LATEX HOMEWORK 9TH GRADE
UNIT 1 - METHODS OF PROOF - FORMAL STYLE OF A PROOF
WEEK 2 - STRUCTURE AND STYLE OF PROOF

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1

Explain what is wrong with the following proof:
Theorem: $2 = 1$
Proof: Let $a = b$. Then $a^2 = ab$ so $a^2 - b^2 = ab - b^2$ which we can factor as $(a - b)(a + b) = (a - b)b$. Canceling gives $a + b = b$ and since $a = b$ we get $b + b = b$. Dividing both sides by b gives $2 = 1$.

List of potential issues:

- What is being canceled is not stated
- a and b are not defined
- They never state why $a^2 = ab$ is necessary

2

Prove that for any natural numbers a, b, there exists an n with $an + b$ composite.

Proof. Theorem: $\forall a, b \in \mathbb{N}$, there exists an n with $an + b$ composite. Proof: □

3

For each of the following, give an example and a counterexample:

- $n! - 1$ is prime for $n \geq 3$
- Any 3 distinct lines separate the plane into seven regions. What additional assumptions are needed in order for this to be a true statement?
- If a rational function is bounded, then it is constant.

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