

Understanding the problem statement

Given an unsorted array of positive integers, find the number of triangles that can be formed with three different elements as three sides of triangle input : [2,4,3,1] output : 1 ans : [2,3,4] only can form triangle Triangular property : sum of any two sides should be greater than third side. Sides of triangle [a,b,c] --> $a+b > c$ and $a+c > b$ and $b+c > a$ [1,2,3] cannot form triangle as $1+2 = 3$.

Approach 1

1. Find all the possibilities of 3 elements from given n elements. $nC3$ i.e $O(n^3)$
2. For each possibility check Triangular property condition i.e $a+b > c$ and $a+c > b$ and $b+c > a$. $O(1)$
3. So total time complexity is $O(n^3) * O(1) = O(n^3)$

Approach 2

1. Sort the given array. $O(n \log n)$
2. when elements are sorted we need not check 3 conditions. When [a,b,c] are in ascending order just checking $a+b > c$ will be enough because as c is already greater than a and b, $a+c > b$ and $b+c > a$ will be true.
3. Take each element from the array i, take next element as j and check for the elements k which are smaller than $a[i]+a[j]$. When bigger element is encountered we can stop iterating and update the count. k need not be initialized in the algorithm because once it is true for smaller sum of i,j then it will be true for i and bigger j. $O(n^2)$
4. Once bigger element is encountered we can increase sum $a[i]+a[j]$ by incrementing j.
5. Repeat steps 3 and 4 i.e move i and j and keep updating count.
6. See reference screenshot for complete algorithm.
7. so Total time complexity = $O(n \log n) + O(n^2) = O(n^2)$

Implementation

```
In [8]: def findPossibleTriangleCount(arr,n):
        arr = sorted(arr)
        count = 0
        for i in range(n-2):
            k = i+2
            for j in range(i+1,n-1):
                while((k<n) and ((arr[i]+arr[j])>arr[k])):
                    k+=1
                count = count+(k-j-1)
        return count
```

```
In [15]: arr = [6,7,8,10,12,14,50]
        findPossibleTriangleCount(arr,len(arr))
        # ans 18
```

Out[15]: 18

```
In [16]: arr = [7, 3, 6, 4]
        findPossibleTriangleCount(arr,len(arr))
        # ans 3
```

Out[16]: 3

```
In [17]: arr = [10, 21, 22, 100, 101, 200, 300]
         findPossibleTriangleCount(arr, len(arr))
         # ans 6
```

Out[17]: 6

```
In [ ]:
```