Homework 5

Name: Avinash PV

1) Stock used Is APPLE

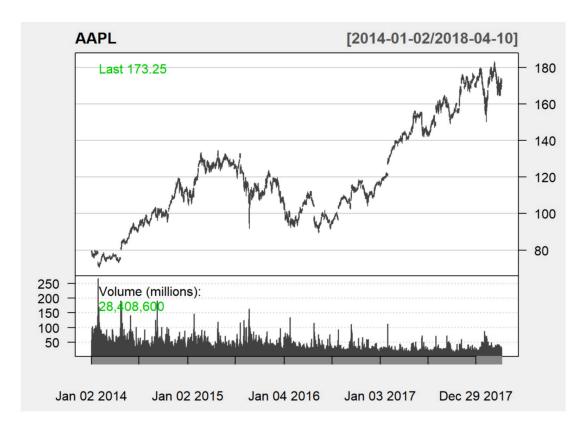
Fit model:

```
appleclose<-as.xts(data.frame(SPYClose = AAPL$"AAPL.Close"))
#daily log returns of the stock
appleclose.log<- log(dailyReturn(appleclose)+1)
#To find any serial correlations in the log returns, lets perform the Box test
Box.test(appleclose.log, lag=10, type = 'Ljung')</pre>
```

```
##
## Box-Ljung test
##
## data: appleclose.log
## X-squared = 9.3513, df = 10, p-value = 0.4991
```

The p value is high. Therefore we can not reject the null hypothesis (serial correlation) and say that there is no serial correlation in the log returns.

Fit the GARCH(1,1) model using a Skewed Student-t distribution for the innovations. Use the fitted model to produce 1-step to 5-step ahead volatility forecasts.



Predict:

```
##
    meanForecast meanError standardDeviation
                                   0.01703075
## 1
               0 0.01703075
## 2
               0 0.01696786
                                   0.01696786
## 3
                0 0.01690949
                                   0.01690949
                                   0.01685534
## 4
                0 0.01685534
                                   0.01680512
## 5
                0 0.01680512
```

Fit an IGARCH(1,1) model with Gaussian innovations to the return series. Write down the fitted model. Use the fitted IGARCH(1,1) model to predict the volatility for the next five trading days.

```
> beta=m2$par[2]
> step1=sqrt((1-beta)*last_return*last_return+beta*last_vol*last_
> step5=sqrt(5)*step1
> step1
   beta
0.01107464
> step5
   beta
0.02476364
The volatility for next five trading days is 0.025
3)
Fit model:
> m3 = garchFit(~aparch(1,1), data = daily_log_return, trace = F, delta = 2, include.delta = F, cond.dist = "std") > summary(m3)
Title:
 GARCH Modelling
 .arr:
garchFit(formula = ~aparch(1, 1), data = daily_log_return, delta = 2,
cond.dist = "std", include.delta = F, trace = F)
data ~ aparch(1, 1)
<environment: 0x000000002c23fa80>
[data = daily_log_return]
Conditional Distribution:
Coefficient(s):
mu omega alpha1 gamma1 beta1 shape 5.4177e-04 6.7811e-05 1.5677e-01 1.9605e-01 8.0251e-01 3.8652e+00
Std. Errors:
based on Hessian
Error Analysis:
    mu 5.418e-04
omega 6.781e-05
alphal 1.568e-01
gammal 1.961e-01
betal 8.025e-01
shape 3.865e+00
                      5.532e-02
4.958e-01
                                    14.506 < 2e-16 ***
7.796 6.44e-15 ***
Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
Log Likelihood:
2146.521 no
               normalized: 2.1316
Description:
  Sun Apr 22 17:17:41 2018 by user: SY
Standardised Residuals Tests:
                                      Statistic p-Value
  Jarque-Bera Test R Chi^2 3183.054
 Jarque-Bera lest R
Shapiro-Wilk Test R
Ljung-Box Test R
Ljung-Box Test R
Ljung-Box Test R
Ljung-Box Test R
                                      0.9259069 0
9.127148 0
                              w
Q(10)
                        R Q(15)
R Q(20)
R^2 Q(10)
R^2 Q(15)
R^2 Q(20)
R TR^2
                                      15.02346
17.14892
3.470468
5.201968
                                                  0.4497287
  Ljung-Box Test
                                      5.973236
4.66591
 Ljung-Box Test
LM Arch Test
Information Criterion Statistics:
AIC BIC SIC HQIC
-4.251283 -4.222000 -4.251354 -4.240157
Model:
r_t = 5.418 * 10^{-4} + a_t, \varepsilon_t \sim t_{3.87}
\sigma_t^2 = 6.781*10^{-5} + 0.1568(|a_{t-1}| - 0.1961*a_{t-1})^2 + 0.8025*\sigma_{t-1}^2
```

```
4)
2、
3、
GE=read.csv("./GE.csv",header=T)
> GE.prices=GE$Adj.Close[length(GE$Adj.Close):1]
> GE.returns=returns(GE.prices)[-1]
> model=Igarch(GE.returns,volcnt=F)
Maximized log-likehood: -4156.492
Coefficient(s):
      Estimate Std. Error t value Pr(>|t|)
     0.00047908 0.00033439 1.4327 0.15194
beta 0.93598715  0.00695296  134.6171  < 2e-16 ***
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
> last_return=GE.returns[length(GE.returns)]
> last_vol=model$volatility[length(GE.returns)]
> beta=model$par[2]
> step1=sqrt((1-beta)*last_return*last_return+beta*last_vol*last_
> VaR1=model$par[1]-step1*1.65> VaR1
        mu
-0.01671023
> VaR1=model$par[1]-step1*2.34
> VaR1
        mu
-0.02389849
> step5=sqrt(5)*step1
> VaR5=model$par[1]-step5*1.65
> VaR5
        mu
-0.03795738
> VaR5=model$par[1]-step5*2.34
> VaR5
         mu
-0.05403082
When p=0.05, one-day VaR=-0.0167, five-day VaR=-0.0380
When p=0.01, one-day VaR=-0.0239, five-day VaR=-0.0540
Yes, r<sub>t</sub><sup>0</sup> is serially correlated because miu is not zero.
```

```
\rho(1) = cov(r_t^0, r_{t-1}^0) / sqrt(var(r_t^0)*var(r_{t-1}^0))
= (-0.05^2*0.4)/(1.5^2+(2*0.4*0.05^2)/(1-0.4))
= -0.000443787
\rho (2) = ( - 0.05<sup>2</sup>*0.4<sup>2</sup>)/(1.5<sup>2</sup>+(2*0.4*0.05<sup>2</sup>)/(1-0.4))
= -0.0001775148
\rho (3) = ( - 0.05<sup>2</sup>*0.4<sup>3</sup>)/(1.5<sup>2</sup>+(2*0.4*0.05<sup>2</sup>)/(1-0.4))
= -7.100592e-05
5、
(a)
> m2=garchFit(~arma(0,0)+garch(1,1),data=GE.returns,trace=F)
> step1=sqrt(m2@fit$params$params[2]+m2@fit$params$params[3]*m2@h.
t[length(m2@h.t)]+m2@fit$params$params[5]*GE.returns[length(GE.re
turns)]^2)
> VaR1=m2@fit$params$params[1]-step1*1.65
> VaR1
          mu
-0.005540696
> VaR1=m2@fit$params$params[1]-step1*2.34
> VaR1
          mu
-0.008041823
> step5=step1*sqrt(5)
> VaR5=m2@fit$params$params[1]-step5*1.65
> VaR5
         mu
-0.01293357
> VaR5=m2@fit$params$params[1]-step5*2.34
> VaR5
         mu
-0.01852626
When p=0.05, one-day VaR=-0.00554, five-day VaR=-0.0129
When p=0.01, one-day VaR=-0.00804, five-day VaR=-0.0185
(b)
> m3=garchFit(~arma(0,0)+garch(1,1),data=GE.returns,trace=F,cond.
dist = "std")
> step1=sqrt(m2@fit$params$params[2]+m2@fit$params$params[3]*m2@h.
t[length(m2@h.t)]+m2@fit$params$params[5]*GE.returns[length(GE.re
turns)]^2)
> VaR1=m3@fit$params$params[1]-step1*1.65
> VaR1
          mu
-0.005636639
```

```
> VaR1=m3@fit$params$params[1]-step1*2.34
> VaR1
        mu
-0.008137766
> step5=step1*sqrt(5)
> VaR5=m3@fit$params$params[1]-step5*1.65
> VaR5
       mu
-0.01302951
> VaR5=m3@fit$params$params[1]-step5*2.34
> VaR5
       mu
-0.0186222
When p=0.05, one-day VaR=-0.00564, five-day VaR=-0.0130
When p=0.01, one-day VaR=-0.00814, five-day VaR=-0.0186
6、
(a)
> IBM=read.csv("./IBM.csv",header=T)
> SP500=IBM$sprtrn
> IBM=IBM$RET
> M=rep(0,length(IBM))
> S=rep(0,length(IBM))
> for (i in 1:length(IBM)){
+ if (IBM[i]>0)\{M[i]=1\}
+ if (SP500[i]>0){S[i]=1}
+ }
> Mt=M[3:length(M)]
> Mt_1=M[2:(length(M)-1)]
> Mt_2=M[1:(length(M)-2)]
> St_1=S[2:(length(M)-1)]
> St_2=S[1:(length(M)-2)]
> model=glm(Mt~Mt_1+Mt_2+St_1+St_2,family=binomial)
> summary(model)
call:
glm(formula = Mt \sim Mt_1 + Mt_2 + St_1 + St_2, family = binomial)
Deviance Residuals:
   Min
             1Q
                 Median
                              3Q
                                     Max
-1.4265 -1.2354 0.9898
                          1.0604
                                     1.2426
Coefficients:
          Estimate Std. Error z value Pr(>|z|)
(Intercept) 0.13546  0.15688  0.863  0.3879
```

```
0.43339
                     0.16902 2.564 0.0103 *
\mathsf{Mt}\_1
                     0.16970 -0.810 0.4179
Mt_2
          -0.13747
St_1
                     0.17043 -0.646
          -0.11002
                                     0.5186
St_2
          Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
(Dispersion parameter for binomial family taken to be 1)
   Null deviance: 1004.07 on 729 degrees of freedom
Residual deviance: 996.36 on 725 degrees of freedom
AIC: 1006.4
Number of Fisher Scoring iterations: 4
It is not useful. From the summary of this model, all coefficients are insignificant.
(b)
> train_M=M[1:(length(M)-50)]
> train_S=S[1:(length(M)-50)]
> test_M=M[(length(M)-49):length(M)]
> test_S=S[(length(M)-49):length(M)]
> train_Mt=train_M[3:length(train_M)]
> train_Mt_1=train_M[2:(length(train_M)-1)]
> train_Mt_2=train_M[1:(length(train_M)-2)]
> train_St_1=train_S[2:(length(train_M)-1)
> train_St_2=train_S[1:(length(train_M)-2)]
> model_new=glm(train_Mt~train_Mt_1+train_Mt_2+train_St_1+train_S
t_2, family=binomial)
> summary(model_new)
call:
glm(formula = train_Mt ~ train_Mt_1 + train_Mt_2 + train_St_1 +
   train_St_2, family = binomial)
Deviance Residuals:
            1Q Median
   Min
                            3Q
                                   Max
-1.3979 -1.2124 0.9959 1.0711
                                  1.2494
Coefficients:
          Estimate Std. Error z value Pr(>|z|)
(Intercept) 0.082010 0.161896 0.507
                                        0.6125
train_Mt_1 0.422840
                      0.175088 2.415
                                        0.0157 *
train_Mt_2 -0.183643  0.175633 -1.046  0.2957
train_St_1 -0.061563
                       0.177114 -0.348
                                         0.7281
train_St_2 -0.004386
                       0.177014 -0.025 0.9802
```

```
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
(Dispersion parameter for binomial family taken to be 1)
   Null deviance: 937.73 on 679 degrees of freedom
Residual deviance: 930.22 on 675 degrees of freedom
AIC: 940.22
Number of Fisher Scoring iterations: 4
> M_estimate=rep(0,50)
> count=0
> for (i in 1:50){
+ if (\exp(0.082+0.423*M[]\operatorname{ength}(M)-51+i]-0.184*S[]\operatorname{ength}(M)-51+i]
          -0.062*M[length(M)-52+i]-0.004*S[length(M)-51+i])
+
     /(1+\exp(0.082+0.423*M[length(M)-51+i]-0.184*S[length(M)-51+i]
+
i]
            -0.062*M[length(M)-52+i])-0.004*S[length(M)-51+i])>0.
+
5){
   M_estimate[i]=1
+
  }
+ if (M_estimate[i]!=M[length(M)-50+i]){
+
    count=count+1
   }
+
+ }
> count
[1] 15
There are 15 errors in prediction.
7、
(a)
> CAT=read.csv("./CAT.csv",header=T
> returns=c()
> start=CAT$PRICE[1]
> end=CAT$PRICE[1]
> time=CAT$min[1]
> count=35> for (i in 2:length(CAT$min)){
   if (((CAT$hour[i]==9) & (CAT$min[i]>=30))|((CAT$hour[i]==16) &
(CAT$min[i]<=30))|
       ((CAT$hour[i]>9) & (CAT$hour[i]<16))){
+ if (CAT$min[i-1]>CAT$min[i]){
     returns=c(returns,log(end/start))
     start=CAT$PRICE[i]
+
     end=CAT$PRICE[i]
```

```
while (count<temp){</pre>
+
       count=count+5
       returns=c(returns,0)
     }
     count=count%%60
+
+
   else{
     if (CAT$min[i]<count){</pre>
+
       end=CAT$PRICE[i]
+
     }else{
       returns=c(returns,log(end/start))
       start=CAT$PRICE[i]
       end=CAT$PRICE[i]
       count=count+5
     }
   }
   }
+
+ }
> Box.test (returns, lag = 10, type = "Ljung")
       Box-Ljung test
data: returns
X-squared = 19.107, df = 10, p-value = 0.03892
According to the box-test, the p value is smaller than 0.05, which means there exists se
rial correlation.
(b)
> length(returns)
[1] 453
> returns
[1] 1.110086e-04 5.704917e-03 -3.448871e-04 1.378597e-03 1.5483
87e-03 1.545994e-03
 [7] 0.000000e+00 2.228891e-03 2.053038e-03 -1.883499e-03 -3.42
4658e-04 1.712475e-04
 [13] 1.209886e-03 -5.491502e-04 0.000000e+00 1.710279e-03 5.12
4263e-04 1.364955e-03
 [19] 1.022147e-03 0.000000e+00 2.890421e-03 0.000000e+00 -9.78
5717e-04 4.248720e-05
 [25] 5.946061e-04 1.154578e-03 4.548031e-04 3.978504e-03 -3.04
5688e-03 -1.017467e-03
 [31] 1.186944e-03 -1.694772e-04 0.000000e+00 3.388682e-04 0.00
0000e+00 -8.472423e-04
```

temp=CAT\$min[i]+60

- [37] -1.866147e-03 3.395009e-04 -6.604476e-04 -5.096407e-04 3.05 8052e-04 0.000000e+00
- [43] 0.000000e+00 -1.019888e-03 8.669857e-04 0.000000e+00 -5.09 9873e-04 6.800408e-04
- [49] -8.501522e-04 -3.402518e-04 1.182078e-03 4.249352e-04 -6.80 0408e-04 -1.700825e-04
- [55] 1.274914e-03 1.698514e-04 -2.209946e-03 -1.701693e-04 0.00 0000e+00 -8.937122e-04
- [61] 4.921289e-04 -4.256859e-05 8.509915e-04 -1.701693e-04 1.70 1693e-04 1.701693e-04
- [67] -1.701693e-04 8.508828e-05 -6.805036e-04 -8.512812e-04 -1.1 75959e-03 0.000000e+00
- [73] 4.944464e-05 8.520065e-04 -1.703432e-04 -6.817795e-04 -1.02 3367e-03 -1.706630e-04
- [79] -5.120765e-04 8.536429e-05 -3.415301e-04 3.414717e-04 -1.53 7279e-03 7.178125e-04
- [85] 0.000000e+00 3.057683e-04 9.799621e-04 0.000000e+00 0.00 0000e+00 0.000000e+00
- [91] 0.000000e+00 -2.051633e-03 -1.397002e-03 -3.428767e-04 -4.3 56230e-04 4.622109e-03
- [97] -6.834102e-04 0.000000e+00 1.709548e-04 -8.546643e-05 2.90 0778e-03 1.191794e-03
- [103] 3.905260e-03 3.214621e-03 -3.378949e-04 6.756757e-04 6.75 3335e-04 5.906999e-05
- [109] 1.687762e-06 1.180737e-03 0.000000e+00 -1.685914e-04 -2.53 2288e-03 -1.607105e-03
- [115] 5.500434e-04 -1.015572e-03 1.015744e-03 -2.032521e-03 3.39 0405e-04 3.389256e-04
- [121] -3.373450e-04 -5.086901e-04 -3.901688e-05 0.000000e+00 1.0 45322e-03 1.779134e-03
- [127] 7.613891e-04 -1.353867e-03 4.215520e-04 -2.522326e-04 -1.7 78147e-04 8.469911e-05
- [133] 6.773921e-04 1.226657e-03 5.072280e-04 1.098483e-03 0.00 0000e+00 3.394694e-04
- [139] -3.377808e-04 1.687479e-03 -8.429216e-05 -1.686198e-04 1.6 83518e-03 -6.737410e-04
- [145] -3.370408e-04 1.515535e-03 -1.768645e-03 -1.096538e-03 -7.1 76478e-04 0.000000e+00
- [151] 2.348447e-04 -3.045688e-03 -2.541834e-04 5.421524e-04 -1.1 86340e-03 -6.803524e-04
- [157] -1.697218e-06 9.330337e-04 -5.105593e-04 1.657658e-03 5.91 0491e-04 1.522457e-03
- [163] 0.000000e+00 -1.690188e-04 -7.083800e-04 9.873071e-04 6.75 7899e-04 -1.689332e-04

```
[169] -1.098669e-03 2.027713e-03 8.441312e-05 4.219587e-04 3.37 4958e-04 -1.154902e-03
```

- [175] -1.689332e-04 0.000000e+00 -1.521684e-03 0.000000e+00 0.00 0000e+00 0.000000e+00
- [181] 5.834865e-03 0.000000e+00 3.656669e-03 -1.196787e-03 0.00 0000e+00 2.792051e-03
- [187] 8.390073e-04 -3.361910e-04 0.000000e+00 3.860685e-03 1.17 2235e-03 1.630674e-03
- [193] 1.670983e-04 -1.504640e-03 1.638495e-03 -1.670568e-03 0.00 0000e+00 1.354730e-03
- [199] -2.342313e-03 1.004689e-03 1.337793e-03 0.000000e+00 -1.00 3009e-03 -6.525067e-04
- [205] -6.713550e-04 9.374425e-04 2.506058e-03 -2.171916e-03 -4.9 86188e-04 1.170862e-03
- [211] 2.089733e-04 5.029664e-04 -4.528634e-04 -8.361904e-04 0.00 0000e+00 5.614673e-04
- [217] -1.479544e-03 -3.682013e-03 -8.388558e-04 -3.458134e-04 -1.3 40949e-03 -1.681379e-04
- [223] -3.346228e-04 7.400207e-05 1.176767e-03 1.679402e-04 5.87 6674e-04 0.000000e+00
- [229] 1.844555e-03 0.000000e+00 3.451182e-04 0.000000e+00 0.00 0000e+00 -5.027231e-04
- [235] 9.214660e-04 -1.674621e-04 8.371704e-04 1.673500e-04 -1.38 9971e-03 1.675744e-04
- [241] 0.000000e+00 0.000000e+00 -3.350645e-04 -5.028074e-04 6.37 1360e-05 5.866823e-04
- [247] -8.381528e-04 1.676586e-04 8.381878e-05 -5.029760e-04 -1.6 93638e-04 3.354016e-04
- [253] -1.492426e-04 0.000000e+00 -1.677149e-04 -1.397964e-03 -1.6 79402e-04 -6.720430e-04
- [259] -1.682086e-03 1.177559e-03 -5.045833e-04 5.044985e-04 -6.7 27212e-04 -2.610198e-03
- [265] 1.347709e-03 1.683360e-04 0.000000e+00 4.293078e-03 0.00 0000e+00 3.033369e-03
- [271] 0.000000e+00 0.000000e+00 0.000000e+00 1.684920e-03 -3.36 5870e-04 2.856425e-03
- [277] -2.856425e-03 -5.909684e-03 -5.946836e-03 0.000000e+00 1.9 58031e-03 1.189970e-03
- [283] 2.036661e-03 -1.357082e-03 1.696066e-03 1.694342e-06 0.00 0000e+00 1.354555e-03
- [289] 3.125398e-03 2.358492e-03 4.036463e-04 -3.364172e-04 0.00 0000e+00 1.682510e-04
- [295] -2.168880e-03 1.852632e-03 -3.365870e-04 -1.178948e-03 -8.4 29571e-04 -5.058596e-04

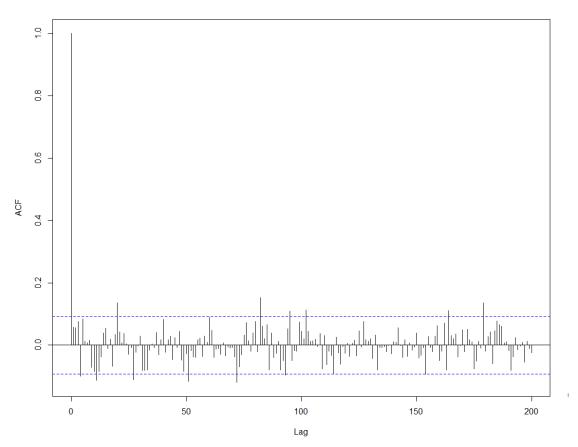
```
[301] -5.061156e-04 1.854819e-03 -8.846762e-04 1.179345e-03 1.64
8750e-03 0.000000e+00
[307] -3.363040e-04 9.244087e-04 0.000000e+00 3.854861e-03 -9.20
```

- 3096e-04 1.171058e-03
- [313] 1.002506e-03 -1.420633e-03 -6.691201e-04 -1.423130e-03 1.8 42716e-04 -1.021895e-04
- [319] 0.000000e+00 -1.005868e-03 -1.845042e-03 1.225933e-03 1.67 7993e-04 -2.015452e-03
- [325] 3.361345e-04 4.200092e-04 -4.199052e-05 1.343184e-03 3.35 5142e-04 0.000000e+00
- [331] 7.546505e-05 0.000000e+00 1.844539e-04 -1.760704e-04 -7.80 0280e-04 1.006374e-03
- [337] -1.341067e-04 -4.191993e-04 1.592023e-03 1.673081e-03 -1.6 71821e-04 7.420679e-04
- [343] 0.000000e+00 -9.193866e-04 0.000000e+00 -4.609655e-03 -1.3 27420e-04 1.680249e-04
- [349] -4.201151e-04 1.679262e-03 -8.389614e-05 1.676446e-03 8.37 1704e-04 -6.696803e-04
- [355] -1.706362e-03 -6.712536e-04 1.176077e-03 0.000000e+00 5.02 8916e-04 0.000000e+00
- [361] -4.030232e-03 0.000000e+00 0.000000e+00 0.000000e+00 3.70 1216e-03 -1.344086e-03
- [367] -1.766413e-03 3.363043e-03 3.357958e-04 1.342282e-03 0.00 0000e+00 -6.708033e-04
- [373] -5.033135e-04 -1.679544e-03 8.402656e-04 6.883873e-04 1.678556e-04 1.442300e-03
- [379] -5.027231e-04 -5.028916e-04 -1.174398e-03 1.719258e-03 1.5 07159e-03 0.000000e+00
- [385] -1.338778e-04 2.674245e-03 0.000000e+00 1.034385e-03 -3.33 5557e-04 1.667918e-04
- [391] -1.667639e-04 -3.319984e-04 4.437157e-04 -1.667639e-04 0.0 00000e+00 -5.005423e-04
- [397] 0.000000e+00 0.000000e+00 -5.007093e-04 1.669310e-04 -4.67 2398e-05 1.652064e-04
- [403] 2.318910e-04 -3.335001e-04 1.667639e-04 5.001250e-04 -4.16 8230e-04 3.334445e-04
- [409] -3.335001e-04 0.000000e+00 -3.336113e-04 1.095496e-03 1.66 7361e-04 -1.167932e-03
- [415] 6.674454e-04 -1.001335e-03 1.668614e-03 -1.667361e-04 -1.6 68892e-03 1.001502e-03
- [421] -1.335559e-03 -1.001002e-03 0.000000e+00 1.671821e-04 -6.4 22393e-04 6.873088e-04
- [427] -1.605432e-04 3.696824e-04 -1.171450e-03 6.863016e-04 -8.3 65751e-05 -7.198038e-04

[433] -5.024705e-04 5.444000e-04 1.171450e-03 0.000000e+00 -7.52 8546e-04 6.692321e-04 [439] 1.504137e-03 -1.670425e-04 5.009602e-04 1.871370e-03 -1.08 3559e-03 2.249158e-03 [445] 1.081216e-03 1.412136e-03 1.327250e-03 3.315650e-04 0.00 0000e+00 0.00000e+00 -1.657138e-04 0.00000e+00

(c)

Series returns



There is no auto-correlation between intrday 5-minute log return series.