

capacity = 10

Item	Weight	Profit
1	3	30
2	4	45
3	2	25
4	3	36

$$V[i, j] = \begin{cases} 0 & \text{if } i=0 \text{ or } j=0 \\ V[i-1, j] & \text{if } w_i > j \\ \max\{V[i-1, j], V[i-1, j-w_i] + P_i\} & \text{if } w_i \leq j \end{cases}$$

	0	1	2	3	4	5	6	7	8	9	10
0	0	0	0	0	0	0	0	0	0	0	0
1	0	0	0	30	30	30	30	30	30	30	30
2	0	0	0	30	45	45	45	75	75	75	75
3	0	0	25	25	25	55	55	70	75	100	100
4	0	0	25	36	36	61	70	75	91	106	111

Step 1

When $i=1, w_1=3, P_1=30$

$$j=1 \quad V[1, 1] = V[0, 1] = 0$$

$$j=2 \quad V[1, 2] = \max\{V[0, 2]\} = 0$$

$$j=3 \quad V[1, 3] = \max\{V[0, 3], V[0, 0] + 30\} = 30$$

$$j=4 \quad V[1, 4] = \max\{V[0, 4], V[0, 1] + 30\} = 30$$

$$j=5 \quad V[1, 5] = \max\{V[0, 5], V[0, 2] + 30\} = 30$$

$$j=6 \quad V[1, 6] = \max\{V[0, 6], V[0, 3] + 30\} = 30$$

$$j=7 \quad V[1, 7] = \max\{V[0, 7], V[0, 4] + 30\} = 30$$

$$j=8 \quad V[1, 8] = \max\{V[0, 8], V[0, 5] + 30\} = 30$$

$$j=9 \quad V[1, 9] = \max\{V[0, 9], V[0, 6] + 30\} = 30$$

$$j=10 \quad V[1, 10] = \max\{V[0, 10], V[0, 7] + 30\} = 30$$

Step 2when $i=2, W_2=4, P_2=45$

$$j=1 \quad V[2,1] = V[1,1] = 0$$

$$j=2 \quad V[2,2] = V[1,2] = 0$$

$$j=3 \quad V[2,3] = V[1,3] = 30$$

$$j=4 \quad V[2,4] = \max\{V[1,4], V[1,0] + 45\} = 45$$

$$j=5 \quad V[2,5] = \max\{V[1,5], V[1,1] + 45\} = 45$$

$$j=6 \quad V[2,6] = \max\{V[1,6], V[1,2] + 45\} = 45$$

$$j=7 \quad V[2,7] = \max\{V[1,7], V[1,3] + 45\} = 75$$

$$j=8 \quad V[2,8] = \max\{V[1,8], V[1,4] + 45\} = 75$$

$$j=9 \quad V[2,9] = \max\{V[1,9], V[1,5] + 45\} = 75$$

$$j=10 \quad V[2,10] = \max\{V[1,10], V[1,6] + 45\} = 75$$

Step 3when $i=3, W_3=2, P_3=25$

$$j=1 \quad V[3,1] = V[2,1] = 0$$

$$j=2 \quad V[3,2] = \max\{V[2,2], V[2,0] + 25\} = 25$$

$$j=3 \quad V[3,3] = \max\{V[2,3], V[2,1] + 25\} = 25$$

$$j=4 \quad V[3,4] = \max\{V[2,4], V[2,2] + 25\} = 25$$

$$j=5 \quad V[3,5] = \max\{V[2,5], V[2,3] + 25\} = 25$$

$$j=6 \quad V[3,6] = \max\{V[2,6], V[2,4] + 25\} = 25$$

$$j=7 \quad V[3,7] = \max\{V[2,7], V[2,5] + 25\} = 95$$

$$j=8 \quad V[3,8] = \max\{V[2,8], V[2,6] + 25\} = 95$$

$$j=9 \quad V[3,9] = \max\{V[2,9], V[2,7] + 25\} = 25$$

$$j=10 \quad V[3,10] = \max\{V[2,10], V[2,8] + 25\} = 25$$

Step 4when $i=4, W_4=3, P_4=36$

$$j=1 \quad V[4,1] = V[3,1] = 0$$

$$V[4,2] = V[3,2] = 25$$

$$V[4,3] = \max\{V[3,3], V[3,0] + 36\} = 36$$

$$V[4,4] = \max\{V[3,4], V[3,1] + 36\} = 36$$

$$V[4,5] = \max[V[3,5], V[3,2] + 36] = 36$$

$$V[4,6] = \max[V[3,6], V[3,3] + 36] = 36$$

$$V[4,7] = \max[V[3,7], V[3,4] + 36] = 36$$

$$V[4,8] = \max[V[3,8], V[3,5] + 36] = 36$$

$$V[4,9] = \max[V[3,9], V[3,6] + 36] = 36$$

$$V[4,10] = \max[V[3,10], V[3,6] + 36] = 36$$

Optimal solⁿ is $V[n, m] = V[4, 10]$

If i th object has selected then $V[i, j] \neq V[i-1, j]$
 • 4th object is has been selected then $V[4, j] \neq$
 as maximum profit.

• So $111 - \text{profit} = 111 - 36 = 75$

So $V[3, 7] = V[2, 7] = 75$

So 3rd obj is not selected.

$V[2, 7] \neq V[1, 7]$

$75 \neq 30$

So 2nd obj is selected

• So $75 - P_2 = 75 - 45 = 30$

$V[1, 3] \neq V[0, 3]$

$30 \neq 0$

So 1st obj is selected

$$\begin{matrix} x_1 & x_2 & x_3 & x_4 \\ \uparrow & 1 & 0 & 1 \end{matrix}$$