

```

% Number of simulations to average over
numSimulations = 1000;

% Array to hold values of L
L_values = [10, 20, 40, 80, 160, 320, 640, 1280, 2560, 5120, 10240];

% Arrays to store results for the average and standard deviation of the sum
of squares of increments
avgSumSquaresIncrements = zeros(size(L_values));
stdSumSquaresIncrements = zeros(size(L_values));

% Loop over different values of L
for j = 1:length(L_values)
    L = L_values(j);
    dt = 2 / L; % delta t

    % Temporary array to store the sum of squares of increments for each
simulation
    tempSumSquares = zeros(1, numSimulations);

    % Perform simulations
    for i = 1:numSimulations
        % Generate Wiener increments
        dW = sqrt(dt) * randn(1, L);

        % Compute the sum of squares of increments
        tempSumSquares(i) = sum(dW.^2);
    end

    % Compute the average and standard deviation of the sum of squares of
increments
    avgSumSquaresIncrements(j) = mean(tempSumSquares);
    stdSumSquaresIncrements(j) = std(tempSumSquares);
end

% Display the table of L, averages, and standard deviations
T = table(L_values', avgSumSquaresIncrements', stdSumSquaresIncrements', ...
    'VariableNames', {'L', 'Average', 'Standard_Deviation'});
disp(T);

```

| L    | Average | Standard_Deviation |
|------|---------|--------------------|
| 10   | 2.0442  | 0.96153            |
| 20   | 2.0007  | 0.65113            |
| 40   | 2.0187  | 0.47457            |
| 80   | 1.9903  | 0.31852            |
| 160  | 1.9929  | 0.22465            |
| 320  | 1.9957  | 0.15678            |
| 640  | 1.9995  | 0.11208            |
| 1280 | 1.9972  | 0.07806            |
| 2560 | 2.0022  | 0.056457           |

|       |        |          |
|-------|--------|----------|
| 5120  | 1.9987 | 0.040946 |
| 10240 | 1.9997 | 0.026844 |

```
% Plotting the results with error bars
figure;
errorbar(L_values, avgSumSquaresIncrements, stdSumSquaresIncrements, 's-');
xlabel('Number of intervals L');
ylabel('Average of Sum of Squares of Increments');
title('Sum of (dWi)^2 vs. L with Standard Deviation');
set(gca, 'XScale', 'log');
grid on;
hold on;
plot(L_values, repmat(2, size(L_values)), 'r--'); % Line at the theoretical
limit 2
legend('Numerical Result with Std Dev', 'Theoretical Limit');
```

