

Macaulay duration 10 yr 6% 1000 bond
annual coupons/redemption of \$1200 if the
yield to maturity is 9%

coupon:

$$Fr = 1000(.06) = 60$$

$$P = Fr a_{\overline{n}|j} + Cv_j^n$$

$$P(.09) = 60 a_{\overline{10}|.09} + 1200 \left(\frac{1}{1.09^{10}} \right)$$

$$\approx \$891.9524304$$

Macaulay duration

$$D(.09, \infty) = \frac{1}{P} \left(\sum_{k=1}^9 60k v_{.09}^k + 10(1260 v_{.09}^{10}) \right)$$

$$* v = \frac{1}{(1+i)^n}$$

$$= \frac{60}{P} (Ia)_{\overline{9}|.09} + \frac{12600 v_{.09}^{10}}{P}$$

$$= \frac{60}{891.9524304} \left(\frac{\ddot{a}_{\overline{9}|.09} - 9 v_{.09}^9}{.09} \right) + \frac{2600 v_{.09}^{10}}{891.9524304}$$

$$= .0672681613 \left(\frac{\frac{1 - v_{.09}^9}{.09} - 4.14385}{.09} \right) + \frac{12600 v_{.09}^{10}}{891.9524304}$$

$$\approx 7.75417537$$

$$= 7.75 \text{ yrs}$$