Code summary (Eng): models and PEVD

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1 IMPORTING DATA

```
# load("import_data.RData")
#
# load("~/UPORABNA STATISTIKA/Spatial Modelling/SM/SlovenianCattleAnalysis/SlovenianCattleAnalysis/Proc
load("workspaces/import_data.RData")
load("workspaces/model_comparison.RData")
```

- phenoData = original dataset, 30314x30, data on Brown-Swiss cattle from Slovenia (years 2004-2019 from 2012 different herds)
- Ainv = inverse of the relationship matrix (56465x56465)

- boundaryOB = map of municipalities (sf data.frame class)
- boundary UE = map of administrative units (sf data.frame class)
- mapOB = map of municipalities (SpatialPolygonsDataFrame class)
- mapUE = map of administrative units (SpatialPolygonsDataFrame class)
- sloveniaBoundary = map of Slovenia

```
# importing results
# load("workspaces/full_models.RData")
# load("workspaces/Eucl_models.RData")
# load("workspaces/spde_big.RData")
# load("workspaces/spde_small.RData")
# load("workspaces/UE_models.RData")
# load("workspaces/mc_samples.RData")
# load("workspaces/small_models_with_MC.RData")
# Eucl_dist <- read.table("workspaces/Euclidean_dist_small.txt", sep=" ")
# Eucl_dist <- data.matrix(Eucl_dist)</pre>
```

2 MODEL DESCRIPTION

We analysed a physical trait describing a body confirmation measure as a response variable (last004_scaled). In all models we included 3 fixed effects: year and scorer of the data (vpliv1), cattle age and stage of lactation (vpliv2) and year and month of calving (vpliv3). We included 3 fixed effects: genetic/pedigree effect (G), herd effect (H) and herd location effect (S) in different combinations (see below):

```
G: y_i = x_i \beta + a_i + e_i;

GH: y_i = x_i \beta + a_i + h_i + e_i;

GS: y_i = x_i \beta + a_i + s_i + e_i;

GHS: y_i = x_i \beta + a_i + h_i + s_i + e_i
```

- β = vector of fixed covariate effects, x_i = covariate vector
- a_i = additive genetic effects (breeding value); modelled using pedigree relationship matrix A
- $h_i = \text{herd effect}$; modelled using herd ids
- s_i = spatial effect; modelled in 3 different ways
- $e_i = \text{residual effect}$

2.1 SPATIAL EFFECT MODELLING

- BESAG/CAR (regional model)
- using Euclidean distances covariance matrix (geostatistical model)
- SPDE (geostatical model)

BESAG/CAR and model based on Euclidean distances were fitted in INLA-R and BLUPF90. SPDE model was fitted in INLA-R.

3 HYPOTHESES

- Accounting for spatial relationships can improve genetic evaluation [low genetic connectedness between small herds, relatively high environmental variation setting]
- Accounting for spatial relationships can improve genetic connectedness between animals

4 DATA PREPARATION

4.1 REGIONAL NEIGBORHOOD MATRIX (accounting for neighborhood structure in BESAG/CAR model)

Neighborhood matrix can be constructed using 'inla.read.graph' function. Construsted graph contains information on number and ids of neighbouring regions for every region. Then, the region id (UE_MID and OB_MID) in the phenoData dataset is merged with the consecutive id number of the region (1 to number of regions).

```
# administrative units
nb.mapUE <- poly2nb(mapUE) #class nb</pre>
nb2INLA("map.graphUE",nb.mapUE)
gUE <- inla.read.graph(filename = "map.graphUE")</pre>
#obcine
nb.mapOB <- poly2nb(mapOB)</pre>
nb2INLA("map.graphOB",nb.mapOB)
gOB <- inla.read.graph(filename = "map.graphOB")</pre>
# assinging a sequence number to regional id
grafID_UE <- data.frame("UE" = mapUE[,"UE_MID"], "idUE" = mapUE[,"UE_ID"])</pre>
names(grafID_UE) <- c("UE", "idUE")</pre>
grafID_0B <- data.frame("OB" = mapOB[,"OB_MID"], "idOB" = mapOB[,"OB_ID"])</pre>
names(grafID OB) <- c("OB", "idOB")</pre>
phenoData <- as.data.frame(merge(phenoData, grafID_UE, all.x=T))</pre>
## Warning in '[<-.factor'('*tmp*', ri, value = c(10051851L, 10051860L,
## 10051878L, : invalid factor level, NA generated
phenoData <- as.data.frame(merge(phenoData, grafID_OB, all.x=T))</pre>
## Warning in '[<-.factor'('*tmp*', ri, value = c(11026923L, 11027776L,
## 11027997L, : invalid factor level, NA generated
```

4.2 DEFINING PRIORS

```
# priors
hyperVarPed = list(theta = list(prior="pc.prec", param=c(0.1,0.5)))
hyperVarIdlok.GH = list(theta = list(prior="pc.prec", param=c(0.25,0.5)))
hyperVarIdlok.GHS = list(theta = list(prior="pc.prec", param=c(0.15,0.5)))
hyperResVarG = list(theta = list(prior="pc.prec", param=c(0.3,0.5)))
hyperResVarGHS = list(theta = list(prior="pc.prec", param=c(0.15,0.5)))
```

4.3 PREPARING SUBSET OF DATA

```
• n = 3800
```

• sampling 3800 individuals without replacement, with sampling probability equal to the inverse herd size

```
# podset podatkov
herd_n <- data.frame(table(phenoData$idlok))
colnames(herd_n) <- c("idlok", "herd_n")
phenoData <- merge(phenoData, herd_n, all.x=T)
set.seed(85940)
phenoData.small <- phenoData[sample(1:nrow(phenoData), size = 3800, replace = FALSE, prob = 1/phenoData
phenoData.small <- drop.levels(phenoData.small)</pre>
```

4.4 SPDE MODEL PREPARATION (STACK) (Maria)

Full data.

```
# Prior values
hyperRange = c(50, 0.8)# <
hyperVarSpdeS = c(1, 0.05) \# >
hyperVarSpdeHS = c(0.6, 0.05) # >
hyperVarPed = list(theta = list(prior="pc.prec", param=c(0.4,0.05)))
hyperVarIdlokH = list(theta = list(prior="pc.prec", param=c(1,0.05)))
hyperVarIdlokHS = list(theta = list(prior="pc.prec", param=c(0.6,0.05)))
hyperResVarG = list(theta = list(prior="pc.prec", param=c(1,0.1)))
hyperResVarRest = list(theta = list(prior="pc.prec", param=c(0.6,0.05)))
# Use model matrix to fit factor effects
M = model.matrix(~1 + vpliv1 + vpliv2 + vpliv3, phenoData)
# Store in a stack
FactorNames = tail(colnames(M), ncol(M)-1)
FactorStack = pasteO( "list(", FactorNames, " = M[,", 2:(ncol(M)), "]),", collapse = "" )
FactorStack = ( gsub('.{1}$', '', FactorStack ) )
FactorStack= paste0("c(", FactorStack, ")")
# Make the formula
FormulaStack = paste("+", FactorNames, collapse = " ")
formulaS.1 = 'last004scaled ~ intercept + f(rowNumberAinv, model = "generic0", Cmatrix = Ainv, hyper = h
formulaHS.1 = 'last004scaled ~intercept + f(rowNumberAinv, model = "generic0", Cmatrix = Ainv, hyper = h
formulaS = as.formula( pasteO(formulaS.1, FormulaStack))
formulaHS = as.formula( pasteO(formulaHS.1, FormulaStack))
# Make mesh and SPDE
mesh = inla.mesh.2d(cbind(phenoData$xpos, phenoData$ypos), max.edge=c(10, 20), cutoff = 2.5, offset = 3
A = inla.spde.make.A(mesh = mesh, loc = cbind(phenoData$xpos, phenoData$ypos) )
spdeStatS = inla.spde2.pcmatern(mesh = mesh, alpha = 2 , prior.range = hyperRange, prior.sigma = hyper
meshIndexS = inla.spde.make.index(name = "fieldID", n.spde = spdeStatS$n.spde)
spdeStatHS = inla.spde2.pcmatern(mesh = mesh, alpha = 2 , prior.range = hyperRange, prior.sigma = hyper
meshIndexHS = inla.spde.make.index(name = "fieldID", n.spde = spdeStatHS$n.spde)
```

Data subset.

```
# Use model matrix to fit factor effects
M.small = model.matrix(~1 + vpliv1 + vpliv2 + vpliv3, phenoData.small)
# Store in a stack
FactorNames.small = tail(colnames(M.small), ncol(M.small)-1)
FactorStack.small = paste0( "list(", FactorNames.small, " = M.small[,", 2:(ncol(M.small)), "]),", colla
FactorStack.small = ( gsub('.{1}$', '', FactorStack.small ) )
FactorStack.small= pasteO("c(", FactorStack.small, ")")
# Make the formula
FormulaStack.small = paste("+", FactorNames.small, collapse = " ")
formulaS.1.small = 'last004scaled ~ intercept + f(rowNumberAinv, model = "generic0", Cmatrix = Ainv,hyp
formulaHS.1.small = 'last004scaled ~intercept + f(rowNumberAinv, model = "generic0", Cmatrix = Ainv,hyp
formulaS.small = as.formula( paste0(formulaS.1.small, FormulaStack.small))
formulaHS.small = as.formula( pasteO(formulaHS.1.small, FormulaStack.small))
# Make mesh and SPDE
mesh.small = inla.mesh.2d(cbind(phenoData.small$xpos, phenoData.small$ypos), max.edge=c(10, 20), cutoff
A.small = inla.spde.make.A(mesh = mesh.small, loc = cbind(phenoData.small$xpos, phenoData.small$ypos) )
spdeStatS.small = inla.spde2.pcmatern(mesh = mesh.small, alpha = 2 , prior.range = hyperRange, prior.s
meshIndexS.small = inla.spde.make.index(name = "fieldID", n.spde = spdeStatS.small$n.spde)
spdeStatHS.small = inla.spde2.pcmatern(mesh = mesh.small, alpha = 2 , prior.range = hyperRange, prior.
meshIndexHS.small = inla.spde.make.index(name = "fieldID", n.spde = spdeStatHS.small$n.spde)
# Make stack
stack.small = inla.stack(data = list(last004scaled = phenoData.small$last004scaled),
                   A = list(A.small, 1, 1),
                   effects = list(c(meshIndexS.small, list(intercept = 1)),
                                  c(list(rowNumberAinv = phenoData.small$rowNumberAinv),list(idlok = ph
                                  c(eval(parse(text = FactorStack.small ) ) )), tag = "est")
stackHS.small = inla.stack(data = list(last004scaled = phenoData.small$last004scaled),
                     A = list(A.small, 1, 1),
                     effects = list(c(meshIndexHS.small, list(intercept = 1)),
                                    c(list(rowNumberAinv = phenoData.small$rowNumberAinv),list(idlok = )
                                    c(eval(parse(text = FactorStack.small ) ) ) ), tag = "est")
```

4.5 SET MODEL FORMULAS

Full dataset models.

```
# G MODEL (G)

formulaB.G = last004scaled ~ 1 + vpliv1 + vpliv2 + vpliv3 + f(rowNumberAinv, model = "generic0", Cmat.

# H MODEL (G + H: herd effect)

formulaB.H = last004scaled ~ 1 + vpliv1 + vpliv2 + vpliv3 + f(rowNumberAinv, model = "generic0", Cmat.

# S MODEL (G + field (regional effect)) BESAG

# UE = administrative regions

# OB = municipalities

formulaB.S.UE = last004scaled ~ 1 + vpliv1 + vpliv2 + vpliv3 + f(rowNumberAinv, model = "generic0", CformulaB.S.OB = last004scaled ~ 1 + vpliv1 + vpliv2 + vpliv3 + f(rowNumberAinv, model = "generic0", CformulaB.HS.UE <- last004scaled ~ 1 + vpliv1 + vpliv2 + vpliv3 + f(rowNumberAinv, model = "generic0", CformulaB.HS.UE <- last004scaled ~ 1 + vpliv1 + vpliv2 + vpliv3 + f(rowNumberAinv, model = "generic0", CformulaB.HS.OB <- last004scaled ~ 1 + vpliv1 + vpliv2 + vpliv3 + f(rowNumberAinv, model = "generic0", CformulaB.S.Eucl = last004scaled ~ 1 + vpliv1 + vpliv2 + vpliv3 + f(rowNumberAinv, model = "generic0", CformulaB.HS.Eucl <- last004scaled ~ 1 + vpliv1 + vpliv2 + vpliv3 + f(rowNumberAinv, model = "generic0", formulaB.HS.Eucl <- last004scaled ~ 1 + vpliv1 + vpliv2 + vpliv3 + f(rowNumberAinv, model = "generic0", formulaB.HS.Eucl <- last004scaled ~ 1 + vpliv1 + vpliv2 + vpliv3 + f(rowNumberAinv, model = "generic0", formulaB.HS.Eucl <- last004scaled ~ 1 + vpliv1 + vpliv2 + vpliv3 + f(rowNumberAinv, model = "generic0", formulaB.HS.Eucl <- last004scaled ~ 1 + vpliv1 + vpliv2 + vpliv3 + f(rowNumberAinv, model = "generic0", formulaB.HS.Eucl <- last004scaled ~ 1 + vpliv1 + vpliv2 + vpliv3 + f(rowNumberAinv, model = "generic0", formulaB.HS.Eucl <- last004scaled ~ 1 + vpliv1 + vpliv2 + vpliv3 + f(rowNumberAinv, model = "generic0", formulaB.HS.Eucl <- last004scaled ~ 1 + vpliv1 + vpliv2 + vpliv3 + f(rowNumberAinv, model = "generic0", formulaB.HS.Eucl <- last004scaled ~ 1 + vpliv1 + vpliv2 + vpliv3 + f(rowNumberAinv, model = "generic0", formulaB.HS.Eucl <- last004scaled ~ 1 + vpliv1 + vpliv2 + vpliv3 + f(rowNumberAinv, model = "generic0", formulaB.HS.Eucl <- last004scaled ~
```

Data subset models.

```
# Euclidean
formulaB.S.Eucl.small = last004scaled ~ 1 + vpliv1 + vpliv2 + vpliv3 + f(rowNumberAinv, model = "gener
formulaB.HS.Eucl.small <- last004scaled ~ 1 + vpliv1 + vpliv2 + vpliv3 + f(rowNumberAinv, model = "generation")</pre>
```

5 FIT MODELS

Full dataset.

```
model.G <- inla(formulaB.G, family = "gaussian", data = phenoData, control.compute = list(dic=T,cpo=F,</pre>
model.H <- inla(formulaB.H, family = "gaussian", data = phenoData, control.compute = list(dic=T,cpo=F,</pre>
model.besag.S.UE <- inla(formulaB.S.UE, family = "gaussian", data = phenoData, control.compute = list(
model.besag.S.OB <- inla(formulaB.S.OB, family = "gaussian", data = phenoData, control.compute = list(
model.besag.HS.UE <- inla(formulaB.HS.UE, family = "gaussian", data = phenoData, control.compute = lis
model.besag.HS.OB <- inla(formulaB.HS.OB, family = "gaussian", data = phenoData, control.compute = lis
# Euclidean
model.Eucl.S <- inla(formulaB.S.Eucl, family = "gaussian", data = phenoData, control.compute = list(di
model.Eucl.HS <- inla(formulaB.HS.Eucl, family = "gaussian", data = phenoData, control.compute = list(
# SPDE
model.SPDE.S = inla(formula = formulaS, data = inla.stack.data(stack),
            family = "normal", control.predictor =list(A=inla.stack.A(stack),compute = T),
            control.family=list(list(hyper=hyperResVarRest)),
            control.compute = list(dic=T,cpo=F), verbose=T)
model.SPDE.HS = inla(formula = formulaHS, data = inla.stack.data(stackHS),
             family = "normal", control.predictor =list(A=inla.stack.A(stackHS),compute = T),
             control.family=list(list(hyper=hyperResVarRest)),
             control.compute = list(dic=T,cpo=F), verbose=T)
```

Data subset model fitting.

```
model.G.small <- inla(formulaB.G.small, family = "gaussian", data = phenoData.small, control.compute =</pre>
model.H.small <- inla(formulaB.H.small, family = "gaussian", data = phenoData.small, control.compute =</pre>
model.besag.S.UE.small <- inla(formulaB.S.UE.small, family = "gaussian", data = phenoData.small, contr
model.besag.S.OB.small <- inla(formulaB.S.OB.small, family = "gaussian", data = phenoData.small, contr</pre>
model.besag.HS.UE.small <- inla(formulaB.HS.UE.small, family = "gaussian", data = phenoData.small, con model.besag.HS.OB.small <- inla(formulaB.HS.OB.small, family = "gaussian", data = phenoData.small, con
# Euclidean
model.Eucl.S.small <- inla(formulaB.S.Eucl.small, family = "gaussian", data = phenoData.small, control
model.Eucl.HS.small <- inla(formulaB.HS.Eucl.small, family = "gaussian", data = phenoData.small, contr
model.SPDE.S.small = inla(formula = formulaS.small, data = inla.stack.data(stack.small),
             family = "normal", control.predictor =list(A=inla.stack.A.small(stack.small),compute = T),
             control.family=list(list(hyper=hyperResVarRest)),
             control.compute = list(dic=T,cpo=F, config=T), verbose=T)
model.SPDE.HS.small = inla(formula = formulaHS.small, data = inla.stack.data(stackHS.small),
              family = "normal", control.predictor =list(A=inla.stack.A.small(stackHS.small),compute = T
              control.family=list(list(hyper=hyperResVarRest)),
              control.compute = list(dic=T,cpo=F, config=T), verbose=T)
```

6 MODEL COMPARISON (VARIANCE COMPONENTS, DIC VALUES)

Full data.

```
G <- c(round(1/model.G$summary.hyperpar[2,1],2), "/", "ound(1/model.G$summary.hyperpar[1,1],2), round(1/model.H$summary.hyperpar[2,1],2), round(1/model.H$summary.hyperpar[3,1],2), "/", round(GS.besag.OB <- c(round(1/model.besag.S.OB$summary.hyperpar[2,1],2), "/", round(1/model.besag.S.OB$summary.hyperpar[2,1],2), "/", round(1/model.besag.S.UE$summary.hyperpar[2,1],2), "ound(1/model.besag.S.UE$summary.GHS.besag.OB <- c(round(1/model.besag.HS.OB$summary.hyperpar[2,1],2), round(1/model.besag.HS.OB$summary.GHS.besag.UE <- c(round(1/model.besag.HS.UE$summary.hyperpar[2,1],2), round(1/model.besag.HS.UE$summary.ghyperpar[2,1],2), round(1/model.besag.HS.UE$summary.hyperpar[2,1],2), round(1/model.Eucl.S$summary.hyperpar[2,1],2), "/", round(1/model.Eucl.HS$summary.hyperpar[2,1],2), round(1/model.Eucl.HS$summary.hyperpar[2,1],2), round(1/model.Eucl.HS$summary.hyperpar[2,1],2), round(1/model.SPDE.S$summary.hyperpar[2,1],2), "/", round(model.SPDE.HS$summary.hyperpar[2,1],2), "/", round(model.SPDE.HS$summary.hyperpar[3,1],2), "/", round(model.SPDE.HS$summary.hyperpar[3,1],2), round(1/model.SPDE.HS$summary.hyperpar[3,1],2), round(1
```

Small data.

kable_styling("striped",full_width = F, font_size=15)

Table 1: Variance components for random effects

	G	GH	GS.besag.OB	GS.besag.UE	GHS.besag.OB	GHS.besag
genetic effect	0.77	0.2	0.69	0.72	0.19	0.2
herd effect	/	0.27	/	/	0.24	0.25
spatial effect	/	/	0.37	0.15	0.13	0.13
residual	0.31	0.49	0.35	0.32	0.49	0.49
DIC	67307	70939	68092	68000	71048	70902

```
# rm(list=ls())
# load("workspaces/import_data.RData")
# load("workspaces/spde_small.RData")
# load("workspaces/Eucl_models.RData")
# load("workspaces/UE_models.RData")
G.small <- c(round(1/model.G.small$summary.hyperpar[2,1],2), "/", "/", round(1/model.G.small$summary.hy
GH.small <- c(round(1/model.H.small$summary.hyperpar[2,1],2), round(1/model.H.small$summary.hyperpar[3,
GS.besag.OB.small <- c(round(1/model.besag.S.OB.small$summary.hyperpar[2,1],2), "/", round(1/model.besa
GS.besag.UE.small <- c(round(1/model.besag.S.UE.small$summary.hyperpar[2,1],2), "/", round(1/model.besa
GHS.besag.OB.small <- c(round(1/model.besag.HS.OB.small$summary.hyperpar[2,1],2), round(1/model.besag.H
GHS.besag.UE.small <- c(round(1/model.besag.HS.UE.small$summary.hyperpar[2,1],2), round(1/model.besag.H
GS.Eucl.small <- c(round(1/model.Eucl.S.small$summary.hyperpar[2,1],2), "/", round(1/model.Eucl.S.small
GHS.Eucl.small <- c(round(1/model.Eucl.HS.small$summary.hyperpar[2,1],2), round(1/model.Eucl.HS.small$s
GS.SPDE.small <- c(round(1/model.SPDE.S.small$summary.hyperpar[2,1],2), "/", paste(round(model.SPDE.S.small$summary.hyperpar[2,1],2), "/", paste(round(model.SPDE.SSmall$summary.hyperpar[2,1],2), "/", paste(round(model.SPDE.SSmall$summary.hyperpar[2,1],2), "/", paste(round(model.SPDE.SSmall$summary.hyperpar[2,
GHS.SPDE.small <- c(round(1/model.SPDE.HS.small$summary.hyperpar[2,1],2), round(1/model.SPDE.HS.small$s
Modeli <- cbind(G.small, GH.small, GS.besag.OB.small, GS.besag.UE.small, GHS.besag.OB.small, GHS.besag.
rownames(Modeli) <- c("genetic effect", "herd effect", "spatial effect", "residual", "DIC")</pre>
kable(Modeli,caption = "Variance components for random effects (small models)") %>%
    kable_styling("striped",full_width = F, font_size=15)
```

7 INLA POSTERIOR SAMPLING

Table 2: Variance components for random effects (small models)

	G.small	GH.small	GS.besag.OB.small	GS.besag.UE.small	GHS.besag
genetic effect	0.34	0.16	0.33	0.28	0.16
herd effect	/	0.26	/	/	0.23
spatial effect	/		0.06	0.14	0.06
residual	0.63	0.51	0.6	0.67	0.51
DIC	10205	9735	10112	10296	9717

```
# import Euclidean distance matrix
# import posterior samplings
load("workspaces/mc_samples.RData")
load("workspaces/Euclidean_dist_small.RData")
# xxG, xxH, xxS, xxHS, xxS.spde, xxHS.spde
pipeline_conn_1 <- function(nEff=56465, nSample=100, samples_model, data=phenoData.small, nameEff="Geff"
effects_sample <- matrix(NA, nrow=nEff, ncol=nSample)</pre>
nEff_full <- length(samples_model[[1]]$latent)</pre>
for(i in 1:nSample){
  effects_sample_full <- samples_model[[i]]$latent[1:nEff_full,]</pre>
  effects_sample[,i] <- effects_sample_full[grepl("^rowNumber", names(effects_sample_full))]</pre>
df_Row_eff <- data.frame("rowNumberAinv" = 1:nEff, nameEff = effects_sample)</pre>
rowNumber <- data.frame("rowNumberAinv" = data$rowNumberAinv)</pre>
df_Row_eff <- as.data.frame(merge(rowNumber, df_Row_eff, all.x=T))</pre>
row.names(df_Row_eff) <- df_Row_eff$rowNumberAinv</pre>
df_Row_eff$rowNumberAinv <- NULL</pre>
df_Row_eff <- data.matrix(df_Row_eff)</pre>
df_Row_eff
}
sampled.G.gen.small <- pipeline_conn_1(samples_model=sampled.G.small)</pre>
sampled.HS.SPDE.gen.small <- pipeline_conn_1(samples_model=sampled.HS.SPDE.small)</pre>
RowVar <- function(x, ...) {</pre>
  rowSums((x - rowMeans(x, ...))^2, ...)/(dim(x)[2] - 1)
}
variance_animal.G <- RowVar(sampled.G.gen.small)</pre>
variance_animal.HS.SPDE <- RowVar(sampled.HS.SPDE.gen.small)</pre>
pipeline_PEVD <- function(var_animal, samples){</pre>
  sum_var = outer(var_animal, -var_animal, '-')
  varcovM <- cov(t(samples), t(samples))</pre>
  pevd <- sum_var - varcovM</pre>
```

```
pevd[lower.tri(pevd,diag=TRUE)] <- NA</pre>
  pevd_num <- as.vector(pevd)</pre>
  pevd_num <- pevd_num[!is.na(pevd_num)]</pre>
  pevd_num
pevd.G.small <- pipeline_PEVD(var_animal=variance_animal.G, samples=sampled.G.gen.small)</pre>
pevd.HS.SPDE.small <- pipeline_PEVD(var_animal=variance_animal.HS.SPDE, samples=sampled.HS.SPDE.gen.sma
pipeline_Eucl <- function(dist){</pre>
  dist[lower.tri(dist,diag=TRUE)] <- NA</pre>
  Eucl_dist_num <- as.vector(dist)</pre>
  Eucl_dist_num <- Eucl_dist_num[!is.na(Eucl_dist_num)]</pre>
  Eucl_dist_num
pevd.Eucl.small <- pipeline_Eucl(dist=paired.distances)</pre>
cor(pevd.Eucl.small, pevd.G.small)
## [1] -0.00334999
cor(pevd.Eucl.small, pevd.HS.SPDE.small)
## [1] 0.004101414
cor(pevd.G.small, pevd.HS.SPDE.small)
```

[1] 0.3556385