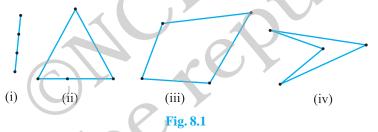
QUADRILATERALS

8.1 Introduction

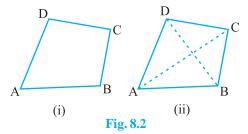
You have studied many properties of a triangle in Chapters 6 and 7 and you know that on joining three non-collinear points in pairs, the figure so obtained is a triangle. Now, let us mark four points and see what we obtain on joining them in pairs in some order.



Note that if all the points are collinear (in the same line), we obtain a line segment [see Fig. 8.1 (i)], if three out of four points are collinear, we get a triangle [see Fig. 8.1 (ii)], and if no three points out of four are collinear, we obtain a closed figure with four sides [see Fig. 8.1 (iii) and (iv)].

Such a figure formed by joining four points in an order is called a *quadrilateral*. In this book, we will consider only quadrilaterals of the type given in Fig. 8.1 (iii) but not as given in Fig. 8.1 (iv).

A quadrilateral has four sides, four angles and four vertices [see Fig. 8.2 (i)].



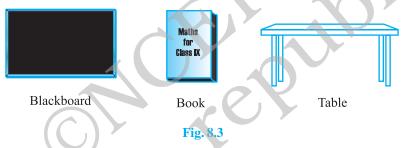
In quadrilateral ABCD, AB, BC, CD and DA are the four sides; A, B, C and D are the four vertices and \angle A, \angle B, \angle C and \angle D are the four angles formed at the vertices.

Now join the opposite vertices A to C and B to D [see Fig. 8.2 (ii)].

AC and BD are the two diagonals of the quadrilateral ABCD.

In this chapter, we will study more about different types of quadrilaterals, their properties and especially those of parallelograms.

You may wonder why should we study about quadrilaterals (or parallelograms) Look around you and you will find so many objects which are of the shape of a quadrilateral - the floor, walls, ceiling, windows of your classroom, the blackboard, each face of the duster, each page of your book, the top of your study table etc. Some of these are given below (see Fig. 8.3).



Although most of the objects we see around are of the shape of special quadrilateral called rectangle, we shall study more about quadrilaterals and especially parallelograms because a rectangle is also a parallelogram and all properties of a parallelogram are true for a rectangle as well.

8.2 Angle Sum Property of a Quadrilateral

Let us now recall the angle sum property of a quadrilateral.

The sum of the angles of a quadrilateral is 360°. This can be verified by drawing a diagonal and dividing the quadrilateral into two triangles.

Let ABCD be a quadrilateral and AC be a diagonal (see Fig. 8.4).

What is the sum of angles in \triangle ADC?

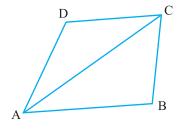


Fig. 8.4

You know that

$$\angle DAC + \angle ACD + \angle D = 180^{\circ}$$
 (1)

Similarly, in \triangle ABC,

$$\angle CAB + \angle ACB + \angle B = 180^{\circ}$$
 (2)

Adding (1) and (2), we get

$$\angle$$
 DAC + \angle ACD + \angle D + \angle CAB + \angle ACB + \angle B = 180° + 180° = 360°

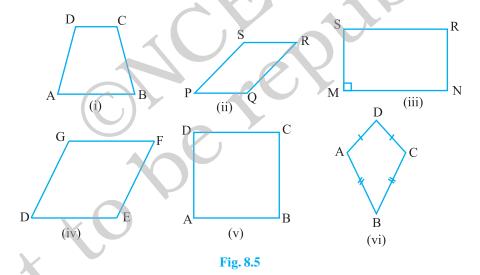
Also,
$$\angle DAC + \angle CAB = \angle A$$
 and $\angle ACD + \angle ACB = \angle C$

So,
$$\angle A + \angle D + \angle B + \angle C = 360^{\circ}$$
.

i.e., the sum of the angles of a quadrilateral is 360°.

8.3 Types of Quadrilaterals

Look at the different quadrilaterals drawn below:



Observe that:

- One pair of opposite sides of quadrilateral ABCD in Fig. 8.5 (i) namely, AB and CD are parallel. You know that it is called a *trapezium*.
- Both pairs of opposite sides of quadrilaterals given in Fig. 8.5 (ii), (iii), (iv) and (v) are parallel. Recall that such quadrilaterals are called *parallelograms*.
 So, quadrilateral PQRS of Fig. 8.5 (ii) is a parallelogram.

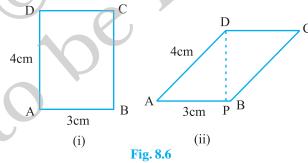
Similarly, all quadrilaterals given in Fig. 8.5 (iii), (iv) and (v) are parallelograms.

- In parallelogram MNRS of Fig. 8.5 (iii), note that one of its angles namely ∠ M is a right angle. What is this special parallelogram called? Try to recall. It is called a *rectangle*.
- The parallelogram DEFG of Fig. 8.5 (iv) has all sides equal and we know that it is called a *rhombus*.
- The parallelogram ABCD of Fig. 8.5 (v) has $\angle A = 90^{\circ}$ and all sides equal; it is called a *square*.
- In quadrilateral ABCD of Fig. 8.5 (vi), AD = CD and AB = CB i.e., two pairs of adjacent sides are equal. It is not a parallelogram. It is called a *kite*.

Note that a square, rectangle and rhombus are all parallelograms.

- A square is a rectangle and also a rhombus.
- A parallelogram is a trapezium.
- A kite is not a parallelogram.
- A trapezium is not a parallelogram (as only one pair of opposite sides is parallel in a trapezium and we require both pairs to be parallel in a parallelogram).
- A rectangle or a rhombus is not a square.

Look at the Fig. 8.6. We have a rectangle and a parallelogram with same perimeter 14 cm.



Here the area of the parallelogram is $DP \times AB$ and this is less than the area of the rectangle i.e., $AB \times AD$ as DP < AD. Generally sweet shopkeepers cut 'Burfis' in the shape of a parallelogram to accommodate more pieces in the same tray (see the shape of the Burfi before you eat it next time!).

Let us now review some properties of a parallelogram learnt in earlier classes.

8.4 Properties of a Parallelogram

Let us perform an activity.

Cut out a parallelogram from a sheet of paper and cut it along a diagonal (see Fig. 8.7). You obtain two triangles. What can you say about these triangles?

Place one triangle over the other. Turn one around, if necessary. What do you observe?

Observe that the two triangles are congruent to each other.

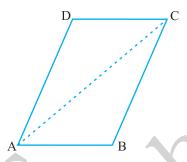


Fig. 8.7

Repeat this activity with some more parallelograms. Each time you will observe that each diagonal divides the parallelogram into two congruent triangles.

Let us now prove this result.

Theorem 8.1: A diagonal of a parallelogram divides it into two congruent triangles.

Proof : Let ABCD be a parallelogram and AC be a diagonal (see Fig. 8.8). Observe that the diagonal AC divides parallelogram ABCD into two triangles, namely, Δ ABC and Δ CDA. We need to prove that these triangles are congruent.

In \triangle ABC and \triangle CDA, note that BC || AD and AC is a transversal.

So,
$$\angle$$
 BCA = \angle DAC (Pair of alternate angles)

Also, AB || DC and AC is a transversal.

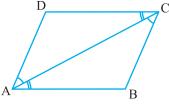
So, \angle BAC = \angle DCA (Pair of alternate angles)

and AC = CA

(Common)

So, \triangle ABC \cong \triangle CDA

(ASA rule)



ruent

or, diagonal AC divides parallelogram ABCD into two congruent triangles ABC and CDA.

Now, measure the opposite sides of parallelogram ABCD. What do you observe?

You will find that AB = DC and AD = BC.

This is another property of a parallelogram stated below:

Theorem 8.2: In a parallelogram, opposite sides are equal.

You have already proved that a diagonal divides the parallelogram into two congruent

triangles; so what can you say about the corresponding parts say, the corresponding sides? They are equal.

So,
$$AB = DC$$
 and $AD = BC$

Now what is the converse of this result? You already know that whatever is given in a theorem, the same is to be proved in the converse and whatever is proved in the theorem it is given in the converse. Thus, Theorem 8.2 can be stated as given below:

If a quadrilateral is a parallelogram, then each pair of its opposite sides is equal. So its converse is :

Theorem 8.3: If each pair of opposite sides of a quadrilateral is equal, then it is a parallelogram.

Can you reason out why?

Let sides AB and CD of the quadrilateral ABCD be equal and also AD = BC (see Fig. 8.9). Draw diagonal AC.

Clearly,
$$\triangle$$
 ABC \cong \triangle CDA (Why?)
So, \angle BAC = \angle DCA (Why?) Fig. 8.9

Can you now say that ABCD is a parallelogram? Why?

You have just seen that in a parallelogram each pair of opposite sides is equal and conversely if each pair of opposite sides of a quadrilateral is equal, then it is a parallelogram. Can we conclude the same result for the pairs of opposite angles?

Draw a parallelogram and measure its angles. What do you observe?

Each pair of opposite angles is equal.

Repeat this with some more parallelograms. We arrive at yet another result as given below.

Theorem 8.4: In a parallelogram, opposite angles are equal.

Now, is the converse of this result also true? Yes. Using the angle sum property of a quadrilateral and the results of parallel lines intersected by a transversal, we can see that the converse is also true. So, we have the following theorem:

Theorem 8.5: If in a quadrilateral, each pair of opposite angles is equal, then it is a parallelogram.

There is yet another property of a parallelogram. Let us study the same. Draw a parallelogram ABCD and draw both its diagonals intersecting at the point O (see Fig. 8.10).

Measure the lengths of OA, OB, OC and OD.

What do you observe? You will observe that

$$OA = OC$$
 and $OB = OD$.

or, O is the mid-point of both the diagonals.

Repeat this activity with some more parallelograms.

Each time you will find that O is the mid-point of both the diagonals.

So, we have the following theorem:

Theorem 8.6: The diagonals of a parallelogram bisect each other.

Now, what would happen, if in a quadrilateral the diagonals bisect each other? Will it be a parallelogram? Indeed this is true.

This result is the converse of the result of Theorem 8.6. It is given below:

Theorem 8.7: If the diagonals of a quadrilateral bisect each other, then it is a parallelogram.

You can reason out this result as follows:

Note that in Fig. 8.11, it is given that OA = OC and OB = OD.

So,
$$\Delta AOB \cong \Delta COD$$
 (Why?)

Therefore,
$$\angle ABO = \angle CDO$$
 (Why?)

From this, we get AB || CD

Therefore ABCD is a parallelogram.

Let us now take some examples.

Example 1: Show that each angle of a rectangle is a right angle.

Solution: Let us recall what a rectangle is.

A rectangle is a parallelogram in which one angle is a

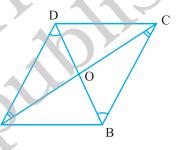


Fig. 8.10

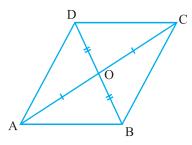


Fig. 8.11

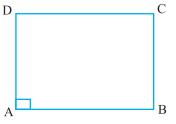
right angle.

Let ABCD be a rectangle in which $\angle A = 90^{\circ}$.

We have to show that $\angle B = \angle C = \angle D = 90^{\circ}$

We have, AD \parallel BC and AB is a transversal (see Fig. 8.12).

So,
$$\angle A + \angle B = 180^{\circ}$$
 (Interior angles on the same side of the transversal)



But,
$$\angle A = 90^{\circ}$$

So,
$$\angle B = 180^{\circ} - \angle A = 180^{\circ} - 90^{\circ} = 90^{\circ}$$

Now,
$$\angle C = \angle A \text{ and } \angle D = \angle B$$

(Opposite angles of the parallellogram)

So,
$$\angle C = 90^{\circ} \text{ and } \angle D = 90^{\circ}.$$

Therefore, each of the angles of a rectangle is a right angle.

Example 2 : Show that the diagonals of a rhombus are perpendicular to each other.

Solution: Consider the rhombus ABCD (see Fig. 8.13).

You know that
$$AB = BC = CD = DA$$
 (Why?)

Now, in \triangle AOD and \triangle COD,

OA = OC (Diagonals of a parallelogram bisect each other)

$$OD = OD$$

(Common)

Example 3: ABC is an isosceles triangle in which AB = AC. AD bisects exterior

$$AD = CD$$

Therefore, \triangle AOD \cong \triangle COD

(SSS congruence rule)

This gives,
$$\angle AOD = \angle COD$$
 (CPCT)

But,
$$\angle AOD + \angle COD = 180^{\circ}$$
 (Linear pair)

So,
$$2\angle AOD = 180^{\circ}$$

or,
$$\angle AOD = 90^{\circ}$$

So, the diagonals of a rhombus are perpendicular to each other.



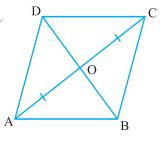


Fig. 8.13

angle PAC and CD || AB (see Fig. 8.14). Show that

(i) \angle DAC = \angle BCA and (ii) ABCD is a parallelogram.

Solution : (i) \triangle ABC is isosceles in which AB = AC (Given)

So,
$$\angle ABC = \angle ACB$$
 (Angles opposite to equal sides)

Also,
$$\angle PAC = \angle ABC + \angle ACB$$

(Exterior angle of a triangle)

or,
$$\angle PAC = 2\angle ACB$$

(1)

Now, AD bisects \angle PAC.

So,
$$\angle PAC = 2\angle DAC$$

(2)

Therefore,

$$2\angle DAC = 2\angle ACB$$
 [From (1) and (2)]



or,
$$\angle DAC = \angle ACB$$

(ii) Now, these equal angles form a pair of alternate angles when line segments BC and AD are intersected by a transversal AC.

So, BC
$$\parallel$$
 AD

(Given)

Now, both pairs of opposite sides of quadrilateral ABCD are parallel.

So, ABCD is a parallelogram.

Example 4: Two parallel lines l and m are intersected by a transversal p (see Fig. 8.15). Show that the quadrilateral formed by the bisectors of interior angles is a rectangle.

Solution : It is given that PS /| QR and transversal p intersects them at points A and C respectively.

The bisectors of \angle PAC and \angle ACQ intersect at B and bisectors of \angle ACR and \angle SAC intersect at D.

We are to show that quadrilateral ABCD is a rectangle.

Now,
$$\angle PAC = \angle ACR$$

(Alternate angles as $l \parallel m$ and p is a transversal)

So,
$$\frac{1}{2} \angle PAC = \frac{1}{2} \angle ACR$$

i.e.,
$$\angle BAC = \angle ACD$$

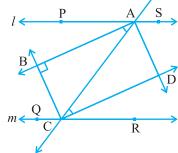


Fig. 8.15

These form a pair of alternate angles for lines AB and DC with AC as transversal and they are equal also.

So,
$$AB \parallel DC$$

Similarly, BC
$$\parallel$$
 AD (Considering \angle ACB and \angle CAD)

Therefore, quadrilateral ABCD is a parallelogram.

Also,
$$\angle PAC + \angle CAS = 180^{\circ}$$
 (Linear pair)

So,
$$\frac{1}{2} \angle PAC + \frac{1}{2} \angle CAS = \frac{1}{2} \times 180^{\circ} = 90^{\circ}$$

or,
$$\angle BAC + \angle CAD = 90^{\circ}$$

or,
$$\angle BAD = 90^{\circ}$$

So, ABCD is a parallelogram in which one angle is 90°.

Therefore, ABCD is a rectangle.

Example 5: Show that the bisectors of angles of a parallelogram form a rectangle.

Solution : Let P, Q, R and S be the points of intersection of the bisectors of \angle A and \angle B, \angle B and \angle C, \angle C and \angle D, and \angle D and \angle A respectively of parallelogram ABCD (see Fig. 8.16).

In \triangle ASD, what do you observe?

Since DS bisects \angle D and AS bisects \angle A, therefore,

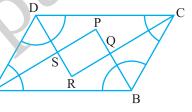


Fig. 8.16

$$\angle DAS + \angle ADS = \frac{1}{2} \angle A + \frac{1}{2} \angle D$$

$$= \frac{1}{2} (\angle A + \angle D)$$

$$= \frac{1}{2} \times 180^{\circ} \quad (\angle A \text{ and } \angle D \text{ are interior angles}$$
on the same side of the transversal)
$$= 90^{\circ}$$

Also,
$$\angle$$
 DAS + \angle ADS + \angle DSA = 180° (Angle sum property of a triangle)

or,
$$90^{\circ} + \angle DSA = 180^{\circ}$$

or,
$$\angle DSA = 90^{\circ}$$

So,
$$\angle PSR = 90^{\circ}$$
 (Being vertically opposite to $\angle DSA$)

Similarly, it can be shown that \angle APB = 90° or \angle SPQ = 90° (as it was shown for \angle DSA). Similarly, \angle PQR = 90° and \angle SRQ = 90°.

So, PQRS is a quadrilateral in which all angles are right angles.

Can we conclude that it is a rectangle? Let us examine. We have shown that $\angle PSR = \angle PQR = 90^{\circ}$ and $\angle SPQ = \angle SRQ = 90^{\circ}$. So both pairs of opposite angles are equal.

Therefore, PQRS is a parallelogram in which one angle (in fact all angles) is 90° and so, PQRS is a rectangle.

8.5 Another Condition for a Quadrilateral to be a Parallelogram

You have studied many properties of a parallelogram in this chapter and you have also verified that if in a quadrilateral any one of those properties is satisfied, then it becomes a parallelogram.

We now study yet another condition which is the least required condition for a quadrilateral to be a parallelogram.

It is stated in the form of a theorem as given below:

Theorem 8.8: A quadrilateral is a parallelogram if a pair of opposite sides is equal and parallel.

Look at Fig 8.17 in which AB = CD and AB \parallel CD. Let us draw a diagonal AC. You can show that Δ ABC \cong Δ CDA by SAS congruence rule.

So, BC
$$\parallel$$
 AD (Why?)

Let us now take an example to apply this property of a parallelogram.

Example 6 : ABCD is a parallelogram in which P and Q are mid-points of opposite sides AB and CD (see Fig. 8.18). If AQ intersects DP at S and BQ intersects CP at R, show that:

- (i) APCQ is a parallelogram.
- (ii) DPBQ is a parallelogram.
- (iii) PSQR is a parallelogram.

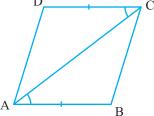


Fig. 8.17

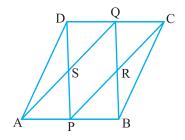


Fig. 8.18

Solution: (i) In quadrilateral APCQ,

$$AP \parallel QC$$
 (Since $AB \parallel CD$) (1)

$$AP = \frac{1}{2} AB$$
, $CQ = \frac{1}{2} CD$ (Given)

Also,
$$AB = CD$$
 (Why?)

So,
$$AP = QC$$
 (2)

Therefore, APCQ is a parallelogram

[From (1) and (2) and Theorem 8.8]

(ii) Similarly, quadrilateral DPBQ is a parallelogram, because

$$DQ \parallel PB$$
 and $DQ = PB$

(iii) In quadrilateral PSQR,

SP || QR (SP is a part of DP and QR is a part of QB)

Similarly,

SQ || PR

So, PSQR is a parallelogram.

EXERCISE 8.1

- **1.** The angles of quadrilateral are in the ratio 3:5:9:13. Find all the angles of the quadrilateral.
- 2. If the diagonals of a parallelogram are equal, then show that it is a rectangle.
- **3.** Show that if the diagonals of a quadrilateral bisect each other at right angles, then it is a rhombus.
- **4.** Show that the diagonals of a square are equal and bisect each other at right angles.
- 5. Show that if the diagonals of a quadrilateral are equal and bisect each other at right angles, then it is a square.
- **6.** Diagonal AC of a parallelogram ABCD bisects ∠ A (see Fig. 8.19). Show that
 - (i) it bisects $\angle C$ also,
 - (ii) ABCD is a rhombus.
- ABCD is a rhombus. Show that diagonal AC bisects ∠ A as well as ∠ C and diagonal BD bisects ∠ B as well as ∠ D.

AB

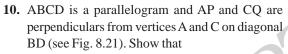
Fig. 8.19

8. ABCD is a rectangle in which diagonal AC bisects \angle A as well as \angle C. Show that: (i) ABCD is a square (ii) diagonal BD bisects \angle B as well as \angle D.

9. In parallelogram ABCD, two points P and Q are taken on diagonal BD such that DP = BQ (see Fig. 8.20). Show that:



- (ii) AP = CQ
- (iii) $\Delta AQB \cong \Delta CPD$
- (iv) AQ = CP
- (v) APCQ is a parallelogram





(ii) AP = CQ

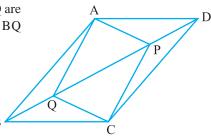


Fig. 8.20

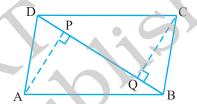


Fig. 8.21

11. In \triangle ABC and \triangle DEF, AB = DE, AB || DE, BC = EF and BC || EF. Vertices A, B and C are joined to vertices D, E and F respectively (see Fig. 8.22). Show that



- (ii) quadrilateral BEFC is a parallelogram
- (iii) $AD \parallel CF$ and AD = CF
- (iv) quadrilateral ACFD is a parallelogram
- (v) AC = DF
- (vi) \triangle ABC \cong \triangle DEF.

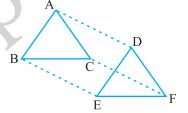


Fig. 8.22

12. ABCD is a trapezium in which AB \parallel CD and AD = BC (see Fig. 8.23). Show that



(ii)
$$\angle C = \angle D$$

(iii)
$$\triangle ABC \cong \triangle BAD$$

(iv) diagonal AC = diagonal BD

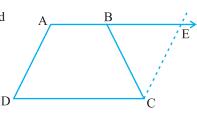


Fig. 8.23

[Hint: Extend AB and draw a line through C parallel to DA intersecting AB produced at E.]

8.6 The Mid-point Theorem

You have studied many properties of a triangle as well as a quadrilateral. Now let us study yet another result which is related to the mid-point of sides of a triangle. Perform the following activity.

Draw a triangle and mark the mid-points E and F of two sides of the triangle. Join the points E and F (see Fig. 8.24).

Measure EF and BC. Measure \angle AEF and \angle ABC.

What do you observe? You will find that:

$$EF = \frac{1}{2} BC \text{ and } \angle AEF = \angle ABC$$

so, EF || BC

Repeat this activity with some more triangles.

So, you arrive at the following theorem:

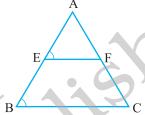


Fig. 8.24

Theorem 8.9: The line segment joining the mid-points of two sides of a triangle is parallel to the third side.

You can prove this theorem using the following clue:

Observe Fig 8.25 in which E and F are mid-points of AB and AC respectively and CD \parallel BA.

$$\Delta AEF \cong \Delta CDF$$
 (ASA Rule)

So,
$$EF = DF$$
 and $BE = AE = DC$ (Why?)

Therefore, BCDE is a parallelogram. (Why?)

This gives EF || BC.

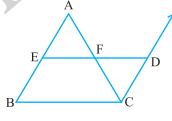


Fig. 8.25

In this case, also note that
$$EF = \frac{1}{2} ED = \frac{1}{2} BC$$
.

Can you state the converse of Theorem 8.9? Is the converse true?

You will see that converse of the above theorem is also true which is stated as below:

Theorem 8.10: The line drawn through the mid-point of one side of a triangle, parallel to another side bisects the third side.

In Fig 8.26, observe that E is the mid-point of AB, line l is passsing through E and is parallel to BC and CM \parallel BA.

Prove that AF = CF by using the congruence of Δ AEF and Δ CDF.

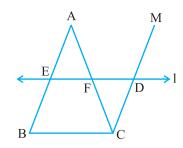


Fig. 8.26

Example 7 : In \triangle ABC, D, E and F are respectively the mid-points of sides AB, BC and CA (see Fig. 8.27). Show that \triangle ABC is divided into four congruent triangles by joining D, E and F.

Solution: As D and E are mid-points of sides AB and BC of the triangle ABC, by Theorem 8.9,

Similarly, DF || BC and EF || AB

B E C

Fig. 8.27

Therefore ADEF, BDFE and DFCE are all parallelograms.

Now DE is a diagonal of the parallelogram BDFE,

therefore, $\Delta BDE \cong \Delta FED$

Similarly $\Delta DAF \cong \Delta FED$

and $\Delta EFC \cong \Delta FED$

So, all the four triangles are congruent.

Example 8 : l, m and n are three parallel lines intersected by transversals p and q such that l, m and n cut off equal intercepts AB and BC on p (see Fig. 8.28). Show that l, m and n cut off equal intercepts DE and EF on q also.

Solution : We are given that AB = BC and have to prove that DE = EF.

Let us join A to F intersecting m at G..

The trapezium ACFD is divided into two triangles;

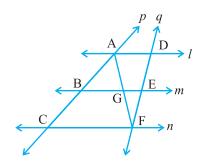


Fig. 8.28

namely Δ ACF and Δ AFD.

In \triangle ACF, it is given that B is the mid-point of AC (AB = BC)

and BG \parallel CF (since $m \parallel n$).

So, G is the mid-point of AF (by using Theorem 8.10)

Now, in Δ AFD, we can apply the same argument as G is the mid-point of AF, GE || AD and so by Theorem 8.10, E is the mid-point of DF,

i.e., DE = EF.

In other words, l, m and n cut off equal intercepts on q also.

EXERCISE 8.2

- 1. ABCD is a quadrilateral in which P, Q, R and S are mid-points of the sides AB, BC, CD and DA (see Fig 8.29). AC is a diagonal. Show that:
 - (i) $SR \parallel AC$ and $SR = \frac{1}{2} AC$
 - (ii) PQ = SR
 - (iii) PQRS is a parallelogram.

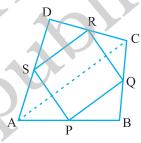


Fig. 8.29

- **2.** ABCD is a rhombus and P, Q, R and S are ©wthe mid-points of the sides AB, BC, CD and DA respectively. Show that the quadrilateral PQRS is a rectangle.
- **3.** ABCD is a rectangle and P, Q, R and S are mid-points of the sides AB, BC, CD and DA respectively. Show that the quadrilateral PQRS is a rhombus.
- **4.** ABCD is a trapezium in which AB || DC, BD is a diagonal and E is the mid-point of AD. A line is drawn through E parallel to AB intersecting BC at F (see Fig. 8.30). Show that F is the mid-point of BC.

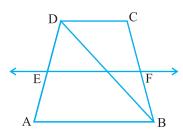


Fig. 8.30

5. In a parallelogram ABCD, E and F are the mid-points of sides AB and CD respectively (see Fig. 8.31). Show that the line segments AF and EC trisect the diagonal BD.

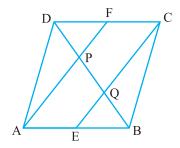


Fig. 8.31

- **6.** Show that the line segments joining the mid-points of the opposite sides of a quadrilateral bisect each other.
- 7. ABC is a triangle right angled at C. A line through the mid-point M of hypotenuse AB and parallel to BC intersects AC at D. Show that
 - (i) D is the mid-point of AC
- (ii) MD⊥AC

(iii)
$$CM = MA = \frac{1}{2}AB$$

8.7 Summary

In this chapter, you have studied the following points:

- 1. Sum of the angles of a quadrilateral is 360°.
- 2. A diagonal of a parallelogram divides it into two congruent triangles.
- 3. In a parallelogram,
 - (i) opposite sides are equal
- (ii) opposite angles are equal
- (iii) diagonals bisect each other
- 4. A quadrilateral is a parallelogram, if
 - (i) opposite sides are equal
- or (ii) opposite angles are equal
- or (iii) diagonals bisect each other
- or (iv)a pair of opposite sides is equal and parallel
- 5. Diagonals of a rectangle bisect each other and are equal and vice-versa.
- 6. Diagonals of a rhombus bisect each other at right angles and vice-versa.
- 7. Diagonals of a square bisect each other at right angles and are equal, and vice-versa.
- **8.** The line-segment joining the mid-points of any two sides of a triangle is parallel to the third side and is half of it.
- **9.** A line through the mid-point of a side of a triangle parallel to another side bisects the third side.
- **10.** The quadrilateral formed by joining the mid-points of the sides of a quadrilateral, in order, is a parallelogram.