3.9 Exam: Area, volume, perimeter; line segments and angles

Do Not Solve!

Label the drawing completely and write an equation in terms of \boldsymbol{x} modeling the situation.

1. Given that O bisects \overline{NP} . NO = 2x, NP = 3x + 10. Find x.

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2. Given \overline{ABC} , with AB = x - 1, BC = 3x + 3, and AC = 26. Find AB.

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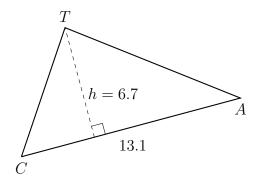
3. The points R, S, and T are collinear, with RS = 3x - 2 and ST = 12. If RT = 7x, find RT.

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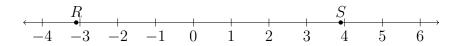
4. The point K is the midpoint of \overline{JL} , JK = 10x + 15, and JL = 18x + 40. Find JK.

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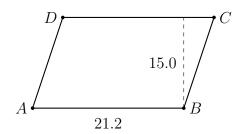
5. Find the area of $\triangle CAT$. The altitude h of the triangle is 6.7 centimeters and the base CA = 13.1 cm. Show work by writing an equation before making the calculation.



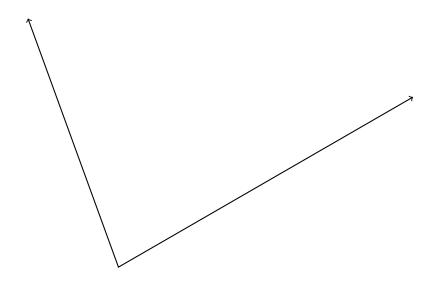
6. Given \overrightarrow{RS} as shown on the number line, with R = -3.1 and S = 3.9.



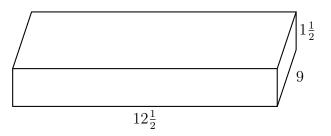
- (a) What is the exact distance on the number line between the points R and S?
- (b) The point T bisects \overline{RS} . Find the value of T, and mark and label it on the numberline \overline{RS} shown above.
- 7. Find the area of the parallelogram ABCD shown below, with AB=21.2 and height h=15.0.



8. Complete the construction of the bisector of the given angle.



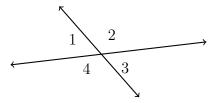
9. A cardboard mailing carton is $12\frac{1}{2}$ inches long, 9 inches wide, and $1\frac{1}{2}$ inches tall. Find the volume of the box. Show the calculation.



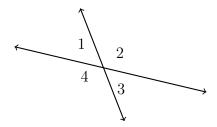
Do Not Solve!

Model the situation with an equation in terms of x. State whether the angles are complementary, supplementary, or vertical angles.

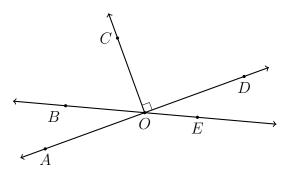
10. Two lines intersect making four angles: $\angle 1$, $\angle 2$, $\angle 3$, and $\angle 4$. Given that $m\angle 3=2x+50$ and $m\angle 4=6x+50$, find x.



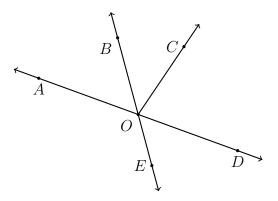
11. Given that $m \angle 1 = 5x + 22$ and $m \angle 3 = 7x + 18$ as shown in the diagram, find $m \angle 2$.



12. In the diagram below $m\angle AOB = 3x + 5$ and $m\angle COB = 4x + 15$. Find x.



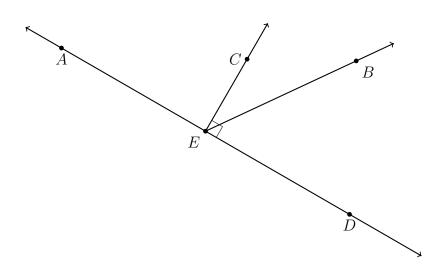
13. In the diagram below $m \angle AOB = 65$, $m \angle BOC = 4x - 10$, and $m \angle DOC = 3x + 55^{\circ}$. Find $m \angle AOB$.



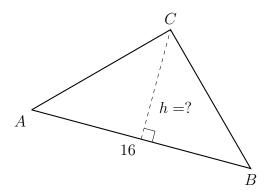
14. Complete the construction of an equilateral triangle with one side as \overline{XY} . Show all construction marks, but make no extra lines.



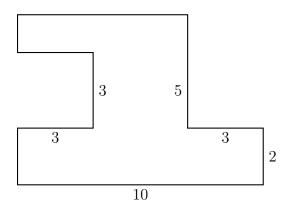
- 15. Given the diagram shown below.
 - (a) Measure the angle AEB. $m \angle AEB =$
 - (b) Name an angle that is complementary to $\angle BEC$:
 - (c) Name a pair of opposite rays:



16. One side of the $\triangle ABC$ has a length AB=16. The triangle's area is 96. Find the length of the altitude h of the triangle to vertex C and perpendicular to side \overline{AB} .

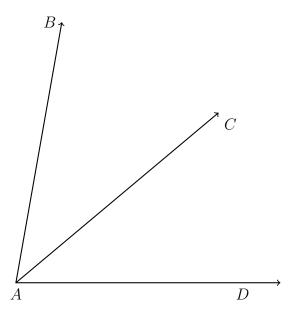


17. The shape shown below is composed of straight lines and right angles, with some lengths as marked. Find the area of the figure. (the figure is not drawn to scale)

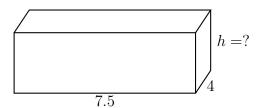


18. Given two complementary angles, $m\angle A = 54$ and $m\angle B = 3x - 3$. Find x. Check your solution.

19. An angle bisector is shown below, with \overrightarrow{AC} bisecting $\angle BAD$. Given $m\angle BAC = 4x + 2$ and $m\angle DAC = 6x - 16$, find $m\angle BAD$. (Show check)



20. The volume of the rectanglar prism shown is 105 cubic meters. Its length is 7.5 meters and depth 4 m. Find its height h. Show the calculation. (not drawn to scale)



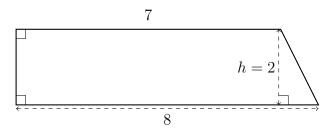
Complete all steps for full credit: the drawing to the top right, an equation and solution for x on the left, followed by the answer to the question. Write the check to the bottom right.

21. Given the collinear points P, Q, and R, with PQ = 7x + 14, QR = 2x + 12, and PR = 12x - 10. Find PQ.

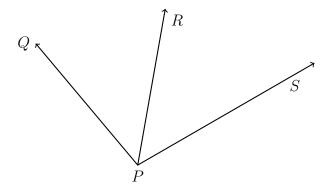
22. Angles U and V are supplementary. $m \angle U = 5x + 61$ and $m \angle V = 3x - 17$. Find $m \angle V$.

23. The shape shown below is a trapezoid. Its height is $2~\mathrm{cm}$ and the longer base is $8~\mathrm{cm}$. The shorter side opposite the base is $7~\mathrm{cm}$.

Find the area of the trapezoid by adding the rectangular area to the triangle part.



24. An angle bisector is shown below, with \overrightarrow{PR} bisecting $\angle QPS$. Given $m\angle QPR = 4x + 2$ and $m\angle QPS = 10x - 20$, find $m\angle QPS$.



25. Given that E bisects \overline{DF} . DE = 12x - 5, EF = 9x + 4. Find EF.

Write the term that best completes each statement.

- 26. Two or more line segments of equal measure are _____
- 27. Points that are located on the same line are _____

Factor and solve for x.

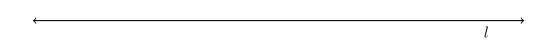
$$28. \ x^2 + 8x + 7 = 0$$

29.
$$x^2 + 7x = 18$$

Early finishers, spicy

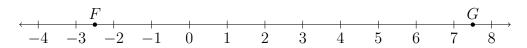
30. Complete the construction of a line perpendicular to line l through the point P. Show all construction marks, but make no extra lines.





31. The perimeter of a square is 52 cm. Find the area of the square.

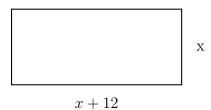
32. Given \overrightarrow{FG} as shown on the number line, with F = -2.5 and G = 7.5.



The point H is $\frac{3}{4}$ of the way from F to G. Find the value of H, and mark and label it on the numberline FG.

33. The length of the given rectangle is 12 more than the width. Its area is 64. Find the length and width of the rectangle using an algebraic method.

(the drawing is not to scale)



34. The circle with center B is shown below with diameter \overline{AC} and radius \overline{BD} . Given BC = 7x - 3 and BD = 5x + 9. Find the diameter of the circle.

