

6th DAY LIVE SESSION

- ① CHI SQUARE ✓
- ② Covariance ✓
- ③ Pearson Correlation Coefficient ✓
- ④ Spearman Rank Correlation ✓
- ⑤ Practical Implementation
 - Z-test, t-test, chi square test
- ⑥ F Test (ANOVA)

CHI SQUARE TEST

- ① Chi Square Test claims about population proportions

It is a non parametric test that is performed on Categorical (nominal or ordinal) data.

- Q) In the 2000 Indian Census, the age of the individual in a small town were found to be the following:

Less than 18	18-35	>35
20%	30%	50%

In 2010, age of $n=500$ individuals were sampled. Below are the results

<18	18-35	>35
121	288	91

Using $\alpha=0.05$, would you conclude the population distribution of ages has changed in the last 10 years?

Ans)

<18	$18-35$	>35
20%	30%	50%

{ Population } 2000

Expected

<18	$18-35$	>35
121	288	91

| n=500 |

Observed

<18	$18-35$	>35
100	500×0.3	500×0.5

Expected

<18	$18-35$	>35
121	288	91

Observation

<18	$18-35$	>35
100	150	250

Expected

{ Chi Square table }

- ① H_0 = The data meets the distribution 2000 census $df = 2$, $\alpha = 0.05$
- ② H_1 = The data does not meet " " "
- ③ Degrees of freedom = $n - 1 = 3 - 1 = 2$
- ④ Decision Boundary



If χ^2 is greater than 5.99 reject H_0

5) Calculate Test Statistics

$$\chi^2 = \sum \frac{(f_0 - f_e)^2}{f_e}$$

$$= \frac{(121 - 100)^2}{100} + \frac{(288 - 150)^2}{150} + \frac{(91 - 250)^2}{250} \\ \approx 132.94$$

$$\chi^2 = 132.94 > 5.99 \quad \left\{ \begin{array}{l} \text{Reject the Null} \\ \text{Hypothesis} \end{array} \right.$$

$$0.11 > 0.05 \quad \boxed{0.11 \times 0.05} \quad \alpha = 0.05 \quad 0.002 < 0.05 \quad \left\{ \begin{array}{l} \text{Domain} \\ \text{Reject the null hypothesis} \end{array} \right.$$

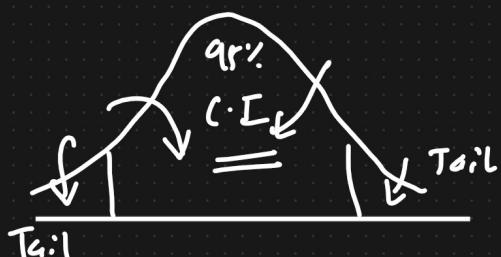
Accept the Null
Reject the hypothesis



I Was Correct Here

$\left\{ \begin{array}{l} P\text{-value} < \text{Significance value} \\ \downarrow \\ \text{Reject the Null Hypothesis.} \end{array} \right.$

OR
 $\left\{ \text{Accept the Null Hypothesis} \right\}$



$$P = 0.11 > 0.05$$

Accept

$$P = \boxed{0.002} < 0.05$$

Reject the Null Hypothesis

② Covariance

<u>X</u>	<u>Y</u>
Weight	Height
50	160
60	170
70	180
75	181

No. of hour Study	play
2	6
3	4
4	3

Quantity relationship between $X \& Y$

Covariance

$$\text{Cov}(x, y) = \sum_{i=1}^n (x_i - \bar{x})(y_i - \bar{y})$$

+ve

positive correlation

<u>X↑</u>	<u>Y↑</u>
<u>X↓</u>	<u>Y↓</u>

-ve



negative correlation

= +ve or -ve

$X \& Y$

<u>X↓</u>	<u>Y↑</u>
<u>X↑</u>	<u>Y↓</u>

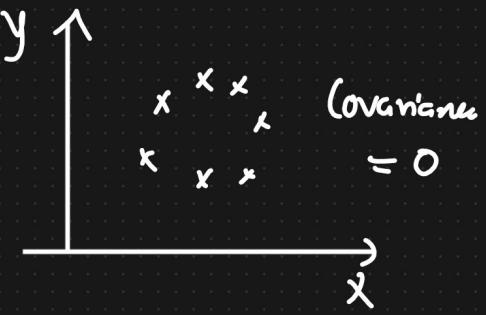
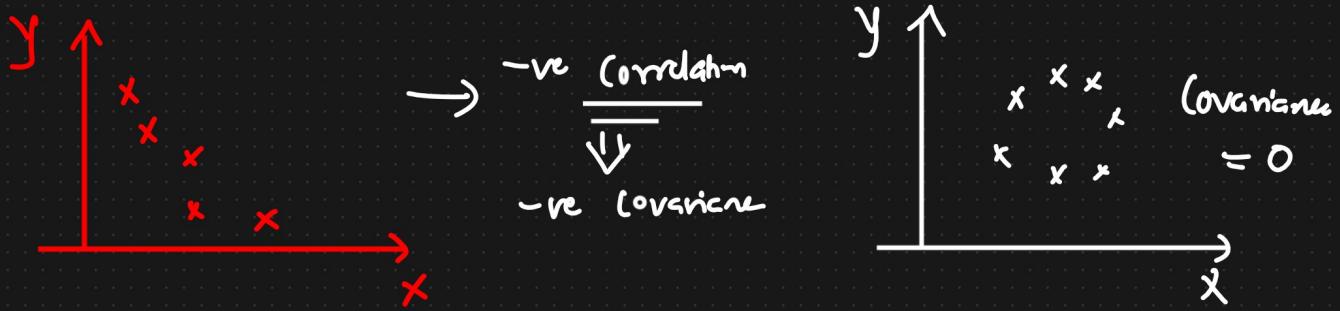
O

$X \& Y$



→ +ve Correlation

↔



Disadvantage of Covariance

① Positive OR Negative ✓

$$\begin{array}{r} +100 \\ -200 \\ \hline -2000 \end{array}$$

$\stackrel{+1000}{=} \stackrel{-200}{=} \stackrel{-2000}{=}$ f Direction

② Pearson Correlation Coefficient

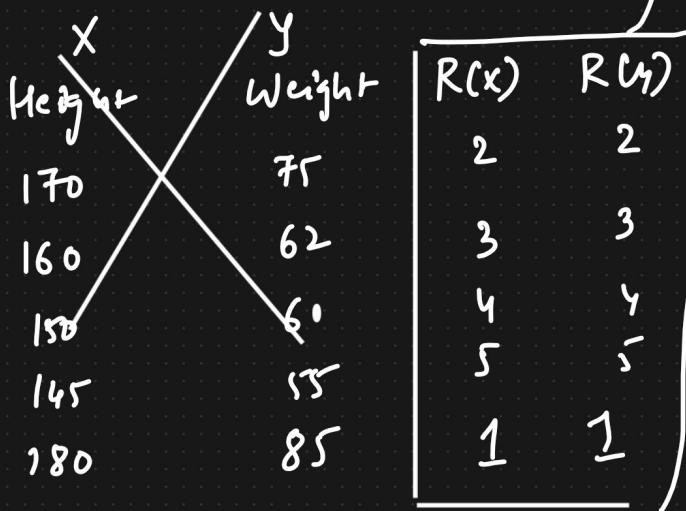
(-1 to 1)

The more towards +1 more positively correlated

The more towards -1 more negatively correlated

$$f(x,y) = \frac{\text{Cov}(x,y)}{\sigma_x \sigma_y} = \left\{ \begin{matrix} -1 & 1 \end{matrix} \right\}$$

$$\text{Spear}(x,y) = \frac{\text{Cov}(R(x), R(y))}{R_{fx} \times R_{fy}}$$



Non linear properties

Using

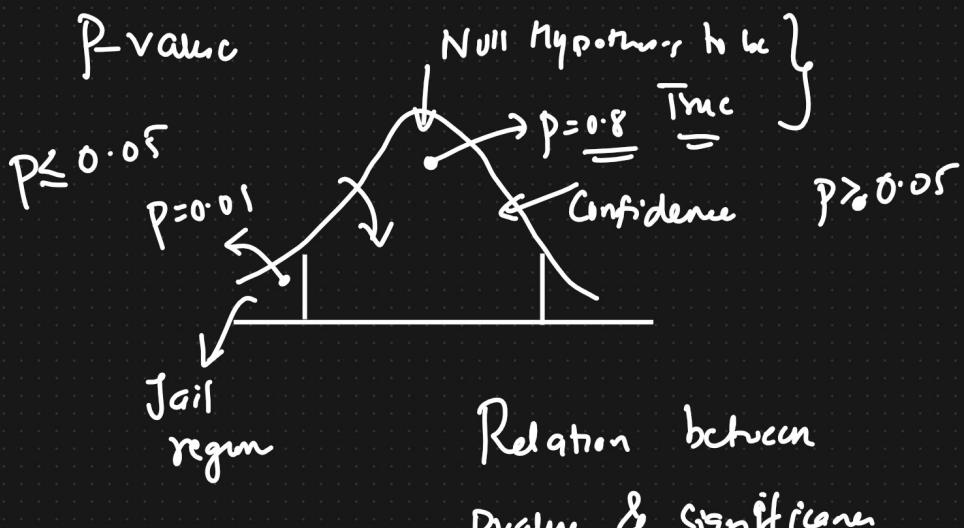
$P \leq 0.05 \rightarrow \text{Reject the Null Hypothesis}$

↓

probability {
5% probability the null hypothesis is correct}

$\alpha = 0.05$

$P \geq 0.05 \rightarrow \text{Accept the Null Hypothesis}$



$P\text{-value} <$ Significant $\boxed{C.I}$

\hookrightarrow Reject the Null Hypothesis

$P \geq \alpha$ \hookrightarrow Accept the Null

① P value and Significance value