

**LATEX HOMEWORK 9TH GRADE**  
**UNIT 1 - METHODS OF PROOF - FORMAL STYLE OF A PROOF**  
**WEEK 2 - STRUCTURE AND STYLE OF PROOF**

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1

Explain what is wrong with the following proof:

Theorem:  $2 = 1$

Proof: Let  $a = b$ . Then  $a^2 = ab$  so  $a^2 - b^2 = ab - b^2$  which we can factor as  $(a - b)(a + b) = (a - b)b$ . Canceling gives  $a + b = b$  and since  $a = b$  we get  $b + b = b$ . Dividing both sides by  $b$  gives  $2 = 1$ .

If  $a = b$ , then  $(a - b)$

2

Prove that for any natural numbers  $a, b$ , there exists an  $n$  with  $an + b$  composite.

*Proof.* Theorem:  $\forall a, b \in \mathbb{N}$ , there exists an  $n$  with  $an + b$  composite. Proof:

□

3

For each of the following, give an example and a counterexample:

- $n! - 1$  is prime for  $n \geq 3$
- Any 3 distinct lines separate the plane into seven regions. What additional assumptions are needed in order for this to be a true statement?
- If a rational function is bounded, then it is constant.