

Module 03

### Module 03: CS31003: Compilers:

Syntax Analysis or Parsing

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### Module Objectives

Module 03

Objectives & Outline

Understand Parsing Fundamental

Understand LR Parsing



### Module Outline

Module 03

#### Objectives & Outline

- Objectives & Outline
- $Infix \rightarrow Postfix$
- Grammar
  - Derivations
  - Parsing Fundamentals
- **RD Parsers** 
  - Left-Recursion
  - Ambiguous Grammar
- Shift-Reduce Parser
  - SR Parsers
  - LR Fundamentals
  - LR(0) Parser
  - SLR(1) Parser
  - LR(1) Parser
  - LALR(1) Parser



Module 03

 $Infix \rightarrow$ Postfix

# Infix $\rightarrow$ Postfix



### Resolving Ambiguity by Infix $\rightarrow$ Postfix

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Objectives & Outline

 $\begin{array}{c} \mathsf{Infix} \to \\ \mathsf{Postfix} \end{array}$ 

Gramm: Derivation

Parsing Fundamenta

Left-Recursion

Ambiguous Gramma

LR Parser

LR Fundamentals

LR(0) Parser

SLR(1) Pars LR(1) Parse

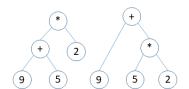
LR(1) Parser LALR(1) Pars Let us recap what we did in PDS:

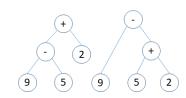
$$9 + 5 * 2 =$$
 $((9 + 5) * 2) = 28$ 
 $(9 + (5 * 2)) = 19$ 

$$9 - 5 + 2 =$$

$$((9 - 5) + 2) = 6$$

$$(9 - (5 + 2)) = 2$$







### Expression Ambiguity Resolution: Infix $\rightarrow$ Postfix

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 $\begin{array}{c} \mathsf{Infix} \to \\ \mathsf{Postfix} \end{array}$ 

Grammar Derivations Parsing

RD Parsers

Left-Recursion

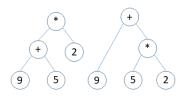
LR Parsers

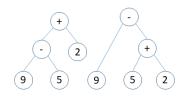
LR Fundamentals

LR(0) Parser SLR(1) Parser LR(1) Parser LALR(1) Parser 9 + 5 \* 2 = (9 + (5 \* 2)) = 9 5 2 \* + ((9 + 5) \* 2) = 9 5 + 2 \*

$$9 - 5 + 2 = (9 - (5 + 2)) = 9 \cdot 5 \cdot 2 + -$$
  
 $((9 - 5) + 2) = 9 \cdot 5 - 2 +$ 

Postfix notation is also called Reverse Polish Notation (RPN)







### Associativity and Precedence

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Infix -> Postfix

### **Operators**

- \*, / (left)
- +, (left)
- <,  $\le$ , >,  $\ge$  (left)
- ! =, == (left)
- = (right)



### $Infix \rightarrow Postfix: Examples$

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 $Infix \rightarrow$ Postfix

Infix	Postfix
A + B	A B +
A + B * C	A B C * +
(A + B) * C	A B + C *
A + B * C + D	A B C * + D +
(A + B) * (C + D)	A B + C D + *
A * B + C * D	A B * C D * +



### Infix $\rightarrow$ Postfix: Rules

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 $\begin{array}{c} \mathsf{Infix} \to \\ \mathsf{Postfix} \end{array}$ 

Grammar

Derivations

Parsing

Fundamentals

RD Parsers

Left-Recursion

Ambiguous Gramma

LR Parsers

SR Parsers

LR Fundamentals

LR(0) Parser

SLR(1) Parser

LR(1) Parser

- Print operands as they arrive.
- If the stack is empty or contains a left parenthesis on top, push the incoming operator onto the stack.
- If the incoming symbol is a left parenthesis, push it on the stack.
- If the incoming symbol is a right parenthesis, pop the stack and print the operators until you see a left parenthesis. Discard the pair of parentheses.
- If the incoming symbol has higher precedence than the top of the stack, push it on the stack.
- If the incoming symbol has equal precedence with the top of the stack, use association. If the association is left to right, pop and print the top of the stack and then push the incoming operator. If the association is right to left, push the incoming operator.
- If the incoming symbol has lower precedence than the symbol on the top of the stack, pop the stack and print the top operator. Then test the incoming operator against the new top of stack.
- At the end of the expression, pop and print all operators on the stack. (No parentheses should remain.)



### Operator Precedence Table

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 $Infix \rightarrow$ Postfix

	Input									
	\$	+	_	*	/	(	)			
\$		«	«	«	«	«				
+	>>	>>	>>	«	«	«	>>			
_	>>	>>	>>	«	«	«	>>			
*	>>	>>	>>	>>	>>	«	>>			
/	>>	>>	>>	>>	>>	«	>>			
(	«	«	«	«	«	«	=			
)										



### $Infix \rightarrow Postfix$ : Rules

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Infix -> Postfix

- Requires operator precedence information
- **Operands**: Add to postfix expression.
- Close parenthesis: Pop stack symbols until an open parenthesis appears.
- Operators: Pop all stack symbols until a symbol of lower precedence appears. Then push the operator.
- End of input: Pop all remaining stack symbols and add to the expression.



### Infix $\rightarrow$ Postfix: Rules

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 $\begin{array}{c} \mathsf{Infix} \to \\ \mathsf{Postfix} \end{array}$ 

Gramma

Parsing Fundamentals

Left-Recursion
Ambiguous Grammar

LR Parser

LR Fundamentals

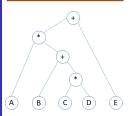
LR(0) Parser
SLR(1) Parser
LR(1) Parser

Expression:

A \* (B + C \* D) + E

becomes

A B C D \* + \* E +



	Current symbol	Operator Stack	Postfix string
- 1	A		A
2	*	*	Α
3	(	* (	A
4	В	* (	A B
5	+	* ( +	A B
6	С	* ( +	ABC
7	*	* ( + *	ABC
8	D	* ( + *	ABCD
9	)	液	A B C D * +
10	+	+	A B C D * + *
-11	E	+	A B C D * + * E
12			A B C D * + * E +

12



### **Evaluating Postfix Expression**

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Objectives & Outline

 $\begin{array}{c} \mathsf{Infix} \to \\ \mathsf{Postfix} \end{array}$ 

Grammar
Derivations
Parsing
Fundamentals

RD Parsers

Left-Recursion

Ambiguous Grammar

LR Parser

LR Fundamentals
LR(0) Parser

LR(0) Parser SLR(1) Parser LR(1) Parser

- Create a stack to store operands (or values)
- Scan the given expression and do following for every scanned element
  - If the element is a number, push it into the stack
  - If the element is a operator, pop operands for the operator from stack. Evaluate the operator and push the result back to the stack
- When the expression is ended, the number in the stack is the final answer



#### Module 03

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Objectives & Outline

Infix — Postfix

#### Grammar

Derivations

Parsing

Fundamentals

Left-Recursion

#### LR Parsers

SR Parsers

LR Fundamenta

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LR(1) Parser

LALR(1) Parse

# **Grammar**



### Grammar

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Grammar

 $G = \langle T, N, S, P \rangle$  is a (context-free) grammar where:

: Set of terminal symbols

: Set of non-terminal symbols :  $S \in N$  is the start symbol

Set of production rules

Every production rule is of the form:  $A \to \alpha$ , where  $A \in N$  and  $\alpha \in (N \cup T)^*$ .

Symbol convention:

a. b. c. · · · Lower case letters at the beginning of alphabet  $\in T$ ∈ T+  $x, y, z, \cdots$ Lower case letters at the end of alphabet  $A, B, C, \cdots$ Upper case letters at the beginning of alphabet  $\in N$ 

 $X, Y, Z, \cdots$ Upper case letters at the end of alphabet

 $\alpha, \beta, \gamma, \cdots$ 

Greek letters

 $\in (N \cup T)$ 

 $\in (N \cup T)^*$ 



### Example Grammar: Derivations

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Derivations

 $G = <\{id, +, *, (, )\}, \{E, T, F\}, E, P > where P is:$ 

1:  $E \rightarrow E + T$ 

2:  $E \rightarrow T$ 3:  $T \rightarrow T*F$ 

4:  $T \rightarrow F$ 5:  $F \rightarrow (E)$ 

Left-most Derivation of id + id \* id \*:

Right-most Derivation of id + id \* id \*:



### Example Grammar: Derivations

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Derivations

 $G = <\{id, +, *, (, )\}, \{E, T, F\}, E, P > where P is:$ 

1:  $E \rightarrow E + T$ 

2:  $E \rightarrow T$ 3:  $T \rightarrow T*F$ 

4:  $T \rightarrow F$ 5:  $F \rightarrow (E)$ 

Left-most Derivation of id \* id + id \$:

Right-most Derivation of id \* id + id \$:



### Parsing Fundamentals

Module 03	Derivation Parsing		Parser	Remarks		
I Sengupta & P P Das	Left-most	Top-Down	Predictive: Recursive Descent,	No Ambiguity No Left-recursion		
Objectives & Outline			LL(1)	Tool: Antlr		
Infix → Postfix	Right-most	Bottom-Up	Shift-Reduce: SLR,	Ambiguity okay Left-recursion okay		
			LALR(1), LR(1)	Tool: YACC, Bison		

Parsing Fundamentals



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Objectives & Outline

Infix → Postfix

Grammar

Derivations

Fundamen

#### RD Parsers

Left-Recursion

LR Parsers

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LR Fundamenta

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LR(1) Parser

LALR(1) Parse



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Objectives & Outline

 $\begin{array}{c} \mathsf{Infix} \to \\ \mathsf{Postfix} \end{array}$ 

Gramm

Parsing

#### RD Parsers

Left-Recursion

Ambiguous Grammar

LR Parsers

LR Fundamentals

LR(0) Parser

LR(0) Parser SLR(1) Parser LR(1) Parser LALR(1) Parser

```
ab | a
int main() {
    1 = getchar();
    S(): // S is a start symbol
    // Here l is lookahead. If l = $, it represents the end of the string
    if (1 == '$')
        printf("Parsing Successful"):
    else printf("Error");
S() { // Definition of S, as per the given production
    match('c');
    A():
    match('d'):
A() { // Definition of A as per the given production
    match('a'):
    if (1 == 'b') { // Look-ahead for decision
        match('b');
match(char t) { // Match function - matches and consumes
    if (1 == t) { 1 = getchar():
    else printf("Error");
}
Check with: cad$ (S \Rightarrow cAd \Rightarrow cad), cabd$ (S \Rightarrow cAd \Rightarrow cabd), caad$
```



c A d

Module 03

```
aAb | a
int main() {
    1 = getchar();
    S(): // S is a start symbol.
    // Here l is lookahead. if l = $, it represents the end of the string
    if (1 == '$')
        printf("Parsing Successful"):
    else printf("Error");
S() { // Definition of S, as per the given production
    match('c');
    A():
    match('d'):
A() { // Definition of A as per the given production
    match('a'):
    if (1 == 'a') { // Look-ahead for decision
        A():
        match('b'):
match(char t) { // Match function - matches and consumes
    if (1 == t) { 1 = getchar():
    else printf("Error");
}
Check with: cad$ (S \Rightarrow cAd \Rightarrow cad), cabd$, caabd$ (S \Rightarrow cAd \Rightarrow caAbd \Rightarrow caabd)
Compilers
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```



a E'

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```
+ a E' \mid \epsilon
int main() {
    1 = getchar():
    E(): // E is a start symbol.
    // Here l is lookahead. If l = $, it represents the end of the string
    if (1 == '$') printf("Parsing Successful");
    else printf("Error"):
E() { // Definition of E, as per the given production
    match('a'):
    E'():
E'() { // Definition of E' as per the given production
    if (1 == '+') { // Look-ahead for decision
         match('+'):
         match('a');
         E'():
    else return (); // epsilon production
match(char t) { // Match function - matches and consumes
    if (1 == t) { 1 = getchar();
    else printf("Error"):
}
Check with: a$ (E \Rightarrow aE' \Rightarrow a), a+a$ (E \Rightarrow aE' \Rightarrow a + aE' \Rightarrow a + a), a+a+a$
(E \Rightarrow aE' \Rightarrow a + aE' \Rightarrow a + aE' \Rightarrow a + a + a)
```



Module 03

```
F
           E + E \mid a
       \rightarrow
int main() {
   1 = getchar();
   E(): // E is a start symbol.
   // Here 1 is lookahead. if 1 = $, it represents the end of the string
   if (1 == '$')
        printf("Parsing Successful");
    else printf("Error");
E() { // Definition of E as per the given production
    if (1 == 'a') { // Terminate ? -- Look-ahead does not work
        match('a');
   E();
                   // Call ?
   match('+'):
   E():
match(char t) { // Match function - matches and consumes
    if (1 == t) { 1 = getchar():
    else printf("Error");
}
Check with: a+a$, a+a+a$
```



### Curse or Boon 1: Left-Recursion

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Left-Recursion

A grammar is left-recursive iff there exists a non-terminal A that can derive to a sentential form with itself as the leftmost symbol. Symbolically,

$$A \Rightarrow^+ A\alpha$$

We cannot have a recursive descent or predictive parser (with left-recursion in the grammar) because we do not know how long should we recur without consuming an input



### Curse or Boon 1: Left-Recursion

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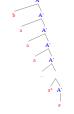
Left-Recursion

Note that, leads to:

> A \$  $A\alpha\alpha\alpha$  \$ Ann \$  $A\alpha^*$  \$  $\beta\alpha^*$  \$

Removing left-recursion leads to:

 $\beta\alpha\alpha A'$  \$ A \$  $\beta \alpha A'$  \$  $\beta\alpha^*$  \$





### Left-Recursive Example

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Left-Recursion

### Grammar $G_1$ before Left-Recursion Removal

1:

4: 5.

(E)

### Grammar $G_2$ after Left-Recursion Removal

T E'

+ T F'

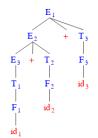
 $\epsilon$ 

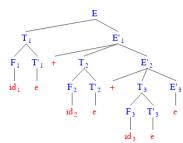
 $\epsilon$ 

(E)

These are syntactically equivalent. But what happens semantically?

- Can left recursion be effectively removed?
- What happens to Associativity?







### Curse or Boon 2: Ambiguous Grammar

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Infix — Postfix

Gramma

Derivations
Parsing
Fundamentals

Left-Recursion

Ambiguous Grammar

LR Parser

LR Fundamentals

LR(0) Parser

LR(1) Parser

1:  $E \rightarrow E + E$ 

2: *E* → *E* \* *E* 

3:  $E \rightarrow (E)$ 

4:  $E \rightarrow id$ 

Ambiguity simplifies. But, ...

Associativity is lost

Precedence is lost

 $\bullet \ \ \mathsf{Can} \ \ \mathit{Operator} \ \mathit{Precedence} \ (\mathit{infix} \rightarrow \mathit{postfix}) \ \mathsf{give} \ \mathsf{us} \ \mathsf{a} \ \mathsf{clue} ?$ 



### Ambiguous Derivation of id + id \* id

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Ambiguous Grammar

Correct derivation: \* has precedence over +

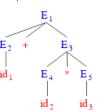
$$E \$ \Rightarrow \underline{E + E} \$$$

$$\Rightarrow E + \underline{E} * \underline{E} \$$$

$$\Rightarrow E + E * \underline{id} \$$$

$$\Rightarrow E + \underline{id} * \underline{id} \$$$

$$\Rightarrow \underline{id} + \underline{id} * \underline{id} \$$$



Wrong derivation: + has precedence over \*

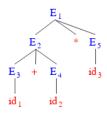
$$E \$ \Rightarrow \underline{E * E} \$$$

$$\Rightarrow E * \underline{id} \$$$

$$\Rightarrow \underline{E + E} * \underline{id} \$$$

$$\Rightarrow E + \underline{id} * \underline{id} \$$$

$$\Rightarrow \underline{id} + \underline{id} * \underline{id} \$$$





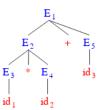
### Ambiguous Derivation of id \* id + id

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Ambiguous Grammar

Correct derivation: \* has precedence over +

$$\begin{array}{ccc} E \$ & \Rightarrow & \underline{E+E} \$ \\ \Rightarrow & \overline{E+\underline{id}} \$ \\ \Rightarrow & \underline{E*E} + \underline{id} \$ \\ \Rightarrow & \underline{E*\underline{id}} + \underline{id} \$ \\ \Rightarrow & \underline{\underline{id}} * \underline{id} + \underline{id} \$ \end{array}$$



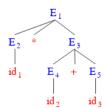
Wrong derivation: + has precedence over \*

$$E \$ \Rightarrow \underline{E * E} \$$$

$$\Rightarrow E * \underline{E + E} \$$$

$$\Rightarrow E * \underline{id} * \underline{id} + \underline{id} \$$$

$$\Rightarrow \underline{id} * \underline{id} + \underline{id} \$$$





### Remove: Ambiguity and Left-Recursion

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Ambiguous Grammar

E + E

E \* E 3: (E)

Ыi

Removing ambiguity:

1: Ε E + T

Ε Т

T \* F

5: (E)

id

Removing left-recursion:

1. Ε TF'

2|3:  $+ T E' \mid \epsilon$ 4. F T'

 $*FT' \mid \epsilon$ 5|6:

7: (E)

8: id



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#### LR Parsers

## LR Parsers



### Shift-Reduce Parser: Example: Grammar

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SR Parsers

### Sample grammar $G_1$ :

1:  $E \rightarrow E + T$ 

5:  $F \rightarrow (E)$ 



### Shift-Reduce Parser: Example: Parse Table

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SR Parsers

State	Action							GO TO		
	id	+	*	( )		\$	Ε	T	F	
0	s5			s4			1	2	3	
1		s6				acc				
2		r2	s7		r2	r2				
3		r4	r4 r4			r4				
4	s5			s4			8	2	3	
5		r6	r6		r6	r6				
6	s5			s4				9	3	
7	s5			s4					10	
8		s6			s11					
9		r1	s7		r1	r1				
10		r3	r3		r3	r3				
11		r5	r5		r5	r5				



# Shift-Reduce Parser: Example: Parsing id \* id + id

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Objectives & Outline

 $\begin{array}{c} \mathsf{Infix} \to \\ \mathsf{Postfix} \end{array}$ 

Gramma Derivations Parsing

RD Parsers

Left-Recursion

Ambiguous Grammar

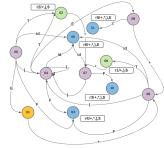
LR Parsers

SR Parsers

LR Fundamentals
LR(0) Parser
SLR(1) Parser

LR(0) Parser SLR(1) Parser LR(1) Parser LALR(1) Parser

Step	Stack	Symbols	Input	Act.
(1)	0		id * id + id \$	s5
(2)	0 5	id	* id + id \$	r6
(3)	0 3	F	* id + id \$	r4
(4)	0 2	T	* id + id \$	s7
(5)	027	T *	id + id \$	s5
(6)	0275	T * id	+ id \$	r6
(7)	0 2 7 10	T * F	+ id \$	r3
(8)	0 2	T	+ id \$	r2
(9)	0 1	E	+ id \$	s6
(10)	016	E +	id \$	s5
(11)	0165	E + id	\$	r6
(12)	0163	E + F	\$	r4
(13)	0169	E + T	\$	r1
(14)	0 1	E	\$	acc



()				T 122								
1: E -	→ E +	т	State	itate Action				(	GO TO	)		
	$\rightarrow$ $T$	•		id	+	*	(	)	\$	E	T	F
	→ T * I	E	0	s5			s4			1	2	3
4: T -	→ F		1		s6				acc			
5: F -	→ (E)		2		r2	s7		r2	r2			
6: F -	→ id ´		3		r4	r4		r4	r4			
E \$ ⇒	E + T\$		4	s5			s4			8	2	3
$\Rightarrow$	$\overline{E+F}$ \$		5		r6	r6		r6	r6			
$\Rightarrow$	$E + \underline{id} \$$		6	s5			s4				9	3
$\Rightarrow$	$\underline{T}$ + id \$		7	s5			s4					10
$\Rightarrow$	T * F +		- 8		s6			s11				
$\Rightarrow$	T * <u>id</u> +		9		r1	s7		r1	r1			
$\Rightarrow$	<u>F</u> * id +		10		r3	r3		r3	r3			
$\Rightarrow$	<u>id</u> * id +	id \$	11		r5	r5		r5	r5			
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LR Fundamentals

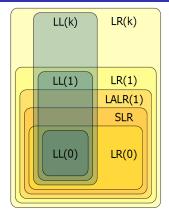
### **LR** Parsers LR Fundamentals



### LR Parsing: CFG Classes

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LR Fundamentals



- LL(k), Top-Down, Predictive: LL parser (Left-to-right, Leftmost derivation) with k look-ahead
- LR(k), Bottom-Up, Shift-Reduce: LR parser (Left-to-right, Rightmost derivation) with k look-ahead



## **IR** Parsers

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LR Fundamentals

- LR parser (Left-to-right, Rightmost derivation in reverse)
- Reads input text from left to right without backing up
- Produces a rightmost derivation in reverse
- Performs bottom-up parse
- To avoid backtracking or guessing, an LR(k) parser peeks ahead at k look-ahead symbols before deciding how to parse earlier symbols. Typically k is 1
- LR parsers are deterministic produces a single correct parse without guesswork or backtracking
- Works in linear time
- Variants of LR parsers and generators:
  - LP(0) Parsers
  - SLR Parsers
  - LALR Parsers Generator: Yacc (AT & T), Byacc (Berkeley Yacc)
  - Canonical LR(1) or CLR Parsers Generator: Bison (GNU)
  - Minimal LR(1) Parsers Generator: Hyacc (Hawaii Yacc)
  - GLR Parsers Generator: Bison (GNU) with %glr-parser declaration
- Minimal LR and GLR parsers have better memory performance CLR Parsers and address reduce/reduce conflicts more effectively

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## **Handles**

Compilers

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LR Fundamentals

- If  $S \Rightarrow_{rm}^+ \alpha$  then  $\alpha$  is called a **right sentential form**
- A handle of a right sentential form is:
  - A substring  $\beta$  that matches the RHS of a production  $A \to \beta$
  - The reduction of  $\beta$  to A is a step along the reverse of a rightmost derivation
- If  $S \Rightarrow_{rm}^+ \gamma Aw \Rightarrow_{rm} \gamma \beta w$  where w is a sequence of tokens then
  - The substring  $\beta$  of  $\gamma\beta w$  and the production  $A \to \beta$  make the handle
- Consider the reduction of id \* id + id to the start symbol E:

	Sentential Form	Production
	<u>id</u> * id + id \$	F  o id
$\Rightarrow$	$\underline{F}$ * id $+$ id \$	T  o F
$\Rightarrow$	$T * \underline{id} + id $ \$	F  o id
$\Rightarrow$	T * F + id \$	$T \rightarrow T * F$
$\Rightarrow$	$\underline{\mathcal{T}} + id \$$	E  o T
$\Rightarrow$	$E + \underline{id} \$$	${\sf F}  o {\sf id}$
$\Rightarrow$	<i>E</i> + <i><u>F</u> \$</i>	T  o F
$\Rightarrow$	E + T \$	$E \rightarrow E + T$
$\Rightarrow$	E \$	

• LR Parsing is about Handle Pruning - Start with the sentence, identify handle, reduce — till the start-symbol is reached



## LR Parsers

Module 03

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Objectives & Outline

Infix  $\rightarrow$  Postfix

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Left-Recursion

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LR Parsers SR Parsers

LR Fundamentals

LR(0) Parser SLR(1) Parser LR(1) Parser LALR(1) Parser

- An LR parser is a DPDA having:
  - An Input Buffer
  - A Stack of Symbols terminals as well as non-terminals
  - A DFA that has four types of actions:
    - Shift Target state on input symbol
    - Reduce Production rule and Target state on non-terminal on reduction (GOTO actions)
    - Accept Successful termination of parsing
    - Reject Failure termination of parsing
- The parser operates by:
  - Shifting tokens onto the stack
  - $\bullet$  When a handle  $\beta$  is on top of stack, parser reduces  $\beta$  to LHS of production
  - Parsing continues until an error is detected or input is reduced to start symbol
- Designing an LR Parser is all about designing its DFA and actions



### Module 03

LR(0) Parser

# **LR** Parsers LR(0) Parser



## FIRST and FOLLOW

Module 03

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LR(0) Parser

SLR(1) Parser

•  $FIRST(\alpha)$ , where  $\alpha$  is any string of grammar symbols, is defined to be the set of terminals that begin strings derived from  $\alpha$ . If  $\alpha \Rightarrow^* \epsilon$ , then  $\epsilon$  is also in  $FIRST(\alpha)$ . Examples:

• Given  $S \to 0|A, A \to AB|1, B \to 2$ ;  $FIRST(B) = \{2\}, FIRST(A) = \{1\}, FIRST(S) = \{0, 1\}$ 

• Given  $E \rightarrow E + E|E * E|(E)|id$ ;  $FIRST(E) = \{id, (\}$ 

• Given  $B \rightarrow A, A \rightarrow Ac|Aad|bd|\epsilon$ ;  $FIRST(B) = FIRST(A) = \{\epsilon, a, b, c\}$ 

• FOLLOW(A), for non-terminal A, is defined to be the set of terminals a that can appear immediately to the right of A in some sentential form; that is, the set of terminals a such that there exists a derivation of the form  $S \Rightarrow^* \alpha A a \beta$ , for some  $\alpha$  and  $\beta$ . \$ can also be in the FOLLOW(A). Examples:

Given E → E + E|E \* E|(E)|id;
 FOLLOW(E) = {+, \*, ),\$}

• Given  $B \rightarrow A$ ,  $A \rightarrow Ac|Aad|bd|\epsilon$ ;  $FOLLOW(B) = \{\$\}$ ,  $FOLLOW(A) = \{a, c, \$\}$ 



# LR(0) Parser Construction

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LR Fundamentals

LR(0) Parser

SLR(1) Parser

SLR(1) Parser LR(1) Parser

- LR(0) grammars can be parsed looking only at the stack
- Making shift/reduce decisions without any look-ahead token
- Based on the idea of an item or a configuration
- An LR(0) item consists of a production and a dot

$$A \to X_1 \cdots X_i \bullet X_{i+1} \cdots X_n$$

- The dot symbol may appear anywhere on the right-hand side
  - Marks how much of a production has already been seen
  - $X_1 \cdots X_i$  appear on top of the stack
  - $X_{i+1} \cdots X_n$  are still expected to appear
- An LR(0) state is a set of LR(0) items
  - It is the set of all items that apply at a given point in parse



# LR(0) Parser Construction

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LAIR(1) Parser

Sample Grammar,  $G_6$  Augmented Grammar,  $G_6$ 

- 4:  $L \rightarrow L, S$  4:  $L \rightarrow L, S$
- LR(0) Item: An LR (0) item is a production in G with dot at some position on the right side of the production. Examples: S → .(L), S → (.L), S → (L), S → (L).
- Closure: Add all items arising from the productions from the non-terminal after the period in an item. Closure is computed transitively. Examples:
  - Closure( $S \rightarrow .(L)$ ) = { $S \rightarrow .(L)$ } • Closure( $S \rightarrow (.L)$ ) = { $S \rightarrow (.L)$ ,  $L \rightarrow .S$ ,  $L \rightarrow .L$ , S,  $S \rightarrow .x$ ,  $S \rightarrow .(L)$ }
- State: Collection of LR(0) items and their closures. Examples:
  - $\begin{array}{l} \bullet \quad \{S' \rightarrow .S, S \rightarrow .x, S \rightarrow .(L)\} \\ \bullet \quad \{S \rightarrow (.L), L \rightarrow .S, L \rightarrow .L, S, S \rightarrow .x, S \rightarrow .(L)\} \end{array}$
- Actions: Shift (s#), Reduce (r#), Accept (acc), Reject (' '), GOTO (#):
  - Shift on input symbol to state# (dot precedes the terminal to shift)
  - Reduction on all input symbols by production# (dot at the end of a production)
  - lacktriangle Accept on reduction by the augmented production S' o S
  - Reject for blank entries cannot be reached for a valid string
  - GOTO on transition of non-terminal after reduction (dot precedes the non-terminal to reduce to)

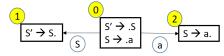


Module 03

LR(0) Parser

•  $G_3 = \{S \to a\}$ 





State	а	\$	S
0	s2		1
1		Acc	
2	r1	r1	

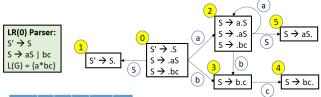




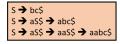
Module 03

LR(0) Parser

•  $G_4 = \{S \rightarrow aS | bc\}$ 



State	а	b	С	\$	S
0	s2	s3			1
1				Acc	
2	s2	s3			5
3			s4		
4	r2	r2	r2	r2	
5	r1	r1	r1	r1	





Module 03

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Objectives & Outline

 $\begin{array}{c} \mathsf{Infix} \to \\ \mathsf{Postfix} \end{array}$ 

Grammar Derivations Parsing Fundamenta

RD Parsers

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LR(0) Parser
SLR(1) Parser
LR(1) Parser

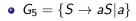
 $\textit{G}_{4} = \{\textit{S} \rightarrow \textit{a} \; \textit{S} \; | \; \textit{b} \; \textit{c} \; \}. \; \textit{S}' \; \$ \Rightarrow \textit{S} \; \$ \Rightarrow \textit{a} \; \textit{S} \; \$ \Rightarrow \textit{a} \; \textit{a} \; \textit{S} \; \$ \Rightarrow \textit{a} \; \textit{a} \; \textit{b} \; \textit{c} \; \$$ 

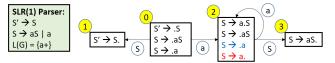
Step	Stack	Symbols	Input	Action	Parse Tree
(1)	0		aaabc\$	shift	
(2)	0 2	a	aabc\$	shift	
(3)	0 2 2	aa	abc\$	shift	
(4)	0 2 2 2	aaa S	bc\$	shift	
(5)	02223	aaab	с \$	shift	
(6)	022234	aaa <u>b c</u>	\$	reduce by $S  o \mathbf{b} \mathbf{c}$	S b c
(7)	0 2 2 2 5	a a a S	\$	reduce by $S \rightarrow \mathbf{a} S$	81 a 82 b c
					8 87 a
(8)	0 2 2 5	a <u>a S</u>	\$	reduce by $S \rightarrow \mathbf{a} S$	b c
(0)	0 2 5	- 6	s		
(9)	025	<u>a S</u>	3	reduce by $S \rightarrow \mathbf{a} S$	
					5 - 5 - 5 - 5 - 5 - 5 - 5 - 5 - 5 - 5 -
(10)	1	<u>s</u>	\$	accept	6 6



Module 03

LR(0) Parser





State	а	\$	S
0	s2		1
1		Acc	
2	s2/r2	r2	3
3	r1	r1	



# LR(0) Parser Construction

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I Sengupta & P P Das

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LR(1) Parser
LALR(1) Parser

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- Closure: Add all items arising from the productions from the non-terminal after the period in an item. Closure is computed transitively. Examples:
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- State: Collection of LR(0) items and their closures. Examples:
  - $\begin{array}{l} \bullet \quad \{S' \rightarrow .S, S \rightarrow .x, S \rightarrow .(L)\} \\ \bullet \quad \{S \rightarrow (.L), L \rightarrow .S, L \rightarrow .L, S, S \rightarrow .x, S \rightarrow .(L)\} \end{array}$
- Actions: Shift (s#), Reduce (r#), Accept (acc), Reject (' '), GOTO (#):
  - Shift on input symbol to state# (dot precedes the terminal to shift)
  - Reduction on all input symbols by production# (dot at the end of a production)
  - Accept on reduction by the augmented production  $S' \to S$
  - Reject for blank entries cannot be reached for a valid string
  - GOTO on transition of non-terminal after reduction (dot precedes the non-terminal to reduce to)



# LR(0) Parser Example

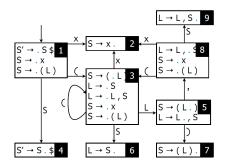
Module 03

LR(0) Parser

0:

S

Х (L)



(	)	х	,	\$	S	ш
<b>s</b> 3		<b>s</b> 2			g 4	
r 1	r 1	r 1	r 1	r 1		
<b>s</b> 3		<b>s</b> 2			g 6	g 5
				а		
	s 7		<b>s</b> 8			
r 3	r 3	r 3	r 3	r 3		
r 2	r 2	r 2	r 2	r 2		
<b>s</b> 3		<b>s</b> 2			g 9	
r 4	r 4	r 4	r 4	r 4		
	r1 s3 r3 r2 s3	r1 r1 s3 s7 r3 r3 r2 r2 s3	\$3	\$3	s3     s2     r1     r1     r1     r1     r1     r1       s3     s2     a       s7     s8     a       r3     r3     r3     r3     r3       r2     r2     r2     r2     r2       s3     s2     e     e	s3     s2     g4       r1     r1     r1     r1     r1     g6       s3     s2     s3     g6       s7     s8     s7       r3     r3     r3     r3     r3       r2     r2     r2     r2     r2       s3     s2     s9     g9

Source: https://www.slideshare.net/eelcovisser/lr-parsing-71059803?from\_action=save



# LR(0) Parser Example: Parsing (x,x)\$

Module 03

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Objectives & Outline

 $\begin{array}{l} \mathsf{Infix} \to \\ \mathsf{Postfix} \end{array}$ 

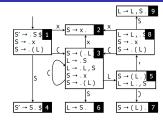
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SLR(1) Parser
LR(1) Parser

	(	)	х	,	\$	S	L
1	<b>s</b> 3		<b>s</b> 2			g 4	
2	r 1	r1	r 1	r 1	r 1		
3	s 3		s 2			g 6	g 5
4					a		
5		s 7		s 8			
6	r 3	r 3	r 3	r 3	r 3		
7	r 2	r 2	r 2	r 2	r 2		
8	<b>s</b> 3		<b>s</b> 2			<b>g</b> 9	
9	r 4	r 4	r 4	r 4	r 4		



Step	Stack	Symbols	Input	Action
(1)	1		(x,x)\$	shift
(2)	1 3	(	x,x)\$	shift
(3)	1 3 2	( x	, x ) \$	reduce by $S \to \mathbf{x}$
(4)	1 3 6	(5	, x ) \$	reduce by $L  o S$
(5)	1 3 5	( L	, x ) \$	shift
(6)	1358	( L ,	x)\$	shift
(7)	13582	( L , x	) \$	reduce by $S \to \mathbf{x}$
(8)	13589	( L , S	) \$	reduce by $L  o L$ , $S$
(9)	1 3 5	( L	) \$	shift
(10)	1357	( L )	\$	reduce by $S \rightarrow (L)$
(11)	1 4	S	\$	accept

Source: https://www.slideshare.net/eelcovisser/lr-parsing-71059803?from\_action=save Compilers I Sengupta & P P Das



# LR(0) Parser: Practice Example

### Module 03

Construct an LR(0) parser for  $G_7$ :

2:  $A \rightarrow a A$ 

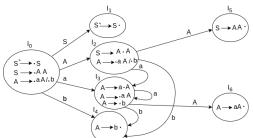


# LR(0) Parser: Practice Example: Solution

Module 03

LR(0) Parser

AAConstruct an LR(0) parser for  $G_7$ : a A



State	Action			GO	TO
	a	b	\$	Α	S
0	s3	s4		2	1
1			acc		
2	s3	s4		5	
3	s3	s4		6	
4	r3	r3	r3		
5	r1	r1	r1		
6	r2	r2	r2		

Source: https://www.iavatpoint.com/canonical-collection-of-lr-0-items Compilers I Sengupta & P P Das



Module 03

# **LR** Parsers SLR(1) Parser



# LR(0) Parser: Shift-Reduce Conflict

Module 03

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Objectives &

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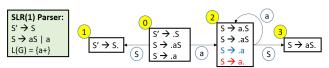
Ambiguous Gramma

LR Parser

LR Fundamental

LR(0) Parser SLR(1) Parser

SLR(1) Parser LR(1) Parser LALR(1) Parser  $G_5 = \{S \rightarrow aS|a\}$ 



State	а	\$	S
0	s2		1
1		Acc	
2	s2/r2	r2	3
3	r1	r1	

S → a\$	
S → aS\$ → aa\$ S → aS\$ → aaS\$ → aaa\$	

- Consider State 2.
  - By  $S \rightarrow .a$ , we should shift on a and remain in state 2
  - ullet By S 
    ightarrow a., we should reduce by production 2
- We have a Shift-Reduce Conflict
- As  $FOLLOW(S) = \{\$\}$ , we decide in favor of shift. Why?



# LR(0) Parser: Shift-Reduce Conflict

Module 03

SLR(1) Parser

		Х	+	\$	Е	Т
	1	<b>s</b> 5			g 2	g 3
$ \begin{array}{c c} \downarrow & E \\ S \rightarrow E & S \rightarrow E & 2 \end{array} $	2			а		
E → . T + E	3	r 2	?	r 2		
$E \rightarrow .T$ $T$ $E \rightarrow T. + E$	4	<b>s</b> 5			g 6	g 3
$T \rightarrow . \times 1 \longrightarrow E \rightarrow T . + E \longrightarrow E \rightarrow T . 3$	5	r 3	r 3	r 3		
<u> </u>	6	r 1	r 1	r 1		
$X \qquad \boxed{E \rightarrow T + . E}$						
E → . T + E E → . T			_		→ T + → T	- E
$T \to X$ . 5 $\stackrel{\times}{\longleftrightarrow} T \to .X$ 4 $\stackrel{E}{\longleftrightarrow} E \to T$	+	E. 6		T	→ X	

- Consider State 3.
  - By  $E \rightarrow T. + E$ , we should shift on + and move to state 4
  - By  $E \rightarrow T$ ., we should reduce by production 2
- We have a Shift-Reduce Conflict
- To resolve, we build SLR(1) Parser



# SLR(1) Parser Construction

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LR Parsers

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LR(0) Parser

SLR(1) Parser LR(1) Parser  LR(0) Item: Canonical collection of LR(0) Items used in SLR(1) as well

• Closure: Same way as LR(0)

• **State**: Collection of LR(0) items and their closures.

Actions: Shift (s#), Reduce (r#), Accept (acc), Reject (<space>), GOTO (#):

Shift on input symbol to state#

 Reduction by production# only on the input symbols that belong to the FOLLOW of the left-hand side

Accept on reduction by the augmented production

• GOTO on transition of non-terminal after reduction



# SLR Parse Table: Shift-Reduce Conflict on LR(0)

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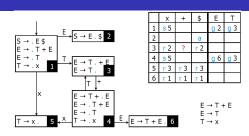
Ambiguous Grammi

LR Parsers

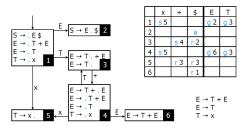
LR Fundament

LR(0) Parser SLR(1) Parser

LR(1) Parser LR(1) Parser LALR(1) Parser



### Reduce a production $S \to ...$ on symbols $k \in T$ if $k \in Follow(S)$



Source: https://www.slideshare.net/eelcovisser/lr-parsing-71059803?from\_action=save



# SLR(1) Parser: Practice Example

Module 03

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LR Parser

LR Fundamenta

LR(0) Parser

LR(1) Parse

LR(1) Parser

Construct an SLR(1) parser for  $G_8$ :

1:  $S \rightarrow E$ 

2:  $E \rightarrow E + T$ 

 $3: E \rightarrow T$ 

4:  $T \rightarrow T * F$ 

5:  $T \rightarrow F$ 

6:  $F \rightarrow id$ 



# SLR(1) Parser: Practice Example: Solution

Module 03

I Sengupta & P P Das

Objectives &

 $\begin{array}{c} \mathsf{Infix} \to \\ \mathsf{Postfix} \end{array}$ 

Gramma

Derivations Parsing

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LR Parsers

LR Fundament

LR(0) Parser

LR(1) Parser

Construct an SLR(1) parser for  $G_8$ :

1: 5 2: E

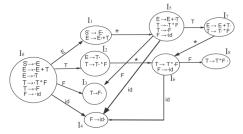
 $E \rightarrow E \rightarrow$ 

E + T

5: 6:

 $\overset{\rightarrow}{\rightarrow}$ 

T \* F F id



States	Action			Go to			
	id	+	*	\$	E	T	F
I <sub>0</sub>	S <sub>4</sub>				1	2	3
I <sub>1</sub>		S <sub>5</sub>		Accept			
I <sub>2</sub>		R <sub>2</sub>	S <sub>6</sub>	R2			
I3		R4	R4	R4			
I4		R5	R5	R5			
I <sub>5</sub>	S4					7	3
I <sub>6</sub>	S4						8
I <sub>7</sub>		R1	S6	R1			
Is		R3	R3	R3			

Source: https://www.javatpoint.com/slr-1-parsing



Module 03

# **LR Parsers** LR(1) Parser



# SLR(1) Parser: Shift-Reduce Conflict

Module 03

LR(1) Parser

Grammar Go

L = R

\*R

id

 $I_0: S' \rightarrow \cdot S$ 

 $S \rightarrow \cdot L = R$  $L \rightarrow \cdot * R$  $L \rightarrow -id$  $R \rightarrow \cdot L$ 

 $I_{\kappa} : L \rightarrow id$ 

 $I_6: S \rightarrow L = \cdot R$ 

 $R \rightarrow \cdot L$  $L \rightarrow \cdot * R$ 

 $L \rightarrow -id$ 

 $I_{7}$ :  $I_{1} \rightarrow *R$ :

 $I_8: R \rightarrow L$ 

 $I_9: S \rightarrow L = R$ 

 $I_2: S \rightarrow L \cdot = R$ 

 $I_9: S \rightarrow R$ 

 $I_1: S' \rightarrow S$ 

 $\bullet = \in FOLLOW(R)$  as  $S \Rightarrow L = R \Rightarrow *R = R$ 

- So in State#2 we have a shift/reduce Conflict on =
- The grammar is not ambiguous. Yet we have the shift/reduce conflict as SLR is not powerful enough to remember enough left context to decide what action the parser should take on input =, having seen a string reducible to I
- To resolve, we build LR(1) Parser

Source: Dragon Book



# LR(1) Parser Construction

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LR Parsers

LR Fundamentals LR(0) Parser

LR(0) Parser SLR(1) Parser LR(1) Parser LALR(1) Parser Sample Grammar  $G_7$  Augmented Grammar  $G_7$ 0:  $S' \rightarrow S$ 

- LR(1) Item: An LR(1) item has the form  $[A \to \alpha.\beta, a]$  where  $A \to \alpha\beta$  is a production and a is the look-ahead symbol which is a terminal or \$. As the dot moves through the right-hand side of the production, token a remains attached to it. LR(1) item  $[A \to \alpha., a]$  calls for a reduce action when the look-ahead is a. Examples:  $[S \to .CC, \$]$ ,  $[S \to C.C, \$]$
- Closure(S):

For each item  $[A \to \alpha.B\beta, t] \in S$ , For each production  $B \to \gamma \in G$ , For each token  $b \in FIRST(\beta t)$ , Add  $[B \to .\gamma, b]$  to S

Closure is computed transitively. Examples:

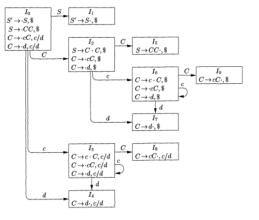
- Closure( $[S \rightarrow C.C, \$]$ ) = { $[S \rightarrow C.C, \$]$ ,  $[C \rightarrow .cC, \$]$ ,  $[C \rightarrow .d, \$]$ }
- Closure( $[C \rightarrow c.C, c/d]$ ) = { $[C \rightarrow c.C, c/d]$ ,  $[C \rightarrow .cC, c/d]$ ,  $[C \rightarrow .d, c/d]$ }
- State: Collection of LR(1) items and their closures. Examples:



# LR(1) Parser: Example

Module 03

Construct an LR(1) parser for  $G_7$ :



STATE	A	CTIC	GOTO		
	c	d	\$	S	C
0	s3	s4		1	2
1			acc		
2	s6	s7			5
3	s3	s4			8
4	r3	r3			
5			r1		
6	s6	s7			9
7	1		r3		
8	r2	r2	- 1		
9			r2		

C.C.

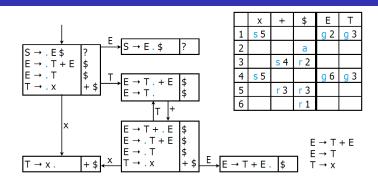
сC

Source: Dragon Book



# LR(1) Parser: Example

Module 03



Source: https://www.slideshare.net/eelcovisser/lr-parsing-71059803?from\_action=save



Module 03

LALR(1) Parser

# **LR** Parsers LALR(1) Parser



# LALR(1) Parser Construction

Module 03

LALR(1) Parser

Sample Grammar  $G_7$ Augmented Grammar G<sub>7</sub>

- LR(1) States: Construct the Canonical LR(1) parse table.
  - LALR(1) States: Two or more LR(1) states having the same set of core LR(0) items may be merged into one by combining the look-ahead symbols for every item. Transitions to and from these merged states may also be merged accordingly. All other states and transitions are retained. Examples:

```
Merge
    State#3 = {[C \rightarrow c, C, c/d], [C \rightarrow .cC, c/d], [C \rightarrow .d, c/d]} with
     State#6 = {[C \rightarrow c.C, \$], [C \rightarrow .cC, \$], [C \rightarrow .d, \$]} to get
    State#36 = {[C \rightarrow c, C, c/d/\$], [C \rightarrow .cC, c/d/\$], [C \rightarrow .d, c/d/\$]}
Merge
    State#4 = {[C \rightarrow d., c/d]} with State#7 = {[C \rightarrow d., \$]} to get
    State#47 = {[C \rightarrow d., c/d/\$]}
```

• Reduce/Reduce Conflict: LR(1) to LALR(1) transformation cannot introduce any new shift/reduce conflict. But it may introduce reduce/reduce conflict.



# LALR(1) Parser: Example

Module 03

I Sengupta & P P Das

Objectives &

 $\begin{array}{c} \mathsf{Infix} \to \\ \mathsf{Postfix} \end{array}$ 

Gramma

Parsing Fundamenta

Left-Recursion

LR Parsers

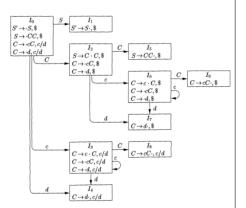
LR Fundament

LR(0) Parser

LR(1) Parser LALR(1) Parser

Source: Dragon Book

Construct an LALR(1) parser for  $G_7$ : 2:  $C \rightarrow S$  3:  $C \rightarrow S$ 



CC
сC
d

STATE	A	CTIC	GOTO		
DIALE	c	d	\$	S	C
0	s3	s4		1	2
1			acc		
2	s6	s7			5
3	s3	s4			8
4	r3	r3			
5			r1		
6	s6	s7			9
7			r3		
8	r2	r2	- 1		
9			r2		

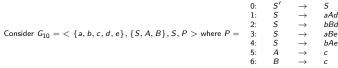
STATE	A	CTION	GOTO		
DIALE	c	d	8	S	C
0	s36	s47		1	2
1			acc		
2	s36	s47			5
36	s36	s47		)	89
47	r3	r3	r3	1	
5			r1	1	
89	r2	r2	r2		



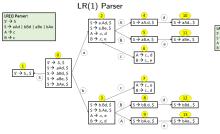
## LALR(1) Parser: Reduce-Reduce Conflict

Module 03

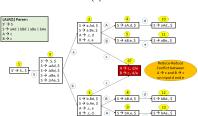
LALR(1) Parser



Clearly,  $L(G) = \{acd, bcd, ace, bce\}$ 



### LALR(1) Parser





## LR Parsers: Practice Examples

Module 03

I Sengupta & P P Das

Objectives & Outline

Infix → Postfix

Gramma Derivations

Parsing Fundamentals

Left-Recursion
Ambiguous Grammar

LR Parser

LR Fundamentals
LR(0) Parser

LR(1) Parser LALR(1) Parser Determine the LR Class (LR(0), SLR(1), LR(1) or LALR(1)) for the following grammars:

•  $G: S \rightarrow aSb \mid b$ 

•  $G: S \rightarrow Sa \mid b$ 

•  $G: S \rightarrow (S) \mid SS \mid \epsilon$ 

•  $G: S \to (S) \mid SS \mid ()$ 

•  $G: S \rightarrow ddX \mid aX \mid \epsilon$ 

• G:  $S \rightarrow E$ ;  $E \rightarrow T + E \mid T$ ;  $T \rightarrow int * T \mid int \mid (E)$ 

•  $G: S \rightarrow V = E \mid E; E \rightarrow V; V \rightarrow x \mid *E$ 

 $\bullet \quad \textit{G: } \textit{S} \rightarrow \textit{AB}; \textit{A} \rightarrow \textit{aAb} \mid \textit{a; } \textit{B} \rightarrow \textit{d}$