Write a program to implement a singly linked list as an ADT that supports the following operations:

- I. Insert an element x at the beginning of the singly linked list.
- II. Insert an element x at i th position in the singly linked list.
- III. Remove an element from the beginning of the singly linked list.
- IV. Remove an element from ith position in the singly linked list.
- V. Search for an element x in the singly linked list and return its pointer.

```
class Node:
    def __init__(self, data):
        self.data = data
        self.next = None
class SinglyLinkedList:
    def __init__(self):
        self.head = None
```

Insert an element x at the beginning of the singly linked list.

```
def insert_at_beginning(self, x):
    new_node = Node(x)
    new_node.next = self.head
    self.head = new node
```

Insert an element x at i-th position in the singly linked list.

```
def insert_at_position(self, x, i):
    new_node = Node(x)
    if i == 0:
        self.insert_at_beginning(x)
        return
    temp = self.head
    count = 0
    while temp is not None and count < i - 1:
        temp = temp.next
        count += 1
    if temp is None:
        print("Index out of bounds")
        return</pre>
```

```
new_node.next = temp.next
temp.next = new_node
```

Remove an element from the beginning of the singly linked list.

```
def remove_from_beginning(self):
    if self.head is None:
        print("List is empty")
        return
    self.head = self.head.next
```

Remove an element from i-th position in the singly linked list.

```
def remove from position(self, i):
      if self.head is None:
          print("List is empty")
          return
      if i == 0:
          self.head = self.head.next
          return
      temp = self.head
      count = 0
      while temp is not None and count < i - 1:
          temp = temp.next
          count += 1
      if temp is None or temp.next is None:
          print("Index out of bounds")
          return
      temp.next = temp.next.next
```

Search for an element x in the singly linked list and return its pointer.

```
def search(self, x):
    temp = self.head
    while temp:
        if temp.data == x:
            return temp
        temp = temp.next
        return None

def display(self):
    temp = self.head
```

```
elements = []
        while temp:
            elements.append(str(temp.data))
            temp = temp.next
        print(" -> ".join(elements) + " -> None")
# Example usage:
if name == " main ":
    11 = SinglyLinkedList()
    11.insert at beginning(10)
    11.insert at beginning(20)
    11.insert at position(30, 1)
    ll.display()
    search result = ll.search(10)
    if search result:
        print("Search 10: Found")
    else:
        print("Search 10: Not Found")
    11.remove from position(1)
    ll.display()
```

Output:

```
20 -> 30 -> 10 -> None
Search 10: Found
20 -> 10 -> None
```

Write a program to implement a doubly linked list as an ADT that supports the following operations

- i. Insert an element x at the beginning of the doubly linked list.
- ii. Insert an element x at the end of the doubly linked list.
- iii. Remove an element from the beginning of the doubly linked list.
- iv. Remove an element from the end of the doubly linked list.

```
class Node:
    def __init__(self, data):
        self.data = data
        self.next = None
        self.prev = None

class DoublyLinkedList:
    def __init__(self):
        self.head = None
        self.tail = None
```

Insert an element x at the beginning of the doubly linked list.

```
def insert_at_beginning(self, x):
    new_node = Node(x)
    if self.head is None:
        self.head = self.tail = new_node
    else:
        new_node.next = self.head
        self.head.prev = new_node
        self.head = new_node
```

Insert an element x at the end of the doubly linked list.

```
def insert_at_end(self, x):
    new_node = Node(x)
    if self.tail is None:
        self.head = self.tail = new_node
    else:
        self.tail.next = new_node
        new node.prev = self.tail
```

```
self.tail = new node
```

Remove an element from the beginning of the doubly linked list.

```
def remove_from_beginning(self):
    if self.head is None:
        print("List is empty")
        return
    if self.head == self.tail:
        self.head = self.tail = None
    else:
        self.head = self.head.next
        self.head.prev = None
```

Remove an element from the end of the doubly linked list.

```
def remove from end(self):
        if self.tail is None:
            print("List is empty")
            return
        if self.head == self.tail:
            self.head = self.tail = None
        else:
            self.tail = self.tail.prev
            self.tail.next = None
 def display(self):
        temp = self.head
        elements = []
        while temp:
            elements.append(str(temp.data))
            temp = temp.next
        print(" <-> ".join(elements) + " <-> None")
# Example usage:
if name == " main ":
    dll = DoublyLinkedList()
    dll.insert at beginning(10)
    dll.insert at beginning(20)
    dll.insert at end(30)
    dll.display()
```

```
dll.remove_from_beginning()
dll.display()

dll.remove_from_end()
dll.display()
```

Output:

```
20 <-> 10 <-> 30 <-> None
10 <-> 30 <-> None
10 <-> None
```

Write a program to implement a circular linked list as an ADT that supports the following operations:

- i. Insert an element x in the list.
- ii. Remove an element from the list.
- iii. Search for an element x in the list and return its pointer.

```
class Node:
    def __init__(self, data):
        self.data = data
        self.next = None

class CircularLinkedList:
    def __init__(self):
        self.head = None
```

I. Insert an element x in the list.

```
def insert(self, x):
    new_node = Node(x)
    if self.head is None:
        self.head = new_node
        new_node.next = self.head
    else:
        temp = self.head
        while temp.next != self.head:
            temp = temp.next
        temp.next = new_node
        new node.next = self.head
```

Remove an element from the list.

```
def remove(self, x):
    if self.head is None:
        print("List is empty")
        return
    temp = self.head
    prev = None
    while True:
```

```
if temp.data == x:
        if prev is None:
            if temp.next == self.head:
                self.head = None
            else:
                last = self.head
                while last.next != self.head:
                     last = last.next
                self.head = temp.next
                last.next = self.head
        else:
            prev.next = temp.next
        return
    prev = temp
    temp = temp.next
    if temp == self.head:
        break
print("Element not found")
```

Search for an element x in the list and return its pointer.

```
def search(self, x):
    if self.head is None:
        return None
    temp = self.head
    while True:
        if temp.data == x:
            return temp
        temp = temp.next
        if temp == self.head:
            break
    return None
def display(self):
    if self.head is None:
        print("List is empty")
        return
    temp = self.head
    elements = []
    while True:
        elements.append(str(temp.data))
```

Example usage:

```
if __name__ == "__main__":
    cll = CircularLinkedList()
    cll.insert(10)
    cll.insert(20)
    cll.insert(30)
    cll.display()

cll.remove(20)
    cll.display()

search_result = cll.search(30)
    if search_result:
        print("Search 30: Found")
    else:
        print("Search 30: Not Found")
```

OUTPUT;

```
10 -> 20 -> 30 -> (head)
10 -> 30 -> (head)
Search 30: Found
```

Implement Stack as an ADT and use it to evaluate a prefix/postfix expression.

```
def push(self, item):
        self.items.append(item)
    def pop(self):
        if not self.is empty():
            return self.items.pop()
        return None
    def peek(self):
        if not self.is empty():
            return self.items[-1]
        return None
    def is empty(self):
        return len(self.items) == 0
    def size(self):
        return len(self.items)
# Function to evaluate a postfix expression
def evaluate postfix (expression):
    stack = Stack()
    for char in expression:
        if char.isdigit():
            stack.push(int(char))
        else:
            b = stack.pop()
            a = stack.pop()
            if char == '+':
                 stack.push(a + b)
            elif char == '-':
                 stack.push(a - b)
            elif char == '*':
```

class Stack:

def init (self):

self.items = []

```
stack.push(a * b)
            elif char == '/':
                stack.push(a / b)
    return stack.pop()
#Function to evaluate a prefix expression
def evaluate prefix(expression):
    stack = Stack()
    for char in reversed (expression):
        if char.isdigit():
            stack.push(int(char))
        else:
            a = stack.pop()
            b = stack.pop()
            if char == '+':
                stack.push(a + b)
            elif char == '-':
                stack.push(a - b)
            elif char == '*':
                stack.push(a * b)
            elif char == '/':
                stack.push(a / b)
    return stack.pop()
# Example usage:
if name == " main ":
    postfix_expr = "53+62/*35*+"
    prefix expr = "+*23/84"
    print("Postfix Evaluation:",
evaluate postfix(postfix expr))
    print("Prefix Evaluation:", evaluate prefix(prefix expr))
```

Output:

Postfix Evaluation: 39.0 Prefix Evaluation: 8.0

Implement Queue as an ADT.

```
class Queue:
    def init (self):
        self.items = []
    def enqueue(self, item):
        self.items.append(item)
    def dequeue(self):
        if not self.is empty():
            return self.items.pop(0)
        return None
    def front(self):
        if not self.is empty():
            return self.items[0]
        return None
    def is empty(self):
        return len(self.items) == 0
    def size(self):
        return len(self.items)
if __name__ == "__main__":
    q = Queue()
   q.enqueue(10)
   q.enqueue(20)
    q.enqueue(30)
   print("Front element:", q.front())
   print("Dequeued element:", q.dequeue())
   print("Queue size:", q.size())
```

```
Front element: 10
Dequeued element: 10
Queue size: 2
```

Write a program to implement a Binary Search Tree as an ADT which supports the following operations:

- i. Insert an element x
- ii. Delete an element x
- iii. Search for an element x in the BST
- iv. Display the elements of the BST in preorder, inorder, and postorder traversal.

```
class Node:
    def init (self, key):
        self.key = key
        self.left = self.right = None
class BST:
    def init (self):
        self.root = None
    def insert(self, key):
        self.root = self. insert(self.root, key)
    def insert(self, root, key):
        if not root:
            return Node (key)
        if key < root.key:
            root.left = self. insert(root.left, key)
        else:
            root.right = self. insert(root.right, key)
        return root
   def delete(self, key):
        self.root = self. delete(self.root, key)
    def delete(self, root, key):
        if not root:
            return root
        if key < root.key:
            root.left = self. delete(root.left, key)
        elif key > root.key:
            root.right = self. delete(root.right, key)
```

```
else:
            if not root.left:
                return root.right
            if not root.right:
                return root.left
            temp = self. min value node(root.right)
            root.key = temp.key
            root.right = self. delete(root.right,
temp.key)
        return root
    def min value node (self, node):
        while node.left:
            node = node.left
        return node
    def search(self, key):
        return self. search(self.root, key)
    def search(self, root, key):
        if not root or root.key == key:
            return root
        return self. search(root.left, key) if key <</pre>
root.key else self. search(root.right, key)
    def preorder(self, root):
        if root:
            print(root.key, end=" ")
            self.preorder(root.left)
            self.preorder(root.right)
 def inorder(self, root):
        if root:
            self.inorder(root.left)
            print(root.key, end=" ")
            self.inorder(root.right)
    def postorder(self, root):
        if root:
```

```
self.postorder(root.left)
    self.postorder(root.right)
    print(root.key, end=" ")

# Example Usage:
bst = BST()
for num in [50, 30, 70, 20, 40, 60, 80]:
    bst.insert(num)

print("Inorder Traversal:")
bst.inorder(bst.root)
print("\nSearch 40:", "Found" if bst.search(40) else "Not Found")
bst.delete(40)
print("Inorder after deleting 40:")
bst.inorder(bst.root)
```

OUTPUT:

```
Inorder Traversal:
20 30 40 50 60 70 80
Search 40: Found
Inorder after deleting 40:
20 30 50 60 70 80
```

Write a program to implement the insert and search operation in AVL trees.

```
class Node:
   def __init__(self, key):
        self.key = key
        self.left = self.right = None
        self.height = 1
def height(n):
    return n.height if n else 0
def balance(n):
    return height(n.left) - height(n.right) if n else 0
def right rotate(y):
    x = y.left
    y.left = x.right
    x.right = y
    y.height = 1 + max(height(y.left), height(y.right))
    x.height = 1 + max(height(x.left), height(x.right))
    return x
def left rotate(x):
    y = x.right
    x.right = y.left
    y.left = x
    x.height = 1 + max(height(x.left), height(x.right))
    y.height = 1 + max(height(y.left), height(y.right))
    return y
def insert(root, key):
    if not root:
        return Node (key)
    if key < root.key:
        root.left = insert(root.left, key)
```

```
else:
        root.right = insert(root.right, key)
    root.height = 1 + max(height(root.left),
height(root.right))
    b = balance(root)
    if b > 1 and key < root.left.key:
        return right rotate(root)
    if b < -1 and key > root.right.key:
        return left rotate(root)
    if b > 1 and key > root.left.key:
        root.left = left rotate(root.left)
        return right rotate(root)
    if b < -1 and key < root.right.key:
        root.right = right rotate(root.right)
        return left rotate(root)
    return root
def search(root, key):
    if not root:
        return False
    if key == root.key:
        return True
    return search(root.left, key) if key < root.key else
search(root.right, key)
# Function to print vertically
def print vertical(root, level=0, prefix="Root: "):
    if root:
        print vertical(root.right, level + 1, "R--- ")
                 " * level + prefix + str(root.key))
        print vertical(root.left, level + 1, "L--- ")
# Main Execution
root = None
values = [30, 20, 40, 10, 25, 50, 5] # Example values
for val in values:
```

```
root = insert(root, val)

print("AVL Tree (vertical layout):")
print_vertical(root)

# Search example
val = 25
print(f"\nSearch {val}: {'Found' if search(root, val) else
'Not Found'}")
```

OUTPUT:

```
AVL Tree (vertical layout):

R--- 50

R--- 40

Root: 30

R--- 25

L--- 20

L--- 10

L--- 5

Search 25: Found
```