

12.1 IB Math - Unit 5: Integration

Bronx Early College Academy

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BECA / Dr. Huson / 12.1 IB Math - Unit 5 Integration

5.1 Drui: Antiderivatives. Friday 4 January

5.2 Drui: Indefinite Integral. Monday 7 January

5.3 Drui: Deltamath Integration Tuesday 8 January

5.4 Drui: Boundary conditions. Wednesday 9 January

5.5 Drui: Deltamath Integration Thursday 10 January

5.6 Drui: Compositions of linear functions. Friday 11 January

5.7 Drui: Compositions of linear functions. Monday 14 January

5.8 Drui: Deltamath Integration Tuesday 15 January

5.9 Drui: Integration - position problems. Wednesday 16 January

5.10 Drui: Definite integrals and area. Thursday 17 January

5.11 Definite integrals and area. Friday 18 January

5.12 Deltamath: definite integrals and area. Tuesday 29 January

5.13 Integration by substitution. Wednesday 30 January

5.14 Deltamath: definite integrals and area. Friday 1 February

5.15 Volumes of rotation. Monday 4 February

5.16 Volumes of rotation. Wednesday 6 February

5.17 Integration review. Thursday 7 February

5.18 Unit test: Integration. Friday 8 February

Kinematics (preview)

Kinematics (preview)

GQ: How do we find the antiderivative of a function?

CCSS: F.IF.B.6 Calculate & interpret the rate of change of a function

5.1 Friday 4

January

Do Now. Find $\frac{dy}{dx}$

1. Given $y = x^3 + x^2 + 17$.
2. Given $y = \frac{1}{4}x^4 + \frac{1}{2}x^2 + 9 - \frac{1}{x}$.
3. If $\frac{dy}{dx} = 3x^2 + x$, find y .
4. Skills check #1 p. 290

Problem sets from January 2,3; Sigma notation, p 290

Lesson: Antiderivatives pp. 291-2

Exam review

Homework: Exercises 9A p. 293; test corrections due Monday

GQ: How do we find the indefinite integral of a function?

CCSS: F.IF.B.6 Calculate & interpret the rate of change of a function 5.2 Monday 7 January

Do Now. Find the antiderivative, $F(x)$, of each function, $f(x)$, such that $F'(x) = f(x)$

1. $f(x) = 4x^3 + 3x^2 + 1.$
2. $f(x) = x^4 + x^2 + 5.$
3. $f(x) = \sqrt{x}$

Test corrections due, review. (take home test tomorrow)

Lesson: Indefinite integral pp. 293-4

Homework: Exercises 9B p. 294

GQ: How do we integrate functions?

CCSS: F.IF.B.6 Calculate & interpret the rate of change of a function

January

5.3 Tuesday 8

Do Now. Handout-test review

Deltamath Integration practice (taking antiderivatives)

Homework: Deltamath project through Thursday

GQ: How do we apply boundary conditions to an integral?

CCSS: F.IF.B.6 Calculate & interpret the rate of change of a function 5.4 Wednesday 9 January

Do Now. Find each indefinite integral.

1. $\int (3x^2 + 2x + 1) dx.$

2. $\int (x^4 + 6x^2 + 1) dx.$

3. $\int \sqrt{x} dx.$

4. $\int \frac{\pi}{4} \sqrt[3]{x^2} dx$

5. $\int x^{-1} dx$

Lesson: Finding the constant C given boundary conditions. pp. 295-6

Homework: Exercises 9C p. 296-7

GQ: How do we integrate functions?

CCSS: F.IF.B.6 Calculate & interpret the rate of change of a function 5.5 Thursday 10 January

Do Now. Handout-test review

Deltamath Integration practice (taking antiderivatives)

Homework: Complete Deltamath calculus project

GQ: How do we integrate compositions of linear functions?

CCSS: F.IF.B.6 Calculate & interpret the rate of change of a function 5.6 Friday 11

January

Do Now. Derivatives and antiderivatives. (Use the chain rule)

1. $f(x) = e^{3x}$. Find $f'(x)$.
2. $f(x) = \ln(5x + 3)$. Find $f'(x)$.
3. $f(x) = (2x - 5)^3$. Find $f'(x)$.
4. Find $\int 4(x^2 + x + 1) dx$.
5. $y' = 2x^3 - 1$ and $y = 3$ when $x = 1$. Find y in terms of x .
6. Given $f'(x) = \sqrt[3]{x}$ and $f(0) = 1$, find $f(x)$.

Lesson: Antiderivatives of form $\int f(ax + b) dx$. pp. 297-9

Homework: Exercises 9D, 9E (odds) p. 298, 300

GQ: How do we integrate compositions of linear functions?

CCSS: F.IF.B.6 Calculate & interpret the rate of change of a function 5.7 Monday 14 January

Do Now. Derivatives and antiderivatives. (Use the chain rule)

1. $f(x) = e^{2x-3}$. Find $f'(x)$.
2. $f(x) = \ln(4x)$. Find $f'(x)$.
3. $f(x) = (3x + 2)^4$. Find $f'(x)$.
4. Find $\int (5x^3 + x^2 + 1) dx$.
5. $y' = 2x^2 - 1$ and $y = 3$ when $x = 3$. Find y in terms of x .
6. Given $f'(x) = \sqrt[3]{x^2}$ and $f(1) = 1$, find $f(x)$.

Lesson: Antiderivatives of form $\int f(ax + b) dx$. pp. 297-9

Homework: Exercises 9D, 9E (evens) p. 298, 300

GQ: How do we integrate functions?

CCSS: F.IF.B.6 Calculate & interpret the rate of change of a function

5.8 Tuesday 15

January

Do Now. Straight to DeltaMath

Deltamath Integration practice (taking antiderivatives)

Homework: Complete Deltamath

GQ: How do we use integration to solve for position?

CCSS: F.IF.B.6 Calculate & interpret the rate of change of a function 5.9 Wednesday 16 January

Do Now. Derivatives and antiderivatives.

1. $f(x) = \sin x$. Find $f'(x)$.
2. Find $\int \sin x \, dx$.
3. $s(t) = 4.9t^2$. Find $v(t) = s'(t)$ and $a(t) = s''(t)$.
What might these functions represent?
4. Given $v(t) = \cos t$, find $s(t) = \int v(t) \, dt$. Assume $s(0) = 0$.

Lesson: Position problems (handout)

Homework: Calculus problem set

GQ: How do we calculate area with integration?

CCSS: F.IF.B.6 Calculate & interpret the rate of change of a function 5.10 Thursday 17 January

Do Now

1. Find $\int (4x^3 - 3x + 1)dx$.
2. Find $\int e^{5x}dx$.
3. Find $\int \frac{1}{3x+1}dx$.

Homework review #1, 5, 6 p. 302

Lesson: Reimann sums and the definite integral

Task: Example 8, page 304

Assessment: Calculator integration

Homework: Exercises 9H evens p. 308

GQ: How do we calculate area with definite integrals?

CCSS: F.IF.B.6 Calculate & interpret the rate of change of a function 5.11 Friday 18 January

Do Now

1. Use a calculator to find $\int_0^{\frac{\pi}{2}} \cos x \, dx$
2. Differentiate $y = \sqrt{3x^3 - x}$
3. Find $\int (6x^2 - 2x - 5)dx$.
4. Differentiate $y = (3x^2 - 5x)^5$
5. Find $\int \frac{3}{x} \, dx$.

Lesson: Properties of definite integrals p. 307

The fundamental theorem of calculus p. 309

Homework: Have a nice break!

GQ: How do we calculate area with definite integrals?

CCSS: F.IF.B.6 Calculate & interpret the rate of change of a function 5.12 Tuesday 29 January

Do Now: 6-1 Calculus Tangent lines spiral review handout

1. Select and solve one of the problems: mild, medium, or spicy.
(early finishers, do another)
2. As a class, check work
3. Record result in personal tracker

Lesson: Definite integrals

Task: Deltamath practice

Homework: Exercises 9I p. 310-1

GQ: How do we anti-differentiate using the chain rule?

CCSS: F.IF.B.6 Calculate & interpret the rate of change of a function 5.13 Wednesday
30 January

Do Now

1. Differentiate $y = \sqrt[3]{5x^2 - 2x}$
2. Find $\int (6x - 2)^4(6) \, dx$.
3. Differentiate $y = (3x^2 - 5x)(\ln x)$
4. Use a calculator to find $\int_{-1}^1 \frac{1}{x+2} \, dx$
5. Find $\int_1^2 \frac{3}{x^2} \, dx$. (check your result with a calculator)

Lesson: The substitution method of integration p. 300

Task: Practice Examples 7 p. 300

Homework: Exercises 9J p. 312-13

GQ: How do we calculate the area between two curves?

CCSS: F.IF.B.6 Calculate & interpret the rate of change of a function 5.14 Friday 1
February

Do Now: 6-1 Calculus Tangents spiral review handout
Early finishers - Take the derivative of each function

1. $f(x) = \sin x^3$
2. $g(x) = \sqrt{x^4 + 2}$
3. $h(x) = \ln(x^2 + 1)$

Lesson: The area between two functions p. 313

Assessment: Example #13 p. 314

Homework: Exercises 9K p. 316

GQ: How do we calculate a volume of rotation?

CCSS: F.IF.B.6 Calculate & interpret the rate of change of a function 5.15 Monday 4 February

Do Now: Sketch the functions $f(x) = 10x + x^2 - 3x^3$ and $g(x) = x^2 - 2x$

1. What are their intersections? (i.e. $f(x) = g(x)$)
2. What is the definite integral representing the area between the curves?
3. Using a calculator, what is the size of the area? (this may not be a trivial question)

Lesson: Integrating circle areas, modeling a solid p. 318

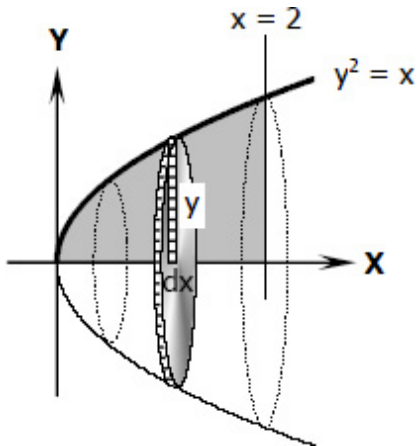
Assessment: Example #15 p. 319

Homework: Exercises 9L & 9M p. 317, 319; probability handout

The volume of a function rotated around the x-axis

Differentiate over x , but use the area of a disk defined by $A = \pi r^2$

video



GQ: How do we calculate a volume of rotation?

CCSS: F.IF.B.6 Calculate & interpret the rate of change of a function 5.16 Wednesday 6
February February

Do Now: Volumes review

1. Volumes review

Lesson: Integrating circle areas, modeling a solid p. 318

Homework: Pretest problem set Unit test Friday

GQ: How do we calculate displacement from velocity?

CCSS: F.IF.B.6 Calculate & interpret the rate of change of a function 12.1

Do Now: Do the calculations below and read the handout

1. Lance Armstrong's average speed in his six Tour de France victories from 1999-2004 was about 24 miles per hour. Assuming that he pedals at his average speed and takes no breaks, how long would it take him to ride 38 miles to the top of a 10,000 ft. volcano?
2. People who are not Lance Armstrong can travel at about 12 miles per hour on a bike. At that speed, how long would it take to reach the top of the volcano?

Lesson: Integrating velocity over time, displacement p. 321

Assessment: Example #18 p. 323

Homework: Exercises 9N & 9O p. 320, 324

GQ: How do we calculate displacement from velocity?

CCSS: F.IF.B.6 Calculate & interpret the rate of change of a function 12.1

Do Now: continued, 38 mile ride in 10 hours

1. Using the velocity vs time graph from yesterday, integrate to show that the areas representing the distance covered by the three riders are equal ($v \times t = d$).
2. Show that a rider accelerating according to $v(t) = \frac{76}{100}t$ also arrives at (10, 38).

Lesson: Integrating velocity over time, displacement p. 321

Task: Review 9F, 9M, probability

Assessment: Example #18 p. 323 (take home test Thursday)

Homework: Exercises 9P p. 326, any remaining problem sets