Parallel FFT

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Algorithm:

Recursive Implementation:

```
DFT of (x_0, x_s, x_{2s}, ..., x_{(N-1)s}):
X_0, \ldots, N-1 \leftarrow \text{ditfft2}(x, N, s):
    if N = 1 then
                                                                        trivial size-1 DFT base case
          X_{\Theta} \leftarrow X_{\Theta}
     else
          X_0, \ldots, N/2-1 \leftarrow \text{ditfft2}(x, N/2, 2s)
                                                                        DFT of (x_0, x_{2s}, x_{4s}, ...)
          X_{N/2,...,N-1} \leftarrow ditfft2(x+s, N/2, 2s)
                                                                       DFT of (x_s, x_{s+2s}, x_{s+4s}, ...)
                                                                         combine DFTs of two halves into full DFT:
          for k = 0 to N/2-1
                t \leftarrow X_k
                X_k \leftarrow t + \exp(-2\pi i \ k/N) \ X_{k+N/2}
                X_{k+N/2} \leftarrow t - \exp(-2\pi i \ k/N) \ X_{k+N/2}
          endfor
     endif
```

In the above method, it is difficult to parallelize the above code. Iterative approaches can be easily parallelized.

Iterative Approach of Cooley-Tukey FFT:

```
algorithm iterative-fft is
    input: Array a of n complex values where n is a power of 2
   output: Array A the DFT of a
   bit-reverse-copy(a,A)
   n \leftarrow a.length
   for s = 1 to log(n)
         m + 25
         \omega_m \leftarrow \exp(-2\pi i/m)
         for k = 0 to n-1 by m
              \omega \leftarrow 1
              for j = 0 to m/2 - 1
                   t \leftarrow \omega A[k+j+m/2]
                   u \leftarrow A[k+j]
                   A[k+j] \leftarrow u+t
                   A[k+j+m/2] \leftarrow u-t
                   \omega \leftarrow \omega \omega_m
    return A
```

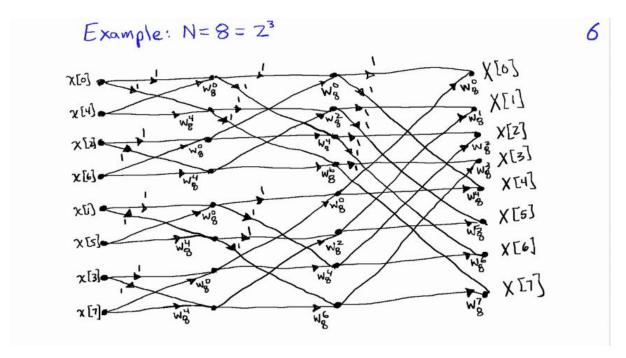
In this method, we are doing bit-reverse copy, pseudocode for this is:

```
algorithm bit-reverse-copy(a, A) is
input: Array a of n complex values where n is a power of 2,
output: Array A of size n

n \in a.length
for k = 0 to n - 1
    A[rev(k)] = a[k]
```

This method can be easily parallelized as it is an iterative approach.

Butterfly representation of above approach is:



Comparison:

For N = 131072

- For recursive code, time taken is 0.025 sec
- For iterative code, time taken is 0.021 sec
- For omp code,
 - o Threads = 4, static schedule, time taken is 0.017 sec
 - Threads = 4, guided schedule, time taken is 0.014 sec
 - Threads = 6, static schedule, time taken is 0.016 sec
 - Threads = 6, guided schedule, time taken is 0.013 sec
 - Threads = 2, static schedule, time taken is 0.019 sec
 - Threads = 2, guided schedule, time taken is 0.017 sec

For N = 262144

- For recursive code, time taken is 0.030
- For iterative code, time taken is 0.024
- For omp code,
 - Threads = 4, static schedule, time taken is 0.019
 - Threads = 4, guided schedule, time taken is 0.016
 - Threads = 6, static schedule, time taken is 0.017

- Threads = 6, guided schedule, time taken is 0.015
- Threads = 2, static schedule, time taken is 0.022
- Threads = 2, guided schedule, time taken is 0.020

Observation

- From the above experiment, we can observe that the time taken by recursive approach is more when compared to iterative approach
- Also, we can observe that the Parallelised iterative approach is faster than other two methods.
- We can also observe that if we increase the threads, speed of execution also increases.
- Also we can observe that, guided works better than static.