# Su20 - Al Project Report

MORRIS GAME - NINE MEN VARIANT

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## Part 1: MiniMax

The **MiniMaxOpening.py** program plays a move in the opening phase of the game using MiniMax algorithm. The **MiniMaxGame.py** program plays in the midgame/endgame phase using MiniMax algorithm.

#### P1. MiniMaxOpening

Depth1: 3

Input1: WBWxxxWBBBBWxWBWxWxBBxW

Board Position: WxWWxxWBBBBWxWBWxWxBBxW

Position evaluated by Static Estimation: 1158

MINIMAX Estimate: 3

Depth2: 2

Input2: WWxBWWxxxWxxWBWBxBxBBxx

Board Position: WWWBWWxxxWxxWBWBxxxBBxx

Position evaluated by Static Estimation: 213

MINIMAX Estimate: 2

#### P2. MiniMaxGame

Depth1: 4

Input1: WxxBBWWBxxxxxxBWxWxBBWx

Board Position: WxxxBWWBxxxxxxBWxxWBBWx Position evaluated by Static Estimation: 19713

MINIMAX Estimate: 989

Depth2: 3

Input2: BxxWxxWBxxWxxxWxxBxxxxW

Board Position: BxxWxxWBxWxxxxWxxBxxxxW Position evaluated by Static Estimation: 2892

## Part 2: Alpha-Beta

The **ABOpening.py** program plays the opening game for white player using Alpha-Beta Pruning Algorithm. The **ABGame.py** program plays in the midgame/endgame phase using Alpha-Beta Pruning Algorithm.

## P1. ABOpening

Depth1: 3

Input1: WBWxxxWBBBBWxWBWxWxBBxW

Board Position: WxWWxxWBBBBWxWBWxWxBBxW

Position evaluated by Static Estimation: 150

MINIMAX Estimate: 3

Depth2: 2

Input2: WWxBWWxxxWxxWBWBxBxBBxx

Board Position: WWWBWWxxxWxxWBWBxxxBBxx

Position evaluated by Static Estimation: 51

MINIMAX Estimate: 2

#### P2. ABGame

Depth1: 4

Input1: WxxBBWWBxxxxxxBWxWxBBWx

Board Position: WxxxBWWBxxxxxxBWxxWBBWx Position evaluated by Static Estimation: 1460

MINIMAX Estimate: 989

Depth2: 3

Input2: BxxWxxWBxxWxxxWxxBxxxxW

Board Position: BxxWxxWBxWxxxxWxxBxxxxW Position evaluated by Static Estimation: 302

#### Part 3: Game for Black

The **MiniMaxOpeningBlack.py** program plays a move in the opening phase of the game, as Black, using MiniMax algorithm. The **MiniMaxGameBlack.py** program plays in the midgame/endgame phase, as Black, using MiniMax algorithm.

#### P1. MiniMaxOpeningBlack

Depth1: 3

Input1: WBWxxxWBBBBWxWBWxWxBBxW

Board Position: WBWBxxWBBBBWxWBWxWxBBxW

Position evaluated by Static Estimation: 638

MINIMAX Estimate: 0

Depth2: 2

Input2: WWxBWWxxxWxxWBWBxBxBBxx

Board Position: xWxBWWxxxWxxWBWBxBBBbxx Position evaluated by Static Estimation: 214

MINIMAX Estimate: 0

#### P2. MiniMaxGameBlack

Depth1: 4

Input1: WxxBBWWBxxxxxxBWxWxBBWx

Board Position: WxxBBWWBxxxxxxBWxWBxBWx Position evaluated by Static Estimation: 16685

MINIMAX Estimate: -13

Depth2: 3

Input2: BxxWxxWBxxWxxxWxxBxxxxW

Board Position: xxBWxxWBxxWxxxWxxBxxxxW Position evaluated by Static Estimation: 15584

## **Part 4: Improved Static Estimation**

The improved static estimation function provides better results as compared to the algorithms using the default static estimation function. The improved static estimation function gives more weight to positions that are likely to form a mill, thus reducing the number of steps. Please refer to the code for the logic.

## P1. MiniMaxOpeningImproved

Depth1: 2

Input1: WBWxxxWBBBBWxWBWxWxBBxW

Board Position: WxWWxxWBBBBWxWBWxWxBBxW

Position evaluated by Static Estimation: 100

MINIMAX Estimate: 2

Depth2: 2

Input2: WWxBWWxxxWxxWBWBxBxBBxx

Board Position: WWWBWWxxxWxxWBWBxBxxBxx

Position evaluated by Static Estimation: 213

MINIMAX Estimate: 3

#### P2. MiniMaxGameImproved

Depth1: 2

Input1: WxxBBWWBxxxxxxBWxWxBBWx

Board Position: WxxxBWWBxxxxxxBWxxWBBWx Position evaluated by Static Estimation: 157

MINIMAX Estimate: 991

Depth2: 2

Input2: BxxWxxWBxxWxxxWxxBxxxxW

Board Position: BxxWxxWBxWxxxxWxxBxxxxW Position evaluated by Static Estimation: 315

# MiniMax Opening vs Alpha-Beta Opening

Depth: 3

Input: WBWxxxWBBBBWxWBWxWxBBxW

**Result: MiniMaxOpening** 

Board Position: WxWWxxWBBBBWxWBWxWxBBxW

Position evaluated by Static Estimation: 1158

MINIMAX Estimate: 3

**Result: ABOpening** 

Board Position: WxWWxxWBBBBWxWBWxWxBBxW

Position evaluated by Static Estimation: 150

MINIMAX Estimate: 3

Depth: 2

Input: WWxBWWxxxWxxWBWBxBxBBxx

**Result: MiniMaxOpening** 

Board Position: WWWBWWxxxWxxWBWBxxxBBxx

Position evaluated by Static Estimation: 213

MINIMAX Estimate: 2

**Result: ABOpening** 

Board Position: WWWBWWxxxWxxWBWBxxxBBxx

Position evaluated by Static Estimation: 51

# MiniMax Game vs Alpha-Beta Game

Depth: 4

Input: WxxBBWWBxxxxxxBWxWxBBWx

Result: MiniMaxGame

Board Position: WxxxBWWBxxxxxxBWxxWBBWx Position evaluated by Static Estimation: 19713

MINIMAX Estimate: 989

Result: ABGame

Board Position: WxxxBWWBxxxxxxBWxxWBBWx Position evaluated by Static Estimation: 1460

MINIMAX Estimate: 989

Depth: 3

Input: BxxWxxWBxxWxxxWxxBxxxxW

Result: MiniMaxGame

Board Position: BxxWxxWBxWxxxxWxxBxxxxW Position evaluated by Static Estimation: 2892

MINIMAX Estimate: 1955

**Result: ABGame** 

Board Position: BxxWxxWBxWxxxxWxxBxxxxW Position evaluated by Static Estimation: 302

# **Static Estimation Opening vs Improved Static Estimation Opening**

Input: WBWxxxWBBBBWxWBWxWxBBxW

**Result: MiniMaxOpening** 

Depth: 3

Board Position: WxWWxxWBBBBWxWBWxWxBBxW

Position evaluated by Static Estimation: 1158

MINIMAX Estimate: 3

Result: MiniMaxOpeningImproved

Depth: 2

Board Position: WxWWxxWBBBBWxWBWxWxBBxW

Position evaluated by Static Estimation: 100

MINIMAX Estimate: 2

Input: WWxBWWxxxWxxWBWBxBxBBxx

**Result: MiniMaxOpening** 

Depth: 2

Board Position: WWWBWWxxxWxxWBWBxxxBBxx

Position evaluated by Static Estimation: 213

MINIMAX Estimate: 2

Result: MiniMaxOpeningImproved

Depth: 2

Board Position: WWWBWWxxxWxxWBWBxBxxBxx

Position evaluated by Static Estimation: 213

# **Static Estimation Game vs Improved Static Estimation Game**

Input: WxxBBWWBxxxxxxBWxWxBBWx

Result: MiniMaxGame

Depth: 4

Board Position: WxxxBWWBxxxxxxBWxxWBBWx Position evaluated by Static Estimation: 19713

MINIMAX Estimate: 989

Result: MiniMaxGameImproved

Depth: 2

Board Position: WxxxBWWBxxxxxxBWxxWBBWx Position evaluated by Static Estimation: 157

MINIMAX Estimate: 991

Input: BxxWxxWBxxWxxxWxxBxxxxW

Result: MiniMaxGame

Depth: 3

Board Position: BxxWxxWBxWxxxxWxxBxxxxW Position evaluated by Static Estimation: 2892

MINIMAX Estimate: 1955

Result: MiniMaxGameImproved

Depth: 2

Board Position: BxxWxxWBxWxxxxWxxBxxxxW Position evaluated by Static Estimation: 315

## Conclusion

- 1. The Alpha-Beta algorithm computes the same results by estimating lesser nodes as compared to the MiniMax algorithm.
- 2. The Improved Static Estimation function, finds better positions at lesser depths and needs significantly lesser position estimates. In some cases, it finds better Board positions as compared to the normal ones.

## References

- 1. Handout Notes and Function algorithms.
- 2. https://en.wikipedia.org/wiki/Nine men%27s morris