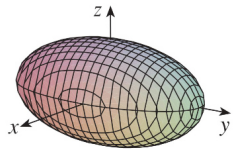
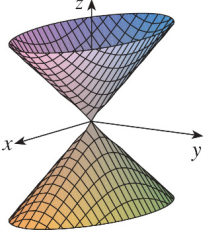
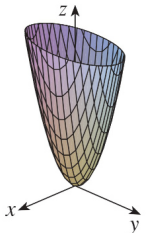
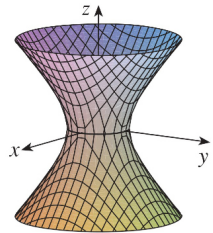
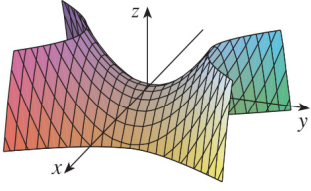
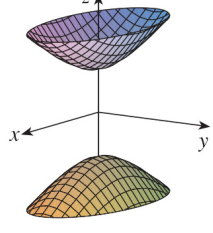


## 12-6: Cylinders and Quadric Surfaces

**TABLE 1** Graphs of quadric surfaces

Surface	Equation	Surface	Equation
<b>Ellipsoid</b> 	$\frac{x^2}{a^2} + \frac{y^2}{b^2} + \frac{z^2}{c^2} = 1$ <p>All traces are ellipses. If <math>a = b = c</math>, the ellipsoid is a sphere.</p>	<b>Cone</b> 	$\frac{z^2}{c^2} = \frac{x^2}{a^2} + \frac{y^2}{b^2}$ <p>Horizontal traces are ellipses. Vertical traces in the planes <math>x = k</math> and <math>y = k</math> are hyperbolas if <math>k \neq 0</math> but are pairs of lines if <math>k = 0</math>.</p>
<b>Elliptic Paraboloid</b> 	$\frac{z}{c} = \frac{x^2}{a^2} + \frac{y^2}{b^2}$ <p>Horizontal traces are ellipses. Vertical traces are parabolas. The variable raised to the first power indicates the axis of the paraboloid.</p>	<b>Hyperboloid of One Sheet</b> 	$\frac{x^2}{a^2} + \frac{y^2}{b^2} - \frac{z^2}{c^2} = 1$ <p>Horizontal traces are ellipses. Vertical traces are hyperbolas. The axis of symmetry corresponds to the variable whose coefficient is negative.</p>
<b>Hyperbolic Paraboloid</b> 	$\frac{z}{c} = \frac{x^2}{a^2} - \frac{y^2}{b^2}$ <p>Horizontal traces are hyperbolas. Vertical traces are parabolas. The case where <math>c &lt; 0</math> is illustrated.</p>	<b>Hyperboloid of Two Sheets</b> 	$-\frac{x^2}{a^2} - \frac{y^2}{b^2} + \frac{z^2}{c^2} = 1$ <p>Horizontal traces in <math>z = k</math> are ellipses if <math>k &gt; c</math> or <math>k &lt; -c</math>. Vertical traces are hyperbolas. The two minus signs indicate two sheets.</p>

From Stewart's Calculus 7E

- Classify each curve as a: Cylinder, Ellipsoid, Elliptical Paraboloid, Elliptical Cone, Hyperboloid of one sheet, Hyperboloid of two sheets, or a Hyperbolic paraboloid.

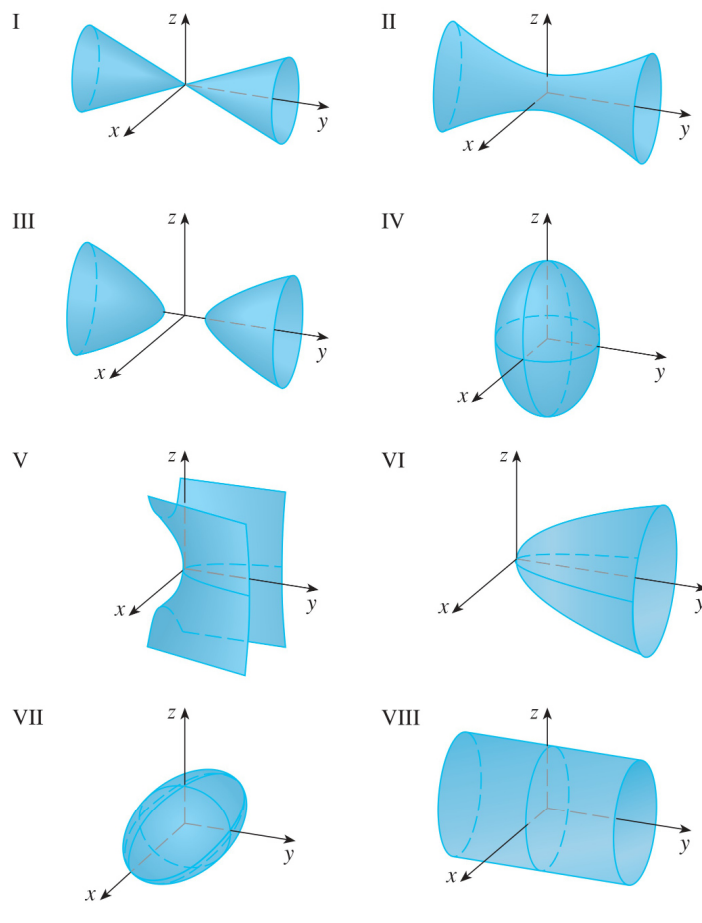
Draw a sketch demonstrating how each surface is oriented in 3-space.

(a)  $x = y^2 + 4z^2$

(b)  $x^2 = y^2 + 4z^2$

(c)  $9x^2 - y^2 + z^2 = 0$

(d)  $-x^2 + y^2 - z^2 = 1$



*From Stewart's Calculus 7e*

2. Identify the shapes above with the equation that represents them.

(a)  $x^2 + 4y^2 + 9z^2 = 1$

(e)  $y = 2x^2 + z^2$

(b)  $9x^2 + 4y^2 + z^2 = 1$

(f)  $y^2 = x^2 + 2z^2$

(c)  $x^2 - y^2 + z^2 = 1$

(g)  $x^2 + 2z^2 = 1$

(d)  $-x^2 + y^2 - z^2 = 1$

(h)  $y = x^2 - z^2$