

**Aids Allowed:** ONLY your *own notes* taken during lectures and office hours, the lecture *slides and recordings* (for all sections), and the *Course Notes* (textbook).

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### Submission Instructions

- Submit your work directly on [MarkUs](#)—even if you are late!
  - You may type your answers or hand-write them *legibly*, on paper or using a tablet and stylus.
  - You may write your answers directly on the question paper, or on another piece of paper/document.
  - You may submit your answers as a single file/document or as multiple files/documents. Each document may contain answers for only part of one question, an entire question, or multiple questions, but *please label each part of your answers* to make it clear what you are answering.
  - There is no “required file”, but *please give short names to your file(s)*, like “Q2.png” or “TT4.pdf”.
  - You **must** submit your answers in PDF or as photos (JPEG/JPG/GIF/PNG/HEIC/HEIF). **Other formats** (e.g., Word documents, L<sup>A</sup>T<sub>E</sub>X source files, ZIP files) **are NOT accepted**—you must **export** or **compile** documents to PDF, **convert** images into a supported format, and upload each file **individually**.
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For all questions in this test, write your proofs *formally*, including a header and a proof body with justifications for each deduction. Remember that we are looking for evidence that you understand the conventions for writing correct proofs, so pay attention to the *structure* of your answers, in addition to their content!

### 3. [7 marks] Algorithm Analysis: Counting Iterations

Consider the following algorithm.

```
1 def woohoo(n: int) -> int:
2     ''' Precondition: n > 0. '''
3     i = 0
4     while i < n:                # Loop 1
5         for j in range(i):      # Loop 2
6             print(j)
7         if i % 5 == 0:
8             if i % 3 == 0:
9                 i = i + 1
10            else:
11                i = i + 2
12        else:
13            i = i + 4
```

- (a) [2 marks] Find a *lower bound* on **the number of iterations** of Loop 1, as a function of the input  $n$ , *without using Omega or Theta notation*. Show your work (in other words, explain how you obtained your answer and show your calculations). *Hint*: Don't try to make your lower bound tight.
- (b) [2 marks] Find an *upper bound* on **the number of iterations** of Loop 1, as a function of the input  $n$ , *without using Big-O or Theta notation*. Show your work (in other words, explain how you obtained your answer and show your calculations). *Hint*: Don't try to make your upper bound tight.
- (c) [3 marks] Give a Theta bound on **the running time** of function `woohoo`, as a function of its input  $n$ . Show your work (in other words, explain how you obtained your answer and show your calculations).

*Reminder: this test contains **five (5)** separate questions, plus the Academic Integrity statement!*