

# CS 383 – Machine Learning

## Notation

### Machine Learning Notation

- $C$  – Number of classes
- $k$  – Number of clusters.
- $C_i$  – The set of data with class or cluster  $i$
- $|C_i|$  – Cardinality (set size) of set  $C_i$
- $D$  – Dimensionality of data vector (number of features)
- $R$  – Number of outputs
- $N$  – Number of data cases (observations, instances)
- $X$  – Complete dataset observations.
- $Y$  – Complete dataset outputs.
- $X_i$  – The  $i^{th}$  observation in dataset  $X$ ,  $i \in \{1, \dots, N\}$
- $Y_i$  – The  $i^{th}$  observation's output,  $i \in \{1, \dots, N\}$
- $X_{:,j}$  – The  $j^{th}$  feature of all the data in the dataset  $X$ ,  $j \in \{1, \dots, D\}$
- $Y_{:,j}$  – The  $j^{th}$  output for all observations.
- $X_{i,j}$  – The  $j^{th}$  feature of observation  $i$ ,  $i \in \{1, \dots, N\}$ ,  $j \in \{1, \dots, D\}$ .
- $Y_{i,j}$  – The  $j^{th}$  output for observation  $i \in \{1, \dots, N\}$
- $x$  – A single sample observation.
- $x_i$  – The  $j^{th}$  feature of observation  $x$ .
- $y$  – A single observation's output.
- $y_i$  – The  $i^{th}$  output for an observation.
- $\theta$  – parameter vector
- $\theta_s - s^{th}$  parameter of the parameter vector
- $J(\theta)$  – Cost function
- $\hat{z}$  – The estimated value of  $z$
- $K$  - number of states
- $\kappa(x, y)$  – Kernel function
- $T$  – Length of a sequence

## Linear Algebra Notation

- $\text{tr}(A)$  – Trace of matrix
- $\det(A) = |A|$  – Determinant of matrix
- $\text{diag}(A)$  = diagonal of matrix
- $A^{-1}$  – Inverse of matrix
- $A^T$  – Transpose of matrix
- $\mathbf{I}$  – Identity matrix
- $\|x\| = \|x\|_2$  - Euclidean norm,  $\sqrt{\sum_{j=1}^d x_j^2}$
- $\|x\|_1$  – L1 norm,  $\sum_{j=1}^d |x_j|$
- $A_{:,j} - j^{th}$  column of matrix
- $A_{i,:} - i^{th}$  row of matrix
- $A_{i,j}$  – Element (i,j) of matrix

## Statistics Notation

- $P(x)$  – Probability of  $x$
- $\text{cov}[x]$  – Covariance of  $x$
- $H(X)$  – Entropy of distribution  $P(X)$
- $I(X; Y)$  – Mutual information between  $X$  and  $Y$
- $\ell(\theta)$  – Log-likelihood function
- $\mu$  – Mean
- $p(x)$  - Probability density function (pdf)
- $\phi$  – pdf of standard normal
- $\sigma^2$  – Variance
- $\Sigma$  – Covariance matrix
- $\mu_{ij}$  – The mean of the  $j^{th}$  feature from class  $i$
- $\sigma_{ij}$  – The standard deviation of the  $j^{th}$  feature from class  $i$