CSC148 - Tracing and Debugging Recursive Functions

On this worksheet, you'll practice the partial tracing technique for recursive functions covered in this week's prep.

1. Here is a partial implementation of a nested list function that returns a brand-new list.

def_flatten(obj: Union[int, List]) -> List[int]
 neturn a (non-nested) list of the integers in <obj>.

The integers are returned in the left-to-right order they appear in <obj>.

>>> flatten(6)
[6]
>>> flatten([1, [-2, 3], -4])
[1, -2, 3, -4]
>>> jim con(10, -1], -2, [[-3, [-5]]]])
[0, -1, -2, -3, -5]

if isinstance(obj, int):

Base case omitted

Verturn [obj]

elso:

(S) = []

for sublist in obj:

(S) extend(flatten(sublist))

return s

is this right? Yes!

Our goal is to determine whether the recursive step is correct without fully tracing (or running) this code. Consider the function call flatten([[0, -1], -2, [[-3, [-5], -7]]]).

(a) What should flatten [[0, -1], -2, [[-3, [-5], -7]]]) return, according to its docstring?

1[0,-1,-2,-3,-5,-7]

(assuming the call works)

(b) We'll use the table below to partially trace the call flatten([[0, -1], 2, [[-3, [-5], -7]]]). Complete the first two columns of this table, assuming that flatten works properly on each recursive call. Remember that filling out these two columns can be done just using the argument value and flatten's docstring; you don't need to worry about the code at all!

Note: the input list [0, -1], -2, [-3, [-5], -7]] has just three sub-nested-lists.

sublist	flatten(sublist)	Value of s at the end of the iteration
N/A	N/A	[] (initial value of s)
Co1-13	[0,-1]	[0:-1]
-2	[-2]	[0,-1,-2]
[[-3, [-5], -7]]	[-3,-5,-7]	[0, -1, -2, -3, -5, -7

- (c) Use the third column of the table to complete the partial trace of the recursive code. Remember that every time you reach a recursive call, don't trace into it—use the value you calculated in the second column!
- (d) Compare the final value of s with the expected return value of flatten. Does this match?

yes!

(e) Finally, write down an implementation of the base case of flatten directly on the code above.

return [obj]

2. Now consider the following function and partial implementation.

```
def uniques(obj: Union[int, List]) -> List[int]:

"""Return a (non-nested) list of the integers in <obj>, with no duplicates.

>>> uniques([13, [2, ]X], 4))

if isinstance(obj, int):

# Base case omitted

else:

s = []

for sublist in obj:

s.extend(uniques(sublist))

return [ obj ]

s.extend(uniques(sublist))

return [ obj ]

return [ obj ]

s.extend(uniques(sublist))
```

It turns out that there is a problem with the recursive step in this function, and it has the insidious feature of being sometimes correct, and sometimes incorrect. To make sure you understand this, find two examples for initial arguments to uniques: one in which partial tracing would lead to us thinking there's no error, and one in which partial tracing would lead us to find an error.

Input that does NOT reveal an error:

Partial trace table (fill it in and verify that the bottom-right corner matches the expected output; you might not need to use all the rows, depending on your chosen input)

sublist	uniques(sublist)	Value of s at the <i>end</i> of the iteration
N/A	N/A	[]
2	(2]	4
[4]	C4J	
6	CLJ	C2,4,6]

Input that DOES reveal an error:

[[[2,2], [[3]] X

Expected output: [1,2,3]

Partial trace table (fill it in and verify that the bottom-right corner doesn't match the expected output; you might not need to use all the rows, depending on your chosen input) assuming that fue recursive calls was.

sublist	uniques(sublist)	Value of s at the <i>end</i> of the iteration
N/A	N/A	[]
		こつ
[2,2]	[2]	[1,2]
[[37]	> C3]	[1,2,3]
3	[3]	[1,2,3,3] X

3. What you've provided above is a *counter-example* that shows that this recursive step is incorrect. This is a good start, but we'd like to go deeper. Analyse the recursive code above, and then describe in words *why* the code is incorrect, i.e., what the problem with the code is.

Never chedis, just adds.

extend
[1,2,3] [5,8] [1,2,3,5,8]
append [1,2,3, [5,8]]