Name:

Spiral Review: 6-1 P1 (No Calculator) Calculus Tangents - A

- 1. 10N.1.sl.TZ0.2 (Mild) Let $g(x) = 2x \sin x$.
 - (a) Find g'(x) [4 marks]
 - (b) Find the gradient of the graph of g at $x = \pi$. [3 marks]
- 2. 10M.1.sl.TZ2.5 [6 marks] (Medium) Let $f(x) = kx^4$. The point P(1,k) lies on the curve of f. At P, the normal to the curve is parallel to $y = -\frac{1}{8}x$. Find the value of k.
- 3. 13M.1.sl.TZ2.9 (Spicy) Let $f(x) = \sin x + \frac{1}{2}x^2 - 2x$, for $0 \le x \le \pi$.
 - (a) Find f'(x). [3 marks]
 - (b) Let g be a quadratic function such that g(0) = 5. The line x = 2 is the axis of symmetry of the graph of g. Find g(4). [3 marks]
 - (c) The function g can be expressed in the form $g(x) = a(x-h)^2 + 3$.
 - i. Write down the value of h.
 - ii. Find the value of a.
 - (d) Find the value of x for which the tangent to the graph of f is parallel to the tangent to the graph of g. [6 marks]

Spiral Review: 6-1 P1 (No Calculator) Calculus Tangents - B

- 1. 12M.1.sl.TZ1.3 (Mild) Let $f(x) = e^{6x}$.
 - (a) Write down f'(x) [1 mark]
 - (b) The tangent to the graph of f at the point P(0,b) has gradient m. [4 marks]
 - i. Show that m = 6.
 - ii. Find b.
 - (c) Hence, write down the equation of this tangent. [1 mark]
- 2. 13N.1.sl.TZ0.6 [6 marks] (Medium) Let $f(x) = e^{2x}$. The line L is the tangent to the curve of f at $(1, e^2)$. Find the equation of L in the form y = ax + b.
- 3. 15M.1.sl.TZ1.9 (Spicy)

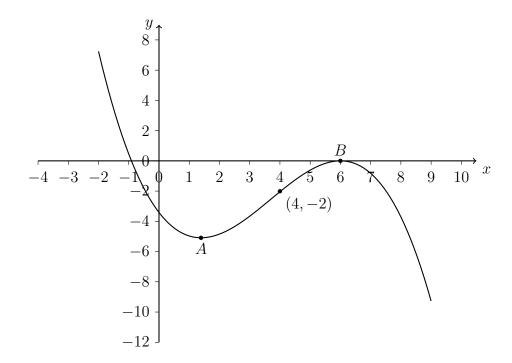
A function f has its derivative given by $f'(x) = 3x^2 - 2kx - 9$, where k is a constant.

- (a) Find f''(x). [2 marks]
- (b) The graph of f has a point of inflexion when x = 1. Show that k = 3. [3 marks]
- (c) Find f'(2). [2 marks]
- (d) Find the equation of the tangent to the curve of f at (-2,1), giving your answer in the form y = ax b. [4 marks]
- (e) Given that f'(-1) = 0, explain why the graph of f has a local maximum when x = -1. [3 marks]

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Spiral Review: 6-1 P1 (No Calculator) Calculus Tangents - C

- 1. 09M.1.sl.TZ1.3 (Mild) Let $f(x) = e^x \cos x$. Find the gradient of the normal to the curve of f at $x = \pi$.
- 2. 17M.1.sl.TZ1.6 (Medium) The following diagram shows the graph of f', the derivative of f.



The graph of f' has a local minimum at A, a local maximum at B and passes through (4,2). The point P(4,3) lies on the graph of the function, f.

- (a) Write down the gradient of the curve of f at P. [1 mark]
- (b) Find the equation of the normal to the curve of f at P. [3 marks]
- (c) Determine the concavity of the graph of f when 4 < x < 5 and justify your answer. [2 marks]

3. 17M.1.sl.TZ1.9 (Spicy)

A quadratic function f can be written in the form f(x) = a(x-p)(x-3). The graph of f has an axis of symmetry x = 2.5 and y-intercept at (0, -6).

- (a) Find the value of p. [3 marks]
- (b) Find the value of a. [3 marks]
- (c) The line y = kx 5 is a tangent to the curve of f. Find the values of k. [8 marks]

Spiral Review: 6-1 P1 (No Calculator) Calculus Tangents - D

1. 13M.1.sl.TZ1.3 (Mild)

Consider $f(x) = x^2 \sin x$.

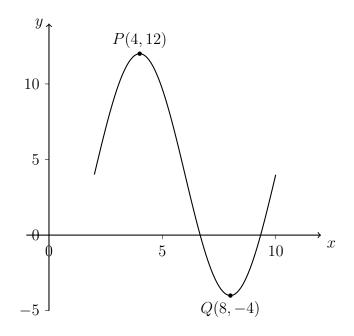
- (a) Find f'(x). [4 marks]
- (b) Find the gradient of the curve of f at $x = \frac{\pi}{2}$. [3 marks]
- 2. 18M.1.sl.TZ1.7 [7 marks] (Medium)

Consider f(x), g(x) and h(x), for $x \in \mathbb{R}$ where $h(x) = (f \circ g)(x)$.

Given that g(x), g'(3) = 4, and f'(7) = -5, find the gradient of the normal to the curve of h at x = 3.

3. 11N.1.sl.TZ0.9b (Spicy)

The following diagram shows the graph of $f(x) = a\sin(b(x-c)) + d$, for $2 \le x \le 10$.



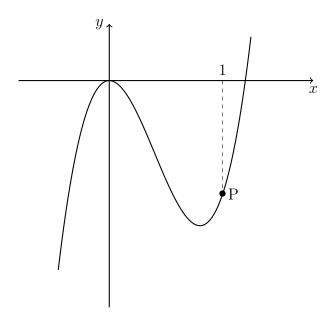
There is a maximum point at P(4,12) and a minimum point ast Q(8,-4).

- (a) Use the graph to write down the value of [3 marks]
 - i. *a*;
 - ii. *c*;
 - iii. d.
- (b) Show that $b = \frac{\pi}{4}$. [2 marks]
- (c) Find f'(x). [2 marks]
- (d) At a point R, the gradient is -2π . Find the x-coordinate of R.

Spiral Review: 6-1 P1 (No Calculator) Calculus Tangents - E

1. 12N.1.sl.TZ0.4 (Mild)

Part of the graph of $f(x) = ax^3 - 6x^2$ is shown below.



The point P lies on the graph of f. At P, x = 1.

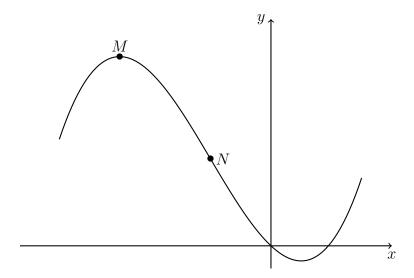
- (a) Find f'(x). [2 marks]
- (b) The graph of f has a gradient of 3 at the point P. Find the value of a. [4 marks]
- 2. 17N.1.sl.TZ0.5 (Medium)

Let $f(x) = 1 + e^{-x}$ and g(x) = 2x + b, for $x \in \mathbb{R}$, where b is a constant.

- (a) Find $(f \circ g)(x)$. [2 marks]
- (b) Given that $\lim_{n\to\infty} (f\circ g)(x) = -3$, find the value of b. [4 marks]

3. 08M.1.sl.TZ1.8 (Spicy)

Consider $f(x) = \frac{1}{3}x^3 + 2x^2 - 5x$. Part of the graph of f is shown below. There is a maximum point at M, and a point of inflexion at N.



- (a) Find f'(x). [3 marks]
- (b) Find the x-coordinate of M. [4 marks]
- (c) Find the x-coordinate of N. [3 marks]
- (d) The line L is the tangent to the curve of f at (3,12). Find the equation of L in the form y = ax + b. [4 marks]

4. 16M.1.sl.TZ1.<u>10 (Spicy)</u>

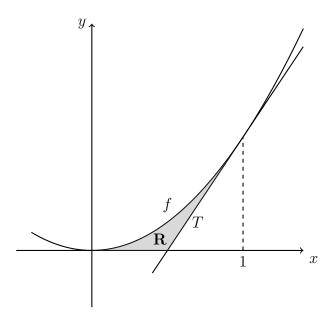
Let $f(x) = \sqrt{4x + 5}$, for $x \ge -1.25$.

- (a) Find f'(1). [4 marks]
- (b) Consider another function g. Let R be a point on the graph of g. The x-coordinate of R is 1. The equation of the tangent to the graph at R is y = 3x + 6. Write down g'(1). [2 marks]
- (c) Find g(1). [2 marks]
- (d) Let $h(x) = f(x) \times g(x)$. Find the equation of the tangent to the graph of h at the point where x = 1. [7 marks]

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5. 11M.1.sl.TZ2.8 (Spicy)

The following diagram shows part of the graph of the function $f(x) = 2x^2$.



The line T is the tangent to the graph of f at x = 1.

- (a) Show that the equation of T is y = 4x 2. [5 marks]
- (b) Find the x-intercept of T. [2 marks]
- (c) The shaded region R is enclosed by the graph of f, the line T, and the x-axis. [9 marks]
 - i. Write down an expression for the area of R.
 - ii. Find the area of R.