

Understanding the problem statement

Input : arr = [1,3,4,5,6] output : we have to find the smallest number that cannot be formed by adding the numbers in the input array. start from 1 . 1 can be formed by 1 then 2 --> cannot be formed from array number. so answer is 2 # ans : 2
Input : arr = [4,13,2,3,1] output : we have to find the smallest number that cannot be formed by adding the numbers in the input array. start from 1 . 1 can be formed by 1 then 2 --> 2 can be formed by 2 3 --> 3 4 --> 4 5 --> 4+1 6 --> 4+2 7 --> 4+3 8 --> 4+3+1 9 --> 4+3+2 10 --> 4+3+2+1 11 --> cannot be formed # ans : 11

Algorithm

1. Sort the array in increasing order 2. Let P be the smallest sum that we cannot make . p = 1 3. If the current number is bigger than smallest sum we cannot make so far i.e $a[i] > P$ then P is the smallest number we cant make. return P 4. else if current number is less than or equal to smallest sum we cannot make so far i.e $a[i] \leq P$ update p as $a[i]+P$ i.e $P=a[i]+P$

Complexity:

Time:

sort takes $O(n \log n)$. Steps 3 and 4 requires traversing the input arr $O(n)$. So total time complexity is $O(n \log n)$

Space:

If we use inplace sorting algorithm space complexity is $O(1)$.
Algorithm itself doesnt use any extra space . Space depends on sorting algorithm that we use

Algorithm explanation with example

input arr : 4,13,2,3,1 sort : 1,2,3,4,13 1. Let P be 1. compare with current element i.e 1 $curr_ele \leq P$ so update P to be 1+1 i.e 2 2. Again compare P with current element i.e 2 $curr_ele \leq P$ so update P to be 2+2 i.e 4 3. Again compare P with current element i.e 3 $curr_ele \leq P$ so update P to be 4+3 i.e 7 That means 7 is the smallest sum that we cannot make with 1,2,3 4. Again compare P with current element i.e 4 $curr_ele \leq P$ so update P to be 7+4 i.e 11 That means 11 is the smallest sum that we cannot make with 1,2,3,4 5. Again compare P with current element i.e 13 $curr_ele > P$. so return P. our required answer is 11. 11 is the smallest sum we cannot make with 4,13,2,3,1. How is it working? ans : suppose n is the smallest sum we cannot make till now.and $curr_ele$ is x. so we can make sums of 1,2,3...(n-1).and with x we can further make sums like $x+1, x+2, \dots, x+(n-1)$ now if we have x

Implementation

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In [4]: def findSmallestSum(arr,size):
        arr = sorted(arr)
        p = 1
        i = 0
        curr_ele = arr[i]
        while(curr_ele <=p and i<size):
            p = p+curr_ele
            i += 1
            curr_ele = arr[i]
        return p
```

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In [5]: arr = [1,3,4,5,6]
        size = len(arr)
        print(findSmallestSum(arr,size))
        # ans 2
```

2

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In [7]: arr = [4,13,2,3,1]
        size = len(arr)
        print(findSmallestSum(arr,size))
        # ans 11
```

11

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In [ ]:
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