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## Clear Environment and change directory

```
clear; close all; clc;
cd /home/avila/Documents/STUDIUM/03SemMaster/makro/assign/assign01
addpath('./functions/');
```

## Q. 01 - Fetch Data

```
startDate = "01/01/1996";
endDate = "01/01/2018";

series = ["FRAPFCEQDSNAQ" "DEUPFCEQDSNAQ" "ITAPFCEQDSNAQ" ...
          "CLVMNACSCAB1GQFR", "CLVMNACSCAB1GQDE", "CLVMNACSCAB1GQIT"];
```

Using `fred` and `fetch` function to retrieve data from FRED this function requires the Datafeed Toolbox. If toolbox is not available try to load the data that should be stored in a subfolder called "data" with the following command:

```
load('data/dataStruct.mat')

% using fred.stloisfed connection
url = 'https://fred.stlouisfed.org/';

% retrieve data struct of the 6 time series
dataStruct = fetch(fred(url), series, startDate, endDate);

% consumption data
con_fr = dataStruct(1).Data(:,2);
con_de = dataStruct(2).Data(:,2);
con_it = dataStruct(3).Data(:,2);

% gdp data
gdp_fr = dataStruct(4).Data(:,2);
gdp_de = dataStruct(5).Data(:,2);
gdp_it = dataStruct(6).Data(:,2);
```

where: \*(:,2) : extract second column vector from \* the row called "Data", from \* the (1:6) row of object defined as dataStruct and \* define as con\_\* and gdp\_\* respectively

---

```

%%% Transform Data

con_fr = con_fr / 10^9;
con_de = con_de / 10^9;
con_it = con_it / 10^9;

gdp_fr = gdp_fr / 10^3;
gdp_de = gdp_de / 10^3;
gdp_it = gdp_it / 10^3;

```

## Q. 02 and 03 - Apply HP Filter

```

lambda = 1600;
rinseAndRepeat("gdp", gdp_fr, gdp_de, gdp_it, con_fr, con_de, con_it,
lambda)
rinseAndRepeat("con", gdp_fr, gdp_de, gdp_it, con_fr, con_de, con_it,
lambda)

```

## Q. 04 - Repeat for lambdas 0

```

%%% lambda -> 0

lambda = 0;
rinseAndRepeat("gdp", gdp_fr, gdp_de, gdp_it, con_fr, con_de, con_it,
lambda)
rinseAndRepeat("con", gdp_fr, gdp_de, gdp_it, con_fr, con_de, con_it,
lambda)

```

ANSWER: In this case we only minimize the first term of the HP-filter minimization problem. So the trend component is exactly the same as the observed data, and the cyclical component is, therefore, zero.

## Q. 04 - Repeat for lambdas inf

```

lambda = 10^10;
rinseAndRepeat("gdp", gdp_fr, gdp_de, gdp_it, con_fr, con_de, con_it,
lambda)
rinseAndRepeat("con", gdp_fr, gdp_de, gdp_it, con_fr, con_de, con_it,
lambda)

```

ANSWER: In the case of  $\lambda \rightarrow \infty$ , the second component in the HP-Filter gets the greatest weight and, therefore, we have a linear trend where the second term of the minimization problem is zero, because the change in the trend is constant. The cyclical component shows the difference between the observed data and the linear trend. Due to (near-) singularity problems, the matrix A from the HP-Filter function is not invertible for very big lambdas. The results are, therefore, nonsensical and for infinity not computable.

```

lambda = 10^50;
rinseAndRepeat("gdp", gdp_fr, gdp_de, gdp_it, con_fr, con_de, con_it,
lambda)
rinseAndRepeat("con", gdp_fr, gdp_de, gdp_it, con_fr, con_de, con_it,
lambda)

```

---

## Q. 05 - Apply Log

```
lgdp_de = log(gdp_de);
lgdp_fr = log(gdp_fr);
lgdp_it = log(gdp_it);

lcon_de = log(con_de);
lcon_fr = log(con_fr);
lcon_it = log(con_it);

%%% hp filter on log data
lambda = 1600;

[lgdp_T_fr, lgdp_C_fr] = hp_filter(lgdp_fr, lambda);
[lcon_T_fr, lcon_C_fr] = hp_filter(lcon_fr, lambda);

%%% germany
[lgdp_T_de, lgdp_C_de] = hp_filter(lgdp_de, lambda);
[lcon_T_de, lcon_C_de] = hp_filter(lcon_de, lambda);

%%% italy
[lgdp_T_it, lgdp_C_it] = hp_filter(lgdp_it, lambda);
[lcon_T_it, lcon_C_it] = hp_filter(lcon_it, lambda);
```

## Q. 05 - Repeat for lambdas inf

```
close all
dates=1996.0:0.25:2018.0;

figure;
titleOfGraph = 'Cyclical Series (\lambda = ' + string(lambda) + ')';
sgtitle(titleOfGraph)
% working on 3 by 1 plots, plot 01
subplot(3,1,1); % GERMANY
plot(dates, lgdp_C_de, 'LineWidth', 1); hold on;
plot(dates, lcon_C_de, 'LineWidth', 1); hold on;
xlabel('Years');
ylabel('Log Billions of dollars');
title('Germany');
legend('GDP', 'Consumptioin');

% working on 3 by 1 plots, plot 02
subplot(3,1,2);
plot(dates, lgdp_C_fr, 'LineWidth', 1); hold on;
plot(dates, lcon_C_fr, 'LineWidth', 1); hold on;
title('France');
ylabel('Log Billions of dollars');
xlabel('Years');

% working on 3 by 1 plots, plot 03
subplot(3,1,3)
plot(dates, lgdp_C_it, 'LineWidth', 1); hold on;
```

---

```
plot(dates, lcon_C_it, 'LineWidth', 1); hold on;
ylabel('Log Billions of dollars');
xlabel('Years');
title('Italy');
```

ANSWER: From the cyclical component above we can notice that GDP has a peak and declines sharply after the financial crises of 2007~08. Especially for Italy one can notice the effects of the Euro sovereign debt crises around 2012. The cyclical series of consumption from Italy and France seem to closely follow the one of GDP. On the other hand, consumption in Germany is less affected by the strong changes in GDP. This could suggest that Households in Germany were less affected by both crises than in the other two countries.

## Q. 06 - Std Deviation

```
std(lgdp_C_de) %      0.0150
std(lgdp_C_fr) %      0.0092
std(lgdp_C_it) %      0.0128

std(lcon_C_de) %      0.0060
std(lcon_C_fr) %      0.0070
std(lcon_C_it) %      0.0110
```

ANSWER: The results show that consumption is less volatile than GDP in all three countries. This could be due to the fact that GDP absorbs also the volatility of its other components, that is, Gov't expenditure, Investments and Net Exports.

The very low std deviation in consumption for Germany corroborates the hypothesis advanced in the previous answer.

## Q. 07 - Cyclical Series

```
%%% Q.7 - a) slice timeseries

lambda = 1600;
startDate = 1996;
endDate = 2009;

lgdp_it_cut = timeseries(lgdp_it,dates);
lgdp_it_cut = getsampleusingtime(lgdp_it_cut, startDate, endDate);
lgdp_de_cut = timeseries(lgdp_de,dates);
lgdp_de_cut = getsampleusingtime(lgdp_de_cut, startDate, endDate);
lgdp_fr_cut = timeseries(lgdp_fr,dates);
lgdp_fr_cut = getsampleusingtime(lgdp_fr_cut, startDate, endDate);

[lgdp_it_cut_T, lgdp_it_cut_C] = hp_filter(lgdp_it_cut.Data, lambda);
[lgdp_de_cut_T, lgdp_de_cut_C] = hp_filter(lgdp_de_cut.Data, lambda);
[lgdp_fr_cut_T, lgdp_fr_cut_C] = hp_filter(lgdp_fr_cut.Data, lambda);

%%% Q.7 - a) plot cyclical series

datesCut = startDate:0.25:endDate;

figure;
% end-point
```

---

```

sgtitle('End-Points Bias')
% working on 3 by 1 plots, plot 01
subplot(3,1,1);
plot(dates, lgdp_C_de, 'LineWidth', 1) ; hold on;
plot(datesCut, lgdp_de_cut_C, 'LineWidth', 1) ; hold on;

xlabel('Years');
ylabel('Log Billions of dollars');
title('Germany');
legend('long', 'short');

% working on 3 by 1 plots, plot 01
subplot(3,1,2);
plot(dates, lgdp_C_fr, 'LineWidth', 1) ; hold on;
plot(datesCut, lgdp_fr_cut_C, 'LineWidth', 1) ; hold on;

xlabel('Years');
ylabel('Log Billions of dollars');
title('France');
legend('long', 'short');

subplot(3,1,3);
plot(dates, lgdp_C_it, 'LineWidth', 1) ; hold on;
plot(datesCut, lgdp_it_cut_C, 'LineWidth', 1) ; hold on;

xlabel('Years');
ylabel('Log Billions of dollars');
title('Italy');
legend('long', 'short');

```

ANSWER: How one can take from the HP-Filter formula of the minimization problem, the first and the last observations of the series, that is, the end-points, are not smoothed by the change in growth trend. That is, the second term is computed only from  $t=2$  to  $T-1$ , whereas the first term is computed for the whole time series. This results in an exaggerated estimation for the trend at the extremes. In our graph, one can see the bias at the right end-point

## plot trend check

```

figure;
plot(dates, lgdp_T_de, 'LineWidth', 1) ; hold on;
plot(datesCut, lgdp_de_cut_T, 'LineWidth', 1) ; hold on;
plot(dates, lgdp_de, 'LineWidth', 1); hold on;

xlabel('Years');
ylabel('Log Billions of dollars');
title('Germany');
legend('Location', 'northwest')
legend('long trend', 'end-point biased', 'log data');

close all

```

