



P ROLOG

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About the Tutorial

Prolog or **PRO**gramming in **LOG**ics is a logical and declarative programming language. It is one major example of the fourth generation language that supports the declarative programming paradigm. This is particularly suitable for programs that involve **symbolic** or **non-numeric computation**.

Audience

This reference has been prepared for the beginners to help them understand the basics of prolog.

Prerequisites

For this tutorial, it is assumed that the reader has a prior knowledge in coding.

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1. Prolog — Introduction

Prolog as the name itself suggests, is the short form of **LOGical PROgramming**. It is a logical and declarative programming language. Before diving deep into the concepts of Prolog, let us first understand what exactly logical programming is.

Logic Programming is one of the Computer Programming Paradigm, in which the program statements express the facts and rules about different problems within a system of formal logic. Here, the rules are written in the form of logical clauses, where head and body are present. For example, H is head and B1, B2, B3 are the elements of the body. Now if we state that "H is true, when B1, B2, B3 all are true", this is a rule. On the other hand, facts are like the rules, but without any body. So, an example of fact is "H is true".

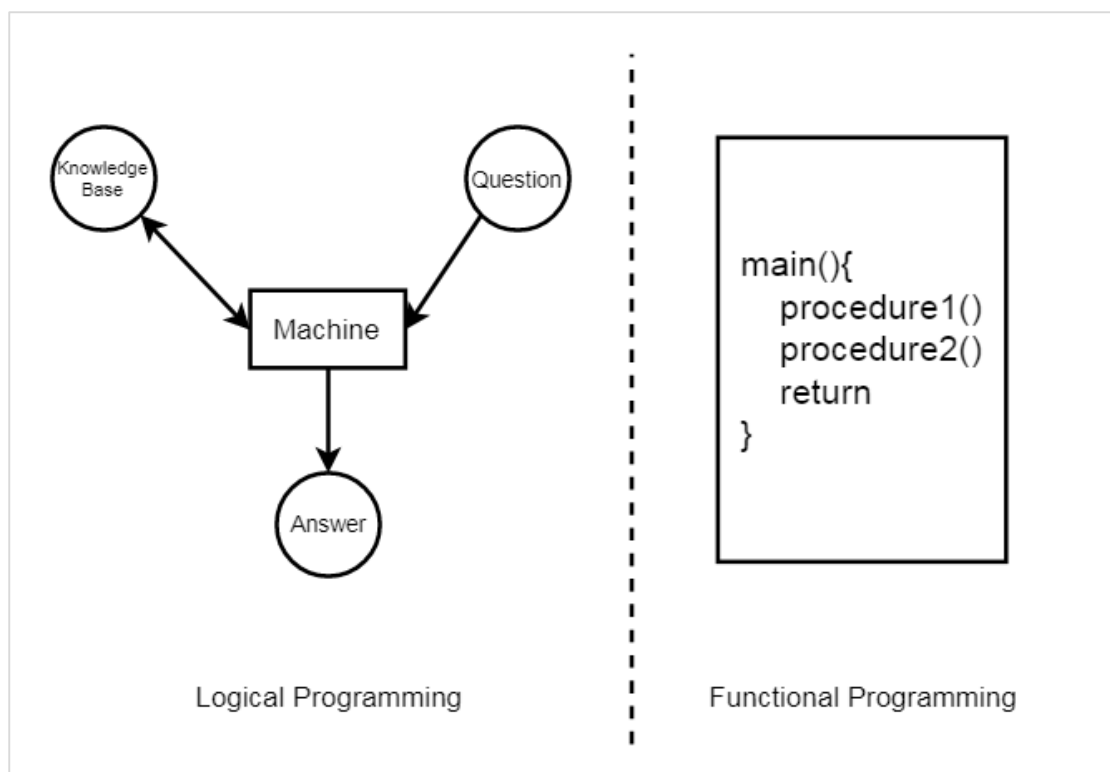
Some logic programming languages like Datalog or ASP (Answer Set Programming) are known as purely declarative languages. These languages allow statements about what the program should accomplish. There is no such step-by-step instruction on how to perform the task. However, other languages like **Prolog, have declarative and also imperative properties. This may also include procedural statements like "To solve the problem H, perform B1, B2 and B3"**.

Some logic programming languages are given below:

- ALF (algebraic logic functional programming language).
- ASP (Answer Set Programming)
- CyCL
- Datalog
- FuzzyCLIPS
- Janus
- Parlog
- Prolog
- Prolog++
- ROOP

Logic and Functional Programming

We will discuss about the differences between Logic programming and the traditional functional programming languages. We can illustrate these two using the below diagram:



From this illustration, we can see that in Functional Programming, we have to define the procedures, and the rule how the procedures work. These procedures work step by step to solve one specific problem based on the algorithm. On the other hand, for the Logic Programming, we will provide knowledge base. Using this knowledge base, the machine can find answers to the given questions, which is totally different from functional programming.

In functional programming, we have to mention how one problem can be solved, but in logic programming we have to specify for which problem we actually want the solution. Then the logic programming automatically finds a suitable solution that will help us solve that specific problem.

Now let us see some more differences below:

Functional Programming	Logic Programming
Functional Programming follows the Von-Neumann Architecture, or uses the sequential steps.	Logic Programming uses abstract model, or deals with objects and their relationships.
The syntax is actually the sequence of statements like (a, s, I).	The syntax is basically the logic formulae (Horn Clauses).
The computation takes part by executing the statements sequentially.	It computes by deducting the clauses.
Logic and controls are mixed together.	Logics and controls can be separated.

What is Prolog?

Prolog or **PRO**gramming in **LOG**ics is a logical and declarative programming language. It is one major example of the fourth generation language that supports the declarative programming paradigm. This is particularly suitable for programs that involve **symbolic or non-numeric computation**. This is the main reason to use Prolog as the programming language in **Artificial Intelligence**, where **symbol manipulation** and **inference manipulation** are the fundamental tasks.

In Prolog, we need not mention the way how one problem can be solved, we just **need to mention what the problem is**, so that Prolog automatically solves it. However, in Prolog we are supposed to **give clues as the solution method**.

Prolog language basically has **three different elements**:

Facts: The fact is predicate that is true, for example, if we say, "Tom is the son of Jack", then this is a fact.

Rules: Rules are extensions of facts that contain conditional clauses. To satisfy a rule these conditions should be met. For example, if we define a rule as:

```
grandfather(X, Y) :- father(X, Z), parent(Z, Y)
```

This implies that for X to be the grandfather of Y , Z should be a parent of Y and X should be father of Z .

Questions: And to run a prolog program, we need some questions, and those questions can be answered by the given facts and rules.

History of Prolog

The heritage of prolog includes the research on theorem provers and some other automated deduction system that were developed in 1960s and 1970s. The Inference mechanism of the Prolog is based on Robinson's Resolution Principle, that was proposed in 1965, and Answer extracting mechanism by Green (1968). These ideas came together forcefully with the advent of linear resolution procedures.

The explicit goal-directed linear resolution procedures, gave impetus to the development of a general purpose logic programming system. The **first** Prolog was the **Marseille Prolog** based on the work by **Colmerauer** in the year 1970. The manual of this Marseille Prolog interpreter (Roussel, 1975) was the first detailed description of the Prolog language.

Prolog is also considered as a fourth generation programming language supporting the declarative programming paradigm. The well-known Japanese Fifth-Generation Computer Project, that was announced in 1981, adopted Prolog as a development language, and thereby grabbed considerable attention on the language and its capabilities.

Some Applications of Prolog

Prolog is used in various domains. It plays a vital role in automation system. Following are some other important fields where Prolog is used:

- Intelligent Database Retrieval
- Natural Language Understanding

- Specification Language
- Machine Learning
- Robot Planning
- Automation System
- Problem Solving

2. Prolog — Environment Setup

In this chapter, we will discuss how to install Prolog in our system.

Prolog Version

In this tutorial, we are using GNU Prolog, Version: 1.4.5

Official Website

This is the official GNU Prolog website where we can see all the necessary details about GNU Prolog, and also get the download link.

<http://www.gprolog.org/>

Direct Download Link

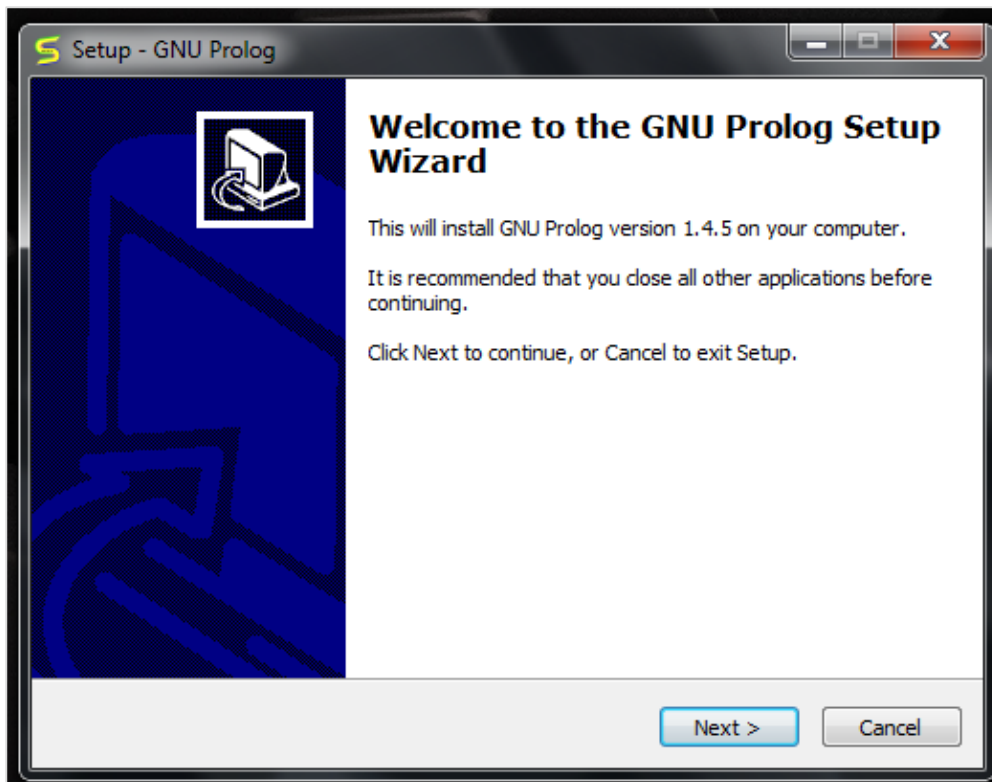
Given below are the direct download links of GNU Prolog for Windows. For other operating systems like Mac or Linux, you can get the download links by visiting the official website (Link is given above):

<http://www.gprolog.org/setup-gprolog-1.4.5-mingw-x86.exe> (32 Bit System)

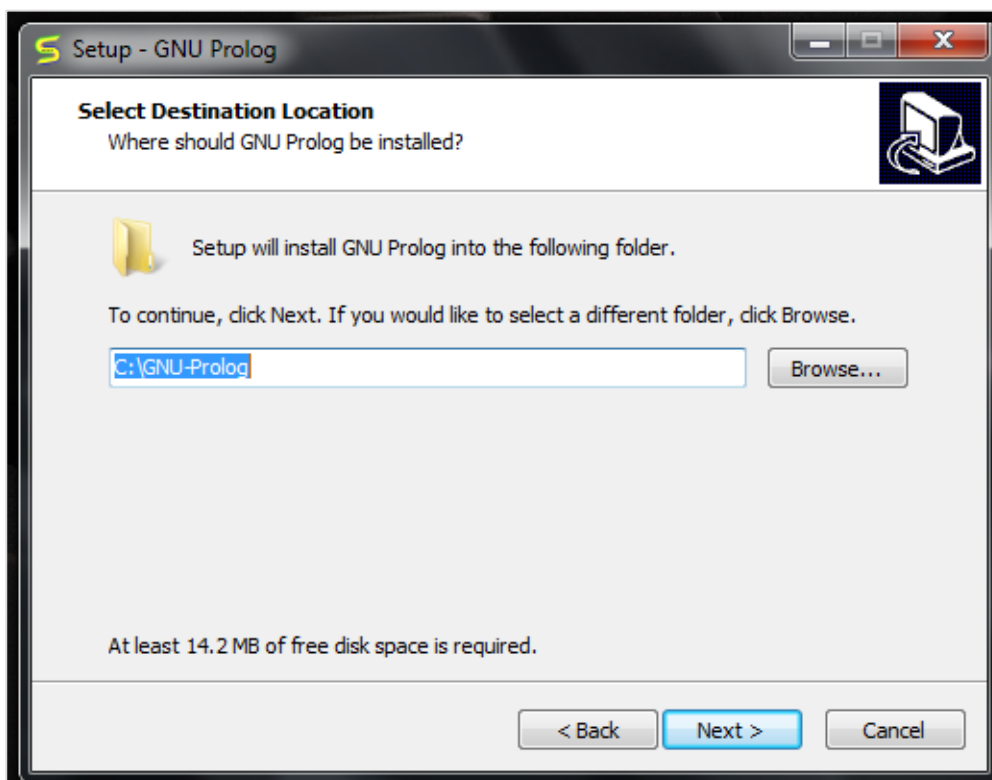
<http://www.gprolog.org/setup-gprolog-1.4.5-mingw-x64.exe> (64 Bit System)

Installation Guide

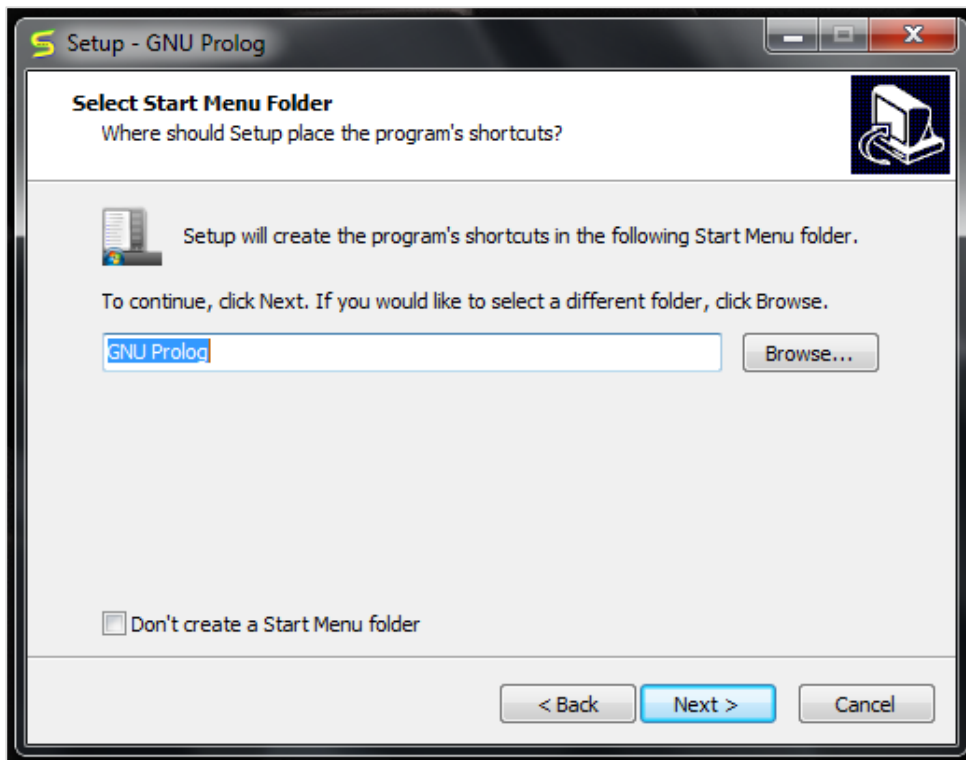
- Download the exe file and run it.
- You will see the window as shown below, then click on **next**:



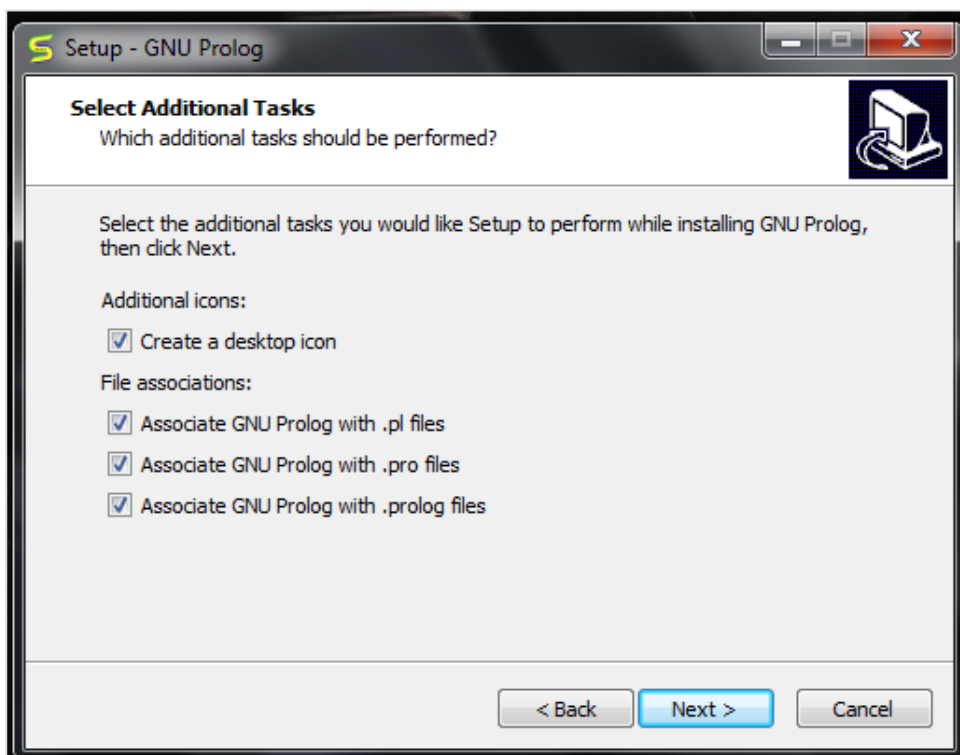
Select proper **directory** where you want to install the software, otherwise let it be installed on the default directory. Then click on **next**.



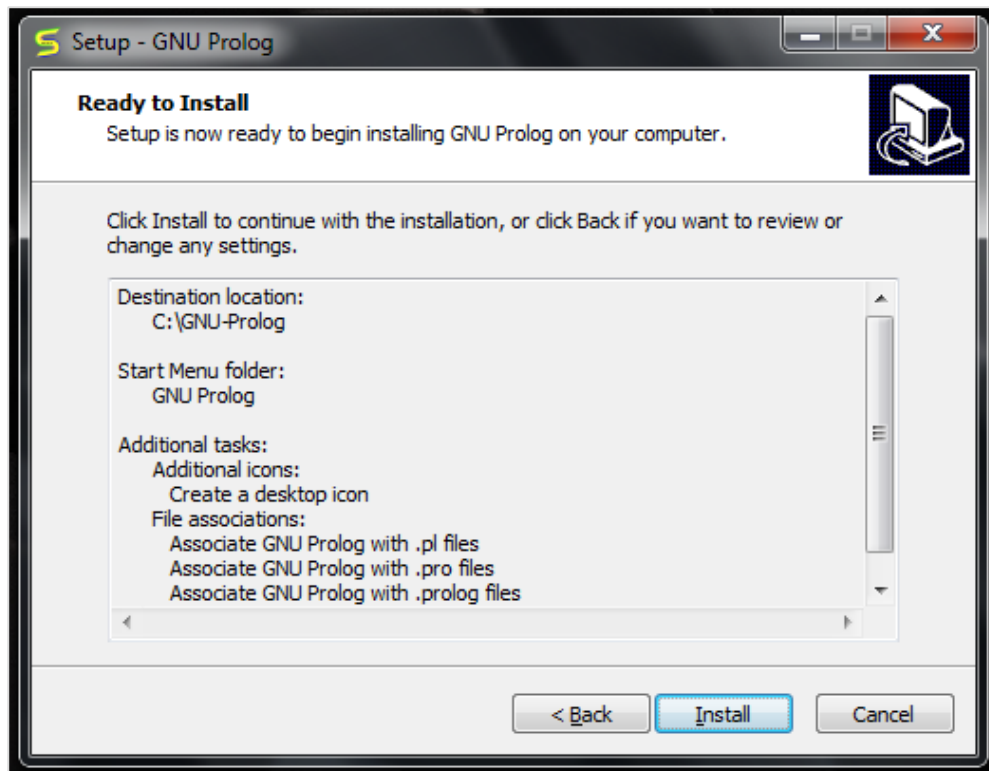
You will get the below screen, simply go to **next**.



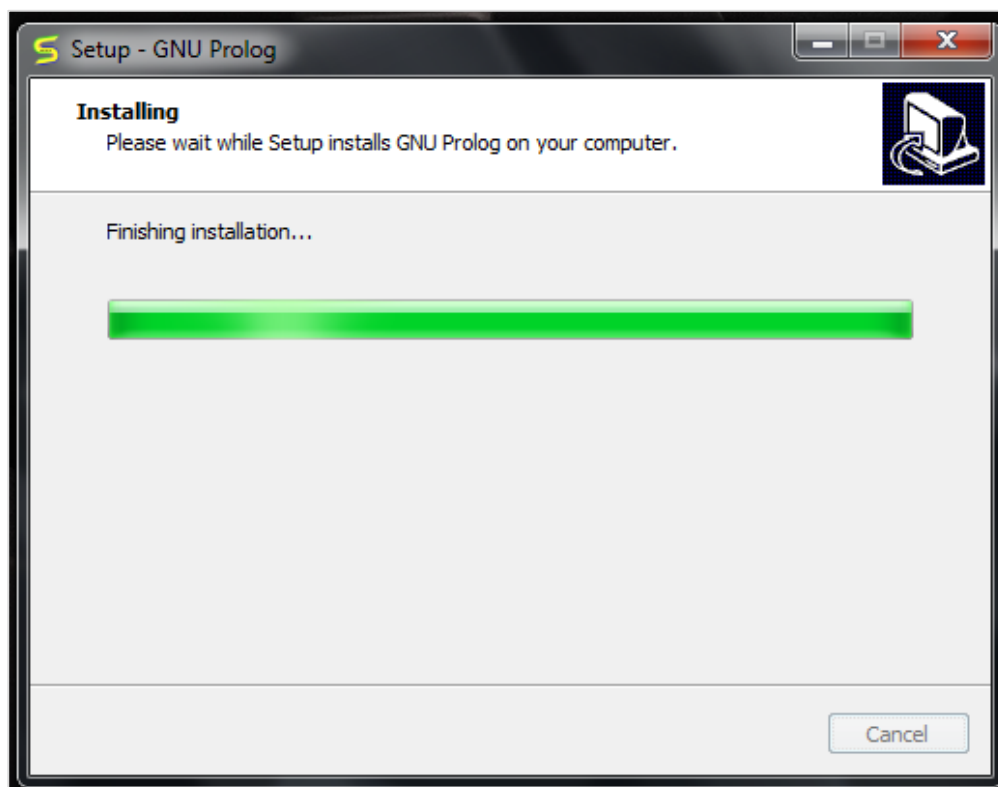
You can verify the below screen, and **check/uncheck** appropriate boxes, otherwise you can leave it as default. Then click on **next**.



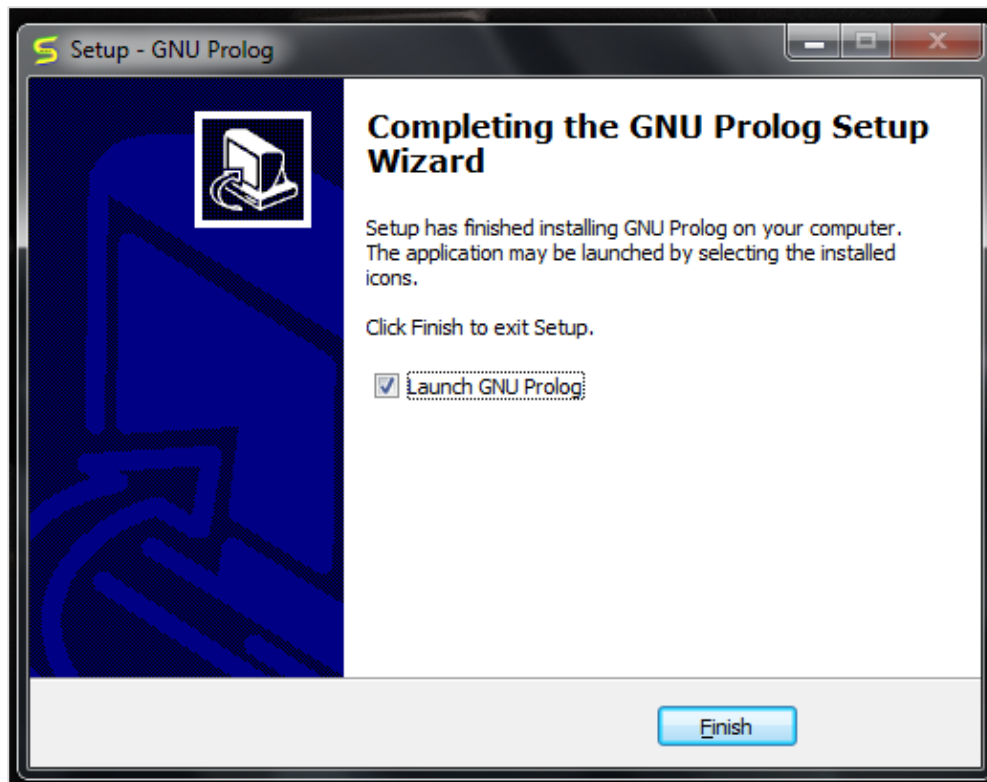
In the next step, you will see the below screen, then click on **Install**.



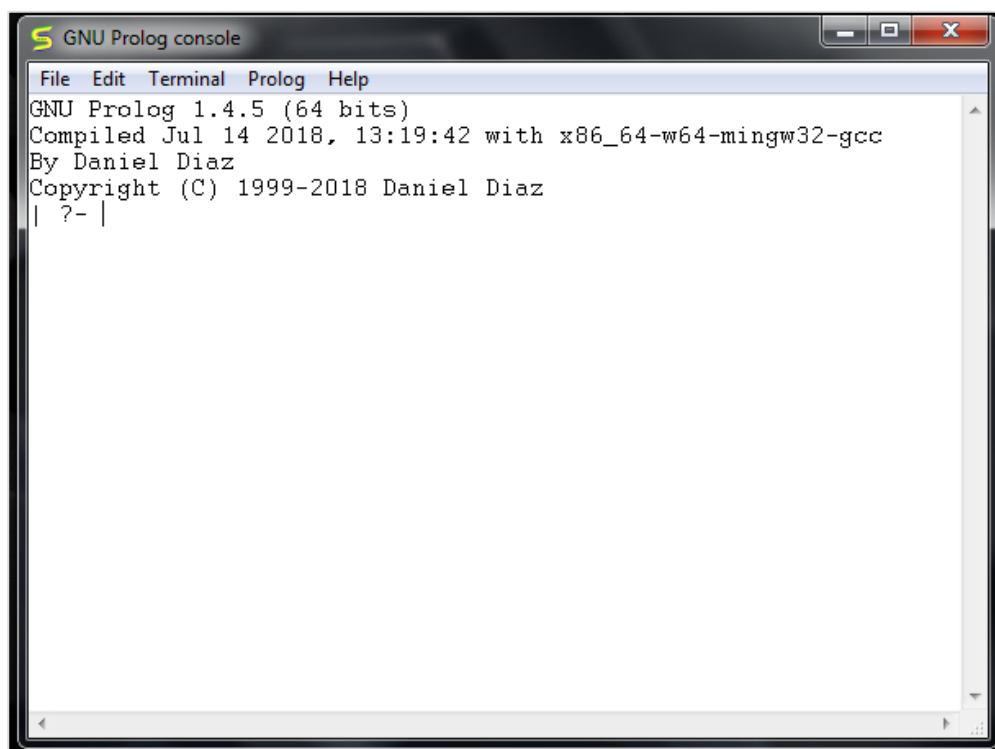
Then wait for the installation process to finish.



Finally click on **Finish** to start GNU Prolog.



The GNU prolog is installed successfully as shown below:



3. Prolog — Hello World

In the previous section, we have seen how to install GNU Prolog. Now, we will see how to write a simple **Hello World** program in our Prolog environment.

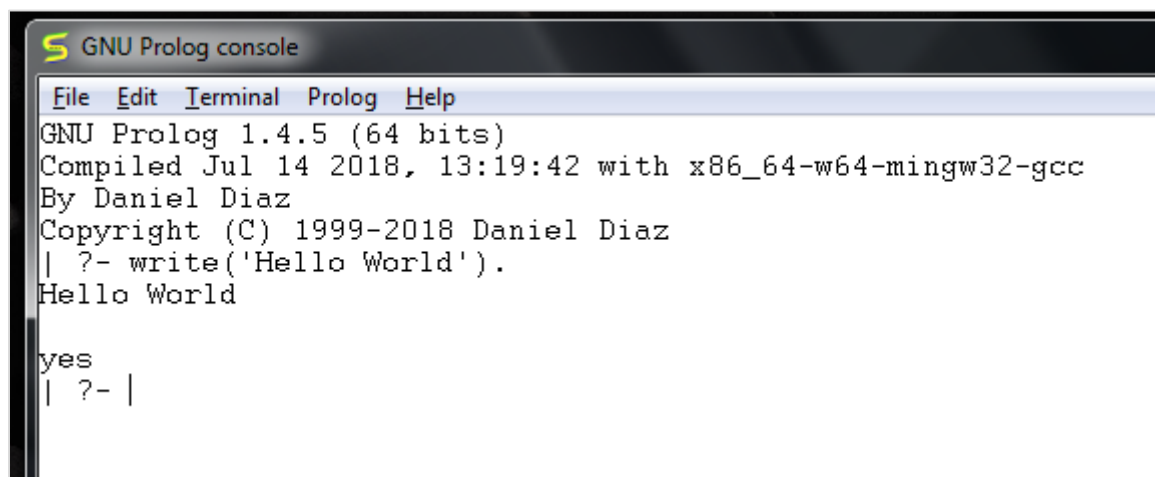
Hello World Program

After running the GNU prolog, we can write hello world program directly from the console. To do so, we have to write the command as follows:

```
write('Hello World').
```

Note: After each line, you have to use one period (.) symbol to show that the line has ended.

The corresponding output will be as shown below:

A screenshot of the GNU Prolog console window. The title bar says "GNU Prolog console". The menu bar includes "File", "Edit", "Terminal", "Prolog", and "Help". The console text shows: "GNU Prolog 1.4.5 (64 bits)", "Compiled Jul 14 2018, 13:19:42 with x86_64-w64-mingw32-gcc", "By Daniel Diaz", "Copyright (C) 1999-2018 Daniel Diaz", "| ?- write('Hello World').", "Hello World", "yes", and "| ?- |".

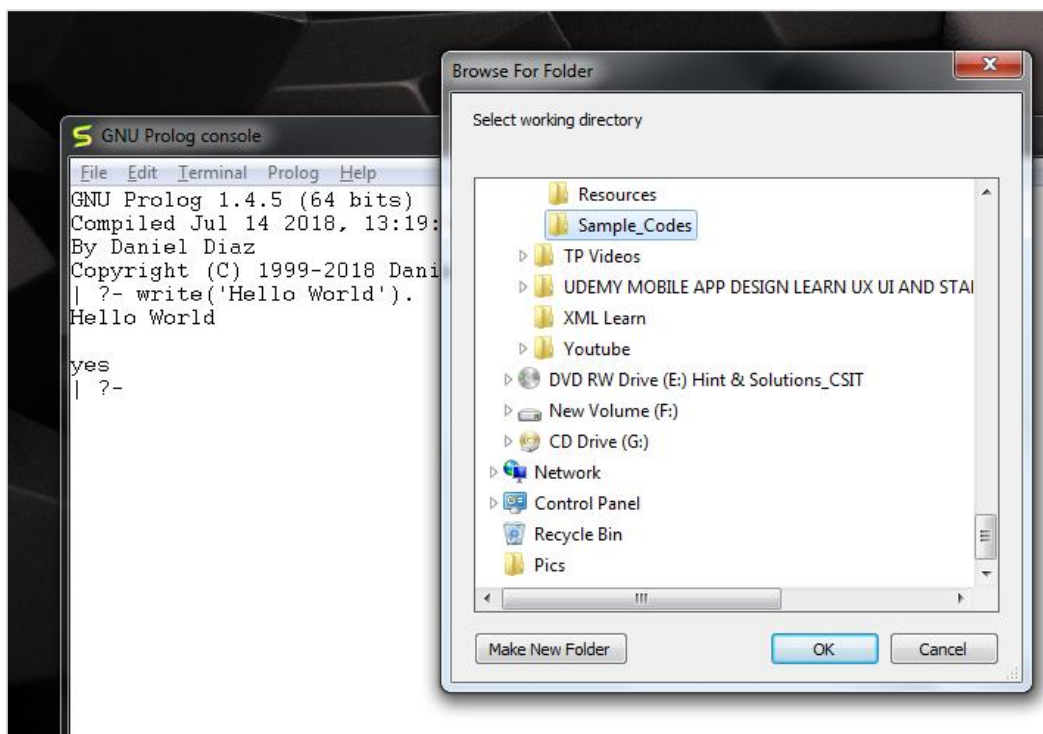
```
GNU Prolog console
File Edit Terminal Prolog Help
GNU Prolog 1.4.5 (64 bits)
Compiled Jul 14 2018, 13:19:42 with x86_64-w64-mingw32-gcc
By Daniel Diaz
Copyright (C) 1999-2018 Daniel Diaz
| ?- write('Hello World').
Hello World
yes
| ?- |
```

Now let us see how to run the Prolog script file (extension is *.pl) into the Prolog console.

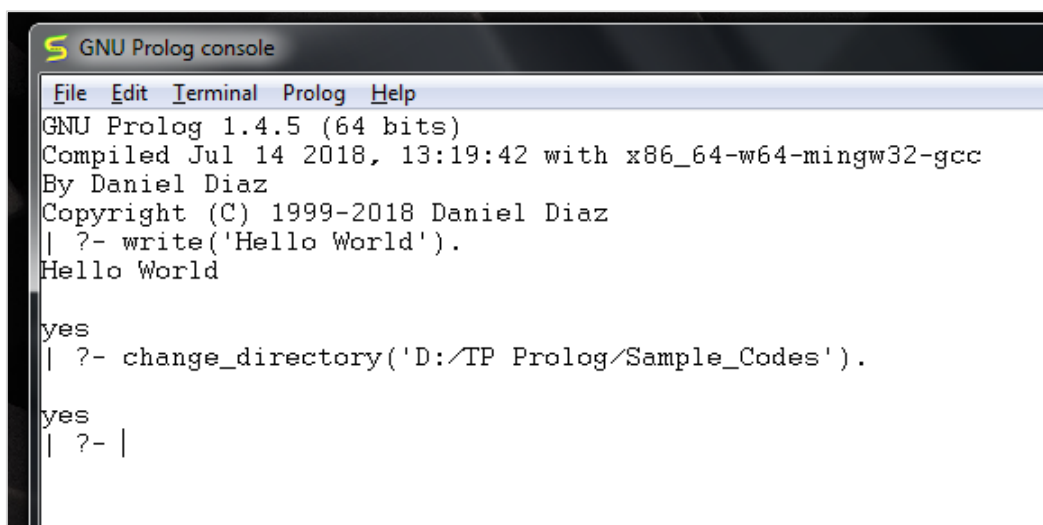
Before running *.pl file, we must store the file into the directory where the GNU prolog console is pointing, otherwise just change the directory by the following steps:

Step 1: From the prolog console, go to File > Change Dir, then click on that menu.

Step 2: Select the proper folder and press **OK**.



Now we can see in the prolog console, it shows that we have successfully changed the directory.



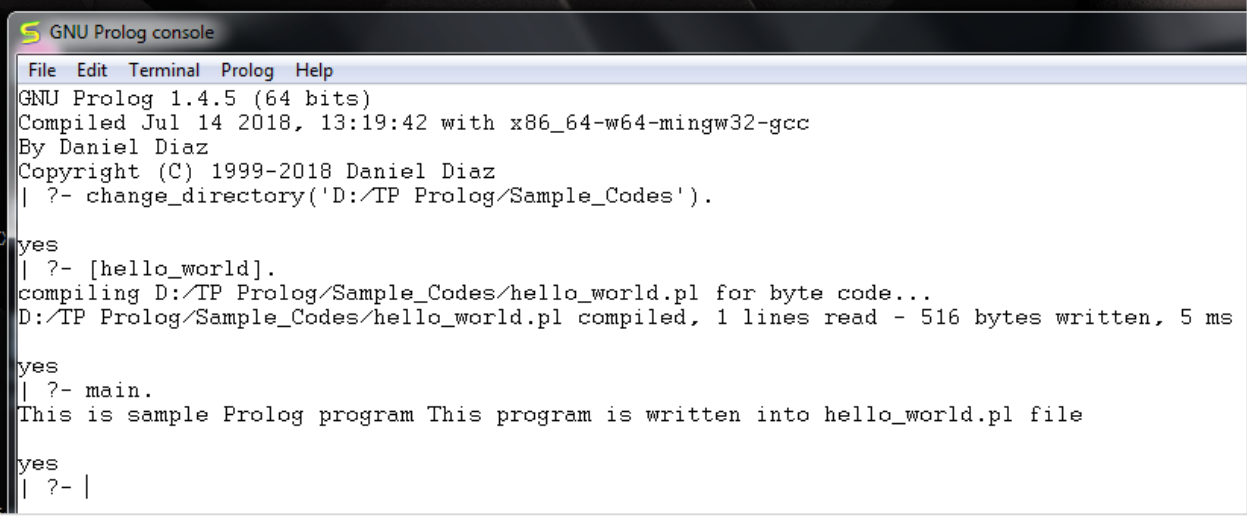
Step 3: Now create one file (extension is *.pl) and write the code as follows:

```
main :- write('This is sample Prolog program'),
write(' This program is written into hello_world.pl file').
```

Now let's run the code. To run it, we have to write the file name as follows:

```
[hello_world]
```

The output is as follows:



```
GNU Prolog console
File Edit Terminal Prolog Help
GNU Prolog 1.4.5 (64 bits)
Compiled Jul 14 2018, 13:19:42 with x86_64-w64-mingw32-gcc
By Daniel Diaz
Copyright (C) 1999-2018 Daniel Diaz
| ?- change_directory('D:/TP Prolog/Sample_Codes').
yes
| ?- [hello_world].
compiling D:/TP Prolog/Sample_Codes/hello_world.pl for byte code...
D:/TP Prolog/Sample_Codes/hello_world.pl compiled, 1 lines read - 516 bytes written, 5 ms
yes
| ?- main.
This is sample Prolog program This program is written into hello_world.pl file
yes
| ?- |
```

4. Prolog — Basics

In this chapter, we will gain some basic knowledge about Prolog. So we will move on to the first step of our Prolog Programming.

The different topics that will be covered in this chapter are:

Knowledge Base: This is one of the fundamental parts of Logic Programming. We will see in detail about the Knowledge Base, and how it helps in logic programming.

Facts, Rules and Queries: These are the building blocks of logic programming. We will get some detailed knowledge about facts and rules, and also see some kind of queries that will be used in logic programming.

Here, we will discuss about the essential building blocks of logic programming. These building blocks are **Facts, Rules and the Queries**.

Facts

We can define fact as an explicit relationship between objects, and properties these objects might have. So facts are unconditionally true in nature. Suppose we have some facts as given below:

- Tom is a cat
- Kunal loves to eat Pasta
- Hair is black
- Nawaz loves to play games
- Pratyusha is lazy.

So these are some facts, that are unconditionally true. These are actually statements, that we have to consider as true.

Following are some guidelines to write facts:

- Names of properties/relationships begin with lower case letters.
- The relationship name appears as the first term.
- Objects appear as comma-separated arguments within parentheses.
- A period "." must end a fact.
- Objects also begin with lower case letters. They also can begin with digits (like 1234), and can be strings of characters enclosed in quotes e.g. color(penink, 'red').
- phoneno(agnibha, 1122334455). is also called a predicate or clause.

Syntax

The syntax for facts is as follows:

```
relation(object1,object2...).
```

Example

Following is an example of the above concept:

```
cat(tom).
loves_to_eat(kunal,pasta).
of_color(hair,black).
loves_to_play_games(nawaz).
lazy(pratyusha).
```

Rules

We can define rule as an implicit relationship between objects. So facts are conditionally true. So when one associated condition is true, then the predicate is also true. Suppose we have some rules as given below:

- Lili is happy if she dances.
- Tom is hungry if he is searching for food.
- Jack and Bili are friends if both of them love to play cricket.
- Ryan will go to play if school is closed, and he is free.

So these are some rules that are **conditionally** true, so when the right hand side is true, then the left hand side is also true.

Here the symbol (:-) will be pronounced as "If", or "is implied by". This is also known as neck symbol, the LHS of this symbol is called the Head, and right hand side is called Body. Here we can use comma (,) which is known as conjunction, and we can also use semicolon, that is known as disjunction.

Syntax

```
rule_name(object1, object2, ...) :- fact/rule(object1, object2, ...)
```

Suppose a clause is like :

```
P :- Q;R.
```

This can also be written as

```
P :- Q.
```

```
P :- R.
```

If one clause is like :

```
P :- Q,R;S,T,U.
```

Is understood as

```
P :- (Q,R);(S,T,U).
Or can also be written as:
P :- Q,R.
P :- S,T,U.
```

Example

```
happy(lili) :- dances(lili).
hungry(tom) :- search_for_food(tom).
friends(jack, bili) :- lovesCricket(jack), lovesCricket(bili).
goToPlay(ryan) :- isClosed(school), free(ryan).
```

Queries

Queries are some questions on the relationships between objects and object properties. So question can be anything, as given below:

- Is tom a cat?
- Does Kunal love to eat pasta?
- Is Lili happy?
- Will Ryan go to play?

So according to these queries, Logic programming language can find the answer and return them.

Knowledge Base in Logic Programming

In this section, we will see what knowledge base in logic programming is.

Well, as we know there are three main components in logic programming: **Facts**, **Rules** and **Queries**. Among these three if we collect the facts and rules as a whole then that forms a **Knowledge Base**. So we can say that the **knowledge base is a collection of facts and rules**.

Now, we will see how to write some knowledge bases. Suppose we have our very first knowledge base called KB1. Here in the KB1, we have some facts. The facts are used to state things, that are unconditionally true of the domain of interest.

Knowledge Base 1

Suppose we have some knowledge, that Priya, Tiyaasha, and Jaya are three girls, among them, Priya can cook. Let's try to write these facts in a more generic way as shown below:

```
girl(priya).
girl(tiyasha).
girl(jaya).
can_cook(priya).
```

Note: Here we have written the name in lowercase letters, because in Prolog, a string starting with uppercase letter indicates a **variable**.

Now we can use this knowledge base by posing some queries. "Is priya a girl?", it will reply "yes", "is jamini a girl?" then it will answer "No", because it does not know who jamini is. Our next question is "Can Priya cook?", it will say "yes", but if we ask the same question for Jaya, it will say "No".

Output

```
GNU Prolog 1.4.5 (64 bits)
Compiled Jul 14 2018, 13:19:42 with x86_64-w64-mingw32-gcc
By Daniel Diaz
Copyright (C) 1999-2018 Daniel Diaz
| ?- change_directory('D:/TP Prolog/Sample_Codes').

yes
| ?- [kb1]
.
compiling D:/TP Prolog/Sample_Codes/kb1.pl for byte code...
D:/TP Prolog/Sample_Codes/kb1.pl compiled, 3 lines read - 489 bytes written, 10
ms

yes
| ?- girl(priya)
.

yes
| ?- girl(jamini).

no
| ?- can_cook(priya).

yes
| ?- can_cook(jaya).

no
| ?-
```

Knowledge Base 2

Let us see another knowledge base, where we have some rules. Rules contain some information that are conditionally true about the domain of interest. Suppose our knowledge base is as follows:

```
sing_a_song(ananya).
listens_to_music(rohit).

listens_to_music(ananya) :- sing_a_song(ananya).
happy(ananya) :- sing_a_song(ananya).
happy(rohit) :- listens_to_music(rohit).
plays_guitar(rohit) :- listens_to_music(rohit).
```

So there are some facts and rules given above. The first two are facts, but the rest are rules. As we know that Ananya sings a song, this implies she also listens to music. So if we ask "Does Ananya listen to music?", the answer will be true. Similarly, "is Rohit happy?", this will also be true because he listens to music. But if our question is "does Ananya play guitar?", then according to the knowledge base, it will say "No". So these are some examples of queries based on this Knowledge base.

Output

```
| ?- [kb2].
compiling D:/TP Prolog/Sample_Codes/kb2.pl for byte code...
D:/TP Prolog/Sample_Codes/kb2.pl compiled, 6 lines read - 1066 bytes written,
15 ms

yes
| ?- happy(rohit).

yes
| ?- sing_a_song(rohit).

no
| ?- sing_a_song(ananya).

yes
| ?- plays_guitar(rohit).

yes
| ?- plays_guitar(ananya).

no
```



```
| ?- listens_to_music(ananya).
```

```
yes
```

```
| ?-
```

Knowledge Base 3

The facts and rules of Knowledge Base 3 are as follows:

```
can_cook(priya).
```

```
can_cook(jaya).
```

```
can_cook(tiyasha).
```

```
likes(priya,jaya) :- can_cook(jaya).
```

```
likes(priya,tiyasha) :- can_cook(tiyasha).
```

Suppose we want to see the members who can cook, we can use one **variable** in our query. The variables should start with uppercase letters. In the result, it will show one by one. If we press enter, then it will come out, otherwise if we press semicolon (;), then it will show the next result.

Let us see one practical demonstration output to understand how it works.

Output

```
| ?- [kb3].
```

```
compiling D:/TP Prolog/Sample_Codes/kb3.pl for byte code...
```

```
D:/TP Prolog/Sample_Codes/kb3.pl compiled, 5 lines read - 737 bytes written, 22 ms
```

```
warning: D:/TP Prolog/Sample_Codes/kb3.pl:1: redefining procedure can_cook/1
         D:/TP Prolog/Sample_Codes/kb1.pl:4: previous definition
```

```
yes
```

```
| ?- can_cook(X).
```

```
X = priya ? ;
```

```
X = jaya ? ;
```

```
X = tiyasha
```

```
yes
```

```
| ?- likes(priya,X).
```

```
X = jaya ? ;
```

```
X = tiyasha
```

```
yes
```

```
| ?-
```

5. Prolog — Relations

Relationship is one of the main features that we have to properly mention in Prolog. These relationships can be expressed as facts and rules. After that we will see about the family relationships, how we can express family based relationships in Prolog, and also see the recursive relationships of the family.

We will create the knowledge base by creating facts and rules, and play query on them.

Relations in Prolog

In Prolog programs, it specifies relationship between objects and properties of the objects.

Suppose, there's a statement, "Amit has a bike", then we are actually declaring the ownership relationship between two objects — one is Amit and the other is bike.

If we ask a question, "Does Amit own a bike?", we are actually trying to find out about one relationship.

There are various kinds of relationships, of which some can be rules as well. A rule can find out about a relationship even if the relationship is not defined explicitly as a fact.

We can define a brother relationship as follows:

Two person are brothers, if,

- They both are male.
- They have the same parent.

Now consider we have the below phrases:

- `parent(sudip, piyus).`
- `parent(sudip, raj).`
- `male(piyus).`
- `male(raj).`
- `brother(X,Y) :- parent(Z,X), parent(Z,Y), male(X), male(Y)`

These clauses can give us the answer that piyus and raj are brothers, but we will get three pairs of output here. They are: (piyus, piyus), (piyus, raj), (raj, raj). For these pairs, given conditions are true, but for the pairs (piyus, piyus), (raj, raj), they are not actually brothers, they are the same persons. So we have to create the clauses properly to form a relationship.

The revised relationship can be as follows:

A and B are brothers if:

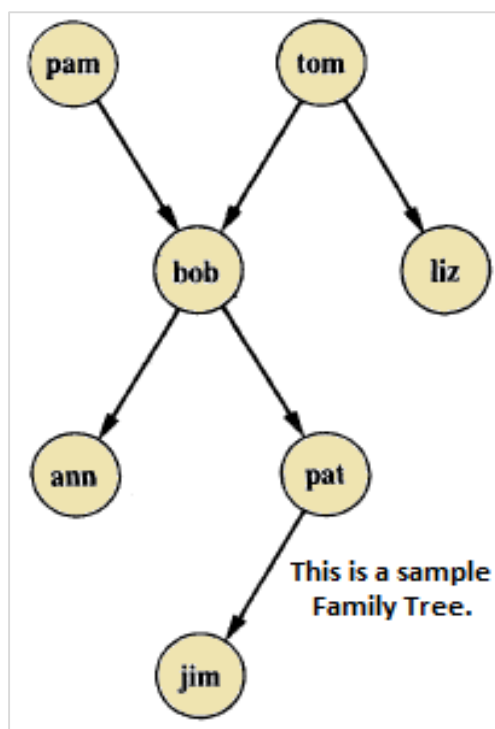
- A and B, both are male
- They have same father
- They have same mother

- A and B are not same

Family Relationship in Prolog

Here we will see the family relationship. This is an example of complex relationship that can be formed using Prolog. We want to make a family tree, and that will be mapped into facts and rules, then we can run some queries on them.

Suppose the family tree is as follows:



Here from this tree, we can understand that there are few relationships. Here bob is a child of pam and tom, and bob also has two children — ann and pat. Bob has one brother liz, whose parent is also tom. So we want to make predicates as follows:

Predicates

- parent(pam, bob).
- parent(tom, bob).
- parent(tom, liz).
- parent(bob, ann).
- parent(bob, pat).
- parent(pat, jim).
- parent(bob, peter).
- parent(peter, jim).

From our example, it has helped to illustrate some important points:

- We have defined parent relation by stating the n-tuples of objects based on the given info in the family tree.
- The user can easily query the Prolog system about relations defined in the program.
- A Prolog program consists of clauses terminated by a full stop.
- The arguments of relations can (among other things) be: concrete objects, or constants (such as pat and jim), or general objects such as X and Y. Objects of the first kind in our program are called atoms. Objects of the second kind are called variables.
- Questions to the system consist of one or more goals.

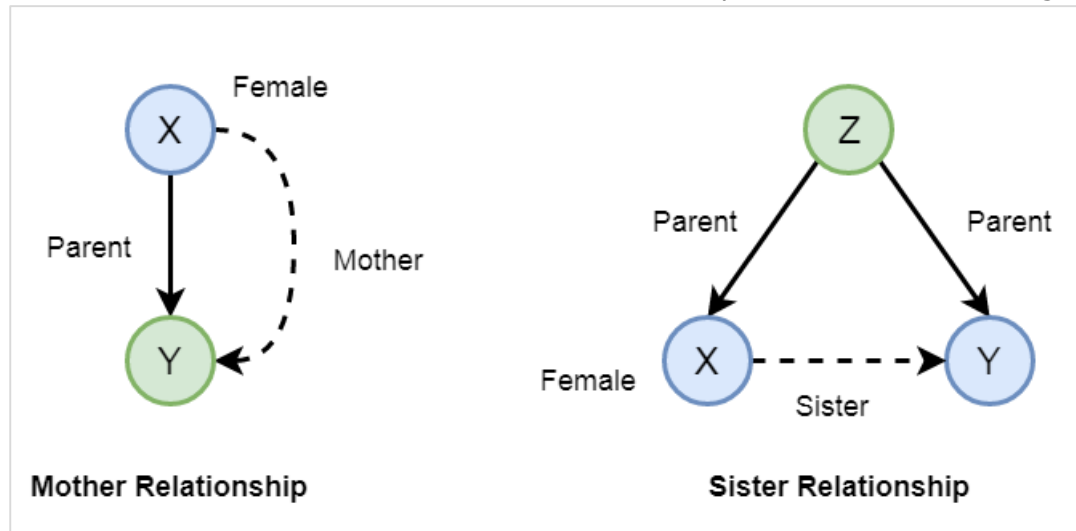
Some facts can be written in two different ways, like sex of family members can be written in either of the forms:

- female(pam).
- male(tom).
- male(bob).
- female(liz).
- female(pat).
- female(ann).
- male(jim).

Or in the below form:

- sex(pam, feminine).
- sex(tom, masculine).
- sex(bob, masculine).
- ... and so on.

Now if we want to make mother and sister relationship, then we can write as given below:



In Prolog syntax, we can write:

- `mother(X,Y) :- parent(X,Y), female(X).`
- `sister(X,Y) :- parent(Z,X), parent(Z,Y), female(X), X \== Y.`

Now let us see the practical demonstration:

Knowledge Base (family.pl)

```
female(pam).
female(liz).
female(pat).
female(ann).

male(jim).
male(bob).
male(tom).
male(peter).

parent(pam,bob).
parent(tom,bob).
parent(tom,liz).
parent(bob,ann).
parent(bob,pat).
parent(pat,jim).
parent(bob,peter).
parent(peter,jim).
```

```

mother(X,Y):- parent(X,Y),female(X).
father(X,Y):- parent(X,Y),male(X).
haschild(X):- parent(X,_).
sister(X,Y):- parent(Z,X),parent(Z,Y),female(X),X\==Y.
brother(X,Y):-parent(Z,X),parent(Z,Y),male(X),X\==Y.

```

Output

```

| ?- [family].
compiling D:/TP Prolog/Sample_Codes/family.pl for byte code...
D:/TP Prolog/Sample_Codes/family.pl compiled, 23 lines read - 3088 bytes
written, 9 ms

yes
| ?- parent(X,jim).

X = pat ? ;

X = peter

yes
| ?-
mother(X,Y).

X = pam
Y = bob ? ;

X = pat
Y = jim ? ;

no
| ?- haschild(X).

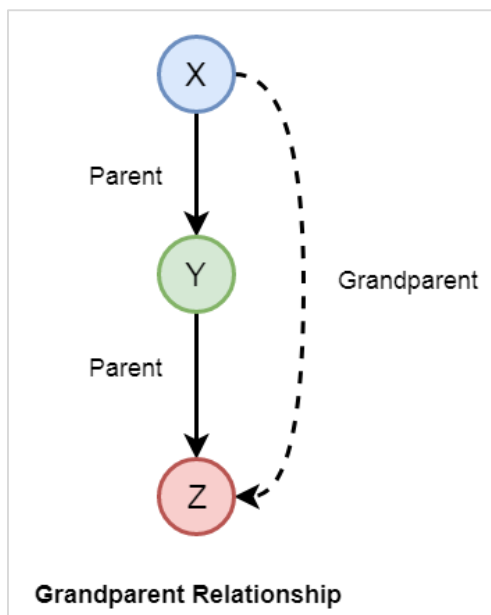
X = pam ? ;

X = tom ? ;

```

```
X = tom ? ;  
  
X = bob ? ;  
  
X = bob ? ;  
  
X = pat ? ;  
  
X = bob ? ;  
  
X = peter  
  
yes  
| ?- sister(X,Y).  
  
X = liz  
Y = bob ? ;  
  
X = ann  
Y = pat ? ;  
  
X = ann  
Y = peter ? ;  
  
X = pat  
Y = ann ? ;  
  
X = pat  
Y = peter ? ;  
  
(16 ms) no  
| ?-
```

Now let us see some more relationships that we can make from the previous relationships of a family. So if we want to make a grandparent relationship, that can be formed as follows:



We can also create some other relationships like wife, uncle, etc. We can write the relationships as given below:

- `grandparent(X,Y) :- parent(X,Z), parent(Z,Y).`
- `grandmother(X,Z) :- mother(X,Y), parent(Y,Z).`
- `grandfather(X,Z) :- father(X,Y), parent(Y,Z).`
- `wife(X,Y) :- parent(X,Z),parent(Y,Z), female(X),male(Y).`
- `uncle(X,Z) :- brother(X,Y), parent(Y,Z).`

So let us write a prolog program to see this in action. Here we will also see the trace to trace-out the execution.

Knowledge Base (family_ext.pl)

```
female(pam).
female(liz).
female(pat).
female(ann).

male(jim).
male(bob).
male(tom).
male(peter).

parent(pam,bob).
parent(tom,bob).
parent(tom,liz).
parent(bob,ann).
```

```

parent(bob,pat).
parent(pat,jim).
parent(bob,peter).
parent(peter,jim).

mother(X,Y):- parent(X,Y),female(X).
father(X,Y):-parent(X,Y),male(X).
sister(X,Y):-parent(Z,X),parent(Z,Y),female(X),X\==Y.
brother(X,Y):-parent(Z,X),parent(Z,Y),male(X),X\==Y.
grandparent(X,Y):-parent(X,Z),parent(Z,Y).
grandmother(X,Z):-mother(X,Y),parent(Y,Z).
grandfather(X,Z):-father(X,Y),parent(Y,Z).
wife(X,Y):-parent(X,Z),parent(Y,Z),female(X),male(Y).
uncle(X,Z):-brother(X,Y),parent(Y,Z).

```

Output

```

| ?- [family_ext].
compiling D:/TP Prolog/Sample_Codes/family_ext.pl for byte code...
D:/TP Prolog/Sample_Codes/family_ext.pl compiled, 27 lines read - 4646 bytes
written, 10 ms

| ?- uncle(X,Y).

X = peter
Y = jim ? ;

no
| ?- grandparent(X,Y).

X = pam
Y = ann ? ;

X = pam
Y = pat ? ;

X = pam
Y = peter ? ;

```

```
X = tom
Y = ann ? ;

X = tom
Y = pat ? ;

X = tom
Y = peter ? ;

X = bob
Y = jim ? ;

X = bob
Y = jim ? ;

no
| ?- wife(X,Y).

X = pam
Y = tom ? ;

X = pat
Y = peter ? ;

(15 ms) no
| ?-
```

Tracing the output

In Prolog we can trace the execution. To trace the output, you have to enter into the trace mode by typing "trace.". Then from the output we can see that we are just tracing "pam is mother of whom?". See the tracing output by taking X = pam, and Y as variable, there Y will be bob as answer. To come out from the tracing mode press "notrace."

Program

```
| ?- [family_ext].
compiling D:/TP Prolog/Sample_Codes/family_ext.pl for byte code...
D:/TP Prolog/Sample_Codes/family_ext.pl compiled, 27 lines read - 4646 bytes
written, 10 ms

(16 ms) yes
| ?- mother(X,Y).

X = pam
Y = bob ? ;

X = pat
Y = jim ? ;

no
| ?- trace.
The debugger will first creep -- showing everything (trace)

yes
{trace}
| ?- mother(pam,Y).
    1    1  Call: mother(pam,_23) ?
    2    2  Call: parent(pam,_23) ?
    2    2  Exit: parent(pam,bob) ?
    3    2  Call: female(pam) ?
    3    2  Exit: female(pam) ?
    1    1  Exit: mother(pam,bob) ?

Y = bob

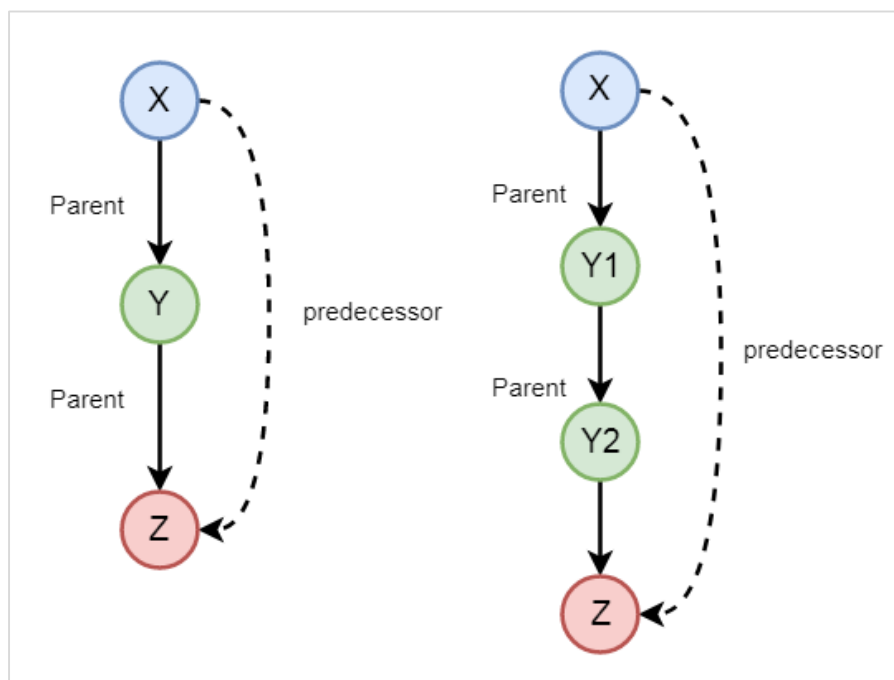
(16 ms) yes
```

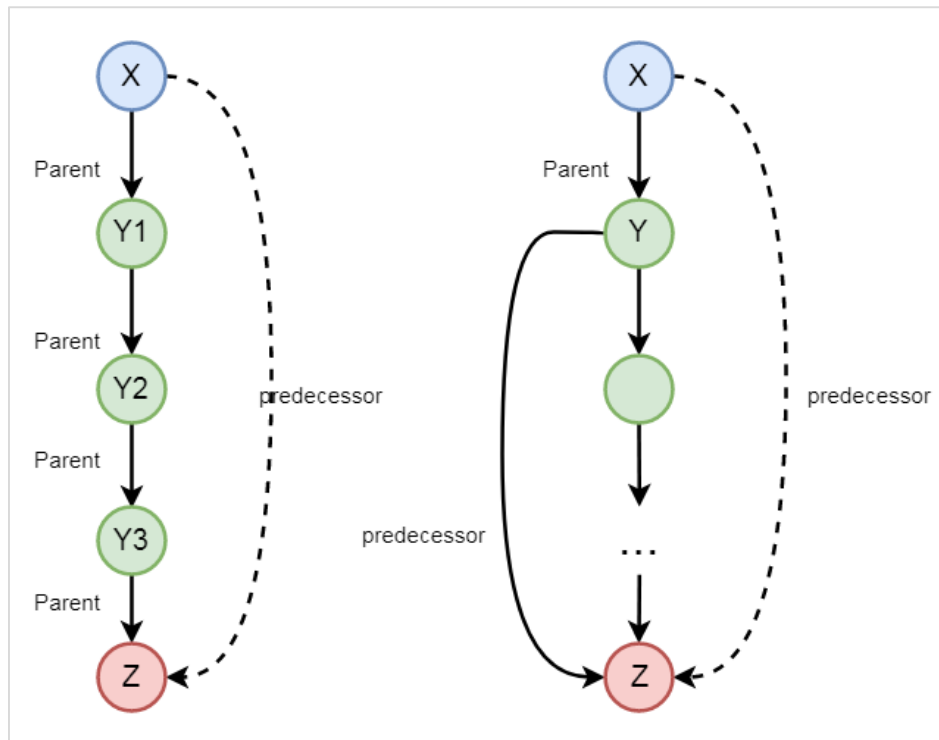
```
{trace}
| ?- notrace.
The debugger is switched off

yes
| ?-
```

Recursion in Family Relationship

In the previous section, we have seen that we can define some family relationships. These relationships are static in nature. We can also create some recursive relationships which can be expressed from the following illustration:





So we can understand that predecessor relationship is recursive. We can express this relationship using the following syntax:

```
predecessor(X, Z) :- parent(X, Z).
predecessor(X, Z) :- parent(X, Y), predecessor(Y, Z).
```

Now let us see the practical demonstration.

Knowledge Base (family_rec.pl)

```
female(pam).
female(liz).
female(pat).
female(ann).

male(jim).
male(bob).
male(tom).
male(peter).

parent(pam,bob).
parent(tom,bob).
parent(tom,liz).
parent(bob,ann).
```

```

parent(bob,pat).
parent(pat,jim).
parent(bob,peter).
parent(peter,jim).

predecessor(X, Z) :- parent(X, Z).
predecessor(X, Z) :- parent(X, Y),predecessor(Y, Z).

```

Output

```

| ?- [family_rec].
compiling D:/TP Prolog/Sample_Codes/family_rec.pl for byte code...
D:/TP Prolog/Sample_Codes/family_rec.pl compiled, 21 lines read - 1851 bytes
written, 14 ms

yes
| ?- predecessor(peter,X).

X = jim ? ;

no
| ?- trace.
The debugger will first creep -- showing everything (trace)

yes
{trace}
| ?- predecessor(bob,X).
    1    1  Call: predecessor(bob,_23) ?
    2    2  Call: parent(bob,_23) ?
    2    2  Exit: parent(bob,ann) ?
    1    1  Exit: predecessor(bob,ann) ?

X = ann ? ;
    1    1  Redo: predecessor(bob,ann) ?
    2    2  Redo: parent(bob,ann) ?

```

```

2    2    Exit: parent(bob,pat) ?
1    1    Exit: predecessor(bob,pat) ?

X = pat ? ;
1    1    Redo: predecessor(bob,pat) ?
2    2    Redo: parent(bob,pat) ?
2    2    Exit: parent(bob,peter) ?
1    1    Exit: predecessor(bob,peter) ?

X = peter ? ;
1    1    Redo: predecessor(bob,peter) ?
2    2    Call: parent(bob,_92) ?
2    2    Exit: parent(bob,ann) ?
3    2    Call: predecessor(ann,_23) ?
4    3    Call: parent(ann,_23) ?
4    3    Fail: parent(ann,_23) ?
4    3    Call: parent(ann,_141) ?
4    3    Fail: parent(ann,_129) ?
3    2    Fail: predecessor(ann,_23) ?
2    2    Redo: parent(bob,ann) ?
2    2    Exit: parent(bob,pat) ?
3    2    Call: predecessor(pat,_23) ?
4    3    Call: parent(pat,_23) ?
4    3    Exit: parent(pat,jim) ?
3    2    Exit: predecessor(pat,jim) ?
1    1    Exit: predecessor(bob,jim) ?

X = jim ? ;
1    1    Redo: predecessor(bob,jim) ?
3    2    Redo: predecessor(pat,jim) ?
4    3    Call: parent(pat,_141) ?
4    3    Exit: parent(pat,jim) ?
5    3    Call: predecessor(jim,_23) ?

```



```
6 4 Call: parent(jim,_23) ?  
6 4 Fail: parent(jim,_23) ?  
6 4 Call: parent(jim,_190) ?  
6 4 Fail: parent(jim,_178) ?  
5 3 Fail: predecessor(jim,_23) ?  
3 2 Fail: predecessor(pat,_23) ?  
2 2 Redo: parent(bob,pat) ?  
2 2 Exit: parent(bob,peter) ?  
3 2 Call: predecessor(peter,_23) ?  
4 3 Call: parent(peter,_23) ?  
4 3 Exit: parent(peter,jim) ?  
3 2 Exit: predecessor(peter,jim) ?  
1 1 Exit: predecessor(bob,jim) ?
```

X = jim ?

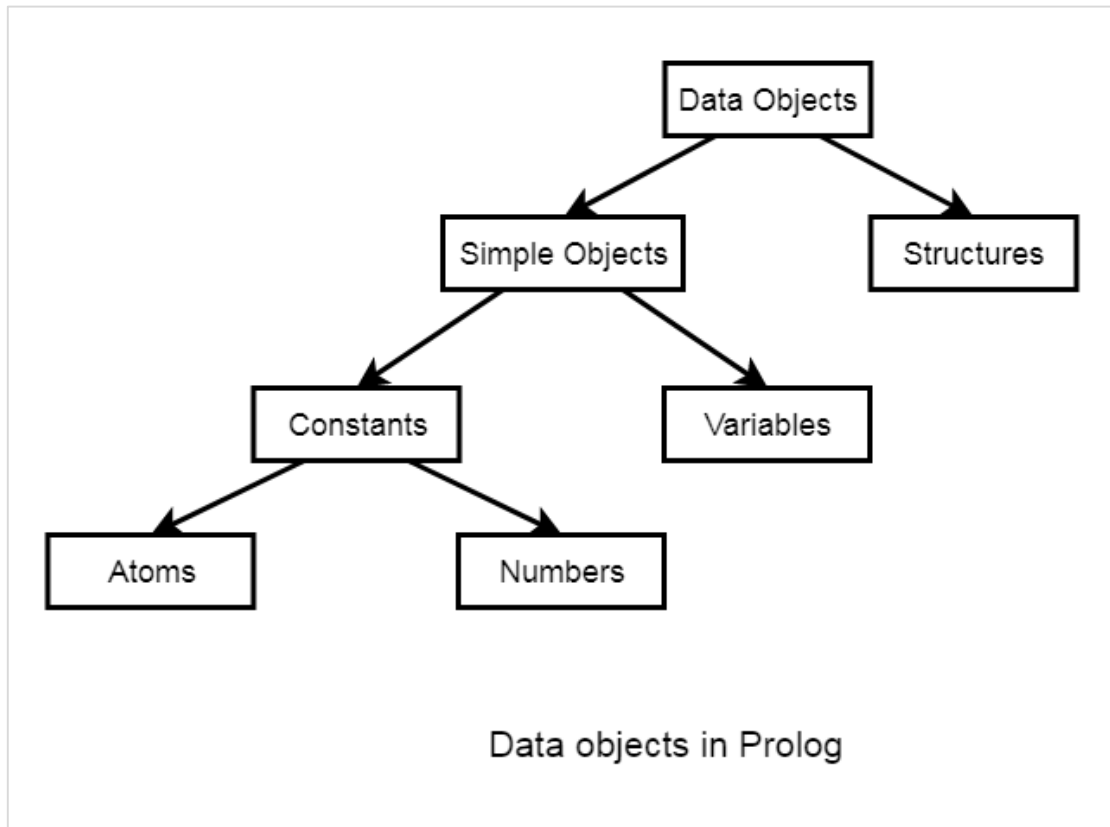
(78 ms) yes

{trace}

| ?-

6. Prolog — Data Objects

In this chapter, we will learn data objects in Prolog. They can be divided into few different categories as shown below:



Below are some examples of different kinds of data objects:

- Atoms: tom, pat, x100, x_45
- Numbers: 100, 1235, 2000.45
- Variables: X, Y, Xval, _X
- Structures: day(9, jun, 2017), point(10, 25)

Atoms and Variables

In this section, we will discuss the atoms, numbers and the variables of Prolog.

Atoms

Atoms are one variation of constants. They can be any names or objects. There are few rules that should be followed when we are trying to use Atoms as given below:

Strings of letters, digits and the underscore character, '_', starting with a lower-case letter. For example:

- azahar
- b59
- b_59
- b_59AB
- b_x25
- antara_sarkar

Strings of special characters

We have to keep in mind that when using atoms of this form, some care is necessary as some strings of special characters already have a predefined meaning; for example ':-'.

- <--->
- =====>
- ...
- .:.
- ::=

Strings of characters enclosed in single quotes.

This is useful if we want to have an atom that starts with a capital letter. By enclosing it in quotes, we make it distinguishable from variables:

- 'Rubai'
- 'Arindam_Chatterjee'
- 'Sumit Mitra'

Numbers

Another variation of constants is the Numbers. So integer numbers can be represented as 100, 4, -81, 1202. In Prolog, the normal range of integers is from -16383 to 16383.

Prolog also supports real numbers, but normally the use-case of floating point number is very less in Prolog programs, because Prolog is for symbolic, non-numeric computation. The treatment of real numbers depends on the implementation of Prolog. Example of real numbers are 3.14159, -0.00062, 450.18, etc.

Variables

The variables come under the **Simple Objects** section. Variables can be used in many such cases in our Prolog program, that we have seen earlier. So there are some rules of defining variables in Prolog.

We can define Prolog variables, such that variables are strings of letters, digits and underscore characters. They **start with** an **upper-case letter** or an **underscore character**. Some examples of Variables are:

- X
- Sum
- Memer_name
- Student_list
- Shoppinglist
- _a50
- _15

Anonymous Variables in Prolog

Anonymous variables have no names. The anonymous variables in prolog is written by a single underscore character `'_'`. And one important thing is that each individual anonymous variable is treated as **different**. They are not same.

Now the question is, where should we use these anonymous variables?

Suppose in our knowledge base we have some facts — “jim hates tom”, “pat hates bob”. So if tom wants to find out who hates him, then he can use variables. However, if he wants to check whether there is someone who hates him, we can use anonymous variables. So when we want to use the variable, but do not want to reveal the value of the variable, then we can use anonymous variables.

So let us see its practical implementation:

Knowledge Base (var_anonymous.pl)

```
hates(jim,tom).
hates(pat,bob).
hates(dog,fox).
hates(peter,tom).
```

Output

```
| ?- [var_anonymous].
compiling D:/TP Prolog/Sample_Codes/var_anonymous.pl for byte code...
D:/TP Prolog/Sample_Codes/var_anonymous.pl compiled, 3 lines read - 536 bytes
written, 16 ms

yes
| ?- hates(X,tom).
```

```
X = jim ? ;  
  
X = peter  
  
yes  
| ?- hates(_,tom).  
  
true ? ;  
  
(16 ms) yes  
| ?- hates(_,pat).  
  
no  
| ?- hates(_,fox).  
  
true ? ;  
  
no  
| ?-
```

7. Prolog — Operators

In the following sections, we will see what are the different types of operators in Prolog. Types of the comparison operators and Arithmetic operators.

We will also see how these are different from any other high level language operators, how they are syntactically different, and how they are different in their work. Also we will see some practical demonstration to understand the usage of different operators.

Comparison Operators

Comparison operators are used to compare two equations or states. Following are different comparison operators:

Operator	Meaning
$X > Y$	X is greater than Y
$X < Y$	X is less than Y
$X \geq Y$	X is greater than or equal to Y
$X \leq Y$	X is less than or equal to Y
$X =:= Y$	the X and Y values are equal
$X \neq Y$	the X and Y values are not equal

You can see that the ' $=<$ ' operator, ' $=:=$ ' operator and ' \neq ' operators are syntactically different from other languages. Let us see some practical demonstration to this.

Example

```
| ?- 1+2:=2+1.
```

```
yes
```

```
| ?- 1+2=2+1.
```

```
no
```

```
| ?- 1+A=B+2.
```

```
A = 2
```

```
B = 1
```

```
yes
```

```
| ?- 5<10.

yes
| ?- 5>10.

no
| ?- 10=\=100.

yes
```

Here we can see $1+2=2+1$ is returning true, but $1+2=2+1$ is returning false. This is because, in the first case it is checking whether the value of $1 + 2$ is same as $2 + 1$ or not, and the other one is checking whether two patterns ' $1+2$ ' and ' $2+1$ ' are same or not. As they are not same, it returns no (false). In the case of $1+A=B+2$, A and B are two variables, and they are automatically assigned to some values that will match the pattern.

Arithmetic Operators in Prolog

Arithmetic operators are used to perform arithmetic operations. There are few different types of arithmetic operators as follows:

Operator	Meaning
+	Addition
-	Subtraction
*	Multiplication
/	Division
**	Power
//	Integer Division
mod	Modulus

Let us see one practical code to understand the usage of these operators.

Program

```
calc :- X is 100 + 200,write('100 + 200 is '),write(X),nl,
        Y is 400 - 150,write('400 - 150 is '),write(Y),nl,
        Z is 10 * 300,write('10 * 300 is '),write(Z),nl,

        A is 100 / 30,write('100 / 30 is '),write(A),nl,
        B is 100 // 30,write('100 // 30 is '),write(B),nl,
        C is 100 ** 2,write('100 ** 2 is '),write(C),nl,
```

```
D is 100 mod 30,write('100 mod 30 is '),write(D),nl.
```

Note: The nl is used to create new line.

Output

```
| ?- change_directory('D:/TP Prolog/Sample_Codes').

yes
| ?- [op_arith].
compiling D:/TP Prolog/Sample_Codes/op_arith.pl for byte code...
D:/TP Prolog/Sample_Codes/op_arith.pl compiled, 6 lines read - 2390 bytes
written, 11 ms

yes
| ?- calc.
100 + 200 is 300
400 - 150 is 250
10 * 300 is 3000
100 / 30 is 3.3333333333333335
100 // 30 is 3
100 ** 2 is 10000.0
100 mod 30 is 10

yes
| ?-
```


8. Prolog — Loop & Decision Making

In this chapter, we will discuss loops and decision making in Prolog.

Loops

Loop statements are used to execute the code block multiple times. In general, for, while, do-while are loop constructs in programming languages (like Java, C, C++).

Code block is executed multiple times using recursive predicate logic. There are no direct loops in some other languages, but we can simulate loops with few different techniques.

Program

```
count_to_10(10) :- write(10),nl.  
count_to_10(X) :-  
    write(X),nl,  
    Y is X + 1,  
    count_to_10(Y).
```

Output

```
| ?- [loop].  
compiling D:/TP Prolog/Sample_Codes/loop.pl for byte code...  
D:/TP Prolog/Sample_Codes/loop.pl compiled, 4 lines read - 751 bytes written,  
16 ms  
  
(16 ms) yes  
| ?- count_to_10(3).  
3  
4  
5  
6  
7  
8  
9  
10  
  
true ?
```

```
yes
| ?-
```

Now create a loop that takes lowest and highest values. So, we can use the `between()` to simulate loops.

Program

Let us see an example program:

```
count_down(L, H) :-
    between(L, H, Y),
    Z is H - Y,
    write(Z), nl.

count_up(L, H) :-
    between(L, H, Y),
    Z is L + Y,
    write(Z), nl.
```

Output

```
| ?- [loop].
compiling D:/TP Prolog/Sample_Codes/loop.pl for byte code...
D:/TP Prolog/Sample_Codes/loop.pl compiled, 14 lines read - 1700 bytes written,
16 ms

yes
| ?- count_down(12,17).
5

true ? ;
4

true ? ;
3

true ? ;
2

true ? ;
```

```
1

true ? ;
0

yes
| ?- count_up(5,12).
10

true ? ;
11

true ? ;
12

true ? ;
13

true ? ;
14

true ? ;
15

true ? ;
16

true ? ;
17

yes
| ?-
```

Decision Making

The decision statements are If-Then-Else statements. So when we try to match some condition, and perform some task, then we use the decision making statements. The basic usage is as follows:

```
If <condition> is true, Then <do this>, Else <do this>
```

In some different programming languages, there are If-Else statements, but in Prolog we have to define our statements in some other manner. Following is an example of decision making in Prolog.

Program

```
% If-Then-Else statement

gt(X,Y) :- X >= Y,write('X is greater or equal').
gt(X,Y) :- X < Y,write('X is smaller').

% If-Elif-Else statement

gte(X,Y) :- X > Y,write('X is greater').
gte(X,Y) :- X == Y,write('X and Y are same').
gte(X,Y) :- X < Y,write('X is smaller').
```

Output

```
| ?- [test].
compiling D:/TP Prolog/Sample_Codes/test.pl for byte code...
D:/TP Prolog/Sample_Codes/test.pl compiled, 3 lines read - 529 bytes written,
15 ms

yes
| ?- gt(10,100).
X is smaller

yes
| ?- gt(150,100).
X is greater or equal

true ?

yes
```

```
| ?- gte(10,20).
```

```
X is smaller
```

```
(15 ms) yes
```

```
| ?- gte(100,20).
```

```
X is greater
```

```
true ?
```

```
yes
```

```
| ?- gte(100,100).
```

```
X and Y are same
```

```
true ?
```

```
yes
```

```
| ?-
```

9. Prolog — Conjunctions & Disjunctions

In this chapter, we shall discuss Conjunction and Disjunction properties. These properties are used in other programming languages using AND and OR logics. Prolog also uses the same logic in its syntax.

Conjunction

Conjunction (AND logic) can be implemented using the comma (,) operator. So two predicates separated by comma are joined with AND statement. Suppose we have a predicate, **parent(jhon, bob)**, which means "Jhon is parent of Bob", and another predicate, **male(jhon)**, which means "Jhon is male". So we can make another predicate that **father(jhon,bob)**, which means "Jhon is father of Bob". We can define predicate **father**, when he is parent **AND** he is male.

Disjunction

Disjunction (OR logic) can be implemented using the semi-colon (;) operator. So two predicates separated by semi-colon are joined with OR statement. Suppose we have a predicate, **father(jhon, bob)**. This tells that "Jhon is father of Bob", and another predicate, **mother(lili,bob)**, this tells that "lili is mother of bob". If we create another predicate as **child()**, this will be true when **father(jhon, bob)** is true **OR** **mother(lili,bob)** is true.

Program

```
parent(jhon,bob).
parent(lili,bob).

male(jhon).
female(lili).

% Conjunction Logic
father(X,Y) :- parent(X,Y),male(X).
mother(X,Y) :- parent(X,Y),female(X).

% Disjunction Logic
child_of(X,Y) :- father(X,Y);mother(X,Y).
```

Output

```
| ?- [conj_disj].
compiling D:/TP Prolog/Sample_Codes/conj_disj.pl for byte code...
```

```
D:/TP Prolog/Sample_Codes/conj_disj.pl compiled, 11 lines read - 1513 bytes  
written, 24 ms
```

```
yes
```

```
| ?- father(jhon,bob).
```

```
yes
```

```
| ?- child_of(jhon,bob).
```

```
true ?
```

```
yes
```

```
| ?- child_of(lili,bob).
```

```
yes
```

```
| ?-
```

10. Prolog — Lists

In this chapter, we will discuss one of the important concepts in Prolog, The Lists. It is a data structure that can be used in different cases for non-numeric programming. Lists are used to store the atoms as a collection.

In the subsequent sections, we will discuss the following topics:

- Representation of lists in Prolog
- Basic operations on prolog such as Insert, delete, update, append.
- Repositioning operators such as permutation, combination, etc.
- Set operations like set union, set intersection, etc.

Representation of Lists

The list is a simple data structure that is widely used in non-numeric programming. List consists of any number of items, for example, red, green, blue, white, dark. It will be represented as, [red, green, blue, white, dark]. The list of elements will be enclosed with **square brackets**.

A list can be either **empty** or **non-empty**. In the first case, the list is simply written as a Prolog atom, []. In the second case, the list consists of two things as given below:

- The first item, called the **head** of the list;
- The remaining part of the list, called the **tail**.

Suppose we have a list like: [red, green, blue, white, dark]. Here the head is red and tail is [green, blue, white, dark]. So the tail is another list.

Now, let us consider we have a list, $L = [a, b, c]$. If we write $\text{Tail} = [b, c]$ then we can also write the list L as $L = [a \mid \text{Tail}]$. Here the vertical bar (|) separates the head and tail parts.

So the following list representations are also valid:

- $[a, b, c] = [x \mid [b, c]]$
- $[a, b, c] = [a, b \mid [c]]$
- $[a, b, c] = [a, b, c \mid []]$

For these properties we can define the list as:

A data structure that is either empty or consists of two parts: a head and a tail. The tail itself has to be a list.

Basic Operations on Lists

Following table contains various operations on prolog lists:

Operations	Definition
Membership Checking	During this operation, we can verify whether a given element is member of specified list or not?
Length Calculation	With this operation, we can find the length of a list.
Concatenation	Concatenation is an operation which is used to join/add two lists.
Delete Items	This operation removes the specified element from a list.
Append Items	Append operation adds one list into another (as an item).
Insert Items	This operation inserts a given item into a list.

Membership Operation

During this operation, we can check whether a member X is present in list L or not? So how to check this? Well, we have to define one predicate to do so. Suppose the predicate name is **list_member(X,L)**. The goal of this predicate is to check whether X is present in L or not.

To design this predicate, we can follow these observations. X is a member of L if either:

- X is head of L , or
- X is a member of the tail of L

Program

```
list_member(X,[X|_]).
list_member(X,[_|TAIL]) :- list_member(X,TAIL).
```

Output

```
| ?- [list_basics].
compiling D:/TP Prolog/Sample_Codes/list_basics.pl for byte code...
D:/TP Prolog/Sample_Codes/list_basics.pl compiled, 1 lines read - 467 bytes
written, 13 ms

yes
```

```
| ?- list_member(b,[a,b,c]).

true ?

yes
| ?- list_member(b,[a,[b,c]]).

no
| ?- list_member([b,c],[a,[b,c]]).

true ?

yes
| ?- list_member(d,[a,b,c]).

no
| ?- list_member(d,[a,b,c]).
```

Length Calculation

This is used to find the length of list L. We will define one predicate to do this task. Suppose the predicate name is **list_length(L,N)**. This takes L and N as input argument. This will count the elements in a list L and instantiate N to their number. As was the case with our previous relations involving lists, it is useful to consider two cases:

- If list is empty, then length is 0.
- If the list is not empty, then $L = [\text{Head}|\text{Tail}]$, then its length is $1 + \text{length of Tail}$.

Program

```
list_length([],0).
list_length(_|TAIL,N) :- list_length(TAIL,N1), N is N1 + 1.
```

Output

```
| ?- [list_basics].
compiling D:/TP Prolog/Sample_Codes/list_basics.pl for byte code...
D:/TP Prolog/Sample_Codes/list_basics.pl compiled, 4 lines read - 985 bytes
written, 23 ms

yes
| ?- list_length([a,b,c,d,e,f,g,h,i,j],Len).
```

```

Len = 10

yes
| ?- list_length([],Len).

Len = 0

yes
| ?- list_length([[a,b],[c,d],[e,f]],Len).

Len = 3

yes
| ?-

```

Concatenation

Concatenation of two lists means adding the list items of the second list after the first one. So if two lists are [a,b,c] and [1,2], then the final list will be [a,b,c,1,2]. So to do this task we will create one predicate called list_concat(), that will take first list L1, second list L2, and the L3 as resultant list. There are two observations here.

- If the first list is empty, and second list is L, then the resultant list will be L.
- If the first list is not empty, then write this as [Head|Tail], concatenate Tail with L2 recursively, and store into new list in the form, [Head|New List].

Program

```

list_concat([],L,L).
list_concat([X1|L1],L2,[X1|L3]) :- list_concat(L1,L2,L3).

```

Output

```

| ?- [list_basics].
compiling D:/TP Prolog/Sample_Codes/list_basics.pl for byte code...
D:/TP Prolog/Sample_Codes/list_basics.pl compiled, 7 lines read - 1367 bytes
written, 19 ms

yes
| ?- list_concat([1,2],[a,b,c],NewList).

```

```

NewList = [1,2,a,b,c]

yes
| ?- list_concat([], [a,b,c], NewList).

NewList = [a,b,c]

yes
| ?- list_concat([1,2,3], [p,q,r], [a,b,c], NewList).

NewList = [[1,2,3], [p,q,r], a,b,c]

yes
| ?-

```

Delete from List

Suppose we have a list L and an element X, we have to delete X from L. So there are three cases:

- If X is the only element, then after deleting it, it will return empty list.
- If X is head of L, the resultant list will be the Tail part.
- If X is present in the Tail part, then delete from there recursively.

Program

```

list_delete(X, [X], []).
list_delete(X, [X|L1], L1).
list_delete(X, [Y|L2], [Y|L1]) :- list_delete(X, L2, L1).

```

Output

```

| ?- [list_basics].
compiling D:/TP Prolog/Sample_Codes/list_basics.pl for byte code...
D:/TP Prolog/Sample_Codes/list_basics.pl compiled, 11 lines read - 1923 bytes
written, 25 ms

yes
| ?- list_delete(a, [a,e,i,o,u], NewList).

```

```

NewList = [e,i,o,u] ?

yes
| ?- list_delete(a,[a],NewList).

NewList = [] ?

yes
| ?- list_delete(X,[a,e,i,o,u],[a,e,o,u]).

X = i ? ;

no
| ?-

```

Append into List

Appending two lists means adding two lists together, or adding one list as an item. Now if the item is present in the list, then the append function will not work. So we will create one predicate namely, `list_append(L1, L2, L3)`. The following are some observations:

- Let A is an element, L1 is a list, the output will be L1 also, when L1 has A already.
- Otherwise new list will be $L2 = [A|L1]$.

Program

```

list_member(X,[X|_]).
list_member(X,[_|TAIL]) :- list_member(X,TAIL).

list_append(A,T,T) :- list_member(A,T),!.
list_append(A,T,[A|T]).

```

In this case, we have used (!) symbol, that is known as cut. So when the first line is executed successfully, then we cut it, so it will not execute the next operation.

Output

```

| ?- [list_basics].
compiling D:/TP Prolog/Sample_Codes/list_basics.pl for byte code...
D:/TP Prolog/Sample_Codes/list_basics.pl compiled, 14 lines read - 2334 bytes
written, 25 ms

(16 ms) yes

```

```
| ?- list_append(a,[e,i,o,u],NewList).

NewList = [a,e,i,o,u]

yes
| ?- list_append(e,[e,i,o,u],NewList).

NewList = [e,i,o,u]

yes
| ?- list_append([a,b],[e,i,o,u],NewList).

NewList = [[a,b],e,i,o,u]

yes
| ?-
```

Insert into List

This method is used to insert an item X into list L, and the resultant list will be R. So the predicate will be in this form `list_insert(X, L, R)`. So this can insert X into L in all possible positions. If we see closer, then there are some observations.

- If we perform `list_insert(X,L,R)`, we can use `list_delete(X,R,L)`, so delete X from R and make new list L.

Program

```
list_delete(X, [X], []).
list_delete(X,[X|L1], L1).
list_delete(X, [Y|L2], [Y|L1]) :- list_delete(X,L2,L1).

list_insert(X,L,R) :- list_delete(X,R,L).
```

Output

```
| ?- [list_basics].
compiling D:/TP Prolog/Sample_Codes/list_basics.pl for byte code...
D:/TP Prolog/Sample_Codes/list_basics.pl compiled, 16 lines read - 2558 bytes
written, 22 ms

(16 ms) yes
```

```
| ?- list_insert(a,[e,i,o,u],NewList).
```

```
NewList = [a,e,i,o,u] ? a
```

```
NewList = [e,a,i,o,u]
```

```
NewList = [e,i,a,o,u]
```

```
NewList = [e,i,o,a,u]
```

```
NewList = [e,i,o,u,a]
```

```
NewList = [e,i,o,u,a]
```

```
(15 ms) no
```

```
| ?-
```

Repositioning operations of list items

Following are repositioning operations:

Repositioning Operations	Definition
Permutation	This operation will change the list item positions and generate all possible outcomes.
Reverse Items	This operation arranges the items of a list in reverse order.
Shift Items	This operation will shift one element of a list to the left rotationally.
Order Items	This operation verifies whether the given list is ordered or not.

Permutation Operation

This operation will change the list item positions and generate all possible outcomes. So we will create one predicate as `list_perm(L1,L2)`, This will generate all permutation of L1, and store them into L2. To do this we need `list_delete()` clause to help.

To design this predicate, we can follow few observations as given below:

X is member of L if either:

- If the first list is empty, then the second list must also be empty.
- If the first list is not empty then it has the form $[X | L]$, and a permutation of such a list can be constructed as, first permute L obtaining $L1$ and then insert X at any position into $L1$.

Program

```
list_delete(X,[X|L1], L1).
list_delete(X, [Y|L2], [Y|L1]) :- list_delete(X,L2,L1).

list_perm([],[]).
list_perm(L,[X|P]) :- list_delete(X,L,L1),list_perm(L1,P).
```

Output

```
| ?- [list_repos].
compiling D:/TP Prolog/Sample_Codes/list_repos.pl for byte code...
D:/TP Prolog/Sample_Codes/list_repos.pl compiled, 4 lines read - 1060 bytes
written, 17 ms

(15 ms) yes
| ?- list_perm([a,b,c,d],X).

X = [a,b,c,d] ? a

X = [a,b,d,c]

X = [a,c,b,d]

X = [a,c,d,b]

X = [a,d,b,c]

X = [a,d,c,b]

X = [b,a,c,d]

X = [b,a,d,c]

X = [b,c,a,d]
```


X = [b,c,d,a]

X = [b,d,a,c]

X = [b,d,c,a]

X = [c,a,b,d]

X = [c,a,d,b]

X = [c,b,a,d]

X = [c,b,d,a]

X = [c,d,a,b]

X = [c,d,b,a]

X = [d,a,b,c]

X = [d,a,c,b]

X = [d,b,a,c]

X = [d,b,c,a]

X = [d,c,a,b]

X = [d,c,b,a]

(31 ms) no

| ?-

Reverse Operation

Suppose we have a list $L = [a,b,c,d,e]$, and we want to reverse the elements, so the output will be $[e,d,c,b,a]$. To do this, we will create a clause, `list_reverse(List, ReversedList)`. Following are some observations:

- If the list is empty, then the resultant list will also be empty.
- Otherwise put the list items namely, $[Head|Tail]$, and reverse the Tail items recursively, and concatenate with the Head.
- This can also be used to check whether two lists are reverse of each other or not.

Program

```
list_concat([],L,L).
list_concat([X1|L1],L2,[X1|L3]) :- list_concat(L1,L2,L3).

list_rev([],[]).
list_rev([Head|Tail],Reversed) :-
    list_rev(Tail, RevTail),list_concat(RevTail, [Head],Reversed).
```

Output

```
| ?- [list_repos].
compiling D:/TP Prolog/Sample_Codes/list_repos.pl for byte code...
D:/TP Prolog/Sample_Codes/list_repos.pl compiled, 10 lines read - 1977 bytes
written, 19 ms

yes
| ?- list_rev([a,b,c,d,e],NewList).

NewList = [e,d,c,b,a]

yes
| ?- list_rev([a,b,c,d,e],[e,d,c,b,a]).

yes
| ?-
```

Shift Operation

Using Shift operation, we can shift one element of a list to the left rotationally. So if the list items are $[a,b,c,d]$, then after shifting, it will be $[b,c,d,a]$. So we will make a clause `list_shift(L1, L2)`.

- We will express the list as [Head|Tail], then recursively concatenate Head after the Tail, so as a result we can feel that the elements are shifted.
- This can also be used to check whether the two lists are shifted at one position or not.

Program

```
list_concat([],L,L).
list_concat([X1|L1],L2,[X1|L3]) :- list_concat(L1,L2,L3).

list_shift([Head|Tail],Shifted) :- list_concat(Tail, [Head],Shifted).
```

Output

```
| ?- [list_repos].
compiling D:/TP Prolog/Sample_Codes/list_repos.pl for byte code...
D:/TP Prolog/Sample_Codes/list_repos.pl compiled, 12 lines read - 2287 bytes
written, 10 ms

yes
| ?- list_shift([a,b,c,d,e],L2).

L2 = [b,c,d,e,a]

(16 ms) yes
| ?- list_shift([a,b,c,d,e],[b,c,d,e,a]).

yes
| ?-
```

Order Operation

Here we will define a predicate `list_order(L)` which checks whether L is ordered or not. So if `L = [1,2,3,4,5,6]`, then the result will be true.

- If there is only one element, that is already ordered.
- Otherwise take first two elements X and Y as Head, and rest as Tail. If $X \leq Y$, then call the clause again with the parameter `[Y|Tail]`, so this will recursively check from the next element.

Program

```
list_order([X]).
```

```
list_order([X, Y | Tail]) :- X =< Y, list_order([Y|Tail]).
```

Output

```
| ?- [list_repos].
compiling D:/TP Prolog/Sample_Codes/list_repos.pl for byte code...
D:/TP Prolog/Sample_Codes/list_repos.pl:15: warning: singleton variables [X]
for list_order/1
D:/TP Prolog/Sample_Codes/list_repos.pl compiled, 15 lines read - 2805 bytes
written, 18 ms

yes
| ?- list_order([1,2,3,4,5,6,6,7,7,8]).

true ?

yes
| ?- list_order([1,4,2,3,6,5]).

no
| ?-
```

Set operations on lists

Following are the set operations:

Set operations	Definition
Subset Finding	Retrieves all the possible subsets of a given list.
Union of two sets	Performs "union" on the given lists.
Intersection of two sets	Performs "Intersection" on the given lists.

Subset Finding Operation

We will try to write a clause that will get all possible subsets of a given set. So if the set is [a,b], then the result will be [], [a], [b], [a,b]. To do so, we will create one clause, list_subset(L, X). It will take L and return each subsets into X. So we will proceed in the following way:

- If list is empty, the subset is also empty.
- Find the subset recursively by retaining the Head, and
- Make another recursive call where we will remove Head.

Program

```
list_subset([],[]).
list_subset([Head|Tail],[Head|Subset]) :- list_subset(Tail,Subset).
list_subset([Head|Tail],Subset) :- list_subset(Tail,Subset).
```

Output

```
| ?- [list_set].
compiling D:/TP Prolog/Sample_Codes/list_set.pl for byte code...
D:/TP Prolog/Sample_Codes/list_set.pl:3: warning: singleton variables [Head]
for list_subset/2
D:/TP Prolog/Sample_Codes/list_set.pl compiled, 2 lines read - 653 bytes
written, 7 ms

yes
| ?- list_subset([a,b],X).

X = [a,b] ? ;

X = [a] ? ;

X = [b] ? ;

X = []

(15 ms) yes
| ?- list_subset([x,y,z],X).

X = [x,y,z] ? a

X = [x,y]

X = [x,z]

X = [x]

X = [y,z]
```

```
X = [y]
```

```
X = [z]
```

```
X = []
```

```
yes
```

```
| ?-
```

Union Operation

Let us define a clause called `list_union(L1,L2,L3)`, So this will take L1 and L2, and perform Union on them, and store the result into L3. As you know if two lists have the same element twice, then after union, there will be only one. So we need another helper clause to check the membership.

Program

```
list_member(X,[X|_]).
list_member(X,[_|TAIL]) :- list_member(X,TAIL).

list_union([X|Y],Z,W) :- list_member(X,Z),list_union(Y,Z,W).
list_union([X|Y],Z,[X|W]) :- \+ list_member(X,Z), list_union(Y,Z,W).
list_union([],Z,Z).
```

Note: In the program, we have used `(\+)` operator, this operator is used for **NOT**.

Output

```
| ?- [list_set].
compiling D:/TP Prolog/Sample_Codes/list_set.pl for byte code...
D:/TP Prolog/Sample_Codes/list_set.pl:6: warning: singleton variables [Head]
for list_subset/2
D:/TP Prolog/Sample_Codes/list_set.pl compiled, 9 lines read - 2004 bytes
written, 18 ms

yes
| ?- list_union([a,b,c,d,e],[a,e,i,o,u],L3).

L3 = [b,c,d,a,e,i,o,u] ?

(16 ms) yes
```

```
| ?- list_union([a,b,c,d,e],[1,2],L3).
```

```
L3 = [a,b,c,d,e,1,2]
```

```
yes
```

Intersection Operation

Let us define a clause called `list_intersection(L1,L2,L3)`, So this will take L1 and L2, and perform Intersection operation, and store the result into L3. Intersection will return those elements that are present in both lists. So L1 = [a,b,c,d,e], L2 = [a,e,i,o,u], then L3 = [a,e]. Here, we will use the `list_member()` clause to check if one element is present in a list or not.

Program

```
list_member(X,[X|_]).
list_member(X,[_|TAIL]) :- list_member(X,TAIL).

list_intersect([X|Y],Z,[X|W]) :-
    list_member(X,Z), list_intersect(Y,Z,W).
list_intersect([X|Y],Z,W) :-
    \+ list_member(X,Z), list_intersect(Y,Z,W).
list_intersect([],Z,[]).
```

Output

```
| ?- [list_set].
compiling D:/TP Prolog/Sample_Codes/list_set.pl for byte code...
D:/TP Prolog/Sample_Codes/list_set.pl compiled, 13 lines read - 3054 bytes
written, 9 ms

(15 ms) yes
| ?- list_intersect([a,b,c,d,e],[a,e,i,o,u],L3).

L3 = [a,e] ?

yes
| ?- list_intersect([a,b,c,d,e],[],L3).

L3 = []
```

```
yes
| ?-
```

Misc Operations on Lists

Following are some miscellaneous operations that can be performed on lists:

Misc Operations	Definition
Even and Odd Length Finding	Verifies whether the list has odd number or even number of elements.
Divide	Divides a list into two lists, and these lists are of approximately same length.
Max	Retrieves the element with maximum value from the given list.
Sum	Returns the sum of elements of the given list.
Merge Sort	Arranges the elements of a given list in order (using Merge Sort algorithm).

Even and Odd Length Operation

In this example, we will see two operations using which we can check whether the list has odd number of elements or the even number of elements. We will define predicates namely, `list_even_len(L)` and `list_odd_len(L)`.

- If the list has no elements, then that is even length list.
- Otherwise we take it as `[Head|Tail]`, then if Tail is of odd length, then the total list is even length string.
- Similarly, if the list has only one element, then that is odd length list.
- By taking it as `[Head|Tail]` and Tail is even length string, then entire list is odd length list.

Program

```
list_even_len([]).
list_even_len([Head|Tail]) :- list_odd_len(Tail).

list_odd_len([_]).
```



```
list_odd_len([Head|Tail]) :- list_even_len(Tail).
```

Output

```
| ?- [list_misc].
compiling D:/TP Prolog/Sample_Codes/list_misc.pl for byte code...
D:/TP Prolog/Sample_Codes/list_misc.pl:2: warning: singleton variables [Head]
for list_even_len/1
D:/TP Prolog/Sample_Codes/list_misc.pl:5: warning: singleton variables [Head]
for list_odd_len/1
D:/TP Prolog/Sample_Codes/list_misc.pl compiled, 4 lines read - 726 bytes
written, 20 ms

yes
| ?- list_odd_len([a,2,b,3,c]).

true ?

yes
| ?- list_odd_len([a,2,b,3]).

no
| ?- list_even_len([a,2,b,3]).

true ?

yes
| ?- list_even_len([a,2,b,3,c]).

no
| ?-
```

Divide List Operation

This operation divides a list into two lists, and these lists are of approximately same length. So if the given list is [a,b,c,d,e], then the result will be [a,c,e],[b,d]. This will place all of the odd placed elements into one list, and all even placed elements into another list. We will define a predicate, list_divide(L1,L2,L3) to solve this task.

- If given list is empty, then it will return empty lists.

- If there is only one element, then the first list will be a list with that element, and the second list will be empty.
- Suppose X,Y are two elements from head, and rest are Tail, So make two lists [X|List1], [Y|List2], these List1 and List2 are separated by dividing Tail.

Program

```
list_divide([],[],[]).
list_divide([X],[X],[]).
list_divide([X,Y|Tail], [X|List1],[Y|List2]) :-
    list_divide(Tail,List1,List2).
```

Output

```
| ?- [list_misc].
compiling D:/TP Prolog/Sample_Codes/list_misc.pl for byte code...
D:/TP Prolog/Sample_Codes/list_misc.pl:2: warning: singleton variables [Head]
for list_even_len/1
D:/TP Prolog/Sample_Codes/list_misc.pl:5: warning: singleton variables [Head]
for list_odd_len/1
D:/TP Prolog/Sample_Codes/list_misc.pl compiled, 8 lines read - 1432 bytes
written, 8 ms

yes
| ?- list_divide([a,1,b,2,c,3,d,5,e],L1,L2).

L1 = [a,b,c,d,e]
L2 = [1,2,3,5] ?

yes
| ?- list_divide([a,b,c,d],L1,L2).

L1 = [a,c]
L2 = [b,d]

yes
| ?-
```

Max Item Operation

This operation is used to find the maximum element from a list. We will define a predicate, **list_max_elem(List, Max)**, then this will find Max element from the list and return.

- If there is only one element, then it will be the max element.
- Divide the list as [X,Y|Tail]. Now recursively find max of [Y|Tail] and store it into MaxRest, and store maximum of X and MaxRest, then store it to Max.

Program

```
max_of_two(X,Y,X) :- X >= Y.
max_of_two(X,Y,Y) :- X < Y.

list_max_elem([X],X).
list_max_elem([X,Y|Rest],Max) :-
    list_max_elem([Y|Rest],MaxRest),
    max_of_two(X,MaxRest,Max).
```

Output

```
| ?- [list_misc].
compiling D:/TP Prolog/Sample_Codes/list_misc.pl for byte code...
D:/TP Prolog/Sample_Codes/list_misc.pl:2: warning: singleton variables [Head]
for list_even_len/1
D:/TP Prolog/Sample_Codes/list_misc.pl:5: warning: singleton variables [Head]
for list_odd_len/1
D:/TP Prolog/Sample_Codes/list_misc.pl compiled, 16 lines read - 2385 bytes
written, 16 ms

yes
| ?- list_max_elem([8,5,3,4,7,9,6,1],Max).

Max = 9 ?

yes
| ?- list_max_elem([5,12,69,112,48,4],Max).

Max = 112 ?

yes
| ?-
```

List Sum Operation

In this example, we will define a clause, `list_sum(List, Sum)`, this will return the sum of the elements of the list.

- If the list is empty, then sum will be 0.
- Represent list as `[Head|Tail]`, find sum of tail recursively and store them into `SumTemp`, then set `Sum = Head + SumTemp`.

Program

```
list_sum([],0).
list_sum([Head|Tail], Sum) :-
    list_sum(Tail,SumTemp),
    Sum is Head + SumTemp.
```

Output

```
yes
| ?- [list_misc].
compiling D:/TP Prolog/Sample_Codes/list_misc.pl for byte code...
D:/TP Prolog/Sample_Codes/list_misc.pl:2: warning: singleton variables [Head]
for list_even_len/1
D:/TP Prolog/Sample_Codes/list_misc.pl:5: warning: singleton variables [Head]
for list_odd_len/1
D:/TP Prolog/Sample_Codes/list_misc.pl compiled, 21 lines read - 2897 bytes
written, 21 ms

(32 ms) yes
| ?- list_sum([5,12,69,112,48,4],Sum).

Sum = 250

yes
| ?- list_sum([8,5,3,4,7,9,6,1],Sum).

Sum = 43

yes
| ?-
```

Merge Sort on a List

If the list is [4,5,3,7,8,1,2], then the result will be [1,2,3,4,5,7,8]. The steps of performing merge sort are shown below:

- Take the list and split them into two sub-lists. This split will be performed recursively.
- Merge each split in sorted order.
- Thus the entire list will be sorted.

We will define a predicate called mergesort(L, SL), it will take L and return result into SL.

Program

```
mergesort([],[]).    /* covers special case */
mergesort([A],[A]).
mergesort([A,B|R],S) :-
    split([A,B|R],L1,L2),
    mergesort(L1,S1),
    mergesort(L2,S2),
    merge(S1,S2,S).

split([],[],[]).
split([A],[A],[]).
split([A,B|R],[A|Ra],[B|Rb]) :-
    split(R,Ra,Rb).

merge(A,[],A).
merge([],B,B).
merge([A|Ra],[B|Rb],[A|M]) :-
    A <= B, merge(Ra,[B|Rb],M).
merge([A|Ra],[B|Rb],[B|M]) :-
    A > B, merge([A|Ra],Rb,M).
```

Output

```
| ?- [merge_sort].
compiling D:/TP Prolog/Sample_Codes/merge_sort.pl for byte code...
D:/TP Prolog/Sample_Codes/merge_sort.pl compiled, 17 lines read - 3048 bytes
written, 19 ms

yes
```

```
| ?- mergesort([4,5,3,7,8,1,2],L).
```

```
L = [1,2,3,4,5,7,8] ?
```

```
yes
```

```
| ?- mergesort([8,5,3,4,7,9,6,1],L).
```

```
L = [1,3,4,5,6,7,8,9] ?
```

```
yes
```

```
| ?-
```

11. Prolog — Recursion and Structures

This chapter covers recursion and structures.

Recursion

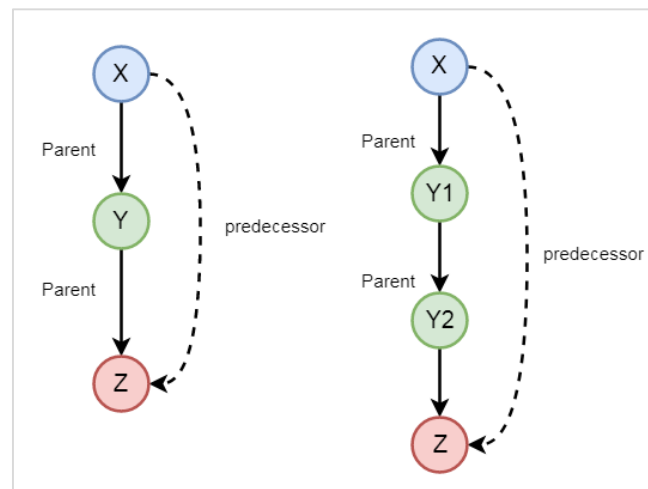
Recursion is a technique in which one predicate uses itself (may be with some other predicates) to find the truth value.

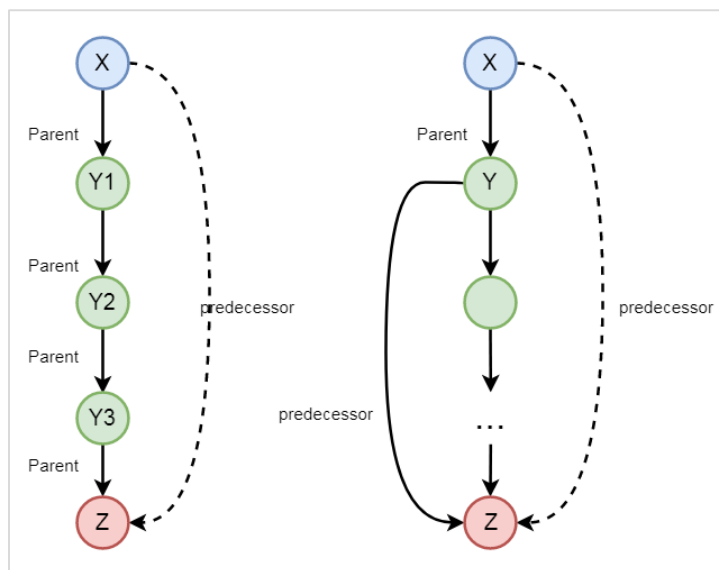
Let us understand this definition with the help of an example:

- `is_digesting(X,Y) :- just_ate(X,Y).`
- `is_digesting(X,Y) :- just_ate(X,Z), is_digesting(Z,Y).`

So this predicate is recursive in nature. Suppose we say that *just_ate(deer, grass)*, it means *is_digesting(deer, grass)* is true. Now if we say *is_digesting(tiger, grass)*, this will be true if *is_digesting(tiger, grass) :- just_ate(tiger, deer), is_digesting(deer, grass)*, then the statement *is_digesting(tiger, grass)* is also true.

There may be some other examples also, so let us see one family example. So if we want to express the predecessor logic, that can be expressed using the following diagram:





So we can understand the predecessor relationship is recursive. We can express this relationship using the following syntax:

- `predecessor(X, Z) :- parent(X, Z).`
- `predecessor(X, Z) :- parent(X, Y), predecessor(Y, Z).`

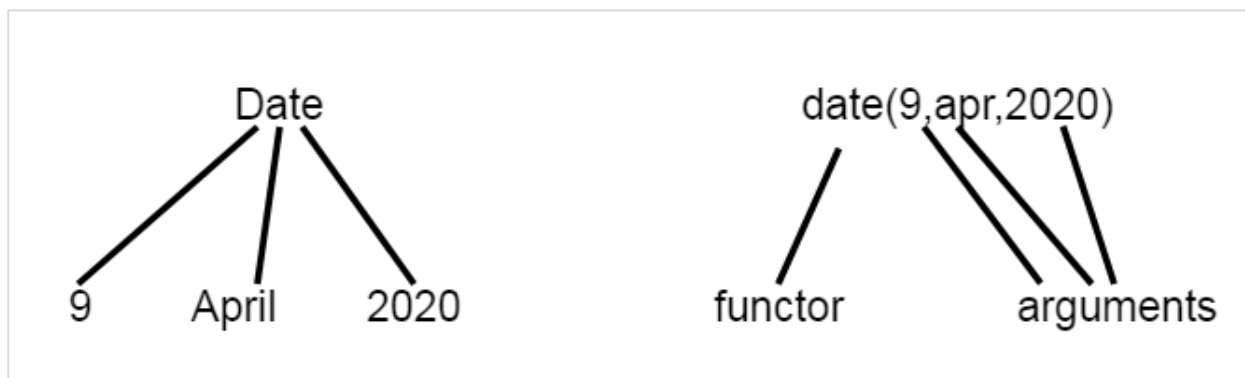
Structures

Structures are Data Objects that contain multiple components.

For example, the date can be viewed as a structure with three components — day, month and year. Then the date 9th April, 2020 can be written as: `date(9, apr, 2020)`.

Note: Structure can in turn have another structure as a component in it.

So we can see views as tree structure and **Prolog Functors**.



Now let us see one example of structures in Prolog. We will define a structure of points, Segments and Triangle as structures.

To represent a point, a line segment and a triangle using structure in Prolog, we can consider following statements:

- `p1 : point(1, 1)`
- `p2: point(2,3)`

- S : seg(P1, P2): seg(point(1,1), point(2,3))
- T : triangle(point(4,Z), point(6,4), point(7,1))

Note: Structures can be naturally pictured as trees. Prolog can be viewed as a language for processing trees.

Matching in Prolog

Matching is used to check whether two given terms are same (identical) or the variables in both terms can have the same objects after being instantiated. Let us see one example.

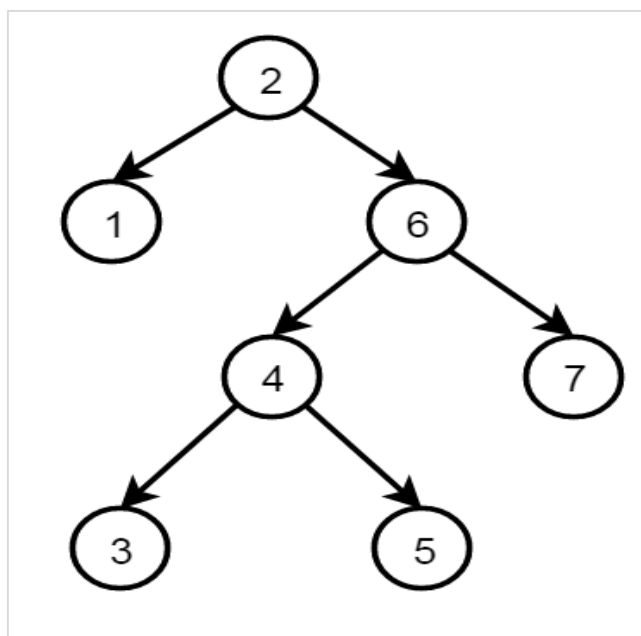
Suppose date structure is defined as `date(D,M,2020) = date(D1,apr, Y1)`, this indicates that `D = D1`, `M = feb` and `Y1 = 2020`.

Following rules are to be used to check whether two terms S and T match:

- If S and T are constants, $S=T$ if both are same objects.
- If S is a variable and T is anything, $T=S$.
- If T is variable and S is anything, $S=T$.
- If S and T are structures, $S=T$ if:
 - S and T have same functor.
 - All their corresponding arguments components have to match.

Binary Trees

Following is the structure of binary tree using recursive structures:



The definition of the structure is as follows:

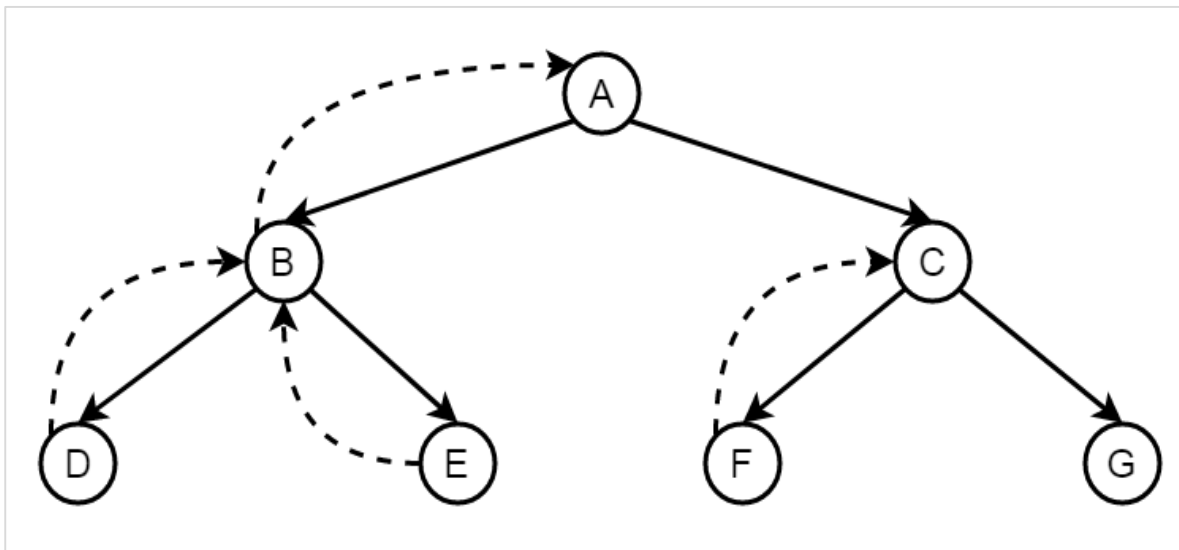
```
node(2, node(1,nil,nil), node(6, node(4,node(3,nil,nil), node(5,nil,nil)),
node(7,nil,nil))
```

Each node has three fields, data and two nodes. One node with no child (leaf node) structure is written as **node(value, nil, nil)**, node with only one left child is written as **node(value, left_node, nil)**, node with only one right child is written as **node(value, nil; right_node)**, and node with both child has **node(value, left_node, right_node)**.

12. Prolog — Backtracking

In this chapter, we will discuss the backtracking in Prolog. Backtracking is a procedure, in which prolog searches the truth value of different predicates by checking whether they are correct or not. The backtracking term is quite common in algorithm designing, and in different programming environments. In Prolog, until it reaches proper destination, it tries to backtrack. When the destination is found, it **stops**.

Let us see how backtracking takes place using one tree like structure:



Suppose A to G are some rules and facts. We start from A and want to reach G. The proper path will be A-C-G, but at first, it will go from A to B, then B to D. When it finds that D is not the destination, it backtracks to B, then go to E, and backtracks again to B, as there is no other child of B, then it backtracks to A, thus it searches for G, and finally found G in the path A-C-G. (Dashed lines are indicating the backtracking.) So when it finds G, it stops.

How Backtracking works?

Now we know, what is the backtracking in Prolog. Let us see one example,

Note: While we are running some prolog code, during backtracking there may be multiple answers, we can press **semicolon (;)** to get next answers one by one, that helps to backtrack. Otherwise when we get one result, it will stop.

Now, consider a situation, where two people X and Y can pay each other, but the condition is that a boy can pay to a girl, so X will be a boy, and Y will be a girl. So for these we have defined some facts and rules:

Knowledge Base

```
boy(tom).  
boy(bob).
```

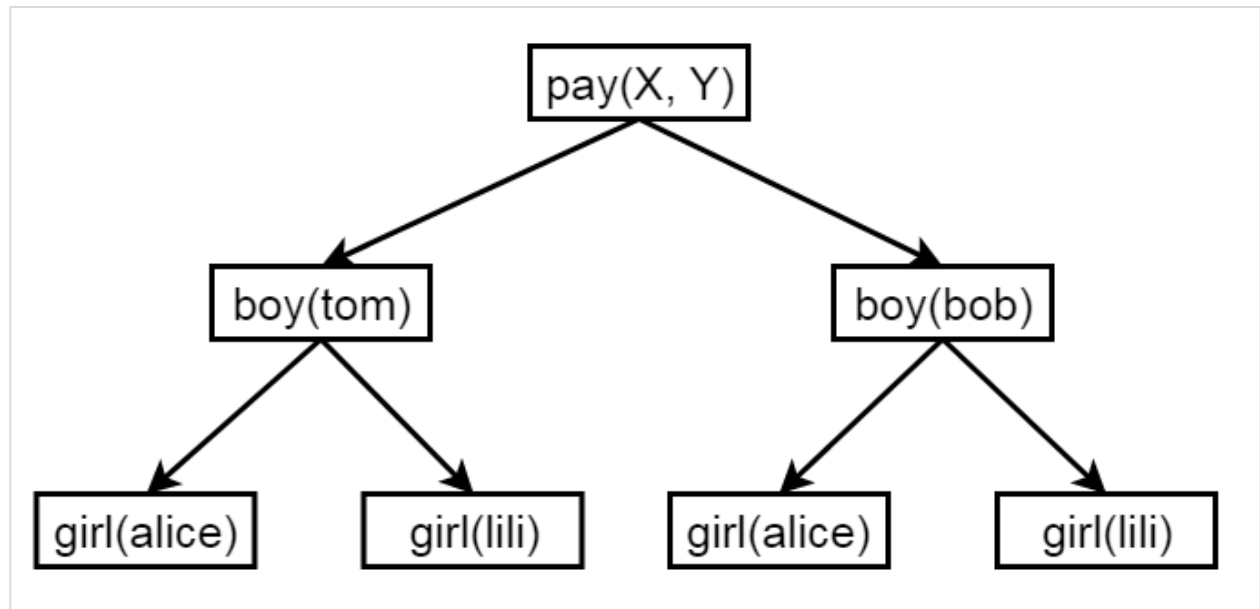
```

girl(alice).
girl(lili).

pay(X,Y) :- boy(X), girl(Y).

```

Following is the illustration of the above scenario:



As X will be a boy, so there are two choices, and for each boy there are two choices alice and lili. Now let us see the output, how backtracking is working.

Output

```

| ?- [backtrack].
compiling D:/TP Prolog/Sample_Codes/backtrack.pl for byte code...
D:/TP Prolog/Sample_Codes/backtrack.pl compiled, 5 lines read - 703 bytes
written, 22 ms

yes
| ?- pay(X,Y).

X = tom
Y = alice ?

(15 ms) yes
| ?- pay(X,Y).

X = tom

```

```

Y = alice ? ;

X = tom
Y = lili ? ;

X = bob
Y = alice ? ;

X = bob
Y = lili

yes
| ?- trace.
The debugger will first creep -- showing everything (trace)

(16 ms) yes
{trace}
| ?- pay(X,Y).
    1    1  Call: pay(_23,_24) ?
    2    2  Call: boy(_23) ?
    2    2  Exit: boy(tom) ?
    3    2  Call: girl(_24) ?
    3    2  Exit: girl(alice) ?
    1    1  Exit: pay(tom,alice) ?

X = tom
Y = alice ? ;
    1    1  Redo: pay(tom,alice) ?
    3    2  Redo: girl(alice) ?
    3    2  Exit: girl(lili) ?
    1    1  Exit: pay(tom,lili) ?

X = tom
Y = lili ? ;
    1    1  Redo: pay(tom,lili) ?
    2    2  Redo: boy(tom) ?
    2    2  Exit: boy(bob) ?

```

```

3    2    Call: girl(_24) ?
3    2    Exit: girl(alice) ?
1    1    Exit: pay(bob,alice) ?

X = bob
Y = alice ? ;
1    1    Redo: pay(bob,alice) ?
3    2    Redo: girl(alice) ?
3    2    Exit: girl(lili) ?
1    1    Exit: pay(bob,lili) ?

X = bob
Y = lili

yes
{trace}
| ?-
```

Preventing Backtracking

So far we have seen some concepts of backtracking. Now let us see some drawbacks of backtracking. Sometimes we write the same predicates more than once when our program demands, for example to write recursive rules or to make some decision making systems. In such cases uncontrolled backtracking may cause inefficiency in a program. To resolve this, we will use the **Cut** in Prolog.

Suppose we have some rules as follows:

Double step function

- Rule 1: if $X < 3$ then $Y = 0$
- Rule 2: if $3 \leq X$ and $X < 6$ then $Y = 2$
- Rule 3: if $6 \leq X$ then $Y = 4$

In Prolog syntax we can write,

- $f(X,0) :- X < 3.$ % Rule 1
- $f(X,2) :- 3 \leq X, X < 6.$ % Rule 2
- $f(X,4) :- 6 \leq X.$ % Rule 3

Now if we ask for a question as $f(1,Y), 2 < Y$.

The first goal $f(1,Y)$ instantiated Y to 0. The second goal becomes $2 < 0$ which fails. Prolog tries through backtracking two unfruitful alternatives (Rule 2 and Rule 3). If we see closer, we can observe that:

- The three rules are mutually exclusive and one of them at most will succeed.
- As soon as one of them succeeds there is no point in trying to use the others as they are bound to fail.

So we can use **cut** to resolve this. The **cut** can be expressed using Exclamation symbol. The prolog syntax is as follows:

- `f(X,0) :- X < 3, !. % Rule 1`
- `f(X,2) :- 3 =< X, X < 6, !. % Rule 2`
- `f(X,4) :- 6 =< X. % Rule 3`

Now if we use the same question, `?- f(1,Y), 2 < Y`. Prolog choose rule 1 since $1 < 3$ and fails the goal $2 < Y$ fails. Prolog will try to backtrack, but not beyond the point marked ! In the program, rule 2 and rule 3 will not be generated.

Let us see this in below execution:

Program

```
f(X,0) :- X < 3.           % Rule 1
f(X,2) :- 3 =< X, X < 6.   % Rule 2
f(X,4) :- 6 =< X.         % Rule 3
```

Output

```
| ?- [backtrack].
compiling D:/TP Prolog/Sample_Codes/backtrack.pl for byte code...
D:/TP Prolog/Sample_Codes/backtrack.pl compiled, 10 lines read - 1224 bytes
written, 17 ms

yes
| ?- f(1,Y), 2<Y.

no
| ?- trace
.
The debugger will first creep -- showing everything (trace)

yes
{trace}
| ?- f(1,Y), 2<Y.
    1    1  Call: f(1,_23) ?
    2    2  Call: 1<3 ?
    2    2  Exit: 1<3 ?
```

```

1 1 Exit: f(1,0) ?
3 1 Call: 2<0 ?
3 1 Fail: 2<0 ?
1 1 Redo: f(1,0) ?
2 2 Call: 3=<1 ?
2 2 Fail: 3=<1 ?
2 2 Call: 6=<1 ?
2 2 Fail: 6=<1 ?
1 1 Fail: f(1,_23) ?

```

(46 ms) no

{trace}

| ?-

Let us see the same using cut.

Program

```

f(X,0) :- X < 3,! .           % Rule 1
f(X,2) :- 3 <= X, X < 6,! .   % Rule 2
f(X,4) :- 6 <= X.             % Rule 3

```

Output

| ?- [backtrack].

```

1 1 Call: [backtrack] ?

```

compiling D:/TP Prolog/Sample_Codes/backtrack.pl for byte code...

D:/TP Prolog/Sample_Codes/backtrack.pl compiled, 10 lines read - 1373 bytes written, 15 ms

```

1 1 Exit: [backtrack] ?

```

(16 ms) yes

{trace}

| ?- f(1,Y), 2<Y.

```

1 1 Call: f(1,_23) ?
2 2 Call: 1<3 ?
2 2 Exit: 1<3 ?
1 1 Exit: f(1,0) ?
3 1 Call: 2<0 ?
3 1 Fail: 2<0 ?

```



```
no
{trace}
| ?-
```

Negation as Failure

Here we will perform failure when condition does not satisfy. Suppose we have a statement, "Mary likes all animals but snakes", we will express this in Prolog.

It would be very easy and straight forward, if the statement is "Mary likes all animals". In that case we can write "Mary likes X if X is an animal". And in prolog we can write this statement as, `likes(mary, X) :- animal(X)`.

Our actual statement can be expressed as:

- If X is snake, then "Mary likes X" is not true
- Otherwise if X is an animal, then Mary likes X.

In prolog we can write this as:

- `likes(mary,X) :- snake(X), !, fail.`
- `likes(mary, X) :- animal(X).`

The 'fail' statement causes the failure. Now let us see how it works in Prolog.

Program

```
animal(dog).
animal(cat).
animal(elephant).
animal(tiger).
animal(cobra).
animal(python).

snake(cobra).
snake(python).

likes(mary, X) :- snake(X), !, fail.
likes(mary, X) :- animal(X).
```

Output

```
| ?- [negate_fail].
compiling D:/TP Prolog/Sample_Codes/negate_fail.pl for byte code...
D:/TP Prolog/Sample_Codes/negate_fail.pl compiled, 11 lines read - 1118 bytes
written, 17 ms
```

```

yes
| ?- likes(mary,elephant).

yes
| ?- likes(mary,tiger).

yes
| ?- likes(mary,python).

no
| ?- likes(mary,cobra).

no
| ?- trace
.
The debugger will first creep -- showing everything (trace)

yes
{trace}
| ?- likes(mary,dog).
    1    1  Call: likes(mary,dog) ?
    2    2  Call: snake(dog) ?
    2    2  Fail: snake(dog) ?
    2    2  Call: animal(dog) ?
    2    2  Exit: animal(dog) ?
    1    1  Exit: likes(mary,dog) ?

yes
{trace}
| ?- likes(mary,python).
    1    1  Call: likes(mary,python) ?
    2    2  Call: snake(python) ?
    2    2  Exit: snake(python) ?
    3    2  Call: fail ?
    3    2  Fail: fail ?
    1    1  Fail: likes(mary,python) ?

```

```
no  
{trace}  
| ?-
```

13. Prolog — Different and Not

Here we will define two predicates — **different** and **not**. The **different** predicate will check whether two given arguments are same or not. If they are same, it will return false, otherwise it will return true. The **not** predicate is used to negate some statement, which means, when a statement is true, then not(statement) will be false, otherwise if the statement is false, then not(statement) will be true.

So the term 'different' can be expressed in three different ways as given below:

- X and Y are not literally the same
- X and Y do not match
- The values of arithmetic expression X and Y are not equal

So in Prolog, we will try to express the statements as follows:

- If X and Y match, then different(X,Y) fails,
- Otherwise different(X,Y) succeeds.

The respective prolog syntax will be as follows:

- different(X, X) :- !, fail.
- different(X, Y).

We can also express it using disjunctive clauses as given below:

- different(X, Y) :- X = Y, !, fail ; true. % true is goal that always succeeds

Program

Following example shows how this can be done in prolog:

```
different(X, X) :- !, fail.  
different(X, Y).
```

Output

```
| ?- [diff_rel].  
compiling D:/TP Prolog/Sample_Codes/diff_rel.pl for byte code...  
D:/TP Prolog/Sample_Codes/diff_rel.pl:2: warning: singleton variables [X,Y] for  
different/2  
D:/TP Prolog/Sample_Codes/diff_rel.pl compiled, 2 lines read - 327 bytes  
written, 11 ms  
  
yes  
| ?- different(100,200).
```

```

yes
| ?- different(100,100).

no
| ?- different(abc,def).

yes
| ?- different(abc,abc).

no
| ?-

```

Let us see a program using the disjunctive clauses:

Program

```
different(X, Y) :- X = Y, !, fail ; true.
```

Output

```

| ?- [diff_rel].
compiling D:/TP Prolog/Sample_Codes/diff_rel.pl for byte code...
D:/TP Prolog/Sample_Codes/diff_rel.pl compiled, 0 lines read - 556 bytes
written, 17 ms

yes
| ?- different(100,200).

yes
| ?- different(100,100).

no
| ?- different(abc,def).

yes
| ?- different(abc,abc).

no
| ?-

```

Not Relation in Prolog

The **not** relation is very much useful in different cases. In our traditional programming languages also, we use the logical not operation to negate some statement. So it means that when a statement is true, then `not(statement)` will be false, otherwise if the statement is false, then `not(statement)` will be true.

In prolog, we can define this as shown below:

```
not(P) :- P, !, fail ; true.
```

So if P is true, then cut and fail, this will return false, otherwise it will be true. Now let us see one simple code to understand this concept.

Program

```
not(P) :- P, !, fail ; true.
```

Output

```
| ?- [not_rel].
compiling D:/TP Prolog/Sample_Codes/not_rel.pl for byte code...
D:/TP Prolog/Sample_Codes/not_rel.pl compiled, 0 lines read - 630 bytes
written, 17 ms

yes
| ?- not(true).

no
| ?- not(fail).

yes
| ?-
```

14. Prolog — Inputs and Outputs

In this chapter, we will see some techniques to handle inputs and outputs through prolog. We will use some built in predicates to do these tasks, and also see file handling techniques.

Following topics will be discussed in detail:

- Handling inputs and outputs
- File handling using Prolog
- Using some external file to read lines and terms
- Character manipulation for input and output
- Constructing and decomposing atoms
- Consulting prolog files into other prolog program techniques.

Handling input and output

So far we have seen that we can write a program and the query on the console to execute. In some cases, we print something on the console, that are written in our prolog code. So here we will see that writing and reading tasks in more detail using prolog. So this will be the input and output handling techniques.

The write() Predicate

To write the output we can use the **write()** predicate. This predicate takes the parameter as input, and writes the content into the console by default. write() can also write in files. Let us see some examples of write() function.

Program

```
| ?- write(56).  
56  
  
yes  
| ?- write('hello').  
hello  
  
yes  
| ?- write('hello'),nl,write('world').  
hello  
world
```

```
yes
| ?- write("ABCDE")
.
[65,66,67,68,69]

yes
```

From the above example, we can see that the write() predicate can write the contents into the console. We can use 'nl' to create a new line. And from this example, it is clear that, if we want to print some string on the console, we have to use single quotes ('string'). But if we use double quote ("string"), then it will return a list of ASCII values.

The read() Predicate

The read() predicate is used to read from console. User can write something in the console, that can be taken as input and process it. The read() is generally used to read from console, but this can also be used to read from files. Now let us see one example to see how read() works.

Program

```
cube :-
    write('Write a number: '),
    read(Number),
    process(Number).

process(stop) :- !.
process(Number) :-
    C is Number * Number * Number,
    write('Cube of '),write(Number),write(': '),write(C),nl,
    cube.
```

Output

```
| ?- [read_write].
compiling D:/TP Prolog/Sample_Codes/read_write.pl for byte code...
D:/TP Prolog/Sample_Codes/read_write.pl compiled, 9 lines read - 1226 bytes
written, 12 ms

(15 ms) yes
| ?- cube.
Write a number: 2.
Cube of 2: 8
```



```

Write a number: 10.
Cube of 10: 1000
Write a number: 12.
Cube of 12: 1728
Write a number: 8.
Cube of 8: 512
Write a number: stop
.

(31 ms) yes
| ?-

```

The tab() Predicate

The `tab()` is one additional predicate that can be used to put some blank-spaces while we write something. So it takes a number as an argument, and prints those many number of blank spaces.

Program

```

| ?- write('hello'),tab(15),write('world').
hello                world

yes
| ?- write('We'),tab(5),write('will'),tab(5),write('use'),tab(5),write('tabs').
We      will      use      tabs

yes
| ?-

```

Reading/Writing Files

In this section, we will see how we can use files to read from, and write into the files. There are some built-in predicates, that can be used to read from file and write into it.

The tell and told

If we want to write into a file, except the console, we can write the **tell()** predicate. This **tell()** predicate takes filename as argument. If that file is not present, then create a new file, and write into it. That file will be opened until we write the **told** command. We can open more than one file using `tell()`. When `told` is called, all files will be closed.

Prolog Commands

```

| ?- told('myFile.txt').
uncaught exception: error(existence_error(procedure,told/1),top_level/0)
| ?- told("myFile.txt").
uncaught exception: error(existence_error(procedure,told/1),top_level/0)
| ?- tell('myFile.txt').

yes
| ?- tell('myFile.txt').

yes
| ?- write('Hello World').

yes
| ?- write(' Writing into a file'),tab(5),write('myFile.txt'),nl.

yes
| ?- write("Write some ASCII values").

yes
| ?- told.

yes
| ?-

```

Output (myFile.txt)

```

Hello World Writing into a file      myFile.txt
[87,114,105,116,101,32,115,111,109,101,32,65,83,67,73,73,32,118,97,108,117,101,
115]

```

Similarly, we can also read from files. Let us see some example of reading from file.

The see and seen

When we want to read from file, not from the keyboard, we have to change current input stream. So we can use **see()** predicate. This will take filename as input. When the read operation is completed, then we will use **seen** command.

Sample File (sample_predicate.txt)

```

likes(lili, cat).
likes(jhon,dog).

```

Output

```
| ?- see('sample_predicate.txt'),
read(X),
read(Y),
seen,
read(Z).
the_end.

X = end_of_file
Y = end_of_file
Z = the_end

yes
| ?-
```

So from this example, we can see that using the `see()` predicate we can read from the file. Now after using **seen** command, the control transfers to the console again. So finally it takes input from console.

Processing files of terms

We have seen how to read specific contents (few lines) of a file. Now if we want to read/process all the contents of a file, we need to write a clause to process file (*process_file*), until we reach the end of the file.

Program

```
process_file :-
    read(Line),
    Line \== end_of_file,    % when Line is not not end of file, call process.
    process(Line).

process_file :- !. % use cut to stop backtracking

process(Line):- %this will print the line into the console
    write(Line),nl,
    process_file.
```

Sample File (sample_predicate.txt)

```
likes(lili, cat).
likes(jhon,dog).
```

```
domestic(dog).
domestic(cat).
```

Output

```
| ?- [process_file].
compiling D:/TP Prolog/Sample_Codes/process_file.pl for byte code...
D:/TP Prolog/Sample_Codes/process_file.pl compiled, 9 lines read - 774 bytes
written, 23 ms

yes
| ?- see('sample_predicate.txt'), process_file, seen.
likes(lili,cat)
likes(jhon,dog)
domestic(dog)
domestic(cat)

true ?

(15 ms) yes
| ?-
```

Manipulating characters

Using `read()` and `write()` we can read or write the value of atoms, predicates, strings, etc. Now in this section we will see how to write single characters into the current output stream, or how to read from current input stream. So there are some predefined predicates to do these tasks.

The `put(C)` and `put_char(C)` predicates

We can use `put(C)` to write one character at a time into the current output stream. The output stream can be a file or the console. This `C` can be a character or an ASCII code in other version of Prolog like SWI prolog, but in GNU prolog, it supports only the ASCII value. To use the character instead of ASCII, we can use `put_char(C)`.

Program

```
| ?- put(97),put(98),put(99),put(100),put(101).
abcde

yes
| ?- put(97),put(66),put(99),put(100),put(101).
```

```

aBcde

(15 ms) yes
| ?- put(65),put(66),put(99),put(100),put(101).
ABcde

yes
| ?-put_char('h'),put_char('e'),put_char('l'),put_char('l'),put_char('o').
hello

yes
| ?-

```

The `get_char(C)` and `get_code(C)` predicates

To read a single character from the current input stream, we can use the `get_char(C)` predicate. This will take the character. if we want the ASCII code, we can use `get_code(C)`.

Program

```

| ?- get_char(X).
A.

X = 'A'

yes
uncaught exception: error(syntax_error('user_input:6 (char:689) expression
expected'),read_term/3)
| ?- get_code(X).
A.

X = 65

yes
uncaught exception: error(syntax_error('user_input:7 (char:14) expression
expected'),read_term/3)
| ?-

```

Constructing Atoms

The atom constructing means from a list of characters, we can make one atom, or from a list of ASCII values also we can make atoms. To do this, we have to use `atom_chars()` and `atom_codes()` predicates. In both cases, the first argument will be one variable, and the second argument will be a list. So `atom_chars()` constructs atom from characters, but `atom_codes()` construct atoms from ASCII sequence.

Example

```
| ?- atom_chars(X, ['t','i','g','e','r']).
```

```
X = tiger
```

```
yes
```

```
| ?- atom_chars(A, ['t','o','m']).
```

```
A = tom
```

```
yes
```

```
| ?- atom_codes(X, [97,98,99,100,101]).
```

```
X = abcde
```

```
yes
```

```
| ?- atom_codes(A, [97,98,99]).
```

```
A = abc
```

```
yes
```

```
| ?-
```

Decomposing Atoms

The atom decomposing means from an atom, we can get a sequence of characters, or a sequence ASCII codes. To do this, we have to use the same `atom_chars()` and `atom_codes()` predicates. But one difference is that, in both cases, the first argument will be one atom, and the second argument will be a variable. So `atom_chars()` decomposes atom to characters, but `atom_codes()` decomposes atoms to ASCII sequence.

Example

```
| ?- atom_chars(tiger,X).
```

```

X = [t,i,g,e,r]

yes
| ?- atom_chars(tom,A).

A = [t,o,m]

yes
| ?- atom_codes(tiger,X).

X = [116,105,103,101,114]

yes
| ?- atom_codes(tom,A).

A = [116,111,109]

(16 ms) yes
| ?-

```

The consult in Prolog

The consulting is a technique, that is used to merge the predicates from different files. We can use the `consult()` predicate, and pass the filename to attach the predicates. Let us see one example program to understand this concept.

Suppose we have two files, namely, `prog1.pl` and `prog2.pl`.

Program (prog1.pl)

```

likes(mary,cat).
likes(joy,rabbit).
likes(tim,duck).

```

Program (prog2.pl)

```

likes(suman,mouse).
likes(angshu,deer).

```

Output

```

| ?- [prog1].
compiling D:/TP Prolog/Sample_Codes/prog1.pl for byte code...
D:/TP Prolog/Sample_Codes/prog1.pl compiled, 2 lines read - 443 bytes written,
23 ms

yes
| ?- likes(joy,rabbit).

yes
| ?- likes(suman,mouse).

no
| ?- consult('prog2.pl').
compiling D:/TP Prolog/Sample_Codes/prog2.pl for byte code...
D:/TP Prolog/Sample_Codes/prog2.pl compiled, 1 lines read - 366 bytes written,
20 ms
warning: D:/TP Prolog/Sample_Codes/prog2.pl:1: redefining procedure likes/2
        D:/TP Prolog/Sample_Codes/prog1.pl:1: previous definition

yes
| ?- likes(suman,mouse).

yes
| ?- likes(joy,rabbit).

no
| ?-

```

Now from this output we can understand that this is not as simple as it seems. If two files have **completely different clauses**, then it will work fine. But if there are same predicates, then while we try to consult the file, it will check the predicates from the second file, when it finds some match, it simply deletes all of the entry of the same predicates from the local database, then load them again from the second file.

15. Prolog — Built-In Predicates

In Prolog, we have seen the user defined predicates in most of the cases, but there are some built-in-predicates. There are three types of built-in predicates as given below:

- Identifying terms
- Decomposing structures
- Collecting all solutions

So this is the list of some predicates that are falls under the identifying terms group:

Predicate	Description
var(X)	succeeds if X is currently an un-instantiated variable.
no var(X)	succeeds if X is not a variable, or already instantiated
atom(X)	is true if X currently stands for an atom
number(X)	is true if X currently stands for a number
integer(X)	is true if X currently stands for an integer
float(X)	is true if X currently stands for a real number.
atomic(X)	is true if X currently stands for a number or an atom.
compound(X)	is true if X currently stands for a structure.
ground(X)	succeeds if X does not contain any un-instantiated variables.

Now, let us see each of them one by one.

The var(X) Predicate

When X is not initialized, then, it will show true, otherwise false. So let us see an example.

Example

```
| ?- var(X).
```

```
yes
```

```
| ?- X = 5, var(X).
```

```
no
```

```
| ?- var([X]).
```

```
no
```

```
| ?-
```

The novar(X) Predicate

When X is not initialized, the, it will show false, otherwise true. So let us see an example.

Example

```
| ?- novar(X).
```

```
no
```

```
| ?- X = 5,novar(X).
```

```
X = 5
```

```
yes
```

```
| ?- novar([X]).
```

```
yes
```

```
| ?-
```

The atom(X) Predicate

This will return true, when a non-variable term with 0 argument and a not numeric term is passed as X, otherwise false.

Example

```
| ?- atom(paul).
```

```
yes
```

```
| ?- X = paul,atom(X).
```

```
X = paul
```

```
yes
```

```
| ?- atom([]).
```

```
yes
```

```
| ?- atom([a,b]).
```

```
no
| ?-
```

The number(X) Predicate

This will return true, X stands for any number, otherwise false.

Example

```
| ?- number(X).

no
| ?- X=5,number(X).

X = 5

yes
| ?- number(5.46).

yes
| ?-
```

The integer(X) Predicate

This will return true, when X is a positive or negative integer value, otherwise false.

Example

```
| ?- integer(5).

yes
| ?- integer(5.46).

no
| ?-
```

The float(X) Predicate

This will return true, X is a floating point number, otherwise false.

Example

```
| ?- float(5).
```

```
no
| ?- float(5.46).

yes
| ?-
```

The atomic(X) Predicate

We have `atom(X)`, that is too specific, it returns false for numeric data, the `atomic(X)` is like `atom(X)` but it accepts number.

Example

```
| ?- atom(5).

no
| ?- atomic(5).

yes
| ?-
```

The compound(X) Predicate

If `atomic(X)` fails, then the terms are either one non-instantiated variable (that can be tested with `var(X)`) or a compound term. Compound will be true when we pass some compound structure.

Example

```
| ?- compound([]).

no
| ?- compound([a]).

yes
| ?- compound(b(a)).

yes
| ?-
```

The ground(X) Predicate

This will return true, if X does not contain any un-instantiated variables. This also checks inside the compound terms, otherwise returns false.

Example

```
| ?- ground(X).

no
| ?- ground(a(b,X)).

no
| ?- ground(a).

yes
| ?- ground([a,b,c]).

yes
| ?-
```

Decomposing Structures

Now we will see, another group of built-in predicates, that is Decomposing structures. We have seen the identifying terms before. So when we are using compound structures we cannot use a variable to check or make a functor. It will return error. So functor name cannot be represented by a variable.

Error

```
X = tree, Y = X(maple).
Syntax error Y=X<<here>>(maple)
```

Now, let us see some inbuilt predicates that falls under the Decomposing structures group.

The functor(T,F,N) Predicate

This returns true if F is the principal functor of T, and N is the arity of F.

Note: Arity means the number of attributes.

Example

```
| ?- functor(t(f(X),a,T),Func,N).

Func = t
```

```
N = 3
```

```
(15 ms) yes
```

```
| ?-
```

The arg(N,Term,A) Predicate

This returns true if A is the Nth argument in Term. Otherwise returns false.

Example

```
| ?- arg(1,t(t(X),[]),A).
```

```
A = t(X)
```

```
yes
```

```
| ?- arg(2,t(t(X),[]),A).
```

```
A = []
```

```
yes
```

```
| ?-
```

Now, let us see another example. In this example, we are checking that the first argument of D will be 12, the second argument will be apr and the third argument will be 2020.

Example

```
| ?- functor(D,date,3), arg(1,D,12), arg(2,D,apr), arg(3,D,2020).
```

```
D = date(12,apr,2020)
```

```
yes
```

```
| ?-
```

The ./2 Predicate

This is another predicate represented as double dot (..). This takes 2 arguments, so './2' is written. So Term = .. L, this is true if L is a list that contains the functor of Term, followed by its arguments.

Example

```
| ?- f(a,b) =.. L.
```

```

L = [f,a,b]

yes
| ?- T =.. [is_blue,sam,today].

T = is_blue(sam,today)

yes
| ?-

```

By representing the component of a structure as a list, they can be recursively processed without knowing the functor name. Let us see another example:

Example

```

| ?- f(2,3)=..[F,N|Y], N1 is N*3, L=..[F,N1|Y].

F = f
L = f(6,3)
N = 2
N1 = 6
Y = [3]

yes
| ?-

```

Collecting All Solutions

Now let us see the third category called the collecting all solutions, that falls under built-in predicates in Prolog.

We have seen that to generate all of the given solutions of a given goal using the semicolon in the prompt. So here is an example of it.

Example

```

| ?- member(X, [1,2,3,4]).

X = 1 ? ;

X = 2 ? ;

```

```
X = 3 ? ;
```

```
X = 4
```

```
yes
```

Sometimes, we need to generate all of the solutions to some goal within a program in some AI related applications. So there are three built-in predicates that will help us to get the results. These predicates are as follows:

- findall/3
- setof/3
- bagof/3

These three predicates take three arguments, so we have written '/3' after the name of the predicates.

These are also known as **meta-predicates**. These are used to manipulate Prolog's Proof strategy.

Syntax

```
findall(X,P,L).
setof(X,P,L)
bagof(X,P,L)
```

These three predicates a list of all objects X, such that the goal P is satisfied (example: age(X,Age)). They all repeatedly call the goal P, by instantiating variable X within P and adding it to the list L. This stops when there is no more solution.

Findall/3, Setof/3 and Bagof/3

Here we will see the three different built-in predicates findall/3, setof/3 and the bagof/3, that fall into the category, **collecting all solutions**.

The findall/3 Predicate

This predicate is used to make a list of all solutions X, from the predicate P. The returned list will be L. So we will read this as "find all of the Xs, such that X is a solution of predicate P and put the list of results in L". Here this predicate stores the results in the same order, in which Prolog finds them. And if there are duplicate solutions, then all will come into the resultant list, and if there is infinite solution, then the process will never terminate.

Now we can also do some advancement on them. The second argument, which is the goal, that might be a compound goal. Then the syntax will be as **findall(X, (Predicate on X, other goal), L)**

And also the first argument can be a term of any complexity. So let us see the examples of these few rules, and check the output.

Example

```
| ?- findall(X, member(X, [1,2,3,4]), Results).

Results = [1,2,3,4]

yes
| ?- findall(X, (member(X, [1,2,3,4]), X > 2), Results).

Results = [3,4]

yes
| ?- findall(X/Y, (member(X,[1,2,3,4]), Y is X * X), Results).

Results = [1/1,2/4,3/9,4/16]

yes
| ?-
```

The setof/3 Predicate

The setof/3 is also like findall/3, but here it removes all of the duplicate outputs, and the answers will be sorted.

If any variable is used in the goal, then that will not appear in the first argument, setof/3 will return a separate result for each possible instantiation of that variable.

Let us see one example to understand this setof/3. Suppose we have a knowledge base as shown below:

```
age(peter, 7).
age(ann, 5).
age(pat, 8).
age(tom, 5).
age(ann, 5).
```

Here we can see that age(ann, 5) has two entries in the knowledge base. And the ages are not sorted, and names are not sorted lexicographically in this case. Now let us see one example of setof/3 usage.

Example 1

```
| ?- setof(Child, age(Child, Age), Results).
```

```

Age = 5
Results = [ann,tom] ? ;

Age = 7
Results = [peter] ? ;

Age = 8
Results = [pat]

(16 ms) yes
| ?-

```

Here we can see the ages and the names both are coming sorted. For age 5, there is two entries, so the predicate has created one list corresponding to the age value, with two elements. And the duplicate entry is present only once.

We can use the nested call of `setof/3`, to collect together the individual results. We will see another example, where the first argument will be `Age/Children`. As the second argument, it will take another `setof` like before. So this will return a list of `(age/Children)` pair. Let us see this in the prolog execution:

Example 2

```

| ?- setof(Age/Children, setof(Child,age(Child,Age), Children), AllResults).

AllResults = [5/[ann,tom],7/[peter],8/[pat]]

yes
| ?-

```

Now if we do not care about a variable that does not appear in the first argument, then we can use the following example:

Example 3

```

| ?- setof(Child, Age^age(Child,Age), Results).

Results = [ann,pat,peter,tom]

yes
| ?-

```

Here we are using the upper caret symbol (^), this indicates that the `Age` is not in the first argument. So we will read this as, "Find the set of all children, such that the child has an `Age` (whatever it may be), and put the result in `Results`".

The bagof/3 Predicate

The bagof/3 is like setof/3, but here it does not remove the duplicate outputs, and the answers may not be sorted.

Let us see one example to understand this bagof/3. Suppose we have a knowledge base as follows:

Knowledge base

```
age(peter, 7).
age(ann, 5).
age(pat, 8).
age(tom, 5).
age(ann, 5).
```

Example

```
| ?- bagof(Child, age(Child, Age), Results).

Age = 5
Results = [ann, tom, ann] ? ;

Age = 7
Results = [peter] ? ;

Age = 8
Results = [pat]

(15 ms) yes
| ?-
```

Here for the Age value 5, the results are [ann, tom, ann]. So the answers are not sorted, and duplicate entries are not removed, so we have got two 'ann' values.

The bagof/3 is different from findall/3, as this generates separate results for all the variables in the goal that do not appear in the first argument. We will see this using an example below:

Example

```
| ?- findall(Child, age(Child, Age), Results).

Results = [peter, ann, pat, tom, ann]
```

```
yes
| ?-
```

Mathematical Predicates

Following are the mathematical predicates:

Predicates	Description
random(L,H,X).	Get random value between L and H
between(L,H,X).	Get all values between L and H
succ(X,Y).	Add 1 and assign it to X
abs(X).	Get absolute value of X
max(X,Y).	Get largest value between X and Y
min(X,Y).	Get smallest value between X and Y
round(X).	Round a value near to X
truncate(X).	Convert float to integer, delete the fractional part
floor(X).	Round down
ceiling(X).	Round up
sqrt(X).	Square root

Besides these, there are some other predicates such as sin, cos, tan, asin, acos, atan, atan2, sinh, cosh, tanh, asinh, acosh, atanh, log, log10, exp, pi, etc.

Now let us see these functions in action using a Prolog program.

Example

```
| ?- random(0,10,X).
```

```
X = 0
```

```
yes
```

```
| ?- random(0,10,X).
```

```
X = 5
```

```
yes
```

```
| ?- random(0,10,X).
```

```
X = 1
```

```
yes
```

```
| ?- between(0,10,X).
```

```
X = 0 ? a
```

```
X = 1
```

```
X = 2
```

```
X = 3
```

```
X = 4
```

```
X = 5
```

```
X = 6
```

```
X = 7
```

```
X = 8
```

```
X = 9
```

```
X = 10
```

```
(31 ms) yes
```

```
| ?- succ(2,X).
```

```
X = 3
```

```
yes
```

```
| ?- X is abs(-8).
```

```
X = 8
```

```
yes
```

```
| ?- X is max(10,5).
```

```
X = 10
```

```
yes
```

```
| ?- X is min(10,5).
```

```
X = 5
```

```
yes
```

```
| ?- X is round(10.56).
```

```
X = 11
```

```
yes
```

```
| ?- X is truncate(10.56).
```

```
X = 10
```

```
yes
```

```
| ?- X is floor(10.56).
```

```
X = 10
```

```
yes
```

```
| ?- X is ceiling(10.56).
```

```
X = 11
```

```
yes
```

```
| ?- X is sqrt(144).
```

```
X = 12.0
```

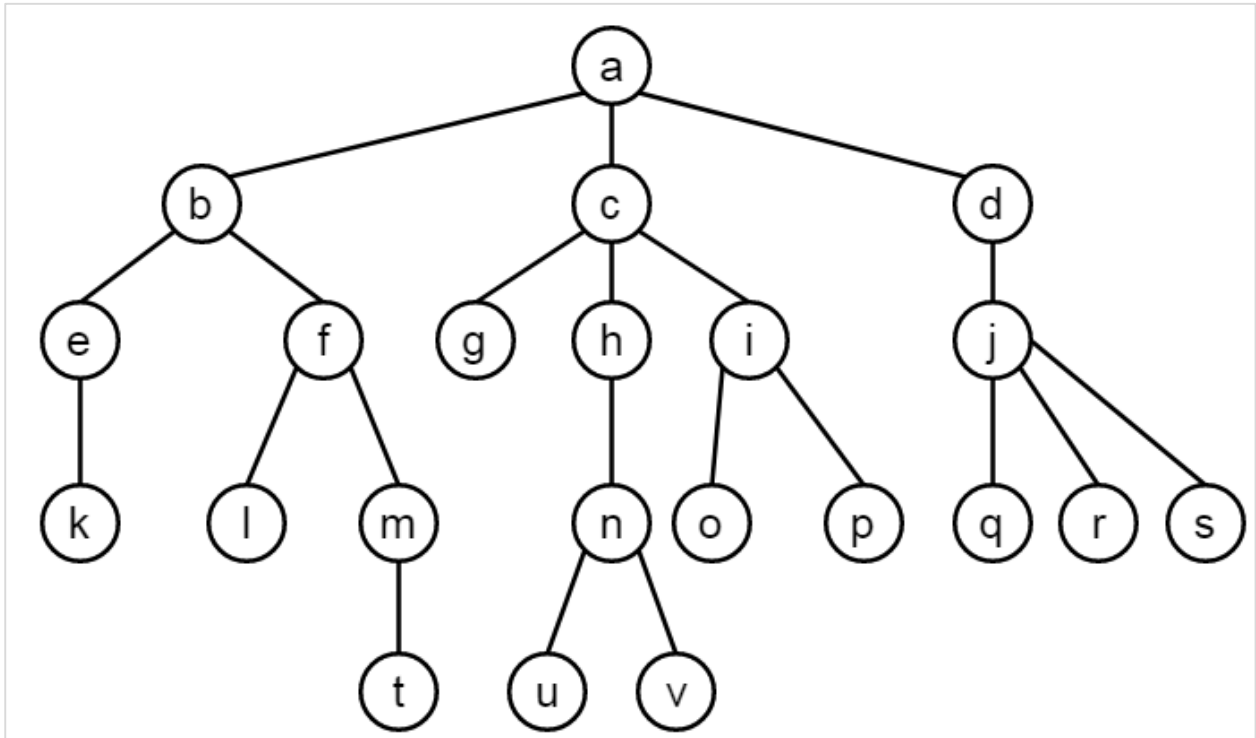
```
yes
```

```
| ?-
```

16. Prolog — Tree Data Structure (Case Study)

So far we have seen different concepts of logic programming in Prolog. Now we will see one case study on Prolog. We will see how to implement a tree data structure using Prolog, and we will create our own operators. So let us start the planning.

Suppose we have a tree as shown below:



We have to implement this tree using prolog. We have some operations as follows:

- `op(500, xfx, 'is_parent')`.
- `op(500, xfx, 'is_sibling_of')`.
- `op(500, xfx, 'is_at_same_level')`.
- And another predicate namely `leaf_node(Node)`

In these operators, you have seen some parameters as `(500, xfx, <operator_name>)`. The first argument (here 500) is the priority of that operator. The 'xfx' indicates that this is a binary operator and the <operator_name> is the name of the operator.

These operators can be used to define the tree database. We can use these operators as follows:

- **a is_parent b**, or **is_parent(a, b)**. So this indicates that node a is the parent of node b.

- **X is_sibling_of Y** or **is_sibling_of(X,Y)**. This indicates that X is the sibling of node Y. So the rule is, if another node Z is parent of X and Z is also the parent of Y and X and Y are different, then X and Y are siblings.
- **leaf_node(Node)**. A node (Node) is said to be a leaf node when a node has no children.
- **X is_at_same_level Y**, or **is_at_same_level(X,Y)**. This will check whether X and Y are at the same level or not. So the condition is when X and Y are same, then it returns true, otherwise W is the parent of X, Z is the parent of Y and W and Z are at the same level.

As shown above, other rules are defined in the code. So let us see the program to get better view.

Program

```
/* The tree database */

:- op(500,xfx,'is_parent').

a is_parent b. c is_parent g. f is_parent l. j is_parent q.
a is_parent c. c is_parent h. f is_parent m. j is_parent r.
a is_parent d. c is_parent i. h is_parent n. j is_parent s.
b is_parent e. d is_parent j. i is_parent o. m is_parent t.
b is_parent f. e is_parent k. i is_parent p. n is_parent u.

is_parent v.

/* X and Y are siblings i.e. child from the same parent */

:- op(500,xfx,'is_sibling_of').

X is_sibling_of Y :- Z is_parent X,
                    Z is_parent Y,
                    X \== Y.

leaf_node(Node) :- \+ is_parent(Node,Child). % Node grounded

/* X and Y are on the same level in the tree. */

:-op(500,xfx,'is_at_same_level').
```



```

X is_at_same_level X .
X is_at_same_level Y :- W is_parent X,
                        Z is_parent Y,
                        W is_at_same_level Z.

```

Output

```

| ?- [case_tree].
compiling D:/TP Prolog/Sample_Codes/case_tree.pl for byte code...
D:/TP Prolog/Sample_Codes/case_tree.pl:20: warning: singleton variables [Child]
for leaf_node/1
D:/TP Prolog/Sample_Codes/case_tree.pl compiled, 28 lines read - 3244 bytes
written, 7 ms

yes
| ?- i is_parent p.

yes
| ?- i is_parent s.

no
| ?- is_parent(i,p).

yes
| ?- e is_sibling_of f.

true ?

yes
| ?- is_sibling_of(e,g).

no
| ?- leaf_node(v).

yes
| ?- leaf_node(a).

no
| ?- is_at_same_level(l,s).

```

```
true ?
```

```
yes
```

```
| ?- l is_at_same_level v.
```

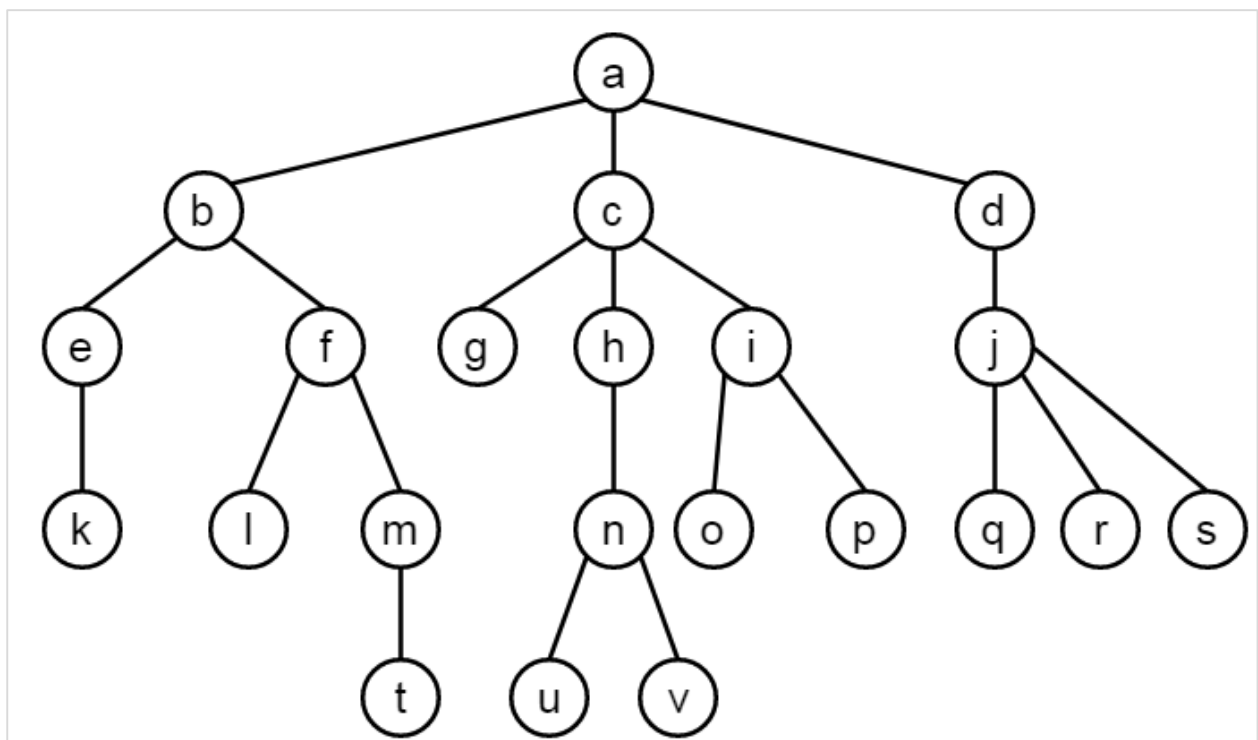
```
no
```

```
| ?-
```

More on Tree Data Structure

Here, we will see some more operations that will be performed on the above given tree data structure.

Let us consider the same tree here:



We will define other operations:

- path(Node)
- locate(Node)

As we have created the last database, we will create a new program that will hold these operations, then consult the new file to use these operations on our pre-existing program.

So let us see what is the purpose of these operators:

- **path(Node):** This will display the path from the root node to the given node. To solve this, suppose X is parent of Node, then find path(X), then write X. When root node 'a' is reached, it will stop.
- **locate(Node):** This will locate a node (Node) from the root of the tree. In this case, we will call the path(Node) and write the Node.

Program

Let us see the program in execution:

```
path(a).                                /* Can start at a. */
path(Node) :- Mother is_parent Node, /* Choose parent, */
              path(Mother),           /* find path and then */
              write(Mother),
              write(' --> ').

/* Locate node by finding a path from root down to the node */
locate(Node) :- path(Node),
                write(Node),
                nl.
```

Output

```
| ?- consult('case_tree_more.pl').
compiling D:/TP Prolog/Sample_Codes/case_tree_more.pl for byte code...
D:/TP Prolog/Sample_Codes/case_tree_more.pl compiled, 9 lines read - 866 bytes
written, 6 ms

yes
| ?- path(n).
a --> c --> h -->

true ?

yes
| ?- path(s).
a --> d --> j -->

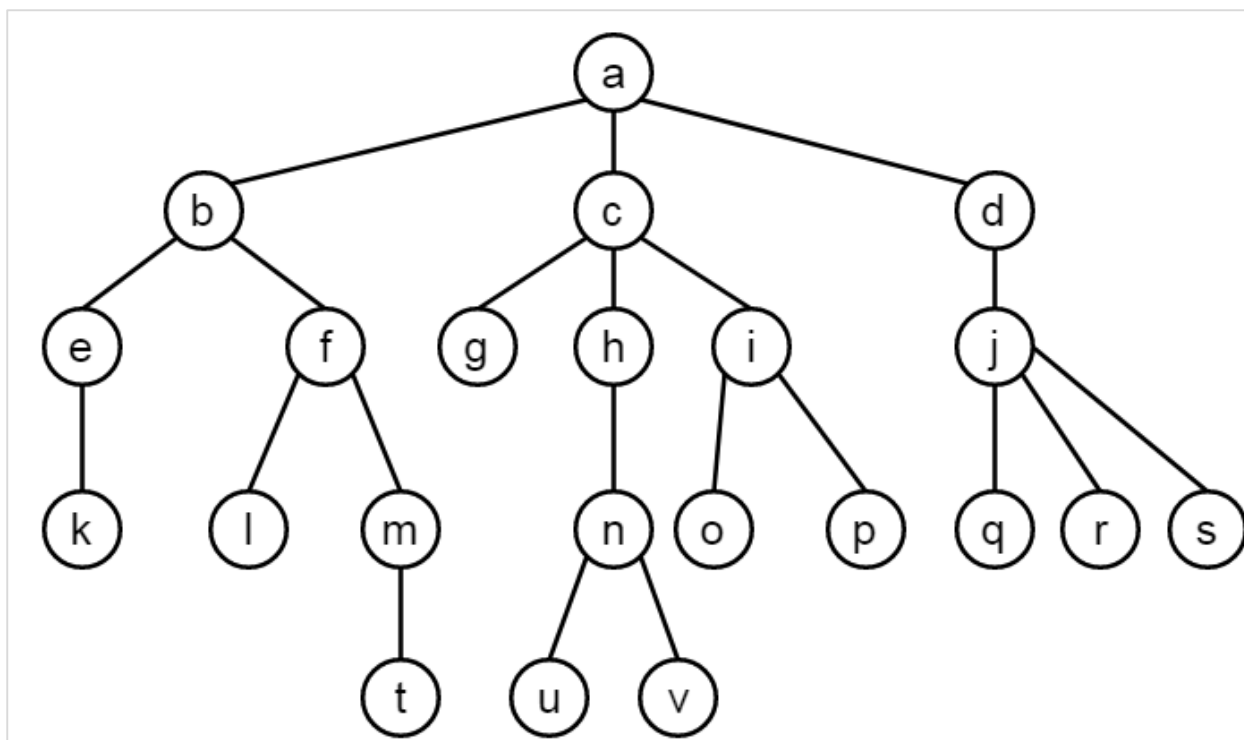
true ?

yes
```

```
| ?- path(w).  
  
no  
| ?- locate(n).  
a --> c --> h --> n  
  
true ?  
  
yes  
| ?- locate(s).  
a --> d --> j --> s  
  
true ?  
  
yes  
| ?- locate(w).  
  
no  
| ?-
```

Advances in Tree Data Structures

Now let us define some advanced operations on the same tree data structure.



Here we will see how to find the height of a node, that is, the length of the longest path from that node, using the Prolog built-in predicate `setof/3`. This predicate takes (Template, Goal, Set). This binds Set to the list of all instances of Template satisfying the goal Goal.

We have already defined the tree before, so we will consult the current code to execute these set of operations without redefining the tree database again.

We will create some predicates as follows:

ht(Node,H). This finds the height. It also checks whether a node is leaf or not, if so, then sets height H as 0, otherwise recursively finds the height of children of Node, and add 1 to them.

max([X|R], M,A). This calculates the max element from the list, and a value M. So if M is maximum, then it returns M, otherwise, it returns the maximum element of list that is greater than M. To solve this, if given list is empty, return M as max element, otherwise check whether Head is greater than M or not, if so, then call `max()` using the tail part and the value X, otherwise call `max()` using tail and the value M.

height(N,H). This uses the `setof/3` predicate. This will find the set of results using the goal `ht(N,Z)` for the template Z and stores into the list type variable called Set. Now find the max of Set, and value 0, store the result into H.

Now let us see the program in execution:

Program

```

height(N,H) :- setof(Z,ht(N,Z),Set),
               max(Set,0,H).

ht(Node,0) :- leaf_node(Node),!.

```

```

ht(Node,H) :- Node is_parent Child,
               ht(Child,H1),
               H is H1 + 1.

max([],M,M).
max([X|R],M,A) :- (X > M -> max(R,X,A) ; max(R,M,A)).

```

Output

```

| ?- consult('case_tree_adv.pl').
compiling D:/TP Prolog/Sample_Codes/case_tree_adv.pl for byte code...
D:/TP Prolog/Sample_Codes/case_tree_adv.pl compiled, 9 lines read - 2060 bytes
written, 9 ms

yes
| ?- ht(c,H).

H = 1 ? a

H = 3

H = 3

H = 2

H = 2

yes
| ?- max([1,5,3,4,2],10,Max).

Max = 10

yes
| ?- max([1,5,3,40,2],10,Max).

Max = 40

yes

```

```
| ?- setof(H, ht(c,H),Set).
```

```
Set = [1,2,3]
```

```
yes
```

```
| ?- max([1,2,3],0,H).
```

```
H = 3
```

```
yes
```

```
| ?- height(c,H).
```

```
H = 3
```

```
yes
```

```
| ?- height(a,H).
```

```
H = 4
```

```
yes
```

```
| ?-
```

Prolog — Examples

17. Prolog — Basic Programs

In the following chapter, we are going to discuss basic prolog examples to:

- Find minimum maximum of two numbers
- Find the equivalent resistance of a resistive circuit
- Verify whether a line segment is horizontal, vertical or oblique

Max and Min of two numbers

Here we will see one Prolog program, that can find the minimum of two numbers and the maximum of two numbers. First, we will create two predicates, **find_max(X,Y,Max)**. This takes X and Y values, and stores the maximum value into the Max. Similarly **find_min(X,Y,Min)** takes X and Y values, and store the minimum value into the Min variable.

Program

```
find_max(X, Y, X) :- X >= Y, !.  
find_max(X, Y, Y) :- X < Y.  
  
find_min(X, Y, X) :- X <= Y, !.  
find_min(X, Y, Y) :- X > Y.
```

Output

```
| ?- find_max(100,200,Max).  
  
Max = 200  
  
yes  
| ?- find_max(40,10,Max).  
  
Max = 40  
  
yes  
| ?- find_min(40,10,Min).  
  
Min = 10
```

```

yes
| ?- find_min(100,200,Min).

Min = 100

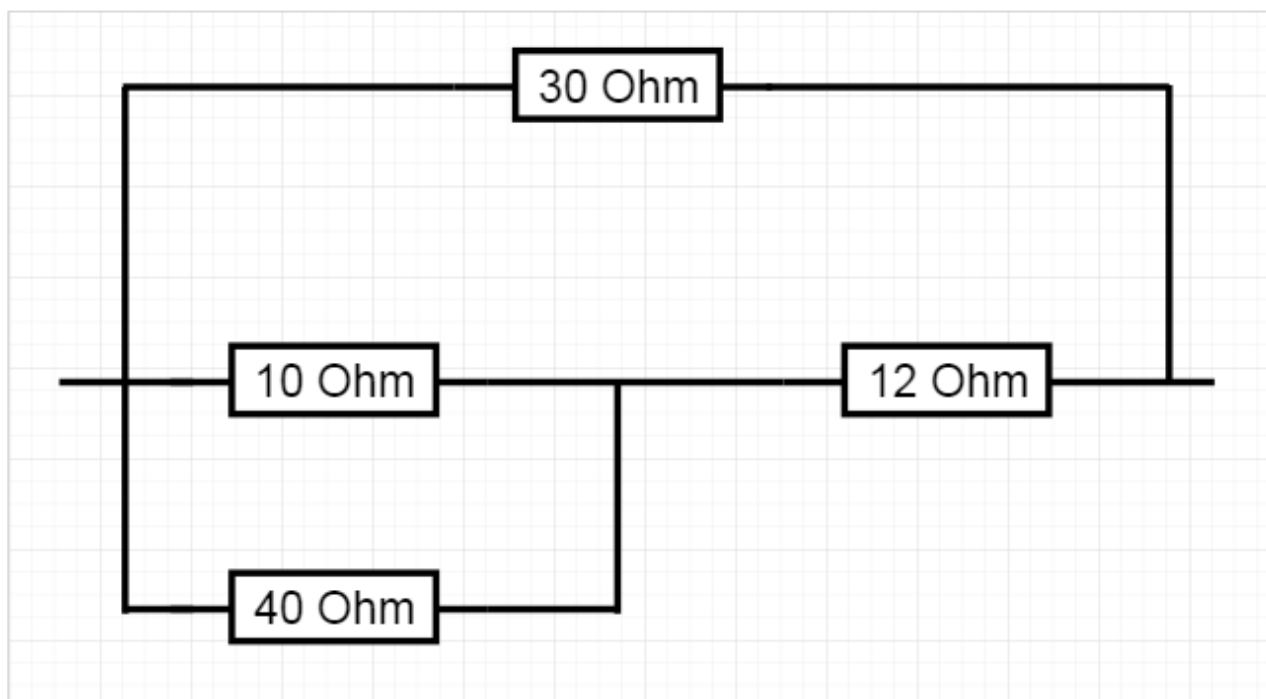
yes
| ?-

```

Resistance and Resistive Circuits

In this section, we will see how to write a prolog program that will help us find the equivalent resistance of a resistive circuit.

Let us consider the following circuit to understand this concept:



We have to find the equivalent resistance of this network. At first, we will try to get the result by hand, then try to see whether the result is matching with the prolog output or not.

We know that there are two rules:

- If R_1 and R_2 are in Series, then equivalent resistor $R_e = R_1 + R_2$.
- If R_1 and R_2 are in Parallel, then equivalent resistor $R_e = (R_1 * R_2) / (R_1 + R_2)$.

Here 10 Ohm and 40 Ohm resistors are in parallel, then that is in series with 12 Ohm, and the equivalent resistor of the lower half is parallel with 30 Ohm. So let's try to calculate the equivalent resistance.

- $R_3 = (10 * 40) / (10 + 40) = 400 / 50 = 8 \text{ Ohm}$

- $R4 = R3 + 12 = 8 + 12 = 20 \text{ Ohm}$
- $R5 = (20 * 30)/(20 + 30) = 12 \text{ Ohm}$

Program

```
series(R1,R2,Re) :- Re is R1 + R2.
parallel(R1,R2,Re) :- Re is ((R1 * R2) / (R1 + R2)).
```

Output

```
| ?- [resistance].
compiling D:/TP Prolog/Sample_Codes/resistance.pl for byte code...
D:/TP Prolog/Sample_Codes/resistance.pl compiled, 1 lines read - 804 bytes
written, 14 ms

yes
| ?- parallel(10,40,R3).

R3 = 8.0

yes
| ?- series(8,12,R4).

R4 = 20

yes
| ?- parallel(20,30,R5).

R5 = 12.0

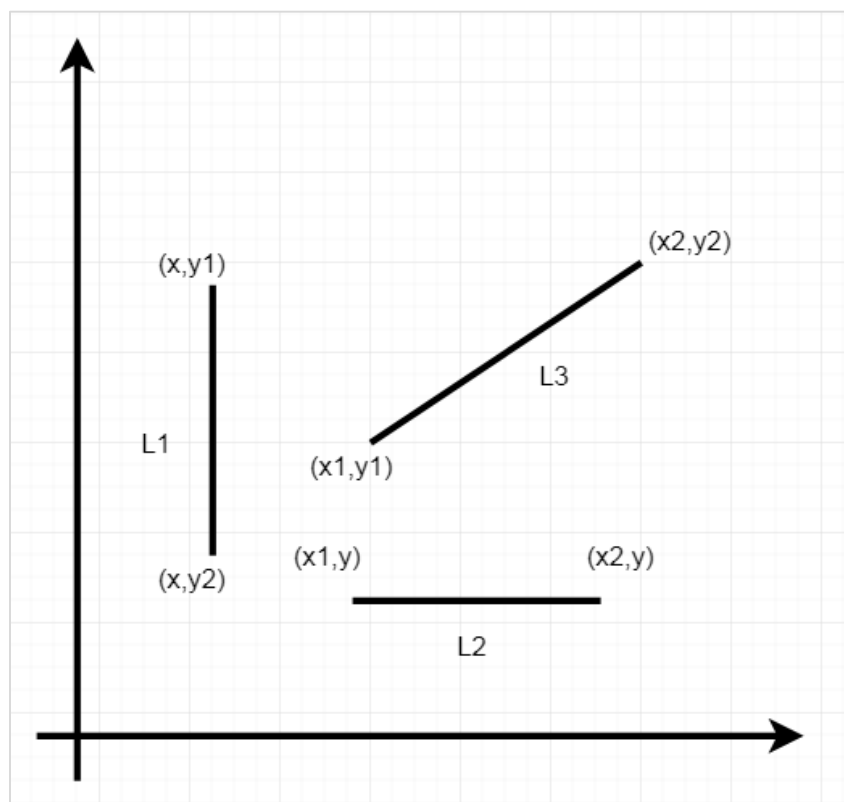
yes
| ?- parallel(10,40,R3),series(R3,12,R4),parallel(R4,30,R5).

R3 = 8.0
R4 = 20.0
R5 = 12.0

yes
| ?-
```

Horizontal and Vertical Line Segments

There are three types of line segments, horizontal, vertical or oblique. This example verifies whether a line segment is horizontal, vertical or oblique.



From this diagram we can understand that:

- For Horizontal lines, the y coordinate values of two endpoints are same.
- For Vertical lines, the x coordinate values of two endpoints are same.
- For Oblique lines, the (x,y) coordinates of two endpoints are different.

Now let us see how to write a program to check this.

Program

```
vertical(seg(point(X,_),point(X,_))).

horizontal(seg(point(_,Y),point(_,Y))).

oblique(seg(point(X1,Y1),point(X2,Y2)))
    :-X1 \== X2,
       Y1 \== Y2.
```

Output

```
| ?- [line_seg].
```

```
compiling D:/TP Prolog/Sample_Codes/line_seg.pl for byte code...
D:/TP Prolog/Sample_Codes/line_seg.pl compiled, 6 lines read - 1276 bytes
written, 26 ms

yes
| ?- vertical(seg(point(10,20), point(10,30))).

yes
| ?- vertical(seg(point(10,20), point(15,30))).

no
| ?- oblique(seg(point(10,20), point(15,30))).

yes
| ?- oblique(seg(point(10,20), point(15,20))).

no
| ?- horizontal(seg(point(10,20), point(15,20))).

yes
| ?-
```

18. Prolog — Examples of Cuts

In this section, we will see some examples of cuts in prolog. Let us consider, we want to find the maximum of two elements. So we will check these two conditions.

- If $X > Y$, then $\text{Max} := X$
- if $X \leq Y$, then $\text{Max} := Y$

Now from these two lines, we can understand that these two statements are mutually exclusive, so when one is true, another one must be false. In such cases we can use the cut. So let us see the program.

We can also define a predicate where we use the two cases using disjunction (OR logic). So when first one satisfies, it does not check for the second one, otherwise, it will check for the second statement.

Program 1

```
max(X,Y,X) :- X >= Y,!.  
max(X,Y,Y) :- X < Y.  
  
max_find(X,Y,Max) :- X >= Y,! , Max = X; Max = Y.
```

Output

```
| ?- [cut_example].  
    1    1  Call: [cut_example] ?  
compiling D:/TP Prolog/Sample_Codes/cut_example.pl for byte code...  
D:/TP Prolog/Sample_Codes/cut_example.pl compiled, 3 lines read - 1195 bytes  
written, 43 ms  
    1    1  Exit: [cut_example] ?  
  
yes  
{trace}  
| ?- max(10,20,Max).  
    1    1  Call: max(10,20,_23) ?  
    2    2  Call: 10>=20 ?  
    2    2  Fail: 10>=20 ?  
    2    2  Call: 10<20 ?  
    2    2  Exit: 10<20 ?  
    1    1  Exit: max(10,20,20) ?
```

```

Max = 20

yes
{trace}
| ?- max_find(20,10,Max).
    1    1  Call: max_find(20,10,_23) ?
    2    2  Call: 20>=10 ?
    2    2  Exit: 20>=10 ?
    1    1  Exit: max_find(20,10,20) ?

Max = 20

yes
{trace}
| ?-

```

Program 2

Let us see another example, where we will use list. In this program we will try to insert an element into a list, if it is not present in the list before. And if the list has the element before we will simply cut it. For the membership checking also, if the item is at the head part, we should not check further, so cut it, otherwise check into the tail part.

```

list_member(X,[X|_]) :- !.
list_member(X,[_|TAIL]) :- list_member(X,TAIL).

list_append(A,T,T) :- list_member(A,T),!.
list_append(A,T,[A|T]).

```

Output

```

| ?- [cut_example].
compiling D:/TP Prolog/Sample_Codes/cut_example.pl for byte code...
D:/TP Prolog/Sample_Codes/cut_example.pl compiled, 9 lines read - 1954 bytes
written, 15 ms

yes
| ?- trace.
The debugger will first creep -- showing everything (trace)

yes

```

```

{trace}
| ?- list_append(a,[a,b,c,d,e], L).
    1    1  Call: list_append(a,[a,b,c,d,e],_33) ?
    2    2  Call: list_member(a,[a,b,c,d,e]) ?
    2    2  Exit: list_member(a,[a,b,c,d,e]) ?
    1    1  Exit: list_append(a,[a,b,c,d,e],[a,b,c,d,e]) ?

L = [a,b,c,d,e]

yes
{trace}
| ?- list_append(k,[a,b,c,d,e], L).
    1    1  Call: list_append(k,[a,b,c,d,e],_33) ?
    2    2  Call: list_member(k,[a,b,c,d,e]) ?
    3    3  Call: list_member(k,[b,c,d,e]) ?
    4    4  Call: list_member(k,[c,d,e]) ?
    5    5  Call: list_member(k,[d,e]) ?
    6    6  Call: list_member(k,[e]) ?
    7    7  Call: list_member(k,[]) ?
    7    7  Fail: list_member(k,[]) ?
    6    6  Fail: list_member(k,[e]) ?
    5    5  Fail: list_member(k,[d,e]) ?
    4    4  Fail: list_member(k,[c,d,e]) ?
    3    3  Fail: list_member(k,[b,c,d,e]) ?
    2    2  Fail: list_member(k,[a,b,c,d,e]) ?
    1    1  Exit: list_append(k,[a,b,c,d,e],[k,a,b,c,d,e]) ?

L = [k,a,b,c,d,e]

(16 ms) yes
{trace}
| ?-

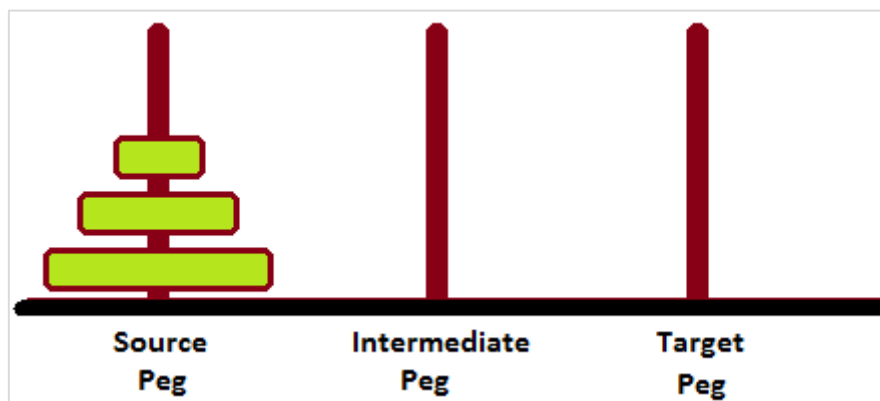
```


19. Prolog — Towers of Hanoi Problem

Towers of Hanoi Problem is a famous puzzle to move N disks from the source peg/tower to the target peg/tower using the intermediate peg as an auxiliary holding peg. There are two conditions that are to be followed while solving this problem:

- A larger disk cannot be placed on a smaller disk.
- Only one disk can be moved at a time.

The following diagram depicts the starting setup for N=3 disks.



To solve this, we have to write one procedure `move(N, Source, Target, auxiliary)`. Here N number of disks will have to be shifted from Source peg to Target peg keeping Auxiliary peg as intermediate.

For example – `move(3, source, target, auxiliary)`.

- Move top disk from source to target
- Move top disk from source to auxiliary
- Move top disk from target to auxiliary
- Move top disk from source to target
- Move top disk from auxiliary to source
- Move top disk from auxiliary to target
- Move top disk from source to target

Program

```
move(1,X,Y,_) :-  
    write('Move top disk from '), write(X), write(' to '), write(Y), nl.  
  
move(N,X,Y,Z) :-  
    N>1,  
    M is N-1,
```

```
move(M,X,Z,Y),  
move(1,X,Y,_),  
move(M,Z,Y,X).
```

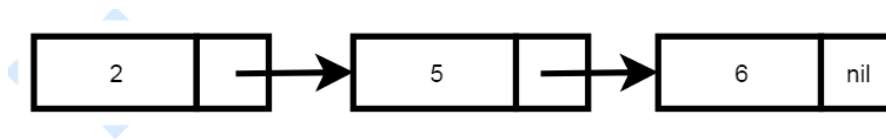
Output

```
| ?- [towersofhanoi].  
compiling D:/TP Prolog/Sample_Codes/towersofhanoi.pl for byte code...  
D:/TP Prolog/Sample_Codes/towersofhanoi.pl compiled, 8 lines read - 1409 bytes  
written, 15 ms  
  
yes  
| ?- move(4,source,target,auxiliary).  
Move top disk from source to auxiliary  
Move top disk from source to target  
Move top disk from auxiliary to target  
Move top disk from source to auxiliary  
Move top disk from target to source  
Move top disk from target to auxiliary  
Move top disk from source to auxiliary  
Move top disk from source to target  
Move top disk from auxiliary to target  
Move top disk from auxiliary to source  
Move top disk from target to source  
Move top disk from auxiliary to target  
Move top disk from source to auxiliary  
Move top disk from source to target  
Move top disk from auxiliary to target  
  
true ?  
  
(31 ms) yes
```

20. Prolog — Linked Lists

Following chapters describe how to generate/create linked lists using recursive structures.

Linked list has two components, the integer part and the link part. The link part will hold another node. End of list will have nil into the link part.



In prolog, we can express this using **node(2, node(5, node(6, nil)))**.

Note: The smallest possible list is nil, and every other list will contain nil as the "next" of the end node. In list terminology, the first element is usually called the **head** of the list, and the rest of the list is called the **tail** part. Thus the head of the above list is 2, and its tail is the list node(5, node(6, nil)).

We can also insert elements into front and back side:

Program

```
add_front(L,E,NList) :- NList = node(E,L).

add_back(nil, E, NList) :-
    NList = node(E,nil).

add_back(node(Head,Tail), E, NList) :-
    add_back(Tail, E, NewTail),
    NList = node(Head,NewTail).
```

Output

```
| ?- [linked_list].
compiling D:/TP Prolog/Sample_Codes/linked_list.pl for byte code...
D:/TP Prolog/Sample_Codes/linked_list.pl compiled, 7 lines read - 966 bytes
written, 14 ms

(15 ms) yes
| ?- add_front(nil, 6, L1), add_front(L1, 5, L2), add_front(L2, 2, L3).

L1 = node(6,nil)
L2 = node(5,node(6,nil))
```

```
L3 = node(2,node(5,node(6,nil)))
```

```
yes
```

```
| ?- add_back(nil, 6, L1), add_back(L1, 5, L2), add_back(L2, 2, L3).
```

```
L1 = node(6,nil)
```

```
L2 = node(6,node(5,nil))
```

```
L3 = node(6,node(5,node(2,nil)))
```

```
yes
```

```
| ?- add_front(nil, 6, L1), add_front(L1, 5, L2), add_back(L2, 2, L3).
```

```
L1 = node(6,nil)
```

```
L2 = node(5,node(6,nil))
```

```
L3 = node(5,node(6,node(2,nil)))
```

```
yes
```

```
| ?-
```

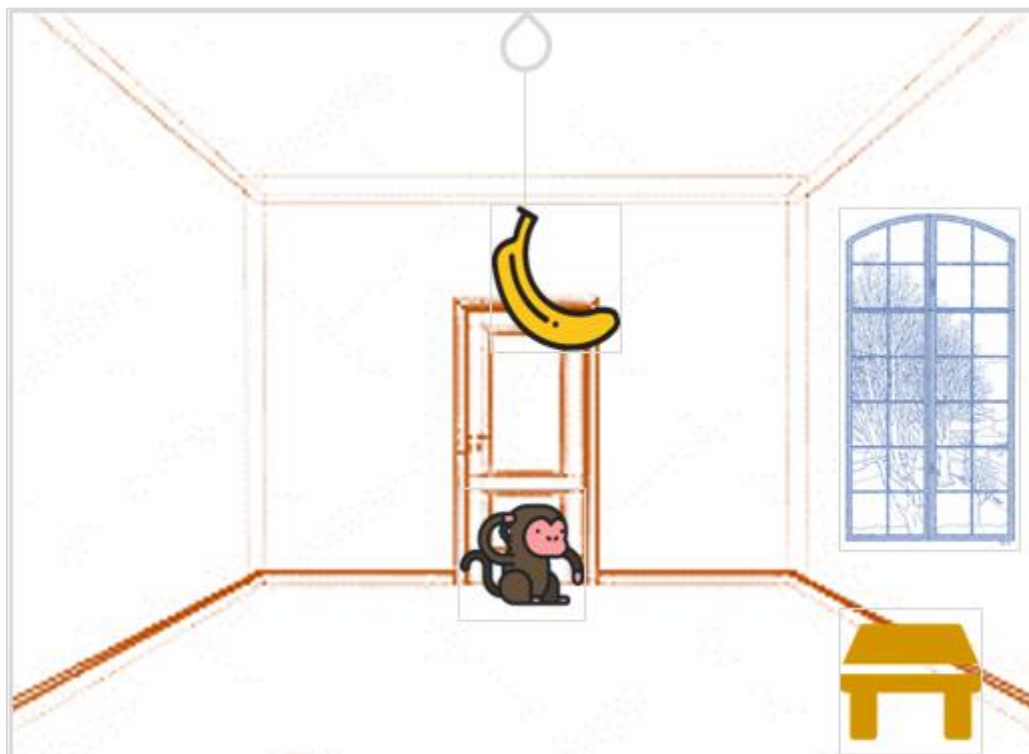
21. Prolog — Monkey and Banana Problem

In this prolog example, we will see one very interesting and famous problem, The Monkey and Banana Problem.

Problem Statement

Suppose the problem is as given below:

- A hungry monkey is in a room, and he is near the door.
- The monkey is on the floor.
- Bananas have been hung from the center of the ceiling of the room.
- There is a block (or chair) present in the room near the window.
- The monkey wants the banana, but cannot reach it.



So how can the monkey get the bananas?

So if the monkey is clever enough, he can come to the block, drag the block to the center, climb on it, and get the banana. Below are few observations in this case:

- Monkey can reach the block, if both of them are at the same level. From the above image, we can see that both the monkey and the block are on the floor.
- If the block position is not at the center, then monkey can drag it to the center.

- If monkey and the block both are on the floor, and block is at the center, then the monkey can climb up on the block. So the vertical position of the monkey will be changed.
- When the monkey is on the block, and block is at the center, then the monkey can get the bananas.

Now, let us see how we can solve this using Prolog. We will create some predicates as follows:

We have some predicates that will move from one state to another state, by performing action.

- When the block is at the middle, and monkey is on top of the block, and monkey does not have the banana (i.e. **has not** state), then using the **grasp** action, it will change from **has not** state to **have** state.
- From the floor, it can move to the top of the block (i.e. **on top** state), by performing the action **climb**.
- The **push** or **drag** operation moves the block from one place to another.
- Monkey can move from one place to another using **walk** or **move** clauses.

Another predicate will be canget(). Here we pass a state, so this will perform move predicate from one state to another using different actions, then perform canget() on state 2. When we have reached to the state '**has**', this indicates '**has banana**'. We will stop the execution.

Program

```
move(state(middle,onbox,middle,hasnot),
    grasp,
    state(middle,onbox,middle,has)).
move(state(P,onfloor,P,H),
    climb,
    state(P,onbox,P,H)).
move(state(P1,onfloor,P1,H),
    drag(P1,P2),
    state(P2,onfloor,P2,H)).
move(state(P1,onfloor,B,H),
    walk(P1,P2),
    state(P2,onfloor,B,H)).

canget(state(_,_,_,has)).
canget(State1) :-
    move(State1,_,State2),
```

```
canget(State2).
```

Output

```
| ?- [monkey_banana].
compiling D:/TP Prolog/Sample_Codes/monkey_banana.pl for byte code...
D:/TP Prolog/Sample_Codes/monkey_banana.pl compiled, 17 lines read - 2167 bytes
written, 19 ms

(31 ms) yes
| ?- canget(state(atdoor, onfloor, atwindow, hasnot)).

true ?

yes
| ?- trace
.
The debugger will first creep -- showing everything (trace)

yes
{trace}
| ?- canget(state(atdoor, onfloor, atwindow, hasnot)).
    1   1  Call: canget(state(atdoor,onfloor,atwindow,hasnot)) ?
    2   2  Call: move(state(atdoor,onfloor,atwindow,hasnot),_52,_92) ?
    2   2  Exit:
move(state(atdoor,onfloor,atwindow,hasnot),walk(atdoor,_80),state(_80,onfloor,a
twindow,hasnot)) ?
    3   2  Call: canget(state(_80,onfloor,atwindow,hasnot)) ?
    4   3  Call: move(state(_80,onfloor,atwindow,hasnot),_110,_150) ?
    4   3  Exit:
move(state(atwindow,onfloor,atwindow,hasnot),climb,state(atwindow,onbox,atwindo
w,hasnot)) ?
    5   3  Call: canget(state(atwindow,onbox,atwindow,hasnot)) ?
    6   4  Call: move(state(atwindow,onbox,atwindow,hasnot),_165,_205) ?
    6   4  Fail: move(state(atwindow,onbox,atwindow,hasnot),_165,_193) ?
    5   3  Fail: canget(state(atwindow,onbox,atwindow,hasnot)) ?
    4   3  Redo:
move(state(atwindow,onfloor,atwindow,hasnot),climb,state(atwindow,onbox,atwindo
w,hasnot)) ?
```

```

4    3  Exit:
move(state(atwindow,onfloor,atwindow,hasnot),drag(atwindow,_138),state(_138,onf
loor,_138,hasnot)) ?

5    3  Call: canget(state(_138,onfloor,_138,hasnot)) ?

6    4  Call: move(state(_138,onfloor,_138,hasnot),_168,_208) ?

6    4  Exit:
move(state(_138,onfloor,_138,hasnot),climb,state(_138,onbox,_138,hasnot)) ?

7    4  Call: canget(state(_138,onbox,_138,hasnot)) ?

8    5  Call: move(state(_138,onbox,_138,hasnot),_223,_263) ?

8    5  Exit:
move(state(middle,onbox,middle,hasnot),grasp,state(middle,onbox,middle,has)) ?

9    5  Call: canget(state(middle,onbox,middle,has)) ?

9    5  Exit: canget(state(middle,onbox,middle,has)) ?

7    4  Exit: canget(state(middle,onbox,middle,hasnot)) ?

5    3  Exit: canget(state(middle,onfloor,middle,hasnot)) ?

3    2  Exit: canget(state(atwindow,onfloor,atwindow,hasnot)) ?

1    1  Exit: canget(state(atdoor,onfloor,atwindow,hasnot)) ?

true ?

(78 ms) yes

```