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CS350 - HW1

1. System consists of CPU, Disk, and Network Interface

Usage of each resource for Processing a request
s:

1. CPU: 2 ms
2. Disk: 6 ms
3. CPU: 1 ms
4. Network Interface: 4 ms
5. CPU: 2 ms

Assume a 1 represents the resource is active and a
n empty cell is idle and each part of the graph re
presents 1 ms

CPU					1	1							
1					1	1							
Disk							1	1	1	1	1	1	1
Network Interface													
	1	1	1	1									

$$\begin{aligned} \text{total running time} &= 2 \text{ ms} + 6 \text{ ms} + 1 \text{ ms} + 4 \text{ ms} \\ &+ 2 \text{ ms} = 15 \text{ ms} \end{aligned}$$

a. Utilization = $1 - (\text{Idle time} / \text{total running time})$

CPU Utilization:

CPU Idle time = 6 ms + 4 ms = 10 ms

$$U = 1 - (10 \text{ ms} / 15 \text{ ms})$$

$$U = (5 \text{ ms} / 15 \text{ ms})$$

$U = 0.33 = 33\%$ CPU Utilization

Disk Utilization:

$$\text{Disk Idle time} = 2 \text{ ms} + 1 \text{ ms} + 4 \text{ ms} + 2 \text{ ms} = 9 \text{ ms}$$

$$U = 1 - (9 \text{ ms} / 15 \text{ ms})$$

$$U = (6 \text{ ms} / 15 \text{ ms})$$

$U = 0.40 = 40\%$ CPU Utilization

Network Interface Utilization:

Network Interface Idle time = 2 ms + 6 ms + 1 ms + 2 ms = 11 ms

$$U = 1 - (11 \text{ ms} / 15 \text{ ms})$$

$$U = (4 \text{ ms} / 15 \text{ ms})$$

$$U = .27 = 27 \% \text{ CPU Utilization}$$

b. Throughput = (number of requests serviced by the system) / total running time

Throughput of server:

number of requests serviced by system = 1 request

$$\text{Throughput of server} = 1 \text{ request} / 15 \text{ ms}$$

$$\text{Throughput of server} = 0.7 \text{ requests} / \text{ms}$$

If MPL = 2, there can be 2 requests that are concurrently serviced

Given Assumptions:

There will always be pending HTTP requests

The system has reached a stable and reliable state

Usage of CPU, Disk, and Network Interface if MPL = 2

Assume A and B represent two different requests and each part of the graph represents 1 ms

c. Utilizations if N = 2

1 cycle can be seen in the period from t=9ms to t=25ms, thus the length of the cycle is 16ms.

t = 0ms	1	2	3	4	5	6	7
8	9	10	11	12	13	14	15
	19	20	21	22	23	24	25
	29	30	31	32	33	34	35
CPU	A				A	A	B
	A				A	A	B
		A	B	B	B	B	A
		A	A	B	A	A	A
Disk							

A	B	B	B	B	B	B				
	A	A	A	A	A	A	B	B	B	B
	B	B								
	Network Interface									
		A	A	A	A				B	B
	B	B						A	A	A
	A				B	B	B	B		

Utilizations:

CPU Utilization = 10 ms active time/16 ms total time per cycle = $10/16 = 62.5\%$

Disk Utilization = 12 ms active time/16 ms total time per cycle = $12/16 = 75\%$

Network Interface Utilization = 8 ms active time/16 ms total time per cycle = $8/16 = 50\%$

d. Throughput of server: 2 requests per 16 ms per cycle

Throughput = 2 requests/16ms per cycle = 0.125 requests per ms

e. If we can set N to any value, the disk utilization can be 100%, thus the maximum throughput of the web server can be represented as $(1/8) * (4/3) = 1/6$

f. No. The limit to the capacity of this system (the bottleneck) is the disk since it takes 6 ms to fetch the file per request, which is necessary for performing any operation after it under my assumptions. Thus, the slow fetching causes the disk to be the bottleneck resource, not the CPU.

g. Minimum speedup for each device

CPU = $5/4 = 1.25$

Disk = $6/4 = 1.5$

h. Resulting capacity

Minimum speedup is $16/13 = 1.23$

$(1/8) * (16/13) = 0.153$ requests/ms

2. Big data

8 hours to run, 20% time on int operations, 35% time in I/O

Option 1: \$1000

reduce the time of integer operations by 25%

Option 2: \$4000

faster I/O devices to reduce latency from 6 us to 5 us ($1 - 5/6 = 0.17 = 17\%$ reduction in time)

Amdahl's law

$y = 1 / ((1 - f)(1 - (1/x)))$ where y is overall performance/speedup, f is the fraction of time a resource is used in serving requests, and x is the performance of that resource x -fold (making the resource x -times faster)

a. Improving int operations

$$f = 20\%, x = 1 / (1 - 25\%) = 1.33$$

$$y = 1 / ((1 - 0.2)(1 - (1/1.33)))$$

$$y = 1.052$$

b. Improving I/O

$$f = 35\%, x = 1 / (1 - 17\%) = 1.20$$

$$y = 1 / ((1 - 0.35)(1 - (1/1.20)))$$

$$y = 1.062$$

c. Cost effectiveness?

Int operations:

$$1.052 \text{ speedup} / \$1000 = 0.001052 \text{ speedup}/\$$$

I/O:

$$1.062 \text{ speedup} / \$4000 = 0.000266 \text{ speedup}/\$$$

On a per dollar basis, improving the int operations would be more cost effective.

d. Both improvements:

$$1 / ((1/5) * (3/4) + 0.35 * 5/6 + 0.45) = 1.121$$

e. Theoretical limit for processor speedup

$$1 / (4/5) = 5/4 = 1.25$$

f. Theoretical limit for I/O speedup
 $1/(1-0.35) = 1.54$

3. Cache accessing

Given assumption: latency of main memory is 10x
latency of the cache

Optimization 1: reduce latency of main memory by 50%

Optimization 2: reduce latency of cache by 25%

a. cache hit rate = 95%

Opt 1:

before opt/after opt = $((.95*1) + (.05*10)) / ((.95*1)+(.05*5))$

before opt/after opt = 1.2083

Opt 2:

before opt/after opt = $((.95*1) + (.05*10)) / ((.95*0.75)+(.05*10))$

before opt/after opt = 1.196

b. Cache hit rate = r

$((r*1)+(1-r)*10) / ((r*1)+(1-r)*5) = ((r*1+(1-r)*10)/(r*0.75+(1-r)*10)$

$0.75*r + (1-r)*10 = r+(1-r)*5$

$0.75*r+10-10*r = r+5-5*r$

$5 = 5.25*r$

$r = 0.95238 = 95.238\%$

If the cache rate is greater than 95.238%, the
the cache optimization would be better. Otherwise
, the main memory optimization would be better.

c. Original/Optimized

$((h*1)+(1-h)*10) / ((h*0.75)+(1-h)*5)$

$(h+10-10*h)/(0.75*h+5-5*h)$

$(10-9*h) / (5-4.25*h)$

4. ad-hoc network

path with H hops (links between two nodes)

link between any two nodes is 10 Mbps

300 bytes carry metadata

P - fraction of lost packets on one link

Assuming 1 MB is about 10^6 bits

a. Effective throughput

packages = $(10 \cdot 10^6 \text{ bits}) / ((1500 \cdot 8) / 1s) = 833.33$ (no loss)

Throughput in bits = $833.3 \cdot (1-P)^H \cdot 1500 \cdot 8$ bits

Effective throughput = $833.3 \cdot (1-P)^H \cdot 1200 \cdot 8$ bits

b. $H=1$, $P=0.01$

Effective throughput = $833.3 \cdot (1-P)^H \cdot 1200 \cdot 8$ bits

Effective throughput = $833.3 \cdot (1-0.01)^1 \cdot 1200 \cdot 8$ bits

Effective throughput = 7.92 Mbps

c. Maximum loss probability

$H = 1$, Effective bandwidth > 6 Mbps for average-length path L

$833.33 \cdot (1-P)^L \cdot 1200 \cdot 8 > 6 \cdot 10^6 \text{ bits}$

5. Finding capacity of general networks (MaxFlow)

0. finding feasible "path" b/w source and dest

1. compute "flow" capacity of that path

2. reducing capacities on links of new paths accordingly and eliminate all links that have capacity 0 (create a residual graph)

3. repeat to get additional flow capacities until all paths are exhausted

Capacity = sum of all flow capacities

$C = f_1 + f_2 + \dots + f_n$

a. (see picture)

b. One algorithm you could use to choose to find which increase in connection would increase the capacity the most would be to just choose the bottleneck connection. Finding the bottleneck is more difficult. One way to do this may be to increase

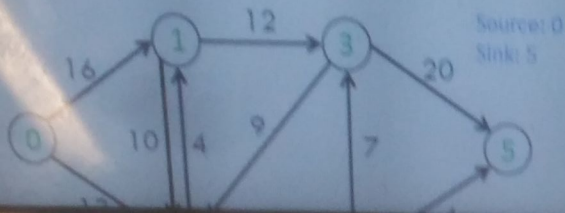
the capacity of the node connected to as many nodes before the output node as possible. This will increase the capacity because if one node before the output node receives too much traffic, it can route some traffic to the other node. In this case, using this algorithm, the best connection to increase would be the connection from 4 to 3. Increasing this connection from 7 to 8 would increase the capacity to 24.

```
/* I found stack overflow links describing  
a the Ford fulkerson algorithm, but I couldn't un-  
derstand it very well so I decided not to make it  
my official answer to this question */
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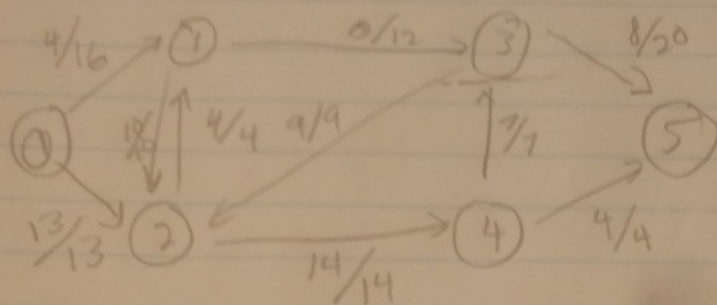
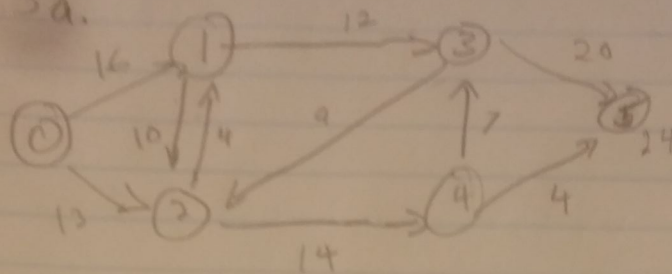
c. In general the capacity is limited based on the bottleneck connection with the lowest capacity. As you increase the capacity of the bottleneck connection, it will eventually reach a point where it won't be the lowest capacity and adding more capacity to the former bottleneck connection would not increase the overall capacity.

d. Performing a DoS attack would best at the connection from 1 to 5 as the capacity would now be 11 instead of 23 because attacking that 12 capacity connection would cause node 2 to receive much more traffic than anticipated as there is no alternative but to route to node 2.

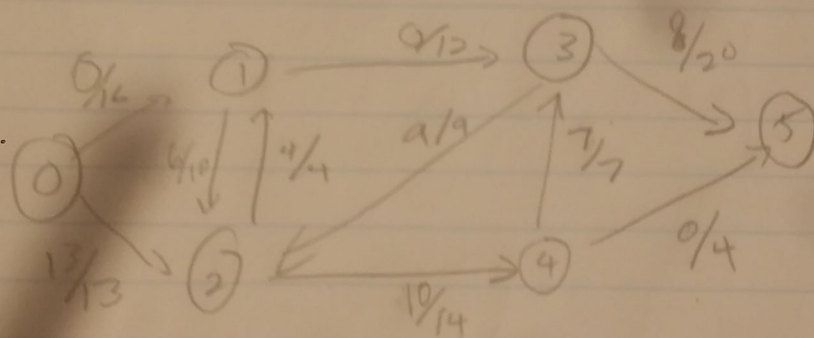
and egress links (e.g. by subjecting it to a Denial of Service)
Which link would you choose and why?



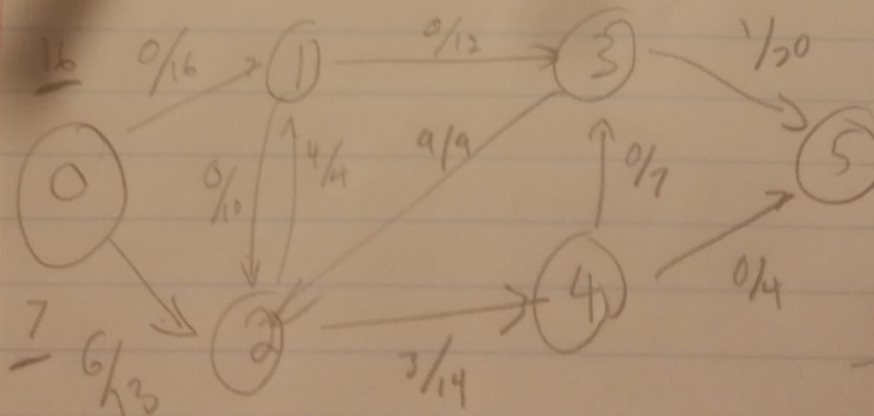
5a.



$$C = 12$$



$$C = 16$$



$$C = 16 + 7$$

$$C = 23$$