Test: Sequences & series

Name:

Answer on lined paper. Show work.

1. In an arithmetic sequence, the first term is 7 and the second term is 11.

- (a) Find the common difference.
- (b) Find the eighth term.
- (c) Find the sum of the first eight terms of the sequence.

2. Given that for a geometric sequence $u_1 = 18$ and $u_3 = 8$

- (a) Find the value of r.
- (b) Given that u_k is the first term of the sequence with a value less than one, find k.
- (c) Find the sum of the infinite series S_{∞}

3. The first three terms of an arithmetic sequence are $u_1 = 5.1$, $u_2 = 5.5$, and $u_3 = 5.9$.

- (a) Find the common difference.
- (b) Given that the kth term of the sequence, $u_k = 11.5$. Find k.

4. Let f(x) = 2x - 3 and $g(x) = (x - 1)^2$

- (a) Find $(f \circ g)(4)$
- (b) Find $f^{-1}(x)$

5. Simplify the expression $\sqrt{a} \cdot \sqrt{a^5}$

6. $(2x^2 - 2x - 5)(x + 3) - 2x(x^2 - x - 4)$

7. What is the inverse of the function $y = \frac{2}{x+3}$?

8. Let x = ln2 and y = ln5. Write down the following expressions in terms of x and y.

- (a) $\ln \frac{2}{5}$
- (b) ln 50
- (c) $\ln 0.1$

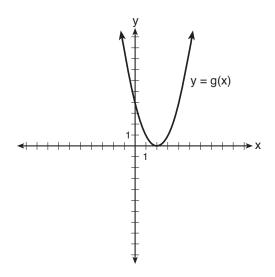
9. Using the quadratic formula or otherwise, find the solution set to $2x^2 - 3x - 5 = 0$.

- 10. Simplify the expression 2xi(4+3i).
- 11. Simplify the expression $\left(\frac{x^{-2}}{x^2}\right)^{\frac{1}{2}}$ to one with positive integer exponents and radicals.

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12. The function g is defined by graph of y = g(x) below.

- (a) Write down the equation for g(x) in factored form.
- (b) The function h(x) is made by reflecting g across the y-axis. What is the equation for h(x)?



13. Let
$$f(x) = x^2 - 6x + 4$$

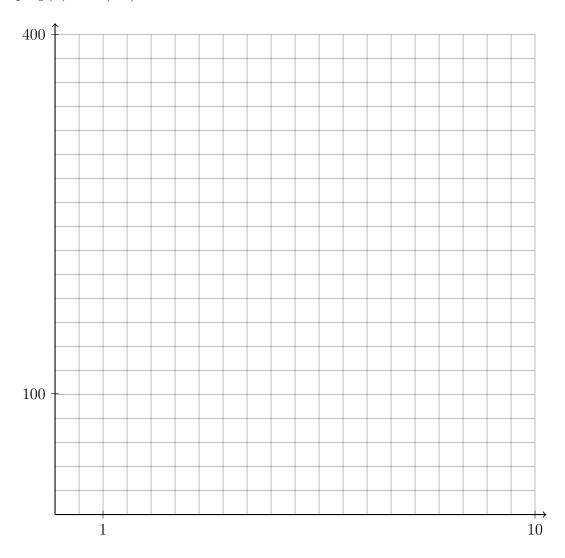
- (a) Rewrite quadratic in vertex form and state the vertex as an ordered pair.
- (b) The parabola is translated vertically by k units to make the function g(x). The equation g(x) = 0 has one solution. Find k.
- 14. For each of the following questions select two applicable words from the following list: revenues, assets, premiums, costs, earnings, expenses, debt, reserves, overhead, investments.
 - (a) What financial measure would a business manager try to *increase* in order to raise profits?
 - (b) What financial measure would a manager try to reduce to improve profitability?
 - (c) Since their customers could have large losses from a storm or other disaster at any time an insurance company maintains large amounts of what?

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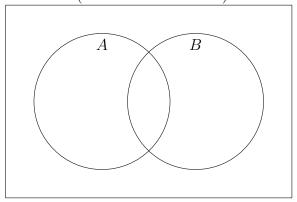
For these last two pages, answer in the space provided

15. Graph $g(x) = 30(1.5)^{\frac{x}{2}} - 5$ on the set of axes below.



Is the function an example of exponential growth or exponential decay? Justify your answer algebraically.

- 16. Let A and B be independent events, where P(A) = 0.5 and P(B) = 0.6.
 - (a) Find $P(A \cap B)$
 - (b) Fill in the probability value for each area in the Venn diagram representing the situation. (there are four values)



- (c) Find $P(A \cup B)$
- (d) Find $P(A \cap B')$
- 17. The function $f(x) = e^x$ is shown on the graph. Sketch g(x) = f(x-3) 1. Plot and label the asymptote(s).

