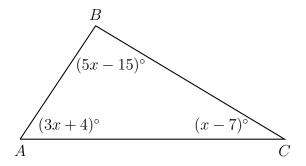
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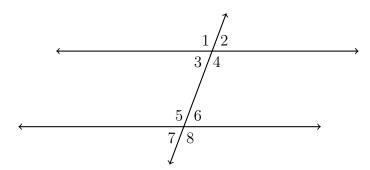
## Test: Triangles, transformations, proof

13 December 2018

1. In  $\triangle ABC$  shown below,  $m \angle A = (3x+4)^{\circ}$ ,  $m \angle B = (5x-15)^{\circ}$ , and  $m \angle C = (x-7)^{\circ}$ . What is  $m \angle A$ ?



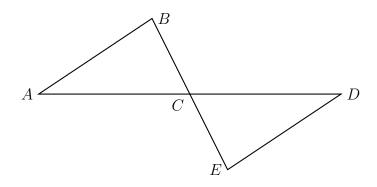
2. Given two parallel lines and a transversal, as shown below.



- (a) State the angle corresponding with  $\angle 5$ .
- (b) Given  $m\angle 3 = 78^{\circ}$  and  $m\angle 5 = 3x^{\circ}$ . Find x.

(c) In a proof, what reason would justify  $\angle 3 \cong \angle 6$ ?

3. Given  $\triangle ABC$  and  $\triangle DEC$  with  $\angle B \cong \angle E$ . C is the midpoint of  $\overline{BE}$ . Prove  $\triangle ABC \cong \triangle DEC$ .



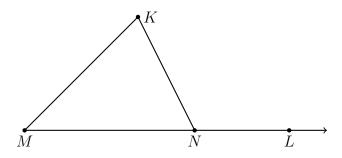
## Statement

1)

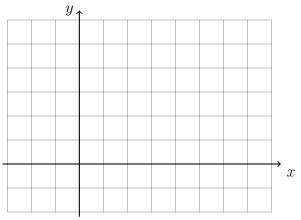
- 2) \_\_\_\_\_
- 3)
- 4)  $\angle BCA \cong \angle ECD$
- 5) \_\_\_\_\_
- 6)  $\triangle ABC \cong \triangle DEC$

## Reason

- 1) Given
- 2) Given
- 3) Given
- 4)
- 5) Definition of a midpoint
- 6) \_\_\_\_\_
- 4. Given  $m \angle K = 38^{\circ}$  and  $m \angle KNL = 111^{\circ}$ . Find  $m \angle M$ .



5. On the graph below, draw  $\overline{AB}$ , with A(-2,1) and B(6,3), labeling the end points. Determine and state the coordinates of the midpoint M of  $\overline{AB}$  and mark and label it on the graph.



6. Express the result to the nearest thousandth.

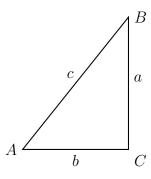
(a) 
$$\sin 60^{\circ} =$$

(c) 
$$\tan 45^{\circ} =$$

(b) 
$$\cos 23^{\circ} =$$

(d) 
$$\sin 81^{\circ} =$$

7.  $\triangle ABC$  is shown with  $m \angle C = 90^{\circ}$ . The lengths of the triangle's sides are a, b, and c. Express each trigonometric ratio as a fraction of two variables.

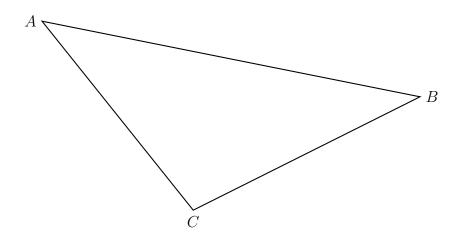


(a) 
$$\sin A =$$

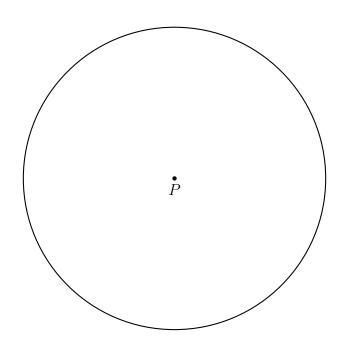
(b) 
$$\cos A =$$

(c) 
$$\tan A =$$

8. Using a compass and straightedge, construct the median to side  $\overline{BC}$  in  $\triangle ABC$  below. (Leave all construction marks.)



9. With a compass and straightedge, construct a square inscribed in circle P. (Leave all construction marks.)



10. A(3,1) is one endpoint of  $\overline{AB}$ . The segment's midpoint is M(7,6). Find the other endpoint, B.

- 11. The line l has the equation  $y = -\frac{3}{2}x 7$ .
  - (a) What is the slope of the line k, given  $k \parallel l$ ?
  - (b) What is the slope of the line m, given  $m \perp l$ ?
- 12. Given P(-2,9) and Q(3,-3), find the length of  $\overline{PQ}$ .

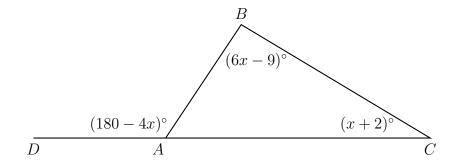
- 13. Apply the translation  $(x,y) \to (x-2,y+4)$  to the point A(2,-1).
- 14. What is the image of B(2,7) under a reflection across the x-axis?
- 15. State the translation that would map C(-3,1) onto C'(4,0).

16. A translation maps  $D(1,9) \to D'(4,3)$ . What is the image of E(6,-2) under the same translation?

17. The image of triangle ABC after a translation is  $\triangle A'B'C'$ . Is the area of the triangle greater, smaller, or the same after the translation? Justify your answer.

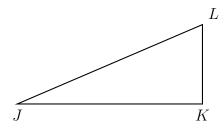
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18. In  $\triangle ABC$  shown below, side  $\overline{AC}$  is extended to point D with  $m \angle DAB = (180 - 4x)^{\circ}$ ,  $m \angle C = (x+2)^{\circ}$ , and  $m \angle B = (6x-9)^{\circ}$ .

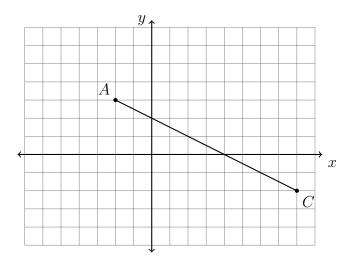


What is  $m \angle BAC$ ?

19. Given right  $\triangle JKL$  with  $\overline{JK} \perp \overline{KL}$ , JL=9,  $m\angle J=32^{\circ}$ . Find the length JK, rounded to the nearest thousandth.

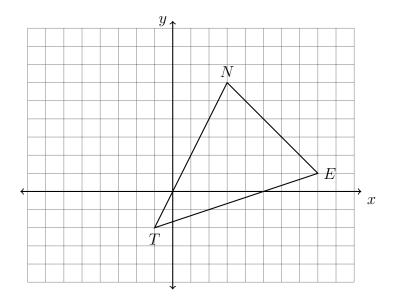


20. Spicy: In the diagram below,  $\overrightarrow{AC}$  has endpoints with coordinates A(-2,3) and C(8,-2).



If B is a point on  $\overline{AC}$  and AB:BC=2:3, what are the coordinates of B?

21. Spicy: Triangle  $\triangle DAN$  is graphed on the set of axes below. The vertices of  $\triangle DAN$  have the coordinates T(-1,-2), E(8,1), and N(3,6).



- (a) Draw an altitude through point N perpendicular to  $\overline{TE}$ .
- (b) What is the length of the altitude drawn through N?

(c) What is the length of the base, TE?

(d) Find the area of  $\triangle DAN$ .