

# EQUILIBRIUM INDEX:

Index such that sum of elements till the index(including it) is equal to the sum of remaining elements.

## Approach 1

For each index test whether it is equilibrium index or not. For each  $i$  check sum till that index and sum of remaining elements and check whether both sums are equal or not. For checking each index -  $O(n)$  For finding sum we have to scan the array -  $O(n)$  Complexity: Time :  $O(n^2)$  Space :  $O(1)$

## Approach 2

First find the cumulative sum list of the array elements. Then for each index check sum till the point and compare it with other sum like below:  
 $\text{cum\_sum}[i] == \text{cum\_sum}[-1] - \text{cum\_sum}[i]$  if condition is satisfied equilibrium index is  $i$  Complexity: finding cum\_sum -  $O(n)$ . Scanning it  $O(n)$   
Time :  $O(n)$  Space:  $O(n)$

```
In [2]: def findEquilibriumIndex(arr):
        cum_sum = []
        curr_sum = 0
        for i in arr:
            curr_sum += i
            cum_sum.append(curr_sum)
        for ix, ele in enumerate(cum_sum):
            if ele == cum_sum[-1] - ele:
                return ix
        return -1
```

```
In [19]: arr = [1,5,10,9,1,2,4]
        findEquilibriumIndex(arr)
        #ans 2
```

Out[19]: 2

```
In [20]: arr = [1,5,10,9,1,2]
        findEquilibriumIndex(arr)
        #ans -1
```

Out[20]: -1

```
In [21]: arr = [1,1,5,10,9,1,2,5]
        findEquilibriumIndex(arr)
        #ans 3
```

Out[21]: 3

You can also do this approach by reducing space complexity to  $O(1)$  as below:

```
In [26]: def findEquilibriumIndex_opt(arr):
        total_sum = 0
        curr_sum = 0
        for i in arr:
            total_sum += i
        for ix in range(len(arr)):
            curr_sum += arr[ix]
            if curr_sum == total_sum - curr_sum:
                return ix
        return -1
```

```
In [27]: arr = [1,5,10,9,1,2]
         findEquilibriumIndex_opt(arr)
         #ans -1
```

Out[27]: -1

```
In [28]: arr = [1,1,5,10,9,1,2,5]
         findEquilibriumIndex_opt(arr)
         #ans 3
```

Out[28]: 3

In [ ]: