## CSC148 - Analysing the Running Time of Linked List Operations

Last week, we began to look at how to analyse the efficiency of Python code, first by counting "steps", and then using Big-Oh notation. On this worksheet, we'll first review what you know about the efficiency of operations for Python's list class, and then analyse our LinkedList class.

- 1. (Review) Suppose we have a Python (array-based) list of length n.
  - (a) Complete the following table by using Big-Oh notation to describe the running time of each of the following operations. Remember:  $\mathcal{O}(1)$  means "constant time", while  $\mathcal{O}(n)$  means "linear time", both with respect to the list length n.

Operation	Running time
Insert at the front of the list	
Insert at the end of the list	
Look up the element at index $i$ , where $0 \le i < n$	

- (b) In general, Big-Oh notation means (roughly) "proportional to". We don't have to just use one variable n in Big-Oh notation! For example,  $\mathcal{O}(n+i)$  translates to "proportional to n+i".
  - Using this idea, write down a Big-Oh expression to capture the running time of the following operation: inserting a new item at index i into a list of length n, where  $0 \le i < n$ .
- 2. Now let's look at our linked list implementation. The key idea behind determining the efficiency of linked list operations is counting how many nodes are traversed during the operation.
  - (a) Review your implementations of LinkedList.append, LinkedList.insert, and LinkedList.\_\_getitem\_.. Then, complete the following table, assuming a linked list of length n.

Operation	Running time
Insert at the front of the linked list	
Insert at the end of the linked list	
Look up the element at index $i$ , where $0 \le i < n$	

- (b) What is the Big-Oh running time of inserting an item at index i into a linked list of length n, where  $0 \le i < n$ ?
- 3. Suppose we have an array-based list of length 1,000,000, and a linked list of length 1,000,000. If we insert a new item at index 500,000 into each list, would it be:
  - significantly faster for the array-based list, or
  - significantly faster for the linked list, or
  - roughly the same amount of time for both lists?

Explain your answer!

4.	Consider this	s implementation of	LinkedList. init	from the lecture notes:
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class LinkedList:
def __init__(self, items: list) -> None:
    self._first = None
    for item in items:
        self.append(item)
```

(a) Suppose we call LinkedList(items) where items has length n. Calculate the total number of nodes traversed when we make this call. Note that the same node can be traversed more than once, and you should count each time the node is traversed. (You may or may not include "1 step" for creating each new node.)

- (b) Based on your calculation in the previous part, write down a Big-Oh expression for the running time of this operation in terms of n, the length of the input items.
- 5. The last topic we'll cover today is looking at how running time can vary, even among inputs of the same size. For example, consider LinkedList.\_\_contains\_\_, and suppose we have a linked list 1st of length  $n \geq 1$ , and we are searching for the item 148. That is, we call lst.\_\_contains\_\_(148)).
  - (a) When would it be possible for lst.\_\_contains\_(148) to return after visiting just a single node?

(b) When would it be necessary for lst.\_contains\_(148) to visit all n nodes in the linked list lst?