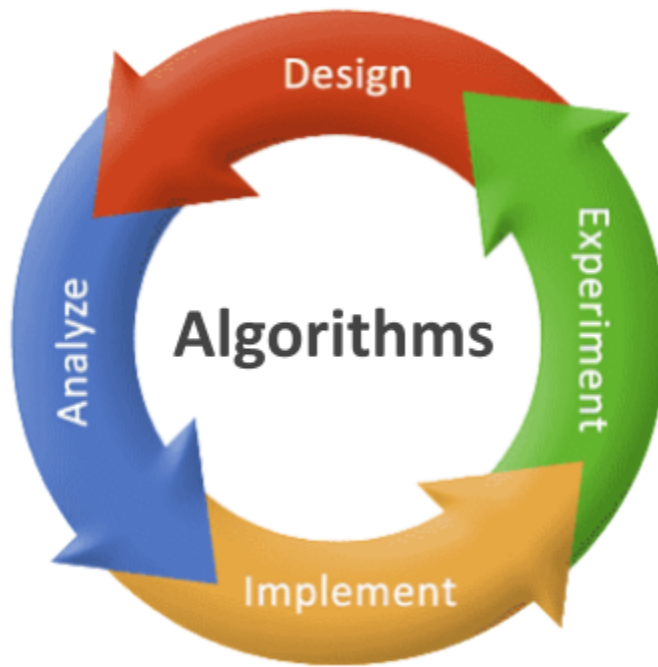


Design & Analysis of Algorithms



Practical File

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For Basic Sorting Algorithms : Algo.hpp

```
#ifndef _algo_hpp_
#define _algo_hpp_

#pragma once

#include <iostream>
#include <cstdlib>

using namespace std;

namespace algo
{
    template <class T>
    void printArray(T *array, const uint &len)
    {
        cout << "\n { ";
        for (uint i = 0; i < len - 1; i++)
            cout << array[i] << ", ";
        cout << array[len - 1] << " }\n";
    }

    template <class T>
    void swap(T *a, T *b)
    {
        T tmp = *a;
```

```
*a = *b;  
*b = tmp;  
}
```

```
/* Insertion Sort */  
template <class Tp, class _Comp = less<Tp>>  
uint insertionSort(Tp *array, const uint &len,  
                  const _Comp &cmp = _Comp())  
{  
    uint count = 0;  
    Tp key;  
    if (len > 1)  
        for (int i = 1, j = 0; i < len; i++)  
        {  
            j = i - 1;  
            key = array[i];  
            while ( j >= 0 && cmp ( key, array[ j ] ))  
            {  
                array[ j + 1] = array[ j ];  
                j--;  
                count++;  
            }  
            array[ j + 1] = key;  
            count++;  
        }  
    return count;  
}
```

```

/* Merge Sort */
template <typename T, class _comp>
uint merge(T *arr, const uint &l, const uint &m,
           const uint &r, const _comp &cmp)
{
    uint n1 = m - l + 1, n2 = r - m, i, j, k;
    T L[n1], R[n2];

    for (i = 0; i < n1; i++)
        L[i] = arr[l + i];
    for (j = 0; j < n2; j++)
        R[j] = arr[m + 1 + j];

    i = j = 0;
    k = l;

    while (i < n1 && j < n2)
    {
        if (cmp(L[i], R[j]))
            arr[k] = L[i++];

        else
            arr[k] = R[j++];

        k++;
    }
}

```

```

while (i < n1)
    arr[k++] = L[i++];

while (j < n2)
    arr[k++] = R[j++];

return k - l - 1;
}

```

```

template <typename T, class _comp = less<T>>
uint mergeSort(T *arr, const uint &begin, const uint &end,
               const _comp &cmp = _comp())
{
    if (begin < end)
    {
        uint mid = (begin + end) / 2;
        return mergeSort(arr, begin, mid, cmp) +
            mergeSort(arr, mid + 1, end, cmp) +
            merge(arr, begin, mid, end, cmp);
    }
    return 1;
}

```

```

/*    Heap Sort    */
template <class T, class _Comp>
void heapify(T array[], const int &i, const uint &len,
             const _Comp &cmp, uint &count)
{
    uint left, right, top = i;
    left = 2 * i + 1;
    right = 2 * i + 2;

    if (left < len && cmp(array[top], array[left]))
        count++, top = left;

    if (right < len && cmp(array[top], array[right]))
        count++, top = right;

    if (top != i)
    {
        swap(array + i, array + top);
        count++;
        heapify(array, top, len, cmp, count);
    }
}

template <class Tp, class _Comp = less<Tp>>
uint heapSort(Tp *array, const uint &len,
              const _Comp &cmp = _Comp())
{
    uint count = 0; // Counter

```

```

// Build a Heap
for (int i = len / 2 - 1; i >= 0; i--)
    heapify(array, i, len, cmp, count);

// One by one extract an element from heap
for (uint i = len - 1; i > 0; i--)
{
    // Move current root to end
    swap(array, array + i);

    // call heapify on the reduced heap
    heapify(array, 0, i, cmp, count);
}
return count;
}

/*      Quick Sort      */
template <class T, class _Comp>
int partition(T *array, const int &start, const int &end,
              const _Comp &cmp)
{
    T x = array[end];
    int i = start;

    for (int j = start; j < end; j++)
        if (cmp(array[j], x))
        {

```

```

        swap(array + j, array + i);
        i++;
    }
    swap(&array[i], array + end);
    return i;
}

template <class T, class _Comp>
int random_partition(T *array, const int &start,
                    const int &end, const _Comp &cmp)
{
    srand(time(NULL));
    swap(&array[start + rand() % (end - start + 1)], &array[end]);
    return partition(array, start, end, cmp);
}

template <class T, class _Comp = less<T>>
uint random_quickSort(T *array, const int &start,
                    const int &end, const _Comp &cmp = _Comp())
{
    if (start < end)
    {
        int piv = random_partition(array, start, end, cmp);
        return (piv - start) +
            random_quickSort(array, start, piv - 1, cmp) +
            random_quickSort(array, piv + 1, end, cmp);
    }
    return 1;
}

```



```

/*    Randomized Select    */
template <typename tp, class _Comp = less<tp>>
tp randomizedSelect(tp *array, const int &start,
                   const int &end, const int &i,
                   const _Comp &cmp = _Comp())
{
    if (i <= 0)
        __throw_invalid_argument("Index Error : Index starts with 1
not from 0 or negative !!!");

    if (start == end)
        return array[start];

    int piv = random_partition(array, start, end, cmp);
    int k = piv - start + 1;

    if (i == k)
        return array[piv];

    else if (i < k)
        return randomizedSelect(array, start, piv - 1, i, cmp);

    else
        return randomizedSelect(array, piv + 1, end, i - k, cmp);
}
}
#endif

```

Practical Questions

Q.1.

i. Implement Insertion Sort. (The program should report the number of comparisons)

Ans.

Code

```
#include "algo.hpp"
using namespace algo;

int main()
{
    int a[] = {1, 0, 2, 3, 6, 4, 9, -2, 5};
    int n = sizeof(a) / sizeof(a[0]);

    cout << "\n\t\t Practical 1\n\t\tA. Insertion Sort\n";

    cout << "\n Unsorted Array: \n";
    printArray(a, n);

    cout << "\n Comparisons in Insertion Sort : "
        << insertionSort(a, n) << endl;

    cout << "\n Sorted array in ascending order: \n";
    printArray(a, n);
}
```

Output

```
Practical 1
A. Insertion Sort

Unsorted Array:
{ 1, 0, 2, 3, 6, 4, 9, -2, 5 }

Comparisons in Insertion Sort : 19

Sorted array in ascending order:
{ -2, 0, 1, 2, 3, 4, 5, 6, 9 }
```

ii. Implement Merge Sort (The program should report the number of comparisons)

Ans.

Code

```
#include "algo.hpp"
using namespace algo;

int main()
{
    int a[] = {5, 10, 2, 0, 3, 4, 8, 9, 6};
    int n = sizeof(a) / sizeof(a[0]);

    cout << "\n\t\t Practical 1\n\t\t B. Merge Sort\n";
```

```

cout << "\n Unsorted Array: \n";
printArray(a, n);

cout << "\n Comparisons in Merge Sort : "
    << mergeSort(a, 0, n - 1) << endl;

cout << "\n Sorted array in ascending order: \n";
printArray(a, n);

}

```

Output

```

                Practical 1
                B. Merge Sort

Unsorted Array:
{ 5, 10, 2, 0, 3, 4, 8, 9, 6 }

Comparisons in Merge Sort : 30

Sorted array in ascending order:
{ 0, 2, 3, 4, 5, 6, 8, 9, 10 }

```

Q.2. Implement Heap Sort (The program should report the number of comparisons)

Ans.

Code

```
#include "algo.hpp"

using namespace algo;

int main()
{
    int a[] = {5,13,2,25,7,17,20,8,4};
    int n = sizeof(a)/sizeof(a[0]);

    cout << "\n\t\t Practical 2\n\t\t Heap Sort\n";

    cout << "\n Unsorted Array: \n";
    printArray(a, n);

    cout << "\n Comparisons in Heap Sort : "
        << heapSort(a, n, greater<int>()) << endl;

    cout << "\n Sorted array in descending order: \n";
    printArray(a, n);
}
```

Output

```
Practical 2
Heap Sort

Unsorted Array:
{ 5, 13, 2, 25, 7, 17, 20, 8, 4 }

Comparisons in Heap Sort : 31

Sorted array in descending order:
{ 25, 20, 17, 13, 8, 7, 5, 4, 2 }
```

Q.3. Implement Randomized Quick sort (The program should report the number of comparisons)

Ans.

Code

```
#include "algo.hpp"
using namespace algo;

int main()
{
    int data[] = {8, 70, 16, 1, 10, 9, 12, 1, 10, 3, 2};
    int n = sizeof(data) / sizeof(data[0]);
```

```

cout << "\n\t\tPractical 3\n\t Randomized Quick Sort\n";
cout << "\n Unsorted Array: \n";
printArray(data, n);

cout << "\n Comparisons in Randomized Quick Sort : "
    << random_quickSort(data, 0, n - 1) << endl;

cout << "\n Sorted array in ascending order: \n";
printArray(data, n);
}

```

Output

```

          Practical 3
    Randomized Quick Sort

Unsorted Array:

{ 8, 70, 16, 1, 10, 9, 12, 1, 10, 3, 2 }

Comparisons in Randomized Quick Sort : 19

Sorted array in ascending order:

{ 1, 1, 2, 3, 8, 9, 10, 10, 12, 16, 70 }

```

Q.4. Implement Radix Sort.

Ans.

Code

```
#include "algo.hpp"
using namespace algo;

int getMax(int *array, const uint &len)
{
    int max = array[0];
    for (uint i = 1; i < len; i++)
        if (max < array[i])
            max = array[i];
    return max;
}

void countSort(int *array, const uint &len, const uint &exp)
{
    int i, *count = new int[10]{0}, *out = new int[len];

    for (i = 0; i < len; i++)
        count[(array[i] / exp) % 10]++;

    for (i = 1; i < 10; i++)
        count[i] += count[i - 1];

    for (i = len - 1; i >= 0; i--)
    {
        out[count[(array[i] / exp) % 10] - 1] = array[i];
```



```

        count[(array[i] / exp) % 10]--;
    }

    for (i = 0; i < len; i++)
        array[i] = out[i];

    delete out;
    delete count;
}

void radixSort(int *array, const uint &len)
{
    uint max = getMax(array, len);
    for (uint i = 1; (max / i) > 0; i *= 10)
        countSort(array, len, i);
}

int main()
{
    int a[] = {10, 1, 20, 300, 5, 7, 4, 1024, 995, 87};
    int n = sizeof(a) / sizeof(a[0]);

    cout << "\n\t\t Practical 4\n\t\t Radix Sort\n";

    cout << "\n Unsorted Array: \n";
    printArray(a, n);

    radixSort(a, n);
    cout << "\n After applying Radix Sort on the Array :\n";

```

```
cout << "\n Sorted array in ascending order: \n";  
printArray(a, n);  
  
}
```

Output

```
Practical 4  
Radix Sort  
  
Unsorted Array:  
{ 10, 1, 20, 300, 5, 7, 4, 1024, 995, 87 }  
  
After applying Radix Sort on the Array :  
  
Sorted array in ascending order:  
{ 1, 4, 5, 7, 10, 20, 87, 300, 995, 1024 }
```

Q.5. Implement Bucket Sort.

Ans.

Code

```
#include <iostream>  
#include <vector>  
#include <algorithm>  
using namespace std;  
void printArray(float *array, const uint &len)
```

```

{
    cout << "\n { ";
    for (uint i = 0; i < len - 1; i++)
        cout << array[i] << ", ";
    cout << array[len - 1] << " }\n";
}

```

```

int main()
{
    vector<float> hash[10];
    float a[] = {0.01, 0.23, 0.13, 0.11, 0.25, 0.35, 0.42, 0.02, 0.9, 0.45, 0.05};
    int n = sizeof(a) / sizeof(a[0]), j = 0;

    cout << "\n\t\t\t\t Practical 5\n\t\t\t\t\t Bucket Sort\n";

    cout << "\n Unsorted Array: \n";
    printArray(a, n);

    // Bucket Sort
    for (float &i : a)
        hash[int(i * 10)].push_back(i);

    for (vector<float> &v : hash)
        sort(v.begin(), v.end());

    for (vector<float> &v : hash)
        for (float &f : v)
            a[j++] = f;
}

```

```

cout << "\n After applying bucket-sort on the array\n"
      << "\n Sorted array in ascending order: \n";
printArray(a, n);
}

```

Output

```

                                     Practical 5
                                     Bucket Sort

Unsorted Array:
{ 0.01, 0.23, 0.13, 0.11, 0.25, 0.35, 0.42, 0.02, 0.9, 0.45, 0.05 }

After applying bucket-sort on the array

Sorted array in ascending order:
{ 0.01, 0.02, 0.05, 0.11, 0.13, 0.23, 0.25, 0.35, 0.42, 0.45, 0.9 }

```

Q.6. Implement Randomized Select.

Ans.

Code

```

#include "algo.hpp"
using namespace algo;

int main()
{
    int a[] = {5, 3, 2, 7, 1, 0, 8, 4};
    int n = sizeof(a) / sizeof(a[0]), loc;

```

```

cout << "\n\t\t Practical 6\n\t Randomized Select Algorithm\n";
cout << "\n Unsorted Array: \n";
printArray(a, n);

loc = randomizedSelect(a, 0, n - 1, 1);
cout << "\n Finding minimum element at position 1 : "
    << loc << "\n\n Now Array is : \n";
printArray(a, n);

loc = randomizedSelect(a, 0, n - 1, 7);
cout << "\n Finding minimum element at position 7 : "
    << loc << "\n\n Now Array is : \n";
printArray(a, n);
}

```

Output

```

                Practical 6
            Randomized Select Algorithm

Unsorted Array:

{ 5, 3, 2, 7, 1, 0, 8, 4 }

Finding minimum element at position 1 : 0

Now Array is :

{ 0, 1, 2, 7, 5, 3, 8, 4 }

Finding minimum element at position 7 : 7

Now Array is :

{ 0, 1, 2, 3, 4, 5, 7, 8 }

```

Q.7. Implement Breadth-First Search in a graph.

Ans.

Code

```
#include <iostream>
#include <queue>

using namespace std;

#define v 5

int Graph[v][v] = {{1, 0, 0, 0, 1},
                   {0, 1, 1, 0, 1},
                   {0, 1, 0, 1, 0},
                   {0, 0, 1, 0, 0},
                   {1, 1, 0, 0, 1}};

bool visited[v] = {false};
queue<int> q;

// Breadth First Search for Graphs
void BFS(int start)
{
    if (start < 0 || start > v - 1)
        return;

    int begin;
    q.push(start);
    visited[start] = true;
```

```

while (!q.empty())
{
    begin = q.front();
    q.pop();

    cout << '\t' << begin;

    for (int i = 0; i < v; i++)
        if (Graph[begin][i] && !visited[i])
        {
            visited[i] = true;
            q.push(i);
        }
    }
}

int main()
{
    cout << "\n\t\t Practical 7\n\tBreadth First Traversal for Graphs\n";

    cout << "\n\n Given Graph is :\n\n\t Nodes   :   Edges\n";
    for (int i = 0; i < v; i++)
        for (int j = 0; j < v; j++)
            if (Graph[i][j] && !(visited[j]))
            {
                visited[i] = true;
                cout << "\t " << i << " -- " << j << " : \t" << Graph[i][j] << endl;
            }
}

```

```

fill(visited, visited + v, false);
cout << "\n Breadth First Traversal for Graph at node 1 :\n";
BFS(1);
}

```

Output

```

/home/avi/Desktop/B.Sc./IV/Design & Analysis _ A
                                     Practical 7
                               Breadth First Traversal for Graphs

Given Graph is :

      Nodes      :      Edges
      0 -- 0      :          1
      0 -- 4      :          1
      1 -- 1      :          1
      1 -- 2      :          1
      1 -- 4      :          1
      2 -- 3      :          1
      4 -- 4      :          1

Breadth First Traversal for Graph at node 1 :
      1          2          4          3          0

```

Q.8. Implement Depth-First Search in a graph.

Ans.

Code

```
#include <iostream>
```



```
using namespace std;
```

```
#define v 5
```

```
int Graph[v][v] = {{1, 0, 0, 1, 0},  
                   {0, 0, 1, 1, 1},  
                   {0, 1, 0, 1, 0},  
                   {1, 1, 1, 0, 0},  
                   {0, 1, 0, 0, 0}};
```

```
bool visited[v] = {false};
```

```
// Depth First Search for Graphs
```

```
void DFS(int start)
```

```
{  
    if (start < 0 || start > v-1)  
        return;
```

```
    visited[start] = true;  
    cout << '\t' << start ;
```

```
    for(int i = 0; i < v; i++)  
        if(Graph[start][i] && !visited[i])  
            DFS(i);  
}
```

```
int main(){
```

```
    cout << "\n\t\t Practical 8\n\tDepth First Traversal for Graphs\n";
```

```

cout << "\n\n Given Graph is :\n\n\t Nodes : Edges\n";
for (int i = 0; i < v; i++)
    for (int j = 0; j < v; j++)
        if (Graph[i][j] && !(visited[j]))
        {
            visited[i] = true;
            cout << "\t " << i << " -- " << j << " : \t" << Graph[i][j] << endl;
        }
fill(visited, visited + v, false);
cout << "\n Depth First Traversal for Graph at node 0 :\n";
DFS(0);
}

```

Output

```

                                Practical 8
                        Depth First Traversal for Graphs

Given Graph is :

      Nodes      :      Edges
    0 -- 0      :          1
    0 -- 3      :          1
    1 -- 2      :          1
    1 -- 3      :          1
    1 -- 4      :          1
    2 -- 3      :          1

Depth First Traversal for Graph at node 0 :
    0          3          1          2          4

```

Q.9. Write a program to determine the minimum spanning tree of a graph using both Prim's and Kruskal's algorithm.

Ans.

Code

```
#include <iostream>
#include <climits>
using namespace std;

#define v 5

int parent[v];
bool visited[v] = {0};

/*****      Kruskal's Algorithm      *****/
int find(int i)
{
    while (parent[i] != i)
        i = parent[i];
    return i;
}

void union1(int i, int j)
{
    int a = find(i), b = find(j);
    parent[a] = b;
}

int kruskal_mst(int cost[][v])
{
    int mincost = 0;
```

```

int edge_count = 0;

for (int i = 0; i < v; i++)
    parent[i] = i;

while (edge_count < v - 1)
{
    int min = INT_MAX, a = -1, b = -1;

    for (int i = 0; i < v; i++)
        for (int j = 0; j < v; j++)
            if (find(i) != find(j) &&
                cost[i][j] < min)
            {
                min = cost[i][j];
                a = i;
                b = j;
            }

    union1(a, b);
    mincost += min;
    cout << "\n\t Edge " << edge_count++ << " ("
         << a << ", " << b << ") : " << min;
}

return mincost;
}

/*****    Prim's Algorithm    *****/
bool validEdge(int a, int b)
{
    if (a == b || visited[a] == visited[b])
        return false;
}

```

```

    return true;
}

int prim_mst(int cost[][v])
{
    int mincost = 0, edge_count = 0;
    fill(visited, visited + v, false);
    visited[0] = true;

    while (edge_count < v - 1)
    {
        int min = INT_MAX, a = -1, b = -1;

        for (int i = 0; i < v; i++)
            for (int j = 0; j < v; j++)
                if (cost[i][j] < min &&
                    validEdge(i, j))
                {
                    min = cost[i][j];
                    a = i;
                    b = j;
                }

        visited[a] = visited[b] = true;
        mincost += min;
        cout << "\n\t Edge " << edge_count++ << " ("
              << a << " , " << b << ") : " << min;
    }
    return mincost;
}

/*****/

```

```

int main()
{
    int Graph[][v] = {
        {INT_MAX, 2, INT_MAX, 6, INT_MAX},
        {2, INT_MAX, 3, 8, 5},
        {INT_MAX, 3, INT_MAX, INT_MAX, 7},
        {6, 8, INT_MAX, INT_MAX, 9},
        {INT_MAX, 5, 7, 9, INT_MAX},
    };

    cout << "\n\t\t Practical 9\n\t\tMinimum Spanning Tree
            Algorithms\n\t\t Kruskal & Prim\n";

    cout << "\n\n Given Graph is :\n\n\t Edges   :   Weights\n";
    for (int i = 0; i < v; i++)
        for (int j = 0; j < v; j++)
            if (Graph[i][j] != INT_MAX && !(visited[j]))
            {
                visited[i] = true;
                cout << "\t " << i << " - " << j << "   :\t" << Graph[i][j] << endl;
            }

    cout << "\n 1. Minimum Spanning Tree using Kruskal's Algorithm : \n";
    int k = kruskal_mst(Graph);
    cout << "\n\n\t Minimum Cost\t: " << k << endl;

    cout << "\n 2. Minimum Spanning Tree using Prim's Algorithm : \n";
    k = prim_mst(Graph);
    cout << "\n\n\t Minimum Cost\t: " << k << endl;
}

```

Output

Practical 9 Minimum Spanning Tree Algorithms Kruskal & Prim

Given Graph is :

Edges	:	Weights
0 - 1	:	2
0 - 3	:	6
1 - 2	:	3
1 - 3	:	8
1 - 4	:	5
2 - 4	:	7
3 - 4	:	9

1. Minimum Spanning Tree using Kruskal's Algorithm :

Edge 0 (0 , 1) : 2
Edge 1 (1 , 2) : 3
Edge 2 (1 , 4) : 5
Edge 3 (0 , 3) : 6

Minimum Cost : 16

2. Minimum Spanning Tree using Prim's Algorithm :

Edge 0 (0 , 1) : 2
Edge 1 (1 , 2) : 3
Edge 2 (1 , 4) : 5
Edge 3 (0 , 3) : 6

Minimum Cost : 16

Q.10. Write a program to solve the weighted interval scheduling problem.

Ans.

Code

```
// Weighted Interval Scheduling
#include <iostream>
#include <algorithm>

using namespace std;

struct job
{
    uint start, finish, profit;

    // Constructor
    job(const uint &s = 0, const uint &f = 0, const uint &p = 0)
    {
        start = s;
        finish = f;
        profit = p;
    }
};

bool cmp(const job &a, const job &b)
{
    return a.finish < b.finish;
}
```



```
int check_Overloop(const job *j, const uint &n)
{
    for (int i = n - 2; i > -1; i--)
        if (j[n - 1].start >= j[i].finish)
            return i;
    return -1;
}
```

```
uint wi_sch(const job *j, const uint &n)
{
    if (n == 0)
        return j[0].profit;

    else
    {
        int i = check_Overloop(j, n);
        int incl = j[n - 1].profit;

        if (i != -1)
            incl += wi_sch(j, i + 1);

        int excl = wi_sch(j, n - 1);
        return (incl > excl ? incl : excl);
    }
}
```

```
uint max_profit(job *j, const uint &n)
{
    sort(j, j + n, cmp);
```

```

cout << "\n\nSorted jobs according to respective finish time are :\n\n"
    << "S.N.\t Start-time\t Finish-time\t\tProfit\n";
for (int i = 0; i < n; i++)
    cout << "\n " << i + 1 << "\t\t" << j[i].start << "\t\t"
        << j[i].finish << "\t\t" << j[i].profit;
return wi_sch(j, n);
}

```

```

int main()
{
    job j[] = {{3, 10, 20}, {1, 24, 50}, {6, 19, 100}, {2, 100, 20}};
    int n = sizeof(j) / sizeof(j[0]);

    cout << "\n\t\t Practical 10 \n\t Weighted Interval Scheduling \n";

    cout << "\nGiven jobs are :\n\nS.N.\t Start-time\t
        Finish-time\t\tProfit\n";

    for (int i = 0; i < n; i++)
        cout << "\n " << i + 1 << "\t\t" << j[i].start << "\t\t"
            << j[i].finish << "\t\t" << j[i].profit;

    int mx = max_profit(j, n);
    cout << "\n\nThe Maximum Optimal Profit is : " << mx << endl;
}

```

Output

```

                Practical 10
        Weighted Interval Schedueling

Given jobs are :

S.N.      Start-time      Finish-time      Profit

  1         3              10         20
  2         1              24         50
  3         6              19        100
  4         2             100         20

Sorted jobs according to respective finish time are :

S.N.      Start-time      Finish-time      Profit

  1         3              10         20
  2         6              19        100
  3         1              24         50
  4         2             100         20

The Maximum Optimal Profit is : 100

```

Q.11. Write a program to solve the 0-1 knapsack problem.

Ans.

Code

```

#include <iostream>
#include <algorithm>

using namespace std;

```

```
#define max(a, b) a > b ? a : b;
```

```
struct Item
```

```
{
```

```
    int val, wt;
```

```
    // Constructor
```

```
    Item(int value, int weight)
```

```
    {
```

```
        this->val = value;
```

```
        this->wt = weight;
```

```
    }
```

```
};
```

```
int knapsack_dynamic(const uint &n, const uint &W, const Item arr[])
```

```
{
```

```
    int dp[W + 1] = {0};
```

```
    for (int i = 1; i <= n; i++)
```

```
        for (int w = W; w >= 0; w--)
```

```
            if (arr[i - 1].wt <= w)
```

```
            {
```

```
                dp[w] = max(dp[w],
```

```
                            dp[w - arr[i - 1].wt] + arr[i - 1].val);
```

```
            }
```

```
    return dp[W];
```

```
}
```

```

double knapsack_greedy(const uint &n, uint W, Item arr[])
{
    sort(arr, arr + n, [](const Item &a, const Item &b){
        return (a.val * 1.0 / a.wt) > (b.val * 1.0 / b.wt);
    });

    double finalVal = 0;

    for (int i = 0; i < n; i++)
    {
        if (arr[i].wt <= W)
        {
            W -= arr[i].wt;
            finalVal += arr[i].val;
        }
        else
        {
            finalVal += arr[i].val * W * 1.0 / arr[i].wt;
            break;
        }
    }
    return finalVal;
}

```

```

int main()
{
    int W = 50; // Weight of knapsack
    Item arr[] = {{60, 10}, {100, 20}, {120, 30}};
    int n = sizeof(arr) / sizeof(arr[0]);
}

```

```

cout << "\n\t\t Practical 11 \n\t\tKnapSack Algorithm \n";

cout << "\n Given Items are :\n\n S.N.\tValues\tWeight\n";
for (int i = 0; i < n; i++)
    cout << "\n " << i + 1 << "\t" << arr[i].val << '\t' << arr[i].wt;

cout << "\n\n Dynamic Approach \n Obtained maximum value : "
    << knapsack_dynamic(n, W, arr) << endl;

cout << "\n Greedy Approach \n Obtained maximum value : "
    << knapsack_greedy(n, W, arr) << endl;
}

```

Output

```

                Practical 11
                KnapSack Algorithm

Given Items are :

S.N.   Values  Weight
1       60     10
2      100     20
3      120     30

Dynamic Approach
Obtained maximum value : 220

Greedy Approach
Obtained maximum value : 240

```

For the algorithms at S.No 1 to 3 test run the algorithm on 100 different inputs of sizes varying from 30 to 1000. Count the number of comparisons and draw the graph. Compare it with a graph of $n \log n$.

Ans.

Code

```
#include "algo.hpp"
#include <iomanip>
#include "pbPlots.hpp"
#include "supportLib.hpp"
using namespace algo;

bool drawGraph(vector<double> &xs, vector<double> &ys,
               const string &file_name)
{
    bool success;
    StringReference *errorMessage = new StringReference();
    RGBABitmapImageReference *imageReference =
        CreateRGBABitmapImageReference()
        ;

    ScatterPlotSeries *series = GetDefaultScatterPlotSeriesSettings();
    series->lineThickness = 2.0;
    series->xs = &xs;
    series->ys = &ys;

    ScatterPlotSettings *settings = GetDefaultScatterPlotSettings();
```

```

settings->width = 800;
settings->height = 600;
settings->autoBoundaries = false;
settings->xMax = GetMaximum(&xs);
settings->yMax = GetMaximum(&ys);
settings->autoPadding = true;
settings->title = toVector(L"Array Length (N) v/s Comparisons (C)");
settings->xLabel = toVector(L"N");
settings->yLabel = toVector(L"C");
settings->scatterPlotSeries->push_back(series);

success = DrawScatterPlotFromSettings(imageReference, settings,
                                     errorMessage);

if (success)
{
    vector<double> *pngdata = ConvertToPNG(imageReference->image);
    WriteToFile(pngdata, file_name);
    DeleteImage(imageReference->image);
}
else
{
    cerr << "Error: ";
    for (wchar_t c : *errorMessage->string)
    {
        wcerr << c;
    }
    cerr << endl;
}
return success;

```



```
}
```

```
void random_array_sim(const uint &begin, const uint &stop,  
                     const uint &n, vector<double> &length,  
                     vector<double> *comparison)
```

```
{
```

```
    if (begin >= stop || n <= 0)  
        return;
```

```
    uint len, arr[stop];
```

```
    for (uint i = 0; i < n; i++)
```

```
    {
```

```
        srand(stop + begin * i);
```

```
        len = begin + rand() % (stop - begin + 1);
```

```
        length.push_back(len);
```

```
        // Random Array Generation
```

```
        for (uint j = 0; j < len; j++)
```

```
            arr[j] = i + j + rand() % (len + n * j);
```

```
        comparison[0].push_back(insertionSort(arr, len));
```

```
        // For randomness
```

```
        for (uint j = 0; j < len; j += rand() % len / 8)
```

```
            swap(&arr[j], &arr[(i + j) % len]);
```

```
        comparison[1].push_back(mergeSort(arr, 0, len - 1));
```

```
        for (uint j = 0; j < len; j += rand() % len / 8)
```

```

        swap(&arr[j], &arr[(i + j) % len]);

comparison[2].push_back(heapSort(arr, len, greater<int>()));

for (uint j = 0; j < len; j += rand() % len / 8)
    swap(&arr[j], &arr[(i + j) % len]);

comparison[3].push_back(random_quickSort(arr, 0, len - 1));
    }
}

int main()
{
    vector<double> lens, cmps[4];

    string names[] = {
        "InsertionSort.png",
        "MergeSort.png",
        "HeapSort.png",
        "Random_QuickSort.png"
    };

    random_array_sim(30, 1000, 100, lens, cmps);

    for (int i = 0; i < 4; i++)
        cout << boolalpha << "\n Creation of " << left << setw(25)
            << names[i] << " : " << drawGraph(lens, cmps[i], names[i]);
}

```

Output

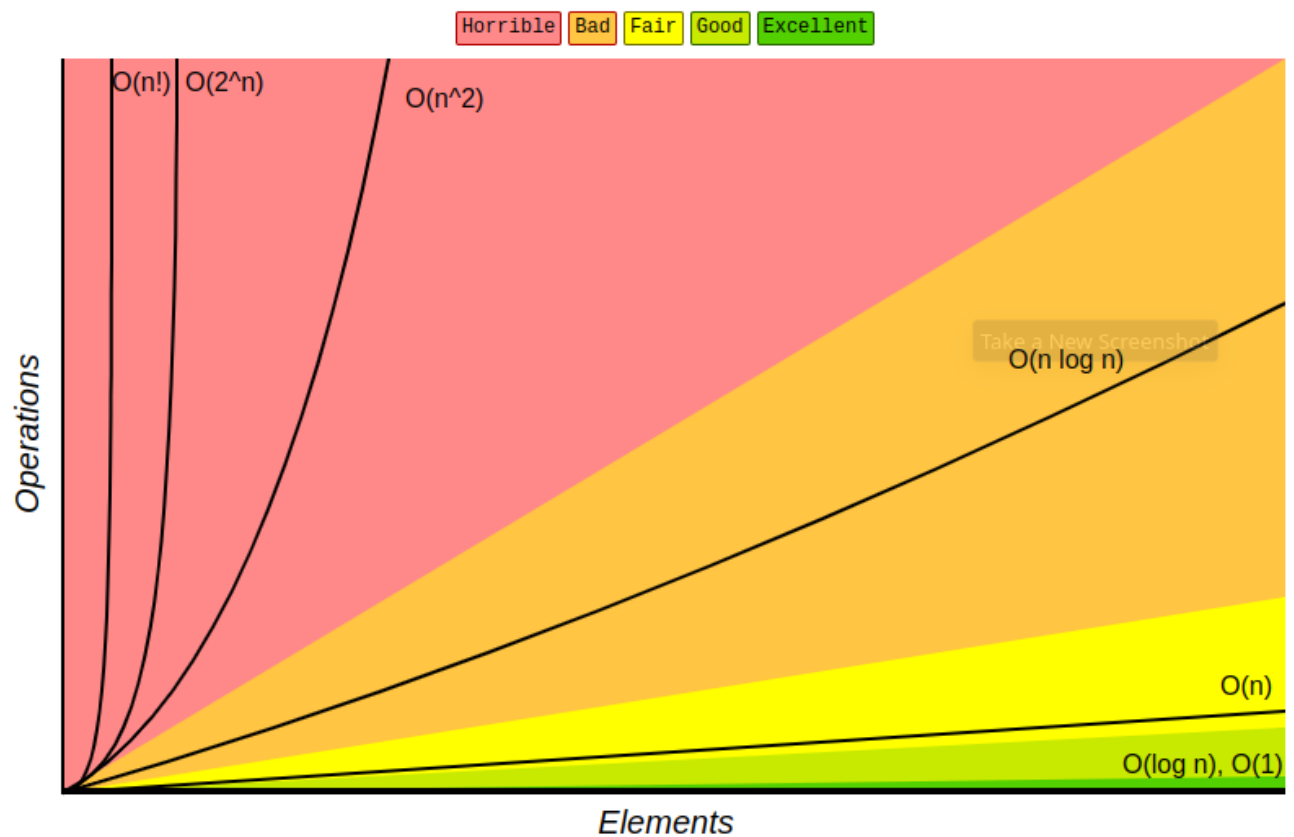
```
(avi@kali)-[~/.../Design & Analysis _ Algorithm/Practical/Practicals/src]
$ g++ main.cpp pbPlots.cpp supportLib.cpp -o main

(avi@kali)-[~/.../Design & Analysis _ Algorithm/Practical/Practicals/src]
$ ./main

Creation of InsertionSort.png      : true
Creation of MergeSort.png         : true
Creation of HeapSort.png          : true
Creation of Random_QuickSort.png  : true

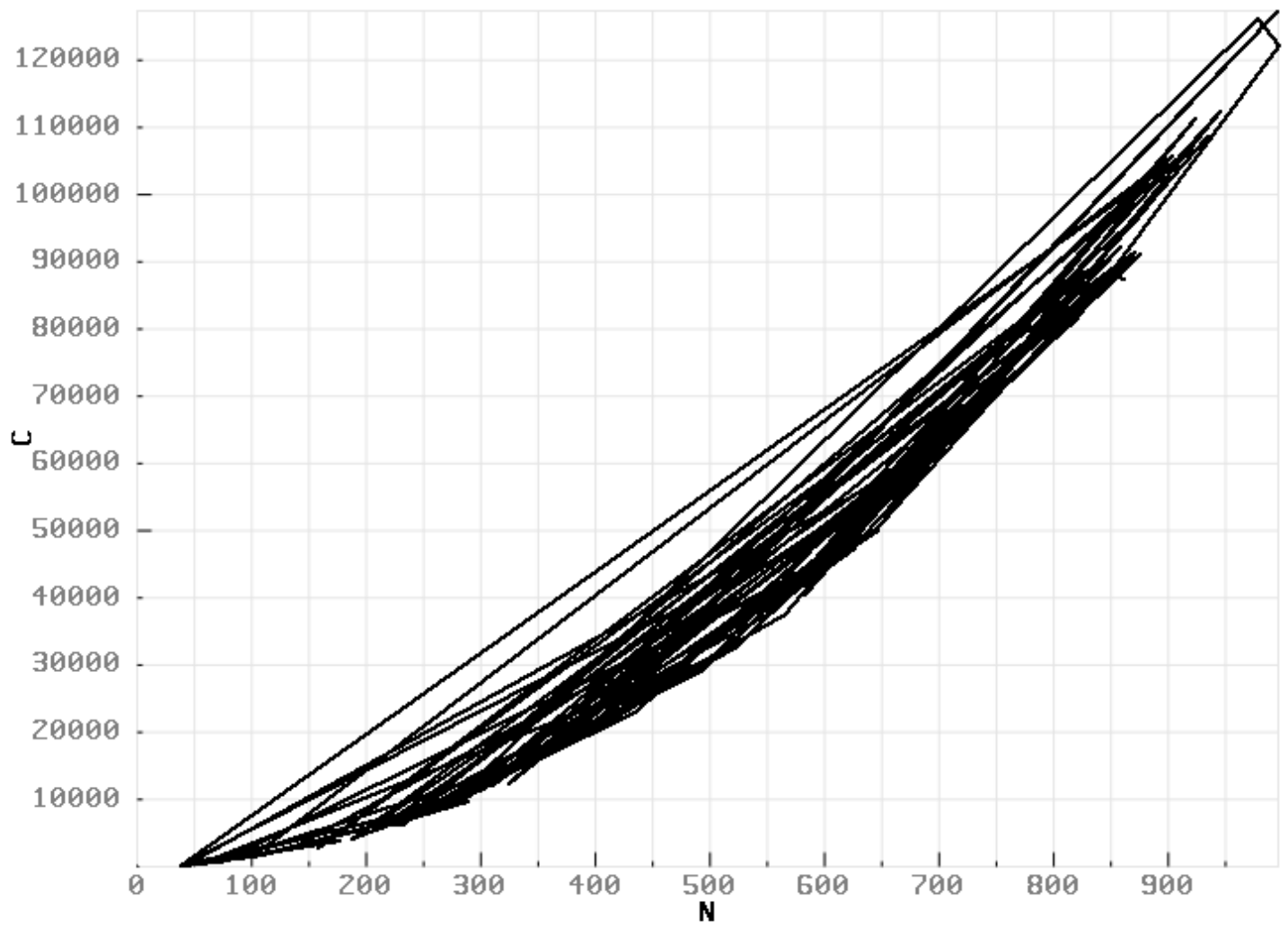
(avi@kali)-[~/.../Design & Analysis _ Algorithm/Practical/Practicals/src]
```

Big-O Complexity Chart



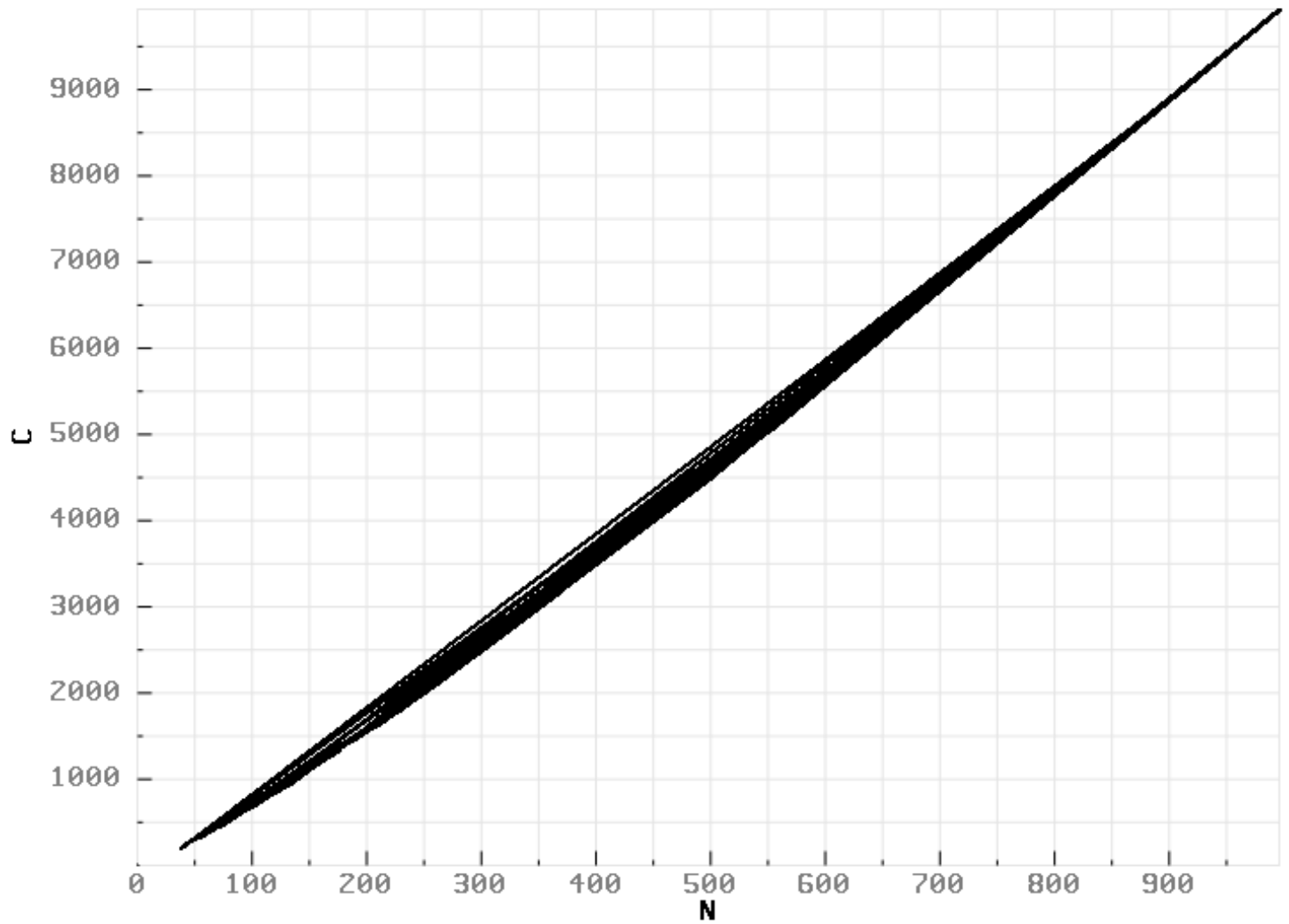
Insertion Sort

Array Length (N) v/s Comparisons (C)



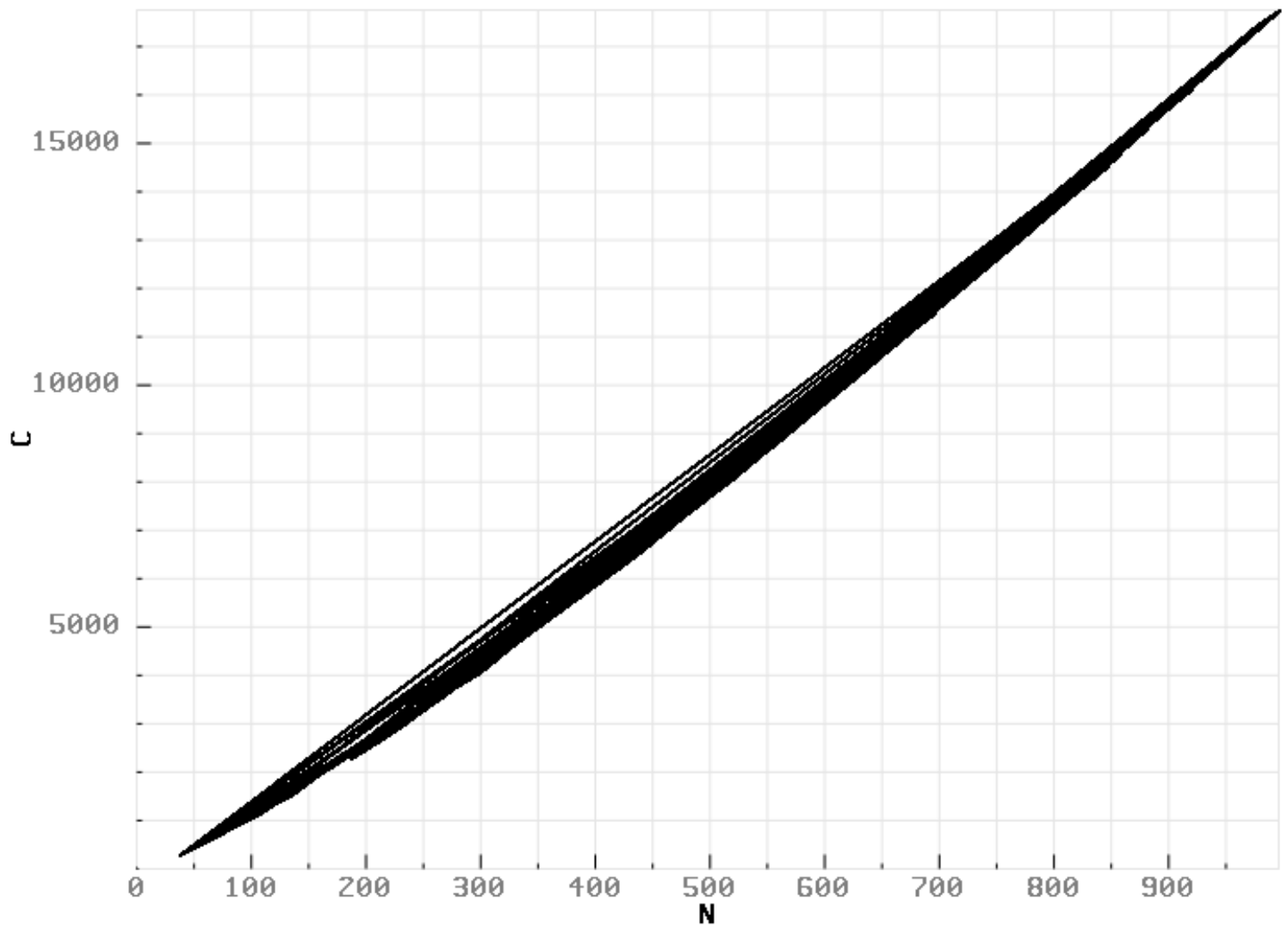
Merge Sort

Array Length (N) v/s Comparisons (C)



Heap Sort

Array Length (N) v/s Comparisons (C)



Randomized Quick Sort

Array Length (N) v/s Comparisons (C)

