

4. Suppose that the present value of annuity-due of  $n$  years is 31.61667882 and the accumulation value of annuity-immediate of  $(n+1)$  years is 64024.90944. Determine the effective annual rate and  $n$ .

Given:

$$\ddot{a}_{\overline{n}|i} = 31.61667882$$

$$s_{\overline{n+1}|i} = 64.024.90944$$

$$\textcircled{1} \ddot{s}_{\overline{n}|i} = 1 = s_{\overline{n+1}|i} \Rightarrow \ddot{s}_{\overline{n}|i} = s_{\overline{n+1}|i} - 1$$

$$\textcircled{2} \ddot{s}_{\overline{n}|i} = (1+i)^n \ddot{a}_{\overline{n}|i} \Rightarrow (1+i)^n = \frac{\ddot{s}_{\overline{n}|i}}{\ddot{a}_{\overline{n}|i}}$$

want:

$i$  and  $n$

$$(1+i)^n = \frac{\ddot{s}_{\overline{n}|i}}{\ddot{a}_{\overline{n}|i}} = \frac{s_{\overline{n+1}|i} - 1}{\ddot{a}_{\overline{n}|i}} = \frac{64.024.90944 - 1}{31.61667882} = 2025.004$$

$$\ddot{a}_{\overline{n}|i} = \frac{(1 - (1+i)^{-n})}{d}$$

$$d = \frac{(1 - (1+i)^{-n})}{\ddot{a}_{\overline{n}|i}}$$

$$d = \frac{\frac{(1 - \ddot{a}_{\overline{n}|i})}{(1 + s_{\overline{n+1}|i})}}{\ddot{a}_{\overline{n}|i}}$$

$$d = \frac{1}{\ddot{a}_{\overline{n}|i}} - \frac{1}{1 + s_{\overline{n+1}|i}}$$

$$d = \frac{1}{31.61667882} - \frac{1}{64.024.90944 - 1} = 0.03161326$$

$$i = \frac{d}{1-d} = 0.03264528$$

$$(1+i)^n = 2025.068 \quad * i = 0.03264528$$

$$(1.03264528)^n = 2025.068$$

$$\log(1.03264528)^n = \log(2025.068)$$

$$n \log(1.03264528) = \log(2025.068)$$

$$n = \frac{\log(2025.068)}{\log(1.03264528)}$$

$$n = 237$$