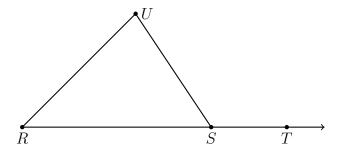
## Exam: Introduction to logic and proof, angle pairs

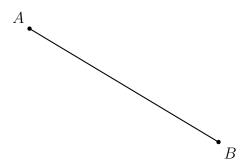
- 1. Points that are all located on the same line are \_\_\_\_\_\_.
- 2. Given C(1,-2) and D(7,9), find the coordinates of the midpoint of  $\overline{CD}$ , the point M.

- 3. Given the conditional statement, "If two triangles' corresponding sides are congruent, then their corresponding angles are congruent."
  - (a) Write down the conclusion of the statement.
  - (b) Write down the negation of the hypothesis.
  - (c) Write down the converse of the statement.

4. Given  $m \angle R = 50$ ,  $m \angle S = 65$ , and  $m \angle UST = 115$ . Find  $m \angle RSU$ .



5. Construct an equilateral triangle with one side the given line segment  $\overline{AB}$ .



- 6. Given the square BECA with BE = 2.50.
  - (a) Find the area of BECA.
  - (b) Find the perimeter of BECA.
- 7. Given  $m \angle A = 75$ ,  $m \angle B = 45$ ,  $m \angle C = 165$ ,  $m \angle DEF = 55$ ,  $m \angle FEG = 15$ .
  - (a) Find a pair of complementary angles. \_\_\_\_\_\_
  - (b) Find a pair of supplementary angles. \_\_\_\_\_\_

8. Find the value of  $|\sqrt{11} - \frac{3}{2}| - \sqrt{11}$ .

9. Given P(-2,4) and Q(1,0), find the length of  $\overline{PQ}$ .

10. In a proof, each of the following statements are written. Write down the reason that would justify each step.

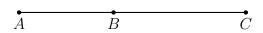
(a) 
$$2(DE + FG) = 2DE + 2FG$$
 property

(b) 
$$\overline{EF} \cong \overline{EF}$$
 \_\_\_\_\_\_ property

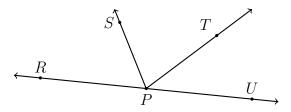
(c) 
$$DE + EF = FG + EF$$
 \_\_\_\_\_\_ property

11. Given  $\overline{ABC}$ , AC = 15, and the point B partitions  $\overline{AC}$  in a ratio of 2:3.

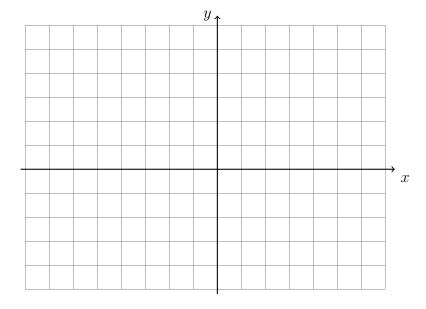
Find AB.



12. Given the situation in the diagram, answer each question. Circle True or False.

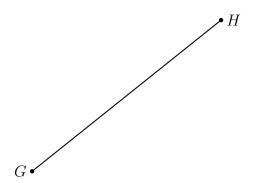


- (a) True or False:  $\angle SPU$  is an obtuse angle.
- (b) True or False:  $\overrightarrow{PR}$  and  $\overrightarrow{PU}$  are opposite rays.
- (c) True or False:  $\angle RPT$  and  $\angle SPU$  are a linear pair.
- (d) True or False:  $\angle SPT$  and  $\angle TPU$  are adjacent.
- 13. Given B(-7,4), U(5,-1), and Z(-7,-1).
  - (a) Plot and label the points on the graph, drawing  $\overline{BU}$
  - (b) Draw the legs of the right triangle,  $\overline{BZ}$  and  $\overline{ZU}$ , marking their lengths.
  - (c) Write down the distance formula for BU, substituting coordinate values.
  - (d) Find the value of BU.



14. Given the circle C with circumference  $10\pi$ . Find the area of C.

15. Construction a perpendicular bisector of the given line segment,  $\overline{GH}$ .



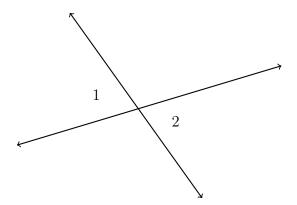
16. Given  $\overrightarrow{QS}$  as shown on the number line, with Q having the coordinate 2.55 and S the coordinate 5.23.



(a) Find the value of the coordinate of the point R, the midpoint of  $\overline{QS}$ .

(b) The point P is collinear with  $\overrightarrow{QS}$  such that Q is the midpoint of  $\overrightarrow{PS}$ . Mark P on the line and state the value of its coordinate.

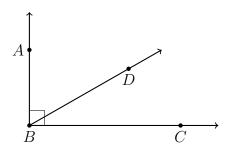
17. Given two vertical angles,  $m\angle 1 = 4x + 6$ ,  $m\angle 2 = 6x - 32$ . Find  $m\angle 1$ . For full credit find the  $m\angle 2$  as a check.



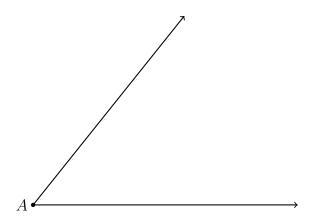
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18. Given  $\overrightarrow{BA} \perp \overrightarrow{BC}$ ,  $m \angle ABD = 2x - 5$ , and  $m \angle DBC = x - 10$ . Find  $m \angle DBC$ .

For full credit, show the check using both angle measures.



19. Construct an angle bisector of the given angle.



20. Spicy: Construct the angle bisectors of the angles of the triangle and their intersection, the incenter.

