Logistic Regression - Supervised Learning - Classification

1. Data preprocessing

```
In [1]: import pandas as pd
       import numpy as np
       import matplotlib.pyplot as plt
       import warnings
       warnings.filterwarnings("ignore")
In [2]: df = pd.read_csv('data.csv')
       df.head()
Out[2]:
          -6 592 0
        0 -5 807 0
       1 -5 -344 0
        2 -5 -126 0
        3 -5 243 0
        4 -5 185 0
In [3]: df.shape
Out[3]: (199, 3)
In [4]: df.info()
```

```
<class 'pandas.core.frame.DataFrame'>
       RangeIndex: 199 entries, 0 to 198
       Data columns (total 3 columns):
            Column Non-Null Count Dtype
            -6
                    199 non-null
                                     int64
            592
                    199 non-null
                                    int64
            0
                    199 non-null
                                     int64
       dtypes: int64(3)
       memory usage: 4.8 KB
In [5]: df.dtypes
Out[5]: -6
                int64
         592
                int64
                int64
         0
         dtype: object
In [6]: df.describe()
Out[6]:
                       -6
                                  592
                                               0
         count 199.000000
                           199.000000 199.000000
                 0.964824
                            325.477387
                                         0.582915
         mean
           std
                 3.636761
                            286.265167
                                         0.494321
                 -5.000000
                           -445.000000
                                         0.000000
          min
          25%
                 -2.000000
                           152.500000
                                         0.000000
                 1.000000
          50%
                            349.000000
                                         1.000000
                 4.000000
          75%
                           538.000000
                                         1.000000
                 8.000000 1056.000000
                                         1.000000
          max
```

In [7]: df.isnull().sum()

```
Out[7]: -6
         592
         0
         dtype: int64
 In [8]: df[df.duplicated()]
 Out[8]:
             -6 592 0
          40 -3 421 1
         169 5 454 1
 In [9]: df.shape
Out[9]: (199, 3)
In [10]: df.drop_duplicates(inplace=True)
In [11]: df.shape
Out[11]: (197, 3)
In [12]: df.rename(columns={'-6':'Feature1','592':'Feature2','0':'Label'},inplace=True)
In [13]: df.head()
Out[13]:
           Feature1 Feature2 Label
         0
                 -5
                        807
                                0
                 -5
                        -344
                                0
         2
                 -5
                        -126
                                0
         3
                 -5
                        243
                                0
                 -5
         4
                        185
                                0
```

```
In [42]: df.to_csv('updated_df.csv')
In [15]: df.nunique()
Out[15]: Feature1
                      14
          Feature2
                     180
          Label
          dtype: int64
         Observations ?
           • 3 Columns available only

    No Null Values

           • 2 Duplicate values found
           • Column Names changed accordingly
In [16]: for i in df.columns:
             print(f'{i} Colum Unique Values :',end='')
             print(df[i].unique())
             print('*'*20)
```

```
Feature1 Colum Unique Values : [-5 -4 -3 -2 -1 0 1 2 3 4 5 6 7 8]
******
Feature2 Colum Unique Values : [ 807 -344 -126 243 185 -89
                                                      -7 -90 161
                                                                   35 611 -45 558 -110
           91 674 697
                       12 426
                                 7 -65 634 342
                                                -39
                                                     314 679
     272 358 -146 326 274 421 -237 465 707 104
                                                 622
 627
                                                     408 454
     683 -181 300
                  389 458 157
                               831
                                     33 719 671
                                                 306
                                                     743 515
 166
     202 356
             333
                  -68 355 416
                               240 270 -445 292
                                                 267
                                                     203 417
     263 691 778
                  135 761 212 1056
                                   490
                                         66 575
                                                623 -140 584
     630
         164 646
                   96
                      388 -206
                               331
                                    95
                                         28 -128
                                                      -4 826
      64 607 148
 404
                  688 649 -187 -185 395
                                        200 768 -338
                                                     282 668
 222 182 285 735
                  452 619 400
                               399 414
                                        579 319
                                                     352 658
                                                  57
     382 -298
             378
                  276 740 564
                               269 -226
                                        572 245
                                                650
                                                     537 654
     428 364 466
                               504 178 193 485
 596
                   65 100
                           571
                                                250
                                                     517 442
                                       219 336 748
-281 339 653 110
                  -49
                       641 460
                               206 -322
                                                    249 287
 528 469 273
             73
                  481 390
                            80 375 959 539 727
                                                 75]
Label Colum Unique Values :[0 1]
******
```

2. Exploratory Data Analysis

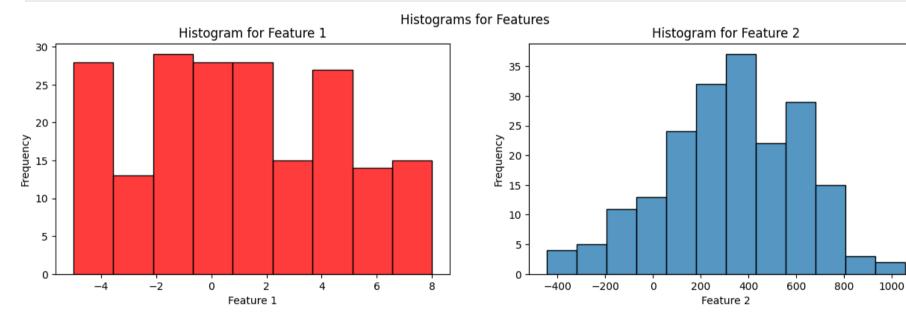
```
In [17]: import seaborn as sns
In [18]: df.head()
             Feature1 Feature2 Label
Out[18]:
                           807
          0
                   -5
                                   0
          1
                   -5
                          -344
                                    0
          2
                          -126
                   -5
                                    0
          3
                   -5
                           243
                                    0
          4
                  -5
                           185
                                    0
```

```
In [19]: plt.figure(figsize=(15,4))
plt.suptitle('Histograms for Features')
```

```
plt.subplot(1,2,1)
sns.histplot(data = df,x = df['Feature1'],color='r')
plt.xlabel('Feature 1')
plt.ylabel('Frequency')
plt.title(f'Histogram for Feature 1')

plt.subplot(1,2,2)
sns.histplot(data = df,x = df['Feature2'])
plt.xlabel('Feature 2')
plt.ylabel('Frequency')
plt.title(f'Histogram for Feature 2')

plt.show()
```



• Observations - Feature 2Data is distributed normally

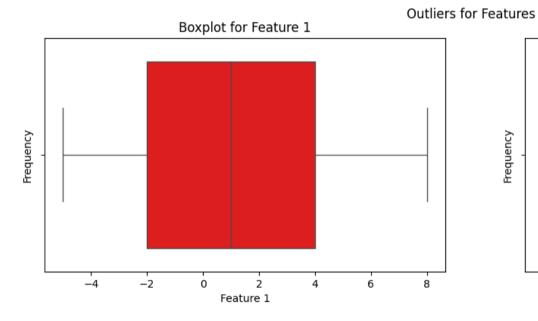
```
In [20]: plt.figure(figsize=(15,4))
    plt.suptitle('Outliers for Features')

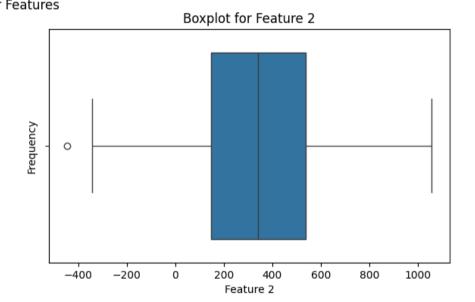
plt.subplot(1,2,1)
    sns.boxplot(data = df,x = df['Feature1'],color='r')
```

```
plt.xlabel('Feature 1')
plt.ylabel('Frequency')
plt.title(f'Boxplot for Feature 1')

plt.subplot(1,2,2)
sns.boxplot(data = df,x = df['Feature2'],orient='v')
plt.xlabel('Feature 2')
plt.ylabel('Frequency')
plt.title(f'Boxplot for Feature 2')

plt.show()
```





```
In [21]: np.percentile(df['Feature1'],0.25),np.percentile(df['Feature1'],0.75),df['Feature1'].median()
Out[21]: (-5.0, -5.0, 1.0)
In [22]: np.percentile(df['Feature2'],0.25),np.percentile(df['Feature2'],0.75),df['Feature2'].median()
Out[22]: (-395.51, -341.18, 342.0)
```

```
In [23]: outlier = df[df['Feature2']<np.percentile(df['Feature2'],0.25)]
outlier</pre>
```

```
Out[23]: Feature1 Feature2 Label

68 -1 -445 0
```

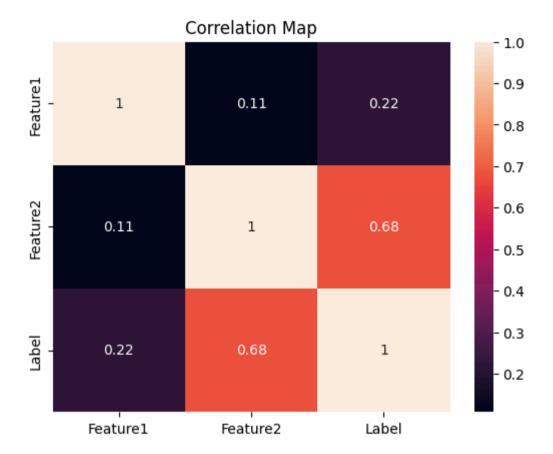
• Observations - Feature2 has outliers

```
In [24]: sns.scatterplot(data=df,x='Feature1',y='Feature2',hue='Label')
    plt.xlabel('Feature1')
    plt.ylabel('Feature2')
    plt.title('Scatterplot for Features')
    plt.grid()
    plt.show()
```

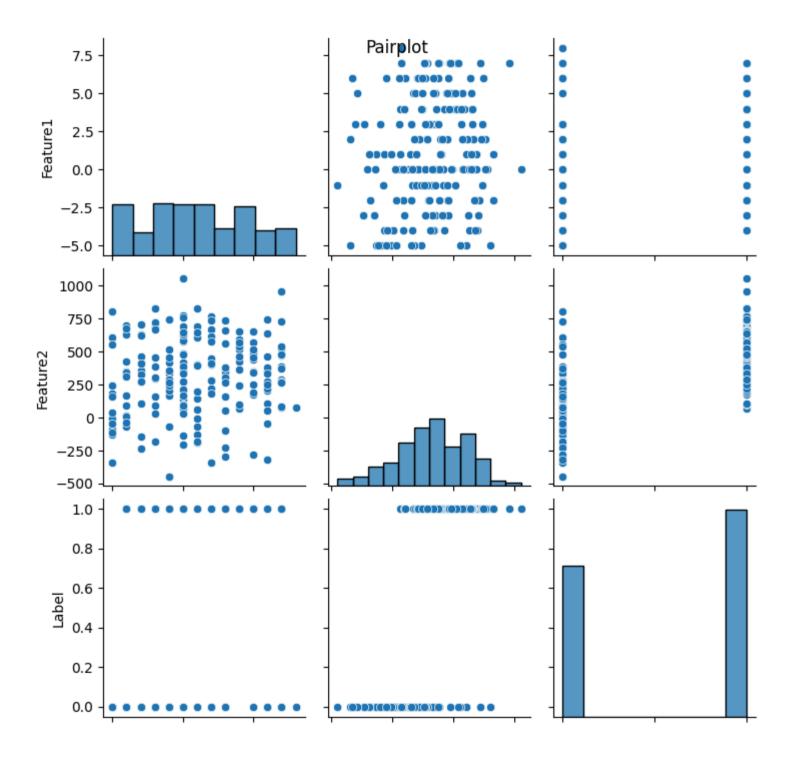
Scatterplot for Features 1000 800 600 400 Feature 2 200 0 -200 Label -400-2 4 2 6 -4 0

Feature1

```
In [25]: sns.heatmap(df.corr(),annot=True,cmap='rocket')
    plt.title('Correlation Map')
    plt.show()
```



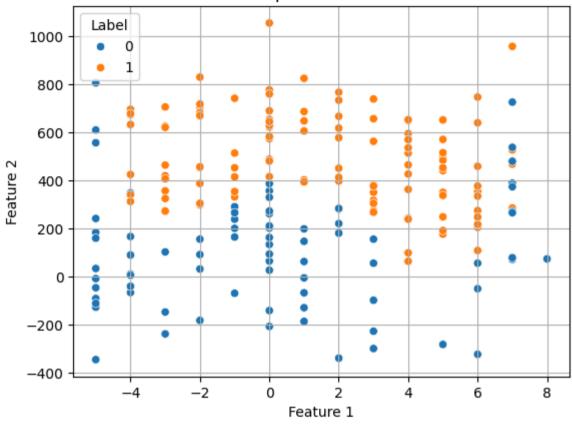
```
In [26]: sns.pairplot(df)
  plt.suptitle('Pairplot')
  plt.show()
```



-5 0 5 -500 0 500 1000 0.0 0.5 1.0 Feature1 Feature2 Label

```
In [27]: df.shape
Out[27]: (197, 3)
In [28]: df.drop(outlier.index,inplace=True)
In [29]: df.shape
Out[29]: (196, 3)
In [30]: sns.scatterplot(data = df, x='Feature1',y='Feature2', hue="Label")
plt.grid()
plt.xlabel('Feature 1')
plt.ylabel('Feature 2')
plt.title('Scatterplot for 2 Features')
plt.show()
```

Scatterplot for 2 Features



In [32]: df.head()

```
0
                  -5
                          807
                                  0
                  -5
                         -344
                                  0
         2
                  -5
                         -126
                                  0
         3
                  -5
                          243
                                  0
          4
                  -5
                          185
                                  0
In [33]: df.isnull().sum()
Out[33]: Feature1
          Feature2
          Label
          dtype: int64
In [34]: df.shape
Out[34]: (196, 3)
In [ ]: # Libraries
         from sklearn.model selection import train test split
         from sklearn.linear model import LogisticRegression
         from sklearn.preprocessing import StandardScaler
         from sklearn.metrics import accuracy score
```

A) Logistic Regression

Feature1 Feature2 Label

Out[32]:

```
In [75]: # Splitting
X_train, X_test, y_train, y_test = train_test_split(df[['Feature1', 'Feature2']], df['Label'], test_size=0.2, random_state=42)
# Standarization
scaler = StandardScaler()
X_train_scaled = scaler.fit_transform(X_train)
X_test_scaled = scaler.transform(X_test)
```

```
# Initializing model
model sklearn = LogisticRegression()
# Training
model sklearn.fit(X train scaled, y train)
# Decision boundary + plotting
def plot decision boundary sklearn scaled(X, y, model, title):
    h = .02 # Step size in the mesh
    x \min, x \max = X[:, 0].\min() - 1, X[:, 0].\max() + 1
   y min, y max = X[:, 1].min() - 1, X[:, 1].max() + 1
   xx, yy = np.meshgrid(np.arange(x min, x max, h), np.arange(y min, y max, h))
    Z = model.predict(np.c [xx.ravel(), yy.ravel()])
    Z = Z.reshape(xx.shape)
    plt.contourf(xx, yy, Z, cmap=plt.cm.Paired, alpha=0.8)
    plt.scatter(X[:, 0], X[:, 1], c=y, edgecolors='k', cmap=plt.cm.Paired)
    plt.title(title)
    plt.xlabel('Feature1')
    plt.ylabel('Feature2 ')
    plt.show()
# For Trained Data
plot decision boundary sklearn scaled(X train scaled, y train, model sklearn, 'Decision Boundary')
# Evaluation
X test scaled = scaler.transform(X test)
y pred sklearn = model sklearn.predict(X test scaled)
accuracy sklearn = accuracy score(y test, y pred sklearn)
# Metric
print(f"Model Accuracy : {accuracy sklearn:.2%}")
```


0

Feature1

Model Accuracy : 85.00%

-2

-1

-3 ·

B) Implementation of Logistic Regression from Scratch without scikit-learn

1

2

```
In [58]: def sigmoid(z):
    return 1 / (1 + np.exp(-z))

def compute_cost(X, y, theta):
    m = len(y)
    h = sigmoid(X @ theta)
    cost = (-1/m) * np.sum(y * np.log(h) + (1 - y) * np.log(1 - h))
    return cost
```

```
def gradient descent(X, y, theta, alpha, iterations):
    m = len(y)
    costs = []
    for i in range(iterations):
        h = sigmoid(X @ theta)
        gradient = (1/m) * X.T @ (h - y)
        theta -= alpha * gradient
        cost = compute cost(X, y, theta)
        costs.append(cost)
    return theta, costs
X train scaled = X train.copy()
X test scaled = X test.copy()
# Scaling
scaler = StandardScaler()
X train scaled[['Feature1', 'Feature2']] = scaler.fit transform(X train[['Feature1', 'Feature2']])
X test scaled[['Feature1', 'Feature2']] = scaler.transform(X test[['Feature1', 'Feature2']])
# Bias
X train b = np.c [np.ones((X train scaled.shape[0], 1)), X train scaled]
X test b = np.c [np.ones((X test scaled.shape[0], 1)), X test scaled]
initial theta = np.zeros(X train b.shape[1])
# Parameters
learning rate = 0.01
num iterations = 1000
# Training
trained theta, costs = gradient descent(X train b, y train, initial theta, learning rate, num iterations)
# Cost Function For Every Iterations
plt.plot(range(1, num iterations + 1), costs)
plt.xlabel('Iterations')
plt.ylabel('Cost')
plt.title('Cost Function during Training - (without scikit-learn)')
plt.show()
```

```
# Decision Boundary
x_values = np.linspace(X_test_scaled['Feature1'].min(), X_test_scaled['Feature1'].max(), 100)
plt.scatter(X_test_scaled['Feature1'], X_test_scaled['Feature2'], c=y_test, cmap='viridis', edgecolors='k', marker='o')
y_values = -(trained_theta[0] + trained_theta[1] * x_values) / trained_theta[2]
plt.plot(x_values, y_values, label='Decision Boundary', color='red')
plt.xlabel('Feature1')
plt.ylabel('Feature2')
plt.title('Decision Boundary - (without scikit-learn)')
plt.legend()
plt.show()

# Prediction & Accuracy
predictions = sigmoid(X_test_b @ trained_theta)
predictions = (predictions >= 0.5).astype(int)
accuracy = np.mean(predictions == y_test)
print(f"Model Accuracy: {accuracy*100:.2f}%")
```

Cost Function during Training - (without scikit-learn) 0.70 0.65 0.60 o.55 0.50 -0.45 -0.40 200 800 400 600 1000 0

Iterations

Decision Boundary - (without scikit-learn) 1.5 **Decision Boundary** 0 0 1.0 0 0 0.5 0.0 Feature 2 -0.5 -1.0-1.5 -2.0 -2.5

Model Accuracy: 92.50%

-1.5

-1.0

C) Implementation of Logistic Regression + Feature Engineering

0.5

0.0

Feature1

-0.5

```
In [61]: df = pd.read_csv('updated_df.csv')
In [62]: df.head()
```

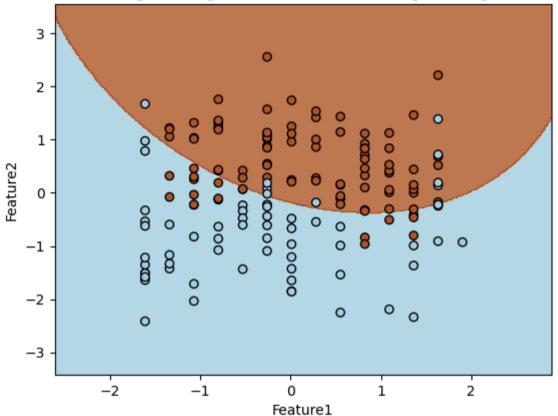
1.0

1.5

```
Out[62]:
            Unnamed: 0 Feature1 Feature2 Label
         0
                      0
                              -5
                                      807
                                              0
         1
                      1
                              -5
                                     -344
                                               0
         2
                      2
                              -5
                                     -126
                                              0
         3
                      3
                              -5
                                      243
                                               0
                              -5
          4
                      4
                                      185
                                              0
In [63]: df.drop(columns='Unnamed: 0',inplace=True)
In [64]: df.shape
Out[64]: (196, 3)
In [65]: df.isnull().sum()
Out[65]: Feature1
                     0
          Feature2
                      0
          Label
                      0
         dtype: int64
        from sklearn.preprocessing import PolynomialFeatures # for Increasing Degree
In [73]:
         poly = PolynomialFeatures(degree=2)
         X poly = poly.fit transform(df[['Feature1', 'Feature2']])
         poly feature names = [f'poly {i}' for i in range(X poly.shape[1])]
         df poly = pd.DataFrame(X poly, columns=poly feature names)
         df poly['Label'] = df['Label']
         # Splitting
         X_train_poly, X_test_poly, y_train_poly, y_test_poly = train_test_split(
             df poly.iloc[:, :-1], df poly['Label'], test size=0.2, random state=42)
         # Standardization
         scaler poly = StandardScaler()
         X train scaled poly = scaler poly.fit transform(X train poly)
```

```
X test scaled poly = scaler poly.transform(X test poly)
# Initializing model
model poly sklearn = LogisticRegression()
# Trainina
model poly sklearn.fit(X_train_scaled_poly, y_train_poly)
# Decision boundary
def plot decision boundary_sklearn_poly(X, y, model, title):
    h = .02
    x \min, x \max = X[:, 1].\min() - 1, X[:, 1].\max() + 1
   y min, y max = X[:, 2].min() - 1, X[:, 2].max() + 1
    xx, yy = np.meshgrid(np.arange(x min, x max, h), np.arange(y min, y max, h))
    meshgrid poly = poly.transform(np.c [xx.ravel(), yy.ravel()])
    Z = model.predict(meshgrid poly)
    Z = Z.reshape(xx.shape)
    plt.contourf(xx, yy, Z, cmap=plt.cm.Paired, alpha=0.8)
    plt.scatter(X[:, 1], X[:, 2], c=y, edgecolors='k', cmap=plt.cm.Paired)
    plt.title(title)
    plt.xlabel('Feature1')
    plt.ylabel('Feature2')
    plt.show()
plot decision boundary sklearn poly(X train scaled poly, y train poly, model poly sklearn, 'Logistic Regression with Feature E
# Evaluation
y pred poly sklearn = model poly sklearn.predict(X test scaled poly)
accuracy poly sklearn = accuracy score(y test poly, y pred poly sklearn)
print(f"Model Accuracy with Feature Engineering: {accuracy poly sklearn:.2%}")
```

Logistic Regression with Feature Engineering



Model Accuracy with Feature Engineering: 82.50%

```
In [72]: X_train_poly.shape, X_test_poly.shape, y_train_poly.shape, y_test_poly.shape
```

Out[72]: ((156, 6), (40, 6), (156,), (40,))

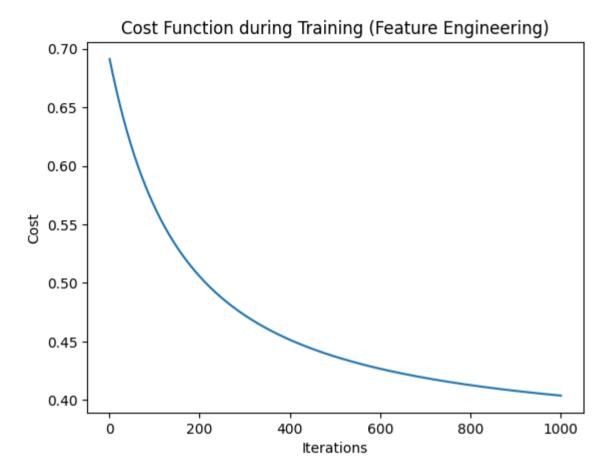
D)Implementation of Logistic Regression from Scratch with Feature Engineering

```
In [71]: def sigmoid(z):
    return 1 / (1 + np.exp(-z))

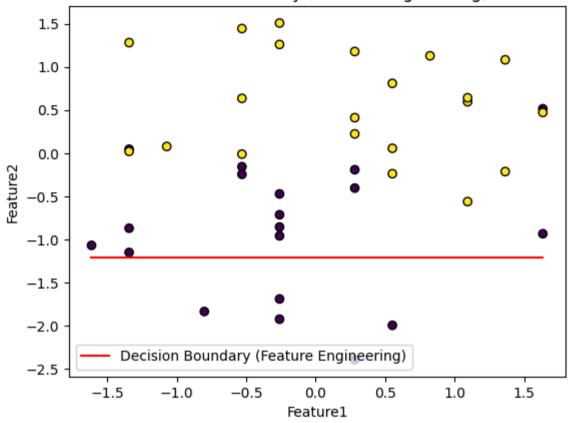
def compute_cost(X, y, theta):
```

```
m = len(y)
    h = sigmoid(X @ theta)
    cost = (-1/m) * np.sum(y * np.log(h) + (1 - y) * np.log(1 - h))
    return cost
def gradient descent(X, y, theta, alpha, iterations):
    m = len(v)
    costs = []
   for i in range(iterations):
        h = sigmoid(X @ theta)
        gradient = (1/m) * X.T @ (h - y)
        theta -= alpha * gradient
        cost = compute cost(X, y, theta)
        costs.append(cost)
    return theta, costs
X train poly scaled = X train poly.copy()
X_test_poly_scaled = X_test_poly.copy()
# Scaling
scaler poly = StandardScaler()
X train poly scaled = scaler poly.fit transform(X train poly)
X test poly scaled = scaler poly.transform(X test poly)
# Bias
X train poly b = np.c [np.ones((X train poly scaled.shape[0], 1)), X train poly scaled]
X test poly b = np \cdot c [np \cdot ones((X test poly scaled \cdot shape[0], 1)), X test poly scaled]
initial theta poly = np.zeros(X train poly b.shape[1])
# Parameters
learning rate poly = 0.01
num iterations poly = 1000
# Training
trained theta poly, costs poly = gradient descent(X train poly b, y train poly, initial theta poly, learning rate poly, num it
# Cost Function For Every Iterations
plt.plot(range(1, num iterations poly + 1), costs poly)
```

```
plt.xlabel('Iterations')
plt.ylabel('Cost')
plt.title('Cost Function during Training (Feature Engineering)')
plt.show()
x values poly = np.linspace(X test poly scaled[:, 1].min(), X test poly scaled[:, 1].max(), 100)
plt.scatter(X test poly scaled[:, 1], X test poly scaled[:, 2], c=y test poly, cmap='viridis', edgecolors='k', marker='o')
y values poly = -(trained theta poly[0] + trained theta poly[1] * x values poly) / trained theta poly[2]
plt.plot(x values poly, y values poly, label='Decision Boundary (Feature Engineering)', color='red')
plt.xlabel('Feature1')
plt.ylabel('Feature2')
plt.title('Decision Boundary (Feature Engineering)')
plt.legend()
plt.show()
# Evalution of Accuracy
predictions poly = sigmoid(X test poly b @ trained theta poly)
predictions_poly = (predictions_poly >= 0.5).astype(int)
accuracy_poly = accuracy_score(y_test_poly, predictions_poly)
print(f"Model Accuracy : {accuracy poly*100:.2f}%")
```



Decision Boundary (Feature Engineering)



Model Accuracy : 87.50%

In []: