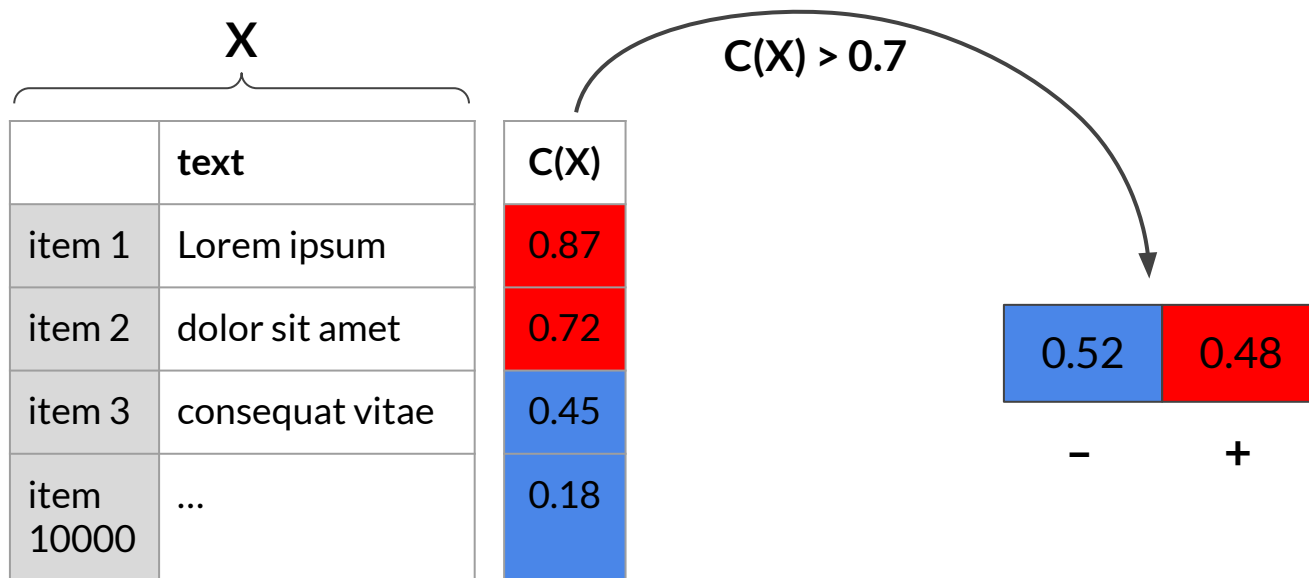
	text	has_url	lang	$\epsilon_1(X)$	$C_2(X)$	GT
item 1	Lorem ipsum	yes	en	<del>0.87</del>	0.55	+
item 2	dolor sit amet	yes	fr	<del>0.72</del>	0.48	?
item 3	consequat vitae	no	en	<del>0.45</del>	0.43	-
item 10000	...			<del>0.18</del>	0.32	?



- *you want to estimate the prevalence of toxic comments on social media*
- *you have a very large dataset*
- *you hear good things about the Perspective API*

<b>X</b>		
	<b>text</b>	<b>C(X)</b>
item 1	Lorem ipsum	0.87
item 2	dolor sit amet	0.72
item 3	consequat vitae	0.45
item 10000	...	0.18

- *"Perspective API suggests 0.7-0.9 as a threshold"*



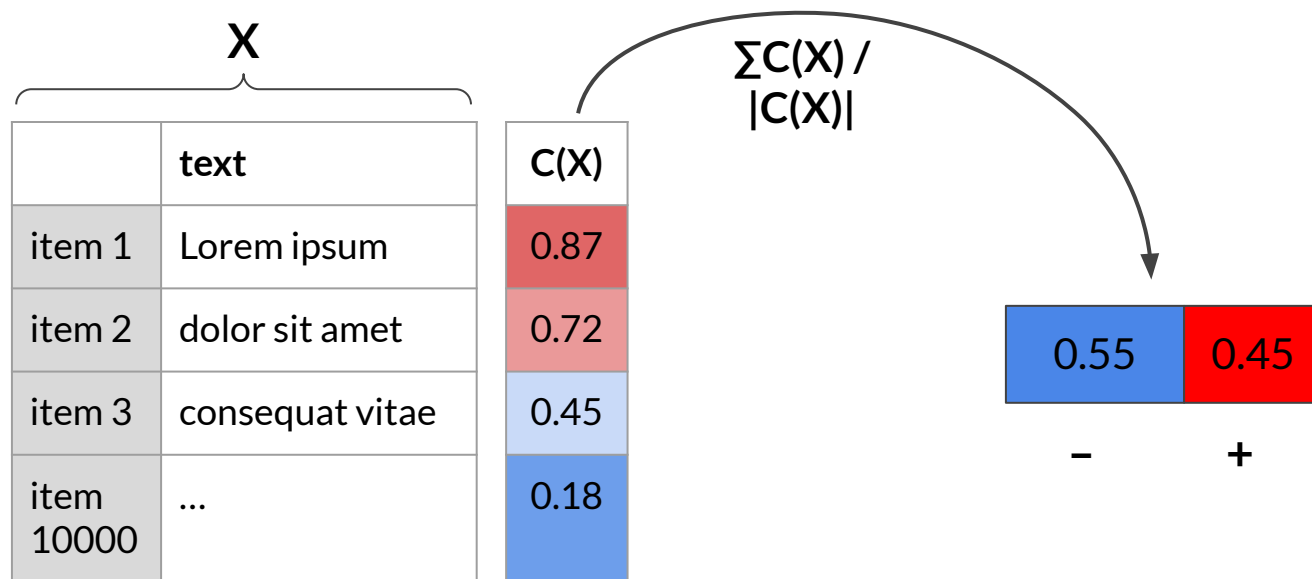


➤ *"Perspective API suggests 0.7-0.9 as a threshold"*

✗ Dataset shift: Training and test datasets differ in important ways  
(Moreno-Torres et al. 2011)

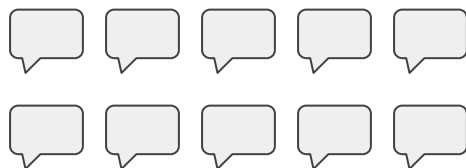


- *"Perspective API returns a probability score"*



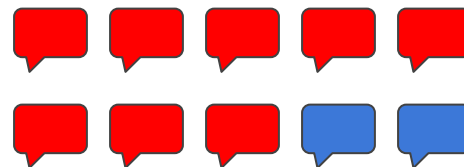
➤ "Perspective API returns a probability score"

✗ Generally, one should not interpret classifier output as **calibrated** probability



$$C(\mathbf{X}) = 0.8$$

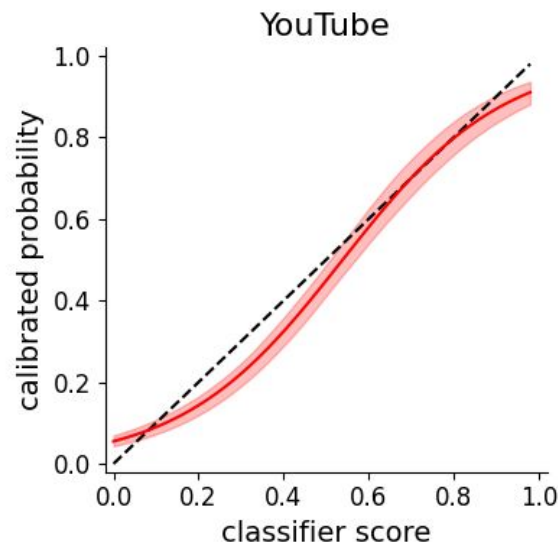
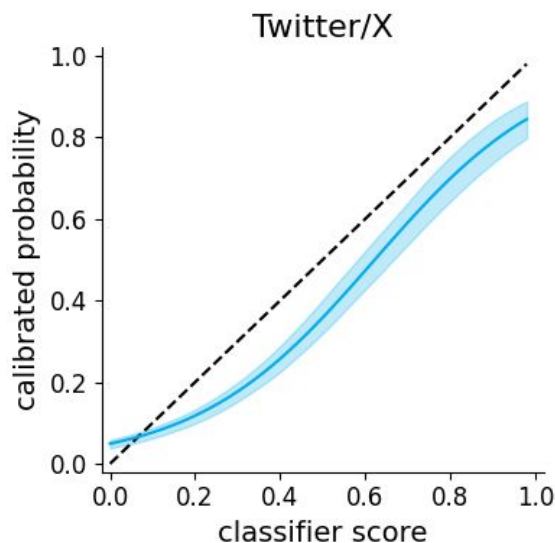
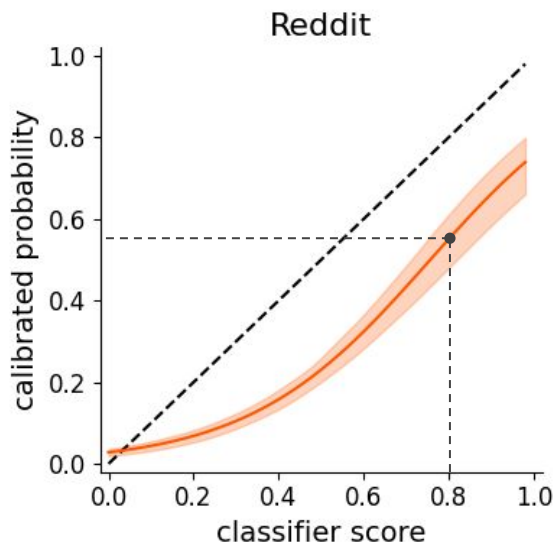
obtain GT labels



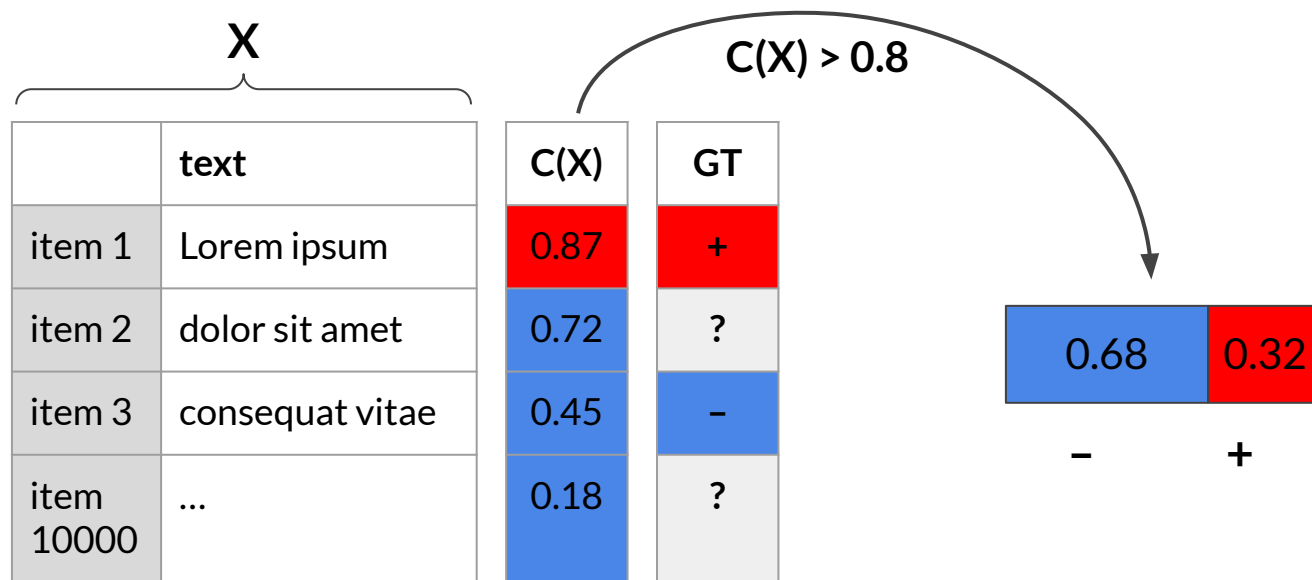
$$P(\text{GT}=+ \mid C(\mathbf{X})=0.8) = 0.8$$

➤ *"Perspective API returns a probability score"*

✗ Generally, one should not interpret classifier output as **calibrated** probability

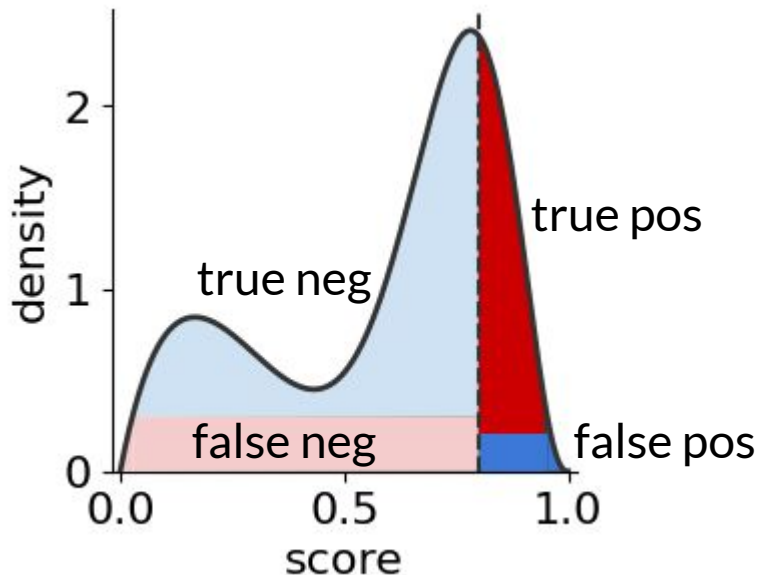


- you subsample the data, collect GT labels for the sample, find that Perspective API works well (e.g.,  $F1=0.9$ ) and the optimal threshold is 0.8



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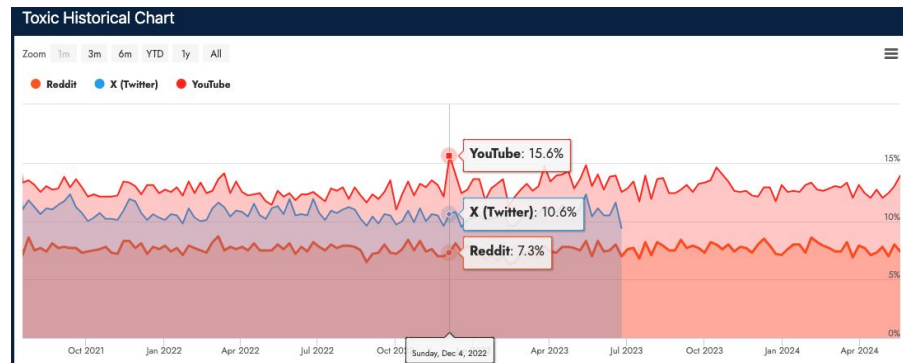
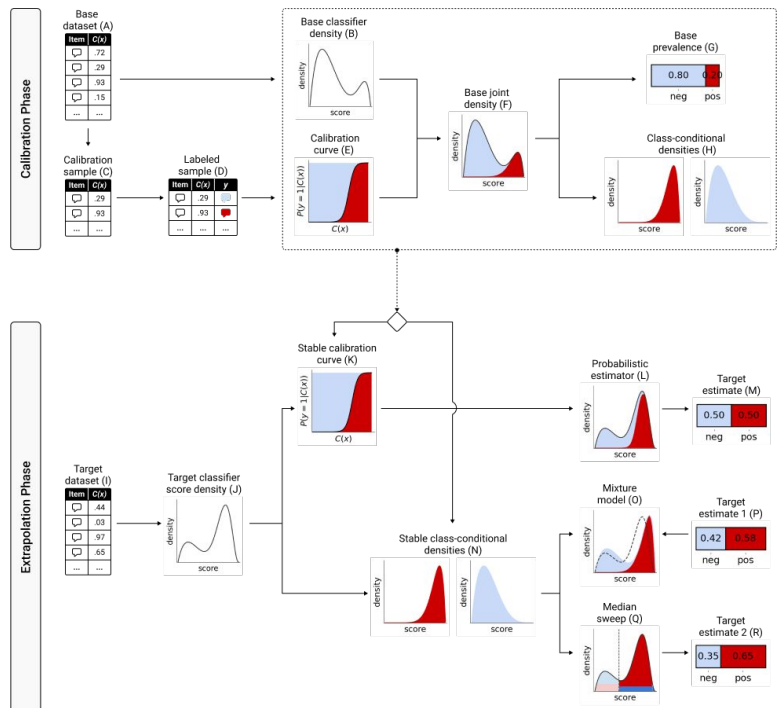
✗ Classifier errors are not accounted for



**estimated** 

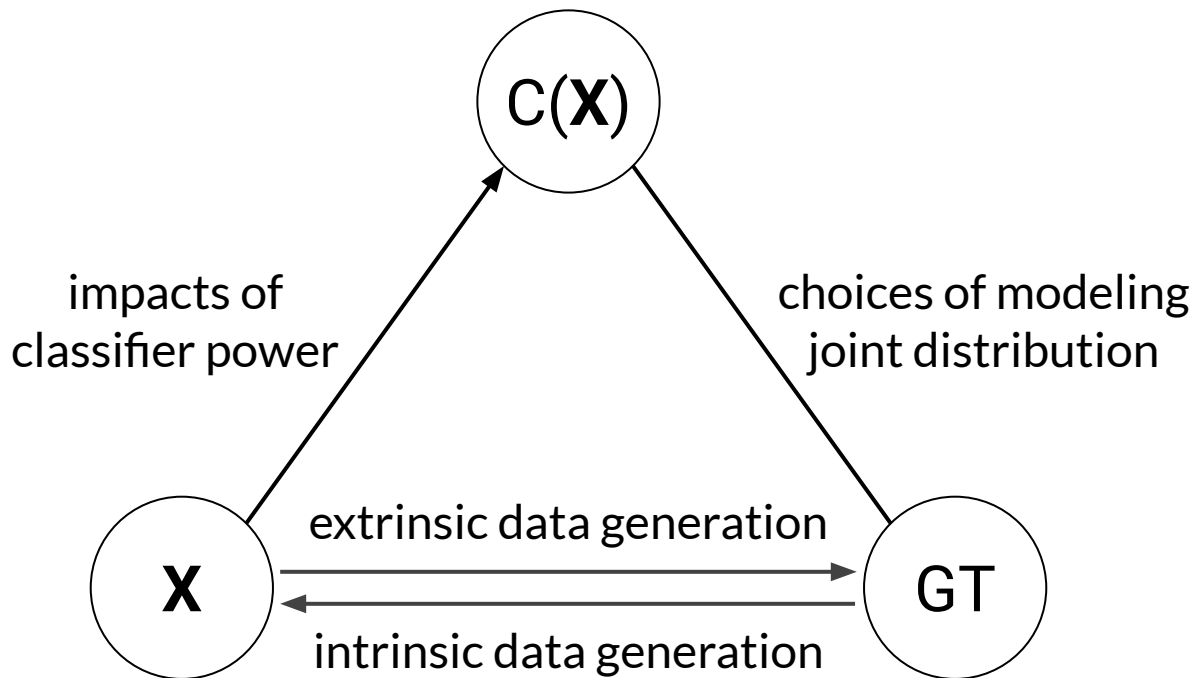
**wanted** 

# Contributions: Conceptual framework + real world application



How many **H|O|T** (hateful, offensive, toxic) comments are posted on social media every day?

Calibrate-Extrapolate  
framework

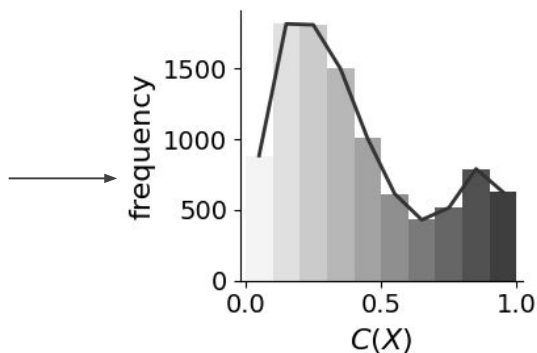




1. Introduction
2. **How to do prevalence estimation? Calibrate & Extrapolate**
3. Application: Estimating the fraction of H|O|T comments on news articles
4. Practical advice for prevalence estimation

classifier score density

	$C(X)$
item 1	0.87
item 2	0.72
item 3	0.45
item 10000	...



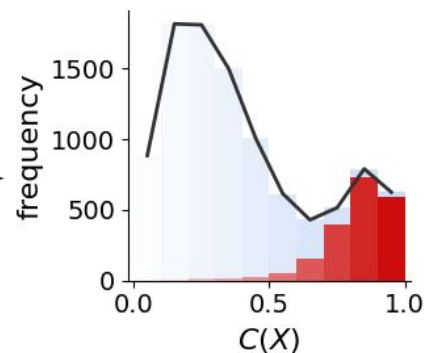
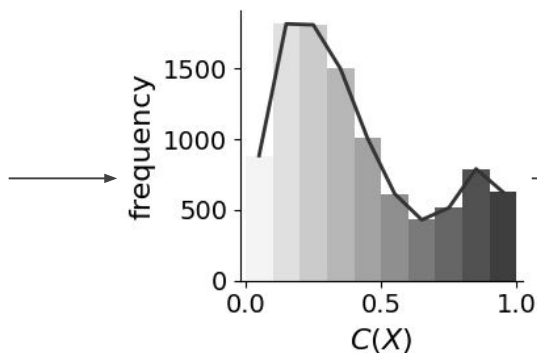
# The (classifier output, ground truth) joint distribution



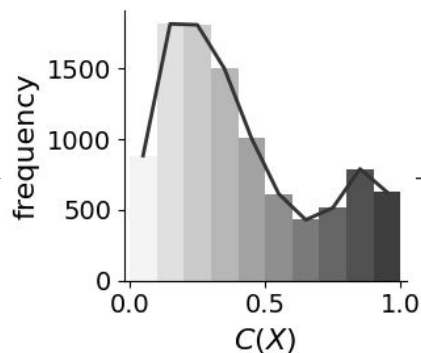
classifier score density

joint distribution

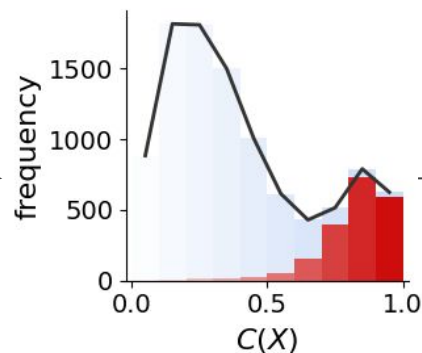
	$C(X)$
item 1	0.87
item 2	0.72
item 3	0.45
item 10000	...



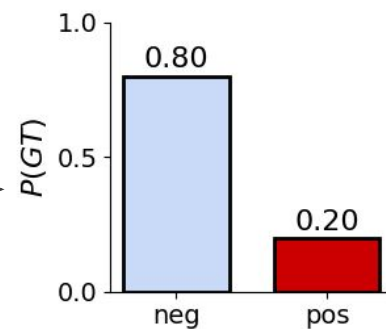
classifier score density



joint distribution

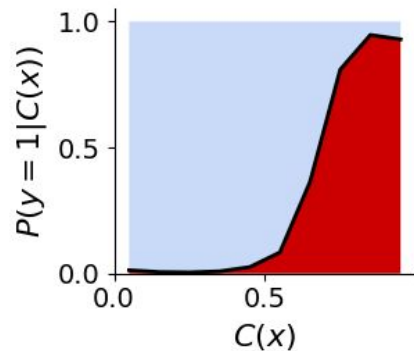
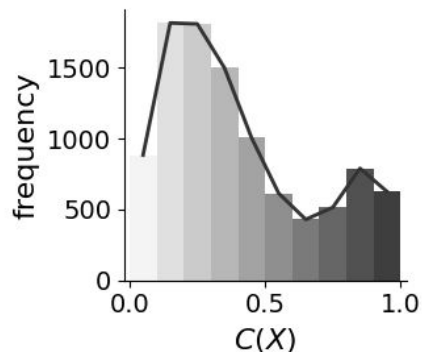


label density



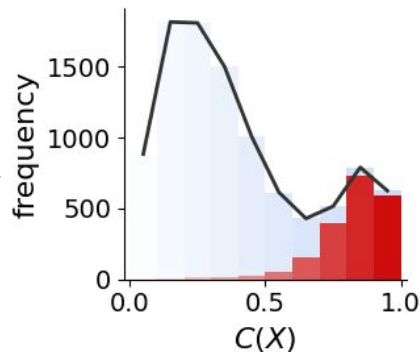
	$C(X)$
item 1	0.87
item 2	0.72
item 3	0.45
item 10000	...

classifier score density

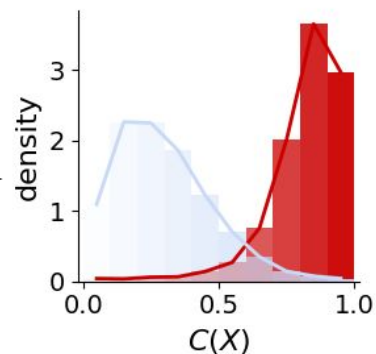
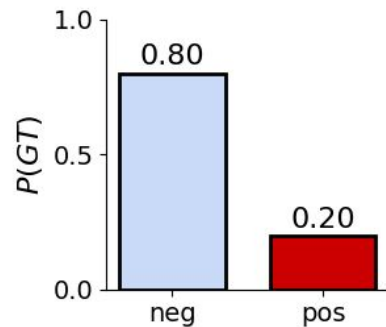


classifier calibration curve

joint distribution







label density



class-conditional densities

# Calibration phase: A one-time prevalence estimate is needed for a single dataset

Base  
dataset (A)

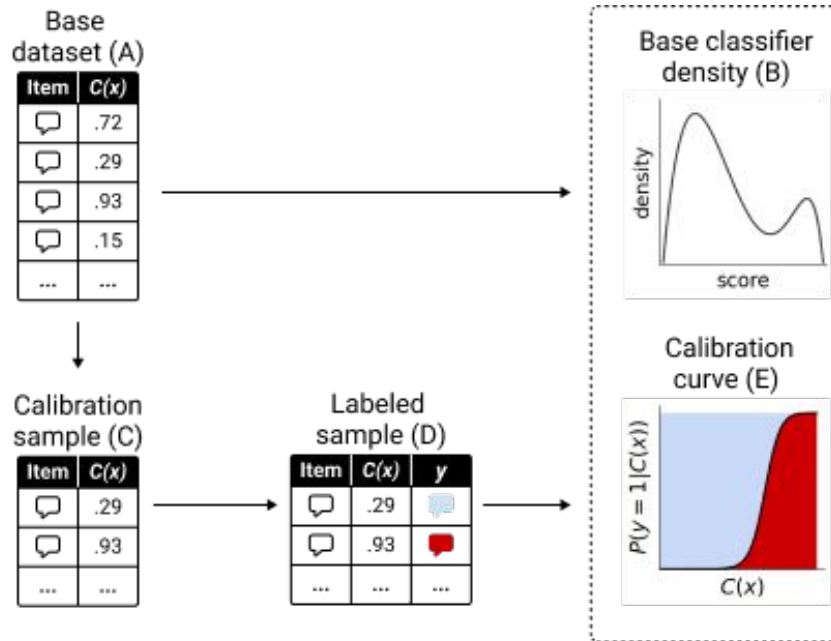
Item	$C(x)$
	.72
	.29
	.93
	.15
...	...



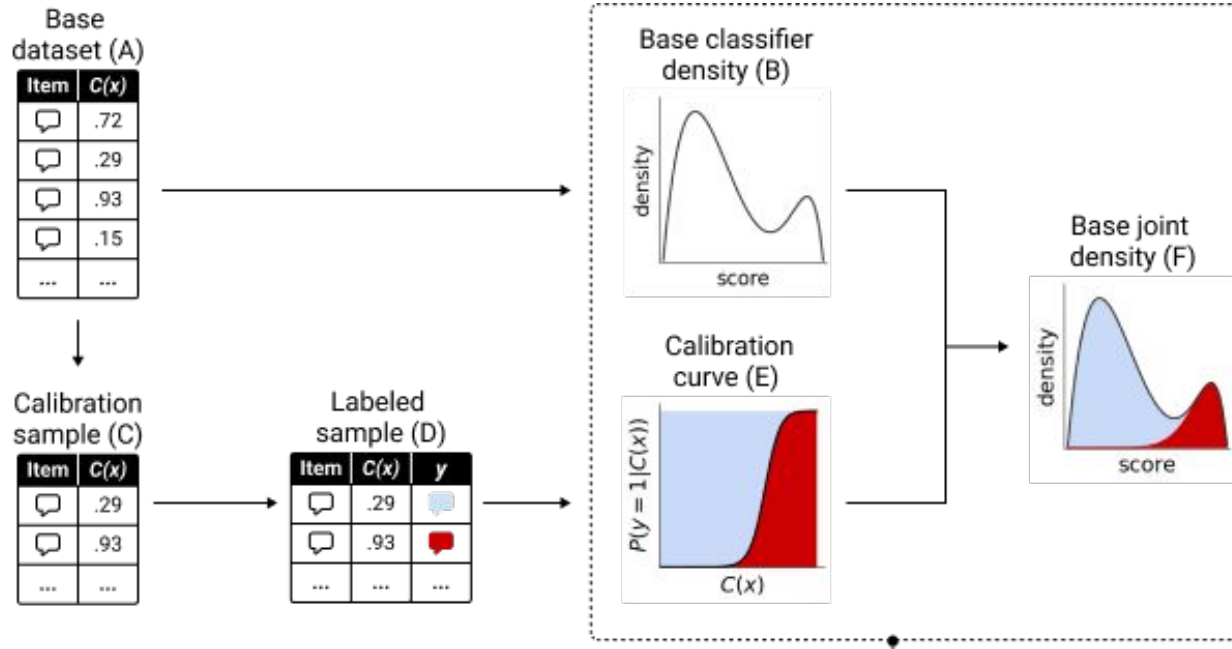
Base classifier  
density (B)



# Calibration phase: A one-time prevalence estimate is needed for a single dataset

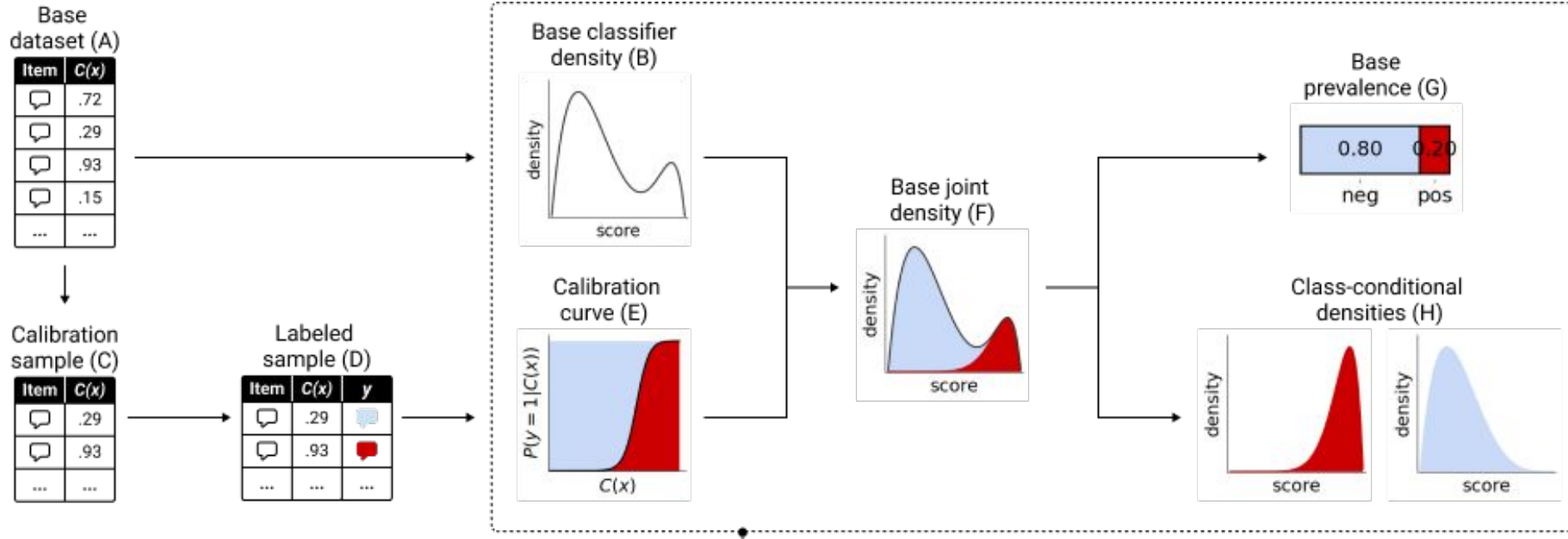


# Calibration phase: A one-time prevalence estimate is needed for a single dataset





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


- Base dataset  $\Leftrightarrow$  Calibration sample, always assume stable calibration curve
- Use purposive sampling to increase the number of potential minority class
- What if we have a weak classifier? Unbiased estimate if repeated many times, but the CI will be wider

# Extrapolation phase: Multiple estimates are needed for *related* datasets

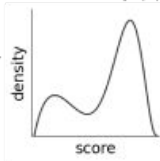


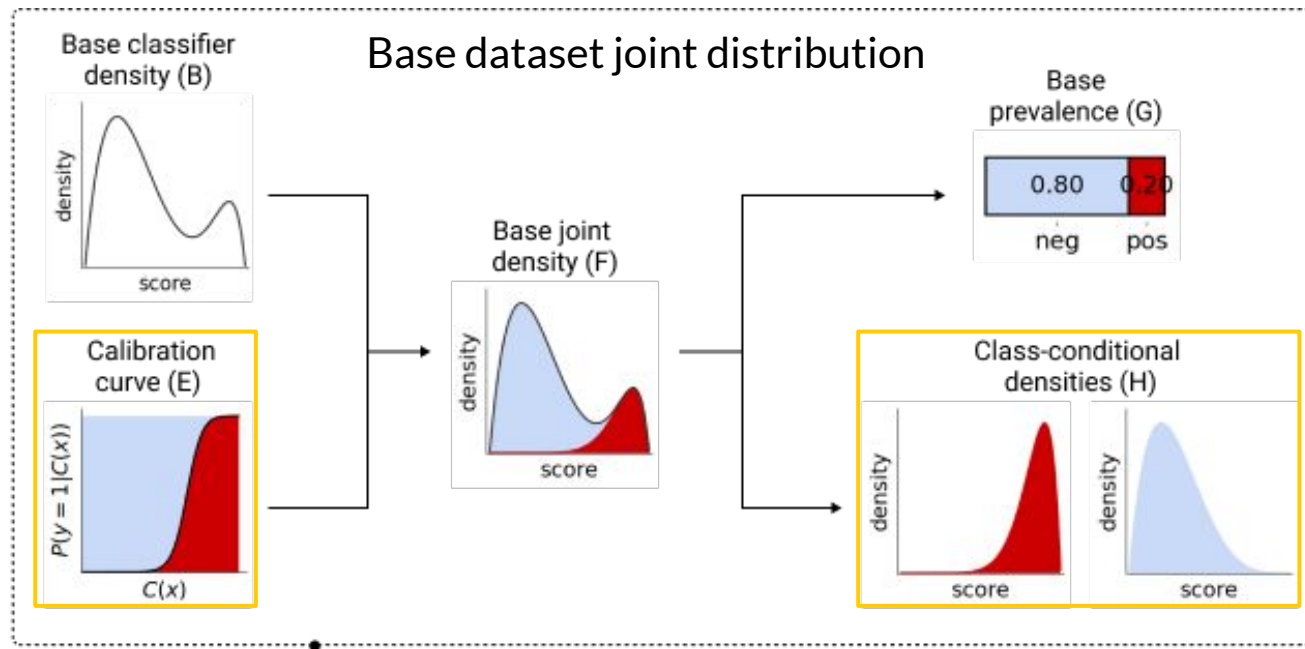
Target  
dataset (I)

Item	$C(x)$
	.44
	.03
	.97
	.65
...	...

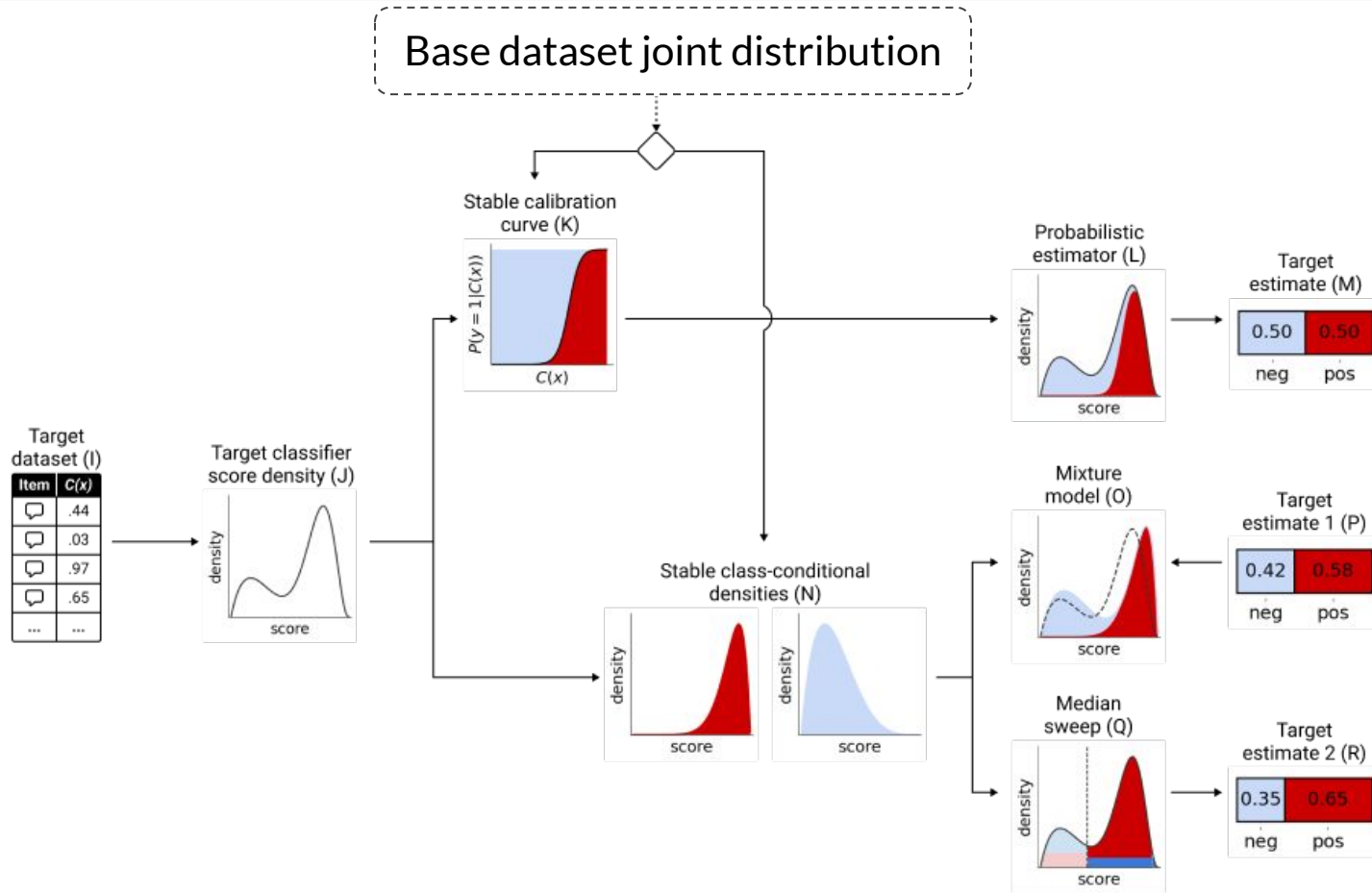


Target classifier  
score density (J)





# Extrapolation phase: Multiple estimates are needed for *related* datasets



Stability assumption	Stable attribute	Data generation	Causal chain	Prevalence estimation technique
Stable calibration curve	$P(\text{GT} \text{C}(\text{X}))$	Extrinsic	$\text{GT} \leftarrow \text{X} \rightarrow \text{C}(\text{X})$	Probabilistic Classify and Count
Stable class-conditional densities	$P(\text{C}(\text{X}) \text{GT})$	Intrinsic	$\text{GT} \rightarrow \text{X} \rightarrow \text{C}(\text{X})$	Mixture model, Median sweep

Dallas Card, and Noah A. Smith. "The importance of calibration for estimating proportions from annotations." In *NAACL*. 2018.

Zhijing Jin, et al. "Causal Direction of Data Collection Matters: Implications of Causal and Anticausal Learning for NLP." In *EMNLP*. 2021.

- Base dataset  $\Rightarrow$  Target dataset, choose stable calibration curve or stable class-conditional densities based on the data generation process
- What if we have a weak classifier? If we pick the correct stability assumption, the estimate will be fine. But a stronger classifier makes it more robust to wrong stability assumption.

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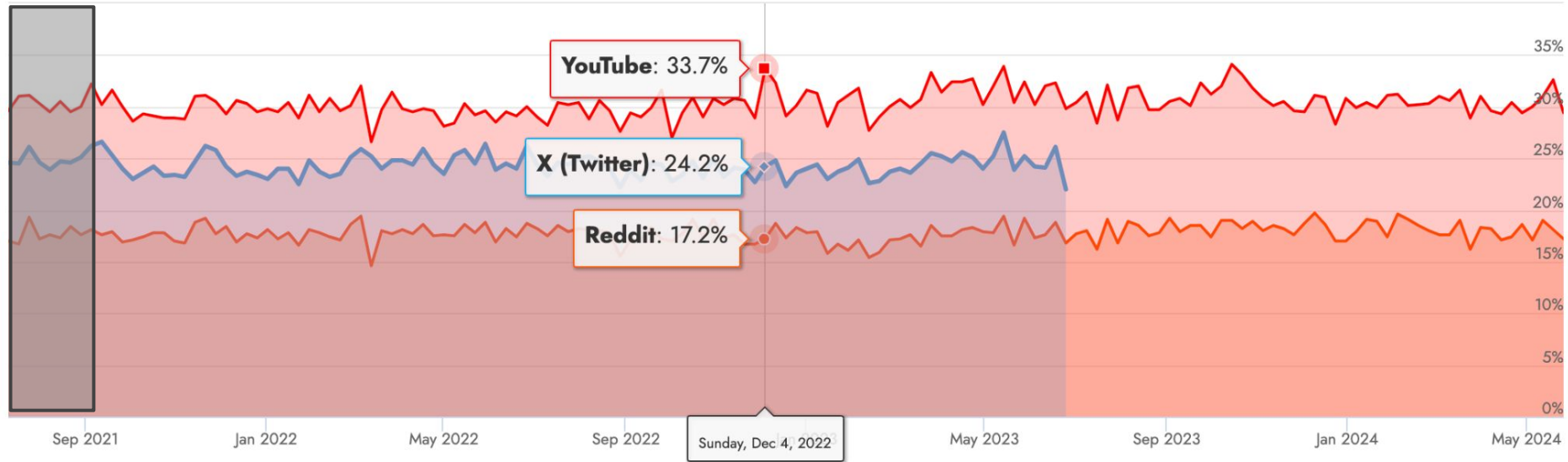
# H|O|T speech: Fraction of hateful, offensive, or toxic comments on news articles



## H|O|T Historical Chart

Zoom 1m 3m 6m YTD 1y All

● Reddit ● X (Twitter) ● YouTube



Project webpage: <https://csmr.umich.edu/projects/hot-speech/>

- Never safe to make a prevalence estimate based on a classifier trained on different datasets, without gathering human labels for calibration
- If a prevalence estimate is needed for a single dataset,
  - Balanced dataset → Random sample to annotate
  - Imbalanced dataset → Purposive sample to produce a calibration sample with more balanced labels
- If prevalence estimates are needed for multiple related datasets,
  - First estimate the joint distribution of a base dataset
  - Then borrow properties from base dataset joint distribution by making stability assumption based on the data generation process