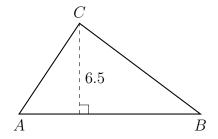
Part 1, Solid Geometry: Volume & Density

1. Find the area of a semi-circle with diameter 8. Round to the nearest tenth.

2. Find the volume of a cylindrical tank with radius of 6 feet and a height of 8 feet, to the nearest cubic foot.

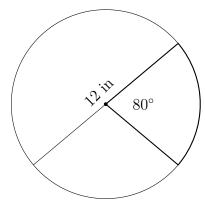
3. A box in the shape of a rectangular prism has a volume of 60 cubic feet. It's length is 5 feet and width 3 feet. How tall is it?

4. The area of $\triangle ABC$ is 68.25 square inches. The altitude of the triangle is 6.5 inches. Find the length of the base AB.

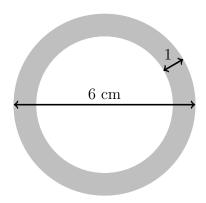


5. Find the weight of a steel ball with a diameter of 1.2 inches, to the *nearest tenth of an ounce*. (The density of steel is 4.6 ounce per cubic inch)

6. A circle with a diameter of 12 in and a central angle of 80° is drawn below. What is the area of the sector formed by the 80° angle, to the nearest tenth of a square inch?

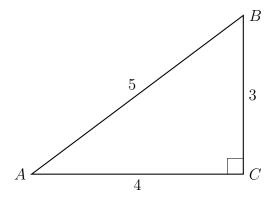


7. A bakery sells hollow chocolate spheres. The outer diameter of each sphere is 6 cm. The thickness of the chocolate of each sphere is 1 cm. Determine and state, to the nearest tenth of a cubic centimeter, the amount of chocolate in each hollow sphere.



- 8. A right cylinder is cut horizontally. The shape of the cross section is a
 - (a) circle
 - (b) cylinder
 - (c) rectangle
 - (d) triangular prism
- 9. Which three-dimensional figure will result when a right triangle 8 inches tall and 3 inches wide is continuously rotated about the longer side?
 - (a) a cone with a height of 6 inches and radius of 8 inches
 - (b) a cone with a height of 8 inches and diameter of 6 inches
 - (c) a cylinder with a radius of 8 inches and a height of 6 inches
 - (d) a cylinder with a diameter of 6 inches and a height of 8 inches

10. $\triangle ABC$ is shown with $m\angle C=90^\circ$ and the lengths of the triangle's sides are BC=3, AC=4, and AB=5.

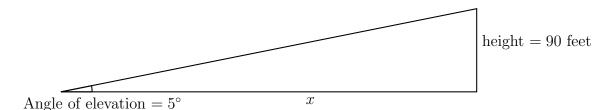


- (a) State, as a decimal, the value of $\sin A$.
- (b) Find the measure of $\angle A$, to the nearest degree.
- (c) Find the degree measure of $\angle B$.
- 11. Express each trigonometric ratio to the *nearest thousandth* and each angle measure to the nearest degree.

(a)
$$\sin 55^{\circ} =$$

(b)
$$\cos^{-1} 0.766 =$$

12. A sailor observes the top of a lighthouse with an angle of elevation of 5° . She knows the lighthouse is 90 feet tall. Determine and state the distance x between the sailor and the lighthouse, to the *nearest foot*.



13. Solve for the value of x.

$$\frac{1}{3}(4x+1) = 3$$

14. Given $f(x) = \frac{3}{2}x - 5$. Solve for x such that for f(x) = 1.

15. Given $g(x) = 2x^2 - 3x + 2$. Simplify g(0).

16. Given $h(x) = x^2 + 8x + 7$. Solve h(x) = 0.

17. Simplify each expression. (Leave it in radical form if necessary, not a decimal.)

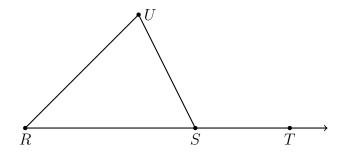
(a)
$$\sqrt{18}$$

(b)
$$\sqrt{\frac{81}{16}}$$

Part 2, Solid Geometry: Volume & Density

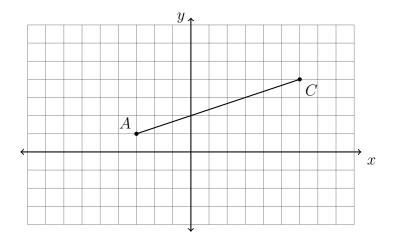
- 18. The line l has the equation $y = \frac{2}{3}x + 7$. To each line below, circle whether l is parallel, perpendicular, or neither.
 - (a) parallel perpendicular neither $y = \frac{2}{3}x 2$
 - (b) parallel perpendicular neither $y = \frac{3}{2}x + 7$
 - (c) parallel perpendicular neither $y = -\frac{2}{3}x + 5$
 - (d) parallel perpendicular neither 3x + 2y = 6

- 19. Write an equation of the line that is parallel to the line whose equation is $y = \frac{1}{3}x + 4$ and passes through the point (4, -1).
- 20. Given $m \angle R = 30$ and $m \angle U = 70$. Find $m \angle UST$.



- 21. Write down the center and radius of each circle.
 - (a) $(x+1)^2 + (y+3)^2 = 1$
- (b) $x^2 + (y-4)^2 = 25$

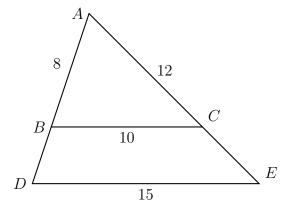
22. In the diagram below, \overline{AC} has endpoints with coordinates A(-3,1) and C(6,4).



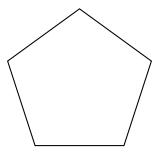
If B is a point on \overline{AC} and AB:BC=2:1, what are the coordinates of B?

23. Triangle ABC is dilated with a scale factor of k centered at A, yielding $\triangle ADE$, as shown. Given AB=8, BC=10, AC=12, and DE=15.

Find BD, AE, and k (the scale factor).

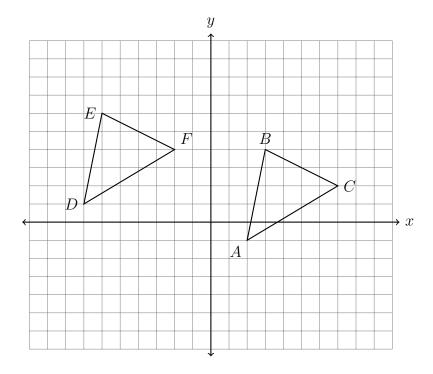


24. What is the smallest non-zero angle of rotation about its center that would map the pentagon onto itself?

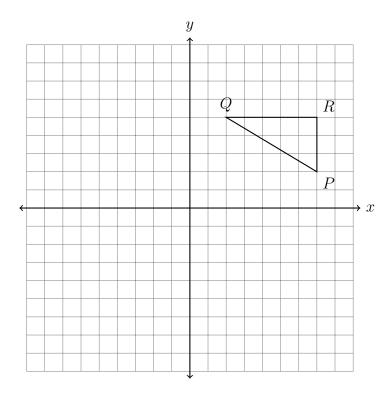


25. A translation maps $A(-1,4) \to A'(-2,14)$. What is the image of B(-4,-7) under the same translation?

26. What transformation maps $\triangle ABC$ onto $\triangle DEF$, shown below? Fully specify the transformation.



27. Reflect $\triangle PQR$ across the x-axis, drawing its image $\triangle P'Q'R'$ and labeling its vertices.

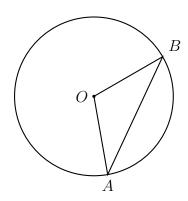


28. In a right triangle, the acute angles have the relationship $\sin x = \cos 30$. Find x.

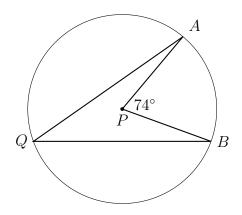
29. If $\sin(2x-8)^{\circ} = \cos 42^{\circ}$, what is the value of x?

30. Find the distance between (0,5) and (6,-3).

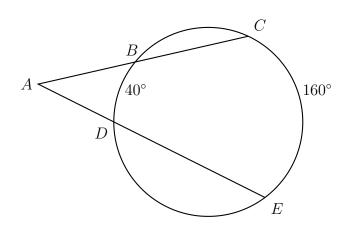
31. Given circle O with inscribed $\triangle AOB$. $m\angle O=110$. Find $m\angle A$.



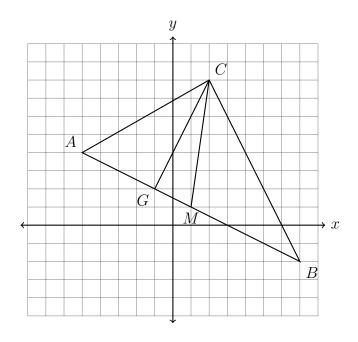
- 32. Given circle P with $m \angle APB = 74^{\circ}$.
 - (a) Write down the \widehat{mAB} .
 - (b) Find the $m \angle AQB$.



33. The secants \overline{ABC} and \overline{ADE} intersect the circle O, as shown in the diagram. Given $\widehat{mBD}=40^\circ$ and $\widehat{mCE}=160^\circ$. Find the $m\angle A$.



34. On the set of axes below, $\triangle ABC$, altitude \overline{GC} , and median \overline{MC} are drawn.



Determine which equations represent the area of the triangle, circling True or False.

(a) T F
$$Area_{\triangle} = \frac{(CG)(AB)}{2}$$
 (c) T F $Area_{\triangle} = \frac{(AC)(AB)}{2}$

(c) T F
$$Area_{\triangle} = \frac{(AC)(AB)}{2}$$

(b) T F
$$Area_{\triangle} = \frac{(CM)(AB)}{2}$$

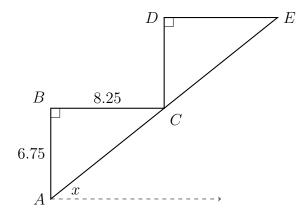
(b) T F
$$Area_{\triangle} = \frac{(CM)(AB)}{2}$$
 (d) T F $Area_{\triangle} = \frac{(CG)(BC)}{2}$

35. The point M(3,7) is the midpoint of \overline{AB} . If the coordinates of A are (2,10), find B.

36. A monument in the shape of a pyramid with a square base has a volume of 128 cubic feet. If its height measures 6 feet, what is the length of the side of the base?

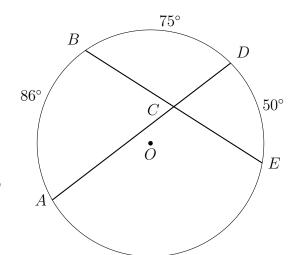
Early finishers

- 37. A staircase riser is cut as a series of congruent triangles with each step's "rise" equal to 6.75 inches, and the "run" of each step is 8.25 inches, as shown below. (AB=6.75 and BC=8.25)
 - (a) What is the angle of inclination of the staircase, x, rounded to the nearest degree?



(b) Find the diagonal length of the two-step riser, the distance AE, to the nearest tenth of an inch.

- 38. Given circle O with chords \overline{AD} and \overline{BE} intersecting at C, as shown in the diagram. Given $\widehat{mAB} = 86^{\circ}$, $\widehat{mBD} = 75^{\circ}$, and $\widehat{mDE} = 50^{\circ}$.
 - (a) Find the $m \angle ACB$.



(b) Find the measure of the minor arc, \widehat{mAE} .