

Physics II: Electromagnetism

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Primary Textbook: Fundamentals of Physics by Halliday, Resnick, and Walker

Teacher: Ali

1 Chapter 21 - Electric Charge

1.1 Charge

1. Matter is composed of specific particles (electrons, protons, and neutrons), each with a property of charge (-ve, +ve, or 0)
 - (a) Charge is measured in Coulombs, generally a unit derived from Amperes for current, such that $1\text{ C} = 1\text{ A}\cdot\text{s}$
 - (b) Electrons have a charge of $-1.6 \times 10^{-19}\text{ C}$ and a mass of $9.11 \times 10^{-31}\text{ kg}$
 - (c) Protons have a charge of $+1.6 \times 10^{-19}\text{ C}$ and a mass of $1.673 \times 10^{-27}\text{ kg}$
 - (d) Neutrons have a charge of 0 C and a mass of $1.674 \times 10^{-27}\text{ kg}$, such that the mass is approximately the sum of that of an electron and proton
 - (e) The signs for electrons and protons were chosen by Benjamin Franklin by arbitrary convention
2. The Law of Charges state that like charges repel and unlike charges attract
3. Quantization of Charge states that the charge of any body is equal to the multiple of the charge of an electron/proton, called the elementary charge
 - (a) Quantized quantities are those which can only have discrete values of specific integer multiples of some constant, rather than any value
4. Conservation of Charge states that charge is conserved, in all bodies, including subatomic, nuclear, and large-scale
 - (a) Thus, in nuclear reactions, charge is either annihilated or pair-produced (producing both charges simultaneously)
5. Materials can be divided into conductors, insulators, and semiconductors
 - (a) The distance between the atomic radiuses of each of the atoms in the material determine the type, such that the further the distance, the less conductive, making conductors dense
 - (b) Conductors have electrons free to move from orbit to orbit, such as metals or impure water
 - i. It is noted that this creates the difference of charged conducting bodies, such that the charges isolate themselves on the outside surface when there is no external field, unlike insulators which are dispersed evenly throughout
 - A. The charges are only uniformly dispersed on the surface of a conducting sphere, while they vary in other conducting bodies, or in conductors with an external field acting on it
 - ii. Thus, conducting spheres act as a spherical shell due to all charges on the outer layer
 - iii. Superconductors are conductors without any hindrance to movement of electrons
 - (c) Insulators have a large energy gap (E_g), such that the electrons are bound to atoms, unable to jump/move, such as wood, glass, rubber, or pure water
 - (d) Semiconductors are not free or bound, such that they can be converted to either a conductor or insulator, such as silicon or germanium
 - i. Adding impurities to the material through doping allows electrons to jump easier, such that it conducts better
 - ii. Increasing temperature increases electron energy, allowing jumps temporarily, while decreasing temperature does the opposite

1.2 Charging

1. Charging by friction is done by rubbing objects together, using the frictional force to force electron transfer to the material with greater attraction to electrons
 - (a) Valence electrons are the ones lost from the material, specifically called conduction electrons when able to be lost (in conductors)
 - (b) Glass and silk are known for producing positively charged glass
 - (c) Plastic and fur are known for producing negatively charged plastic
2. Charging by contact is done by contact between two non-insulators, causing the charge to move until equilibrium
3. Charging by induction is done by placing a charged rod near a neutral conductor, such that the material is polarized into a separation of charges, giving a temporary/induced charge
 - (a) If the object is then split up in the case of a conductor, where the polarization is on a super-molecular scale, it can be charged
 - (b) If the object is an insulator, such that it is on a dipole molecular scale, it is temporary, but can allow it to be attracted to the object
4. Electroscopes have two flat leaves connected to a rod, which is attached to the ball on top, such that it detects charge by charging by contact, after which the leaves separate
 - (a) It can be discharged by attaching it to a grounding wire, attached to the Earth, which acts as a giant neutral body to neutralize the charges

1.3 Coulomb's Law

1. Coulomb's Law determines the electrostatic force of charged bodies, where electrostatic denotes stationary/negligible-movement charges
2. $F_e = \frac{k|q_1||q_2|}{r^2}$, where the direction of the vector is determined by the law of charges
 - (a) $k = 9 * 10^9 \frac{Nm^2}{C^2} = \frac{1}{4\pi\epsilon_0}$
 - (b) The overall force must be found before breaking it up into components, rather than in finding it as components first
3. The ratio of electrostatic force to gravitational force on a molecular scale approximates as 10^{40} , such that gravity can be ignored on that scale
 - (a) Based on the hydrogen atom, with a radius of 0.53 Angstrom ($0.53 * 10^{-10}m$)
4. Shells of uniform charge density are found to have force interactions with charged point masses outside as if it was concentrated at the center
 - (a) Point masses inside the shell have no net electrostatic force acting on it

2 Chapter 22 - Electric Field

2.1 Point Charges

1. The electric field (\vec{E}) is a vector field, or a function of vectors at each point on the cartesian grid, allowing a measurement of the influence of a particle on any other particle at that point
 - (a) It is proportional to the number of field lines per unit area, such that high field line density means a stronger field
 - i. Electric field lines are drawn from positive to negative
 - (b) Electric fields are found by measuring the force on a positive test charge with a small enough size that it doesn't disrupt the surrounding field, though it is noted that fields

- exist independently of the test charge
2. $\vec{E} = \frac{\vec{F}}{q_0} = \frac{k|q|}{r^2}$, where the direction is determined by the type of charge, where q_0 is the test charge, and q is the charge of the point mass producing the field
 - (a) The unit of electric fields is N/C
 - (b) $\vec{E}_{net} = \sum_i \vec{E}_i$, or the electric field at some point/test charge due to a series of additional charges, such that superposition applies
 - i. Superposition assumes that the charges remain in the same locations as when calculated individually, when together
 3. Electric dipoles are created by two point charges of equal magnitude, but opposite charge, separated by some distance
 - (a) Dipole moment (\vec{P}) = qr , where r is the distance between them, and q is the charge of each point, where the vector goes from negative to positive
 - i. The direction of the dipole is based on the direction of the electric field vectors acting on the point charge for any point on the dipole line
 - ii. This is able to be expressed by the asymmetrical charge distribution of even more complicated molecules
 - (b) $\tau_{external \rightarrow dipole} = Px E$, where E is the uniform external electric field
 - (c) $PE = -E \cdot P$ for dipoles in an external electric field, where E is the uniform external electric field
 - (d) $E_{dipole} = \frac{kP}{r^3}$, where r is the distance from the center of the dipole, where the point is on the dipole axis as r becomes far greater than the distance between the dipole charges
 - i. On the other hand, E is proportional to $\frac{1}{r^3}$ at all points on the dipole axis, rather than just at a large distance
 - ii. This proportionality is due to the charges canceling each other out faster as the distance gets further
 - (e) Dipoles can be induced by an electric field, even in a nonpolar molecule, or single atom, such that an induced dipole moment forms in the same direction as the field
 - i. The molecule/atom is then said to have been polarized temporarily by the field
 4. Sparks are due to electrical breakdown as electrons are forced out from atoms as the electrical field gets past the critical value (E_c)
 - (a) These electrons create blue light when they collide with atoms after being separated from their original atoms

2.2 Solid Bodies

1. $\vec{E} = \sum_i \frac{k\Delta q_i}{r_i^2} = \int \frac{k}{r^2} dq$
 - (a) $q = \lambda x, q = \sigma A, q = \rho V$ (depending on the dimensions of the solid body)
 - (b) If the density functions are non-uniform, the integral is taken to solve for q , with respect to each dimension variable
 - (c) These calculations can be made simpler if one of the dimensions of the field cancels out, but a multiplier of some trig function must be added to the equation to remove that component
2. For parallel, nonconducting plates, $\vec{E} = \frac{\sigma}{\epsilon_0}$, such that the field from each plate is half of that value
 - (a) ϵ_0 is the permittivity constant of free space, or $8.854 \times 10^{-12} C^2/Nm^2$, and σ is the charge density of the plates
 - (b) This is due to all field lines moving in a different direction being canceled, assuming

infinitely long parallel plates (or assumed to exist far from the edge of the plate, creating a uniform electric field

- (c) Uniform electric fields are those with the same magnitude and direction at every point
- (d) The fact that parallel plates have double the field of a single plate can also be thought to be due to all the charge moving to the edge, such that double the charge is present, rather than split on both edges
 - i. This is not due to superposition, due to the charges when the plates are together, such that it must be calculated when together, rather than the sum of apart

3 Chapter 23 - Electric Flux

3.1 Electric Flux

1. Electric flux is the measure of flow of the field through an area, or the number of electric field lines passing through an area, such that $\Phi_E = \vec{E} \cdot \vec{A}_n = \vec{E} \vec{A}_n \cos(\theta)$, where \vec{A}_n is the normal to the surface, perpendicular and with a magnitude equal to the area
 - (a) For an enclosed object, lines entering the surface of the object is negative, outward is positive
 - (b) Thus, positively charged objects have lines leaving but not entering, negative objects have vice versa
2. $\Phi = \vec{E} \cdot \vec{A}_n$ for uniform surfaces
 - (a) $\Phi = \lim_{\Delta A_n \rightarrow 0} \sum_i \vec{E}_i \cdot \Delta A_n = \oint \vec{E} \cdot dA_n$
 - (b) Electric flux is a scalar with $N * m^2$ as the unit

3.2 Gauss's Law

1. Gauss's Law is used to calculate the gravitational field at a point, by creating a gaussian surface including that point
 - (a) Gaussian surfaces must be imaginary, closed (compact/effectively-continuous without boundary in any direction), 3D surfaces, with a constant field throughout
 - (b) They also must be symmetrical objects to minimize calculations
 - (c) The electric field must also be parallel to the normal of the tangent plane, A_N , on the surface A
2. Gauss's Law states that $\Phi_{e\epsilon_0} = q_{enc}$, where q_{enc} is the charge of the body inside the surface creating the field
 - (a) Gauss's Law is able to be derived from Coulumb's Law, such that $\Phi_e = \oint \vec{E} dA = \vec{E} \oint dA = \frac{kq_{enc}}{r^2} (4\pi r^2) = \frac{q_{enc}}{\epsilon_0}$
 - (b) By the definition of a surface integral, $\oint dA$ equals the surface area of the Gaussian surface
 - (c) This law only holds true in this form for charges in either a vacuum or air (effect of air is negligible)
 - (d) The electric field can be influenced by charges outside the surface, but the charge calculated is only that within the surface, due to outside charges not contributing to the net electric flux of the surface, but rather just adding field lines that pass fully through
3. Gauss's Law can be applied to an infinitely long line of charge (or line of charge far from the ends), such that a cylinder can be constructed, since the flux through the top and bottom is

parallel, and thus 0, such that the flux through the curved section is counted only

- (a) This is used to derive the field of an infinite (or middle of the) sheet of charge at some distance as well, by creating a cylinder in the center around some area of the sheet of some height, thus the flux of the caps of the cylinder are the only ones used
 - i. This is also used to derive the field between two parallel plates, due to the density doubling by the movement of charges toward the single edge near the center, rather than divided between the two edges when isolated, resulting in the field doubling
 - ii. This is also used to calculate the external field outside a conductor with nonuniform charge distribution, due to it being uniform and the surface flat over a tiny area
 - A. On the other hand, it must be a conductor, or the charge would not be isolated in a flat layer on the edge of the surface
 - (b) It can also be used for spherical symmetry about some body, allowing the shell charge calculations to be shortened, as well as calculate the field within for nonconducting spheres by the charge enclosed
 - (c) Thus, bodies can be created without complete uniform field at the surface, such that the field is parallel to all surfaces that are not uniform, and thus can be not counted
 - (d) On the other hand, symmetry cannot be applied to the edges of an object, due to the edge effect/fringing causing the electric field lines to curve
4. For varying charge density, $q_{enc} = \int \rho dV$ is substituted in, where dV can be converted to cartesian, cylindrical, or spherical depending
5. Gauss's Law is also used to prove that conductors have the charge on the edges, due to if charge existed within, an electric field would, creating a constant internal current which isn't the case
- (a) The same reasoning can be used to show that it is only in the outer surface if there exists a cavity within, rather than the cavity surface as well
 - (b) It is also used to show that a conductor works equally to an infinitely thin insulating shell

4 Chapter 24 - Electric Potential

1. Electric potential energy can be defined in a system from infinity as a reference as the negative work done by electrostatic force to move a particle from infinity towards some stationary, unaffected second charge ($\Delta U = U_r - U_\infty = U_r = -W_{\infty \rightarrow r}$)
 - (a) The electric potential energy can also be thought of as the work done by an external action to counteract the electric field, and move the particle from infinity to some stationary final setup
 - (b) Thus, the reference configuration is some system where each charged particle is an infinite distance from each other, such that reference potential energy is 0
 - (c) Electrostatic force is conservative, and thus path independent
 - (d) Energy is often measured in electron-volts, such that it is the energy required to move an electron through one volt ($1.6 * 10^{-19}$ J)
2. Electric potential (V) is a scalar quantity not dependent on the particle being moved, but rather existing at each point in a field, equal to the potential per unit charge
 - (a) Thus, $V_r q_0 = U_0$, where q_0 is the test charge, and r is the distance from the other particle
 - (b) As a result, it can be found that $V = \frac{kq}{r}$ for a field produced by a point charge, such that positive charges produce positive potential and vice versa
 - i. By the superposition principle for potential energy, the potential at some point due

- to a group of charges is found by $V = \sum_i \frac{kq_i}{r}$
3. ΔV is the electric potential difference, also called the voltage, and measured in Volts, or J/C
 - (a) $\Delta V = \frac{\Delta U}{q} = \frac{-W}{q}$, such that it can be calculated for point charge systems by the work done
 - (b) By extension, $\Delta V = \frac{-\int_i^f \vec{F} \cdot d\vec{s}}{q} = -\int_i^f \vec{E} \cdot d\vec{s}$, allowing it to be calculated by the movement of a particle in both an external field and a system of particles
 - i. In the external field, the initial point can be thought to be the point of zero potential, such that $\Delta V = V_f$
 - ii. As a result, for fields created by point charges, since $V(\infty) = 0$, $V(r) = \int_{\infty}^r -E \cdot dr$
 - A. In this case, the electric field must be found, not just at the point itself, but all points from there to infinity, such that if it is measured by multiple functions at various regions, must be broken up
 - B. This function to find V is commonly used for symmetrical objects by which Gauss's Law can be applied, while the defining function is more commonly used for non-symmetrical ones
 - iii. This is used to prove that the potential within a conducting sphere creates the same potential within the sphere, due to no electric field inside
 - (c) For fields generated by dipoles, $V = \frac{kq(r_- - r_+)}{r_- r_+}$
 - i. As r becomes far greater than the distance between the charges, r_- and r_+ becomes parallel, such that $r_- r_+ = r^2$ and $r_- - r_+ = d \cos \theta$, where θ is the angle between the dipole axis and each r
 - A. θ is also noted to be the angle between the radius from the center of the dipole and the dipole axis
 - ii. Thus, $V = \frac{kq d \cos(\theta)}{r^2} = \frac{k p \cos(\theta)}{r^2}$ for dipoles as the distance from the dipole is far greater than the distance between the charges
 - (d) For a continuous charge distribution, $V = \int \frac{k dq}{r}$
 4. The work moving a series of charges is equal to the sum of the work to move each charge with respect to the work of the charges moved previously
 5. By the relationship of potential energy and force, $E = -\vec{\nabla} V(\vec{r})$
 6. Equipotential regions/points are those where the electric potential is equal, either a real or imaginary surface/region/points
 - (a) By extension, points are equipotential if the work done moving a charge from one to the other is 0, such that either electric field is 0 or the electric field is perpendicular to the movement of the charge
 - (b) Equipotential surfaces can be found by the IVT, such that if on a line between two points, the value moves past the desired potential, there must be some point such that it is equipotential