

# Understanding the problem statement

Consider an array such that  $1 \leq \text{arr}[i] \leq n$  i.e all the elements are in the range of  $[1, n]$ . All the elements in the array occur once except for two repeating elements. suppose if  $n=7$  then elements will be like  $[1, 2, 3, 4, 5, 1, 3]$ . In the example 1 and 3 are repeated, but any elements could repeat but the range will be from 1 to  $n-2$ . Actual range  $1 \leq \text{arr}[i] \leq n-2$ . Input :  $[1, 2, 3, 4, 5, 1, 3]$  Output :  $[1, 3]$

## Approach 1

Find all possible pairs out of  $n$  elements ( $nC2$ ) using two for loops and check if they are repeating or not.

Time Complexity :  $O(n^2)$

Space Complexity :  $O(1)$

## Approach 2

1. Maintain a list of size  $n$ .
2. Traverse the given array and increment value at that index in the list. If 1 is repeated increment count at  $\text{list}[1]$  i.e  $[0, 1, 0, 0, 0]$
3. Traverse the list and print the indexes where count = 2.  $[1, 2, 1, 1, 2]$

Time Complexity:  $O(n)$

Space Complexity:  $O(n)$

## Approach 3

1. Find the sum of the given array  $S$ .
2. Find the sum of first  $(n-2)$  natural numbers using  $n(n+1)/2$  formula  $S1$ .
3. Compute the difference  $S-S1$  which gives sum of repeating elements.  $(X + Y)$
4. Find the product of the given array.  $P$
5. Find the product of first  $(n-2)$  natural numbers using  $n!$ .  $P1$
6. Compute the division  $P/P1$  which gives product of repeating elements.  $(X * Y)$
7. Compute the difference of repeating elements using  $(X-Y) = \sqrt{((X+Y)^2 - 4XY)}$
8. We have  $X+Y$  and  $X-Y$  we can compute  $X$  and  $Y$ .
9. Although the time complexity is  $O(n)$  we don't use this approach because this involves too multiplications and multiplication is computationally expensive.

Time Complexity :  $O(n)$

Space Complexity :  $O(1)$

## Approach 4

1. Find the xor of all elements in the given array. [1,2,3,4,1,2]
2. Xor the obtained result with the first (n-2) natural numbers to obtain the xor of repeating elements.  $(X \oplus Y)$ . Xor with same element cancels out each other.  $(1^2 \oplus 3^4 \oplus 1^2) \oplus (1^2 \oplus 3^4) = 1^2$
3. Now find the right most set bit in  $X \oplus Y$  using formula  $a \& \sim(a-1)$ .
4. Divide the given array based on the right most set bit. Now the two repeating elements goes into two different lists. [1,1,3],[2,2,4]
5. Also divide first n-2 natural numbers based on right most set bit. [1,3],[2,4]
6. Now xor the divided natural numbers list and divided array list to get repeating elements [1,1,3]  $\oplus$  [1,3] = [1] [2,2,4]  $\oplus$  [2,4] = [2]
7. [1,2] are repeating elements

**Time Complexity :  $O(n)$**

**Space Complexity :  $O(1)$**

## Implementation

```
In [3]: def check_set(n,k):
        if (1<=k)&(n):
            return 1
        return 0

def findRepeating(arr,size):
    arr_xor = 0
    for i in range(size):
        arr_xor = arr_xor ^ arr[i]
    for i in range(1,size-1):
        arr_xor = arr_xor ^ i
    set_bit = arr_xor & (~(arr_xor -1))
    first_num = 0
    second_num = 0
    for i in range(size):
        if check_set(arr[i],set_bit):
            first_num = first_num ^ arr[i]
        else:
            second_num = second_num ^ arr[i]
    for i in range(1,size-1):
        if check_set(i,set_bit):
            first_num = first_num ^ i
        else:
            second_num = second_num ^ i
    return [first_num,second_num]
```

```
In [4]: arr = [1,2,3,4,1,2]
size = len(arr)
print(findRepeating(arr,size))
# ans
# [2, 1]
```

[2, 1]

```
In [6]: arr = [1,2,2,3,1,4]
size = len(arr)
print(findRepeating(arr,size))
```

```
# ans  
# [2, 1]
```

[2, 1]

```
In [7]: arr = [1,3,2,3,5,4,5]  
size = len(arr)  
print(findRepeating(arr,size))  
# ans  
# [5, 3]
```

[5, 3]

## Approach 4

1. This is similar to finding duplicates program in  $O(n)$  time and  $O(1)$  extra space.
2. Iterate through the array and make integer at index  $arr[i]$  to negative if it is positive. If it is already negative it means we already have  $arr[i]$  at some other place in array.
3. So  $arr[i]$  is considered as repeated.

In [ ]: