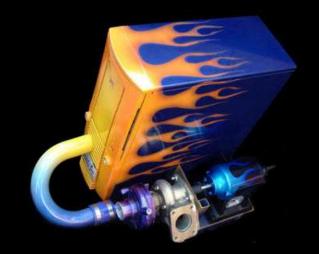
Sequential Circuits

Something to consider...

 Computer specs use terms like "8 GB of RAM" and "2.2GHz processors".



- What do these terms mean?
 - RAM = Random Access Memory; 8GB = 8 billion bytes
 - 2.2 GHz = 2.2 billion clock pulses per second.
- But what does this mean in circuitry?
 - How do you use circuits to store values?
 - What is the purpose of a clock signal?

Something else to consider...

How does the Tickle Me Elmo work?



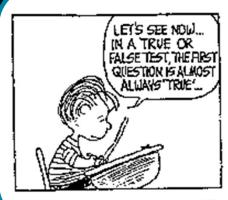


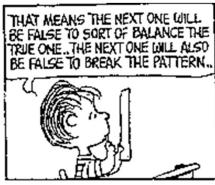
Two kinds of circuits

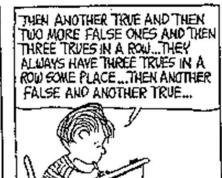
- So far, we've dealt with combinational circuits:
 - Circuits where the output values are entirely dependent and predictable from current inputs.
- Another class of circuits: sequential circuits
 - Circuits that also depend on both the current inputs and the previous state of the circuit.

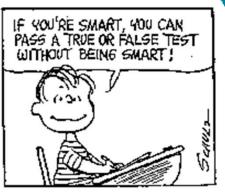
Sequential circuits

- This creates circuits whose internal state can change over time, where the same input values can result in different outputs.
- Why would we need circuits like this?
 - Memory values
 - Reacting to changing inputs





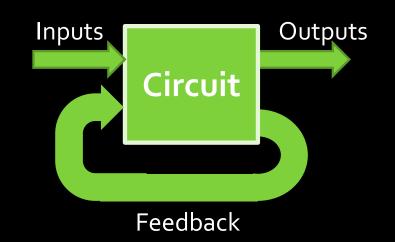


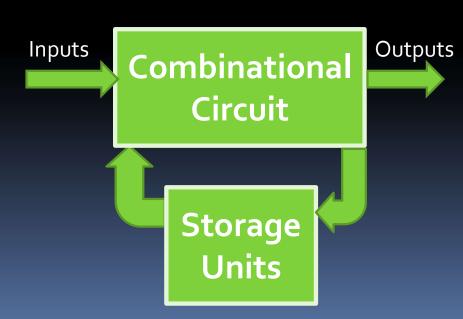


4 1968 United Feature Syndicate, Inc.

Creating sequential circuits

- Essentially, sequential circuits are a result of having feedback in the circuit.
 - How is this accomplished?
 - What is the result of having the output of a component or circuit be connected to its input?



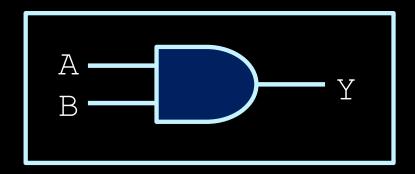


Gate Delay

 Even in combinational circuits, outputs don't change instantaneously.

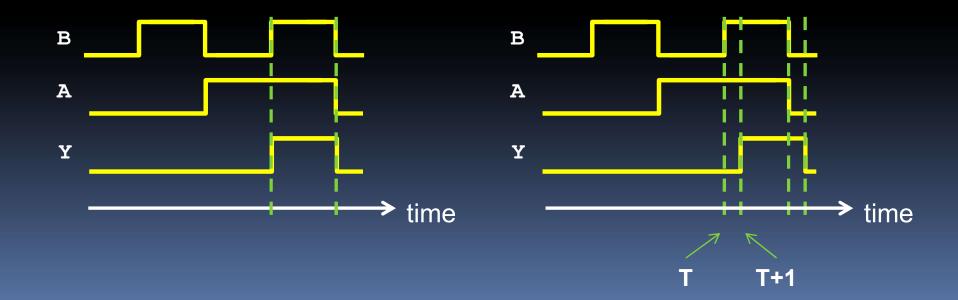
- Gate Delay or Propagation Delay:
 - "The length of time it takes for an input change to result in the corresponding output change."

Gate delay example



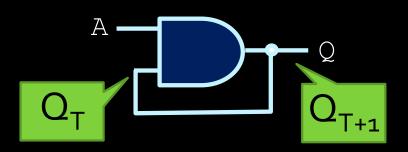
Ideal

Considering delays



Feedback Circuit Example (AND)

 Some gates don't have useful results when outputs are fed back on inputs.



 Q_T and Q_{T+1} represent the values of Q at a time T, and a point in time immediately after (T+1)

A	$Q_{\scriptscriptstyle \mathrm{T}}$	$Q_{\mathtt{T+1}}$
0	0	0
0	1	0
1	0	0
1	1	1

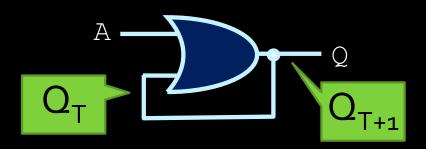
If A=0, Q_{T+1} becomes 0 no matter what Q_T was.

What happens next for later values of A?

 Q_{T+1} gets stuck at 0 and cannot change \otimes

Feedback Circuit Example (OR)

 Some gates don't have useful results when outputs are fed back on inputs.



In this truth table, Q_T and Q_{T+1} represent the values of Q at a time T, and a point in time immediately after (T+1)

A	Q_{T}	Q_{T+1}
0	0	0
0	1	1
1	0	1
1	1	1

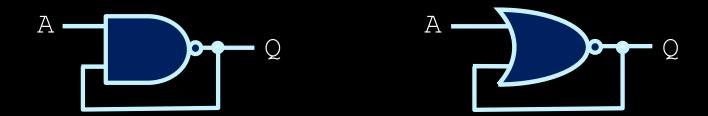
If A=1, Q_{T+1} becomes 1 no matter what Q_T was.

What happens next for later values of A?

 $Q_{\mathbb{T}+1}$ gets stuck at 1. Not very useful \otimes

Feedback Examples (NAND, NOR)

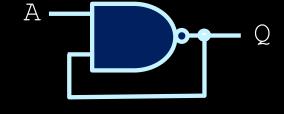
 NAND, NOR gates w/ feedback have more interesting characteristics, which lend themselves to storage devices.



- What makes NAND and NOR feedback circuits different?
 - Unlike the AND and OR gate circuits (which get stuck), the output Q_{T+1} can be changed, based on A.

Feedback Example (NAND)

- Let's assume we set A=0
 - Then, output Q will go to 1.



- If we leave A unchanged we can store 1 indefinitely!
- If we set A=1, Q's value can change, but

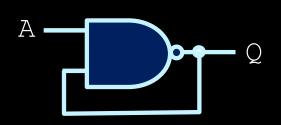
there's a catch!

What happens
in these last
two scenarios?

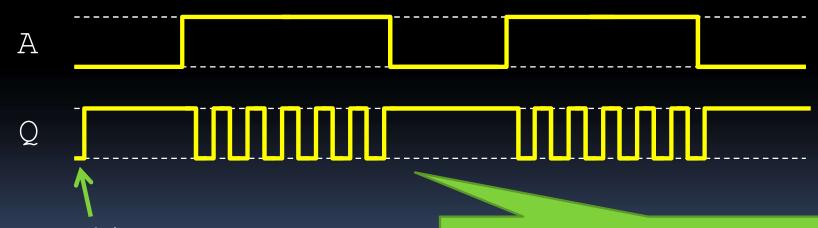
A	$Q_{\mathtt{T}}$	Q_{T+1}
0	0	1
0	1	1
1	0	1
1	1	0

Unsteady state! Can't store 0 long!

NAND waveform behaviour



A	$Q_{\mathtt{T}}$	Q_{T+1}
0	0	1
0	1	1
1	0	1
1	1	0

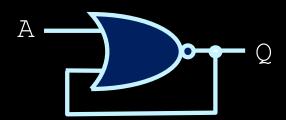


Gate delay. Output does not change instantaneously

We want to avoid this. We should be able to store high and low values for as long as we want, and change those values as needed.

Feedback Example (NOR)

- Let's assume we set A=1
- Then, output Q will go to 0.



If we leave A unchanged we can store 0 indefinitely!

■ If we flip A, we can change Q, but there's a catch here too!

A	$Q_{ extbf{T}}$	Q_{T+1}
0	0	1
0	1	0
1	0	0
1	1	0

Feedback behaviour

NAND behaviour

A	$Q_{\mathtt{T}}$	Q_{T+1}
0	0	1
0	1	1
1	0	1
1	1	0

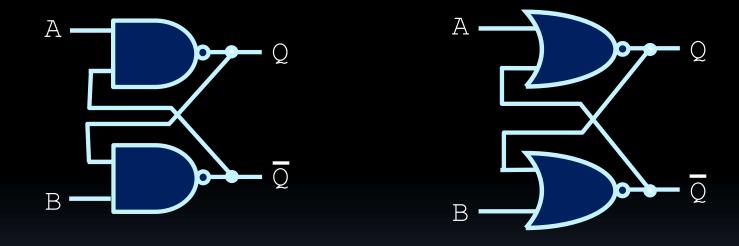
NOR behaviour

A	$Q_{\mathtt{T}}$	Q_{T+1}
0	0	1
0	1	0
1	0	0
1	1	0

- Output Q_{T+1} can be changed, based on A.
- However, gates like these that feed back on themselves could enter an unsteady state.

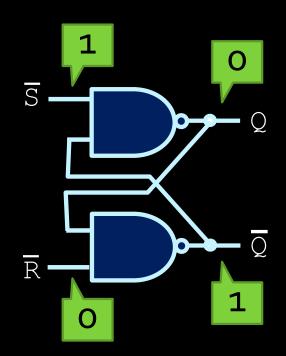
Latches

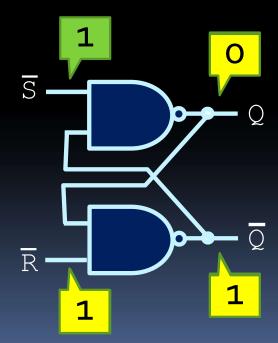
If multiple gates of these types are combined, you can get more steady behaviour.



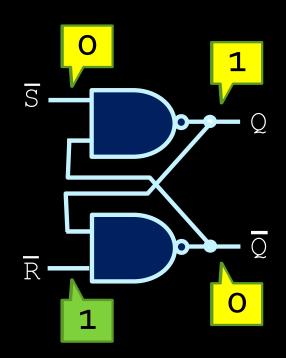
These circuits are called latches.

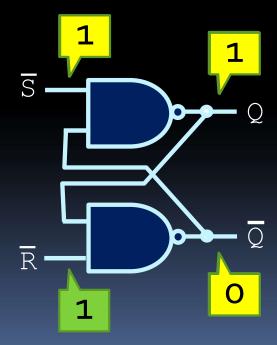
- Let's see what happens when the input values are changed...
 - Assume that $\overline{\mathbb{S}}$ and $\overline{\mathbb{R}}$ are set to 1 and 0 to start.
 - The $\overline{\mathbb{R}}$ input sets the output $\overline{\mathbb{Q}}$ to 1, which sets the output \mathbb{Q} to 0.
 - Setting R to 1 keeps the output value Q at 1, which maintains both output values.

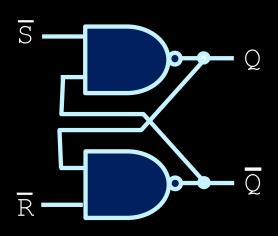




- (continuing from previous)
 - \overline{S} and \overline{R} start with values of 1, when \overline{S} is set to 0.
 - This sets output Q to 1, which sets the output \overline{Q} to 0.
 - Setting $\overline{\mathbb{S}}$ back to 1 keeps the output value $\overline{\mathbb{Q}}$ at 0, which maintains both output values.
- Note: inputs of 11 maintain the previous output state!

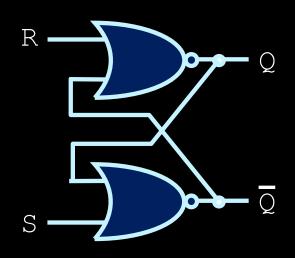






S	≅	Q _T	Q _T	Q _{T+1}	Q _{T+1}
0	1	X	X	1	0
1	0	Χ	Χ	0	1
1	1	0	1	0	1
1	1	1	0	1	0

- lacksquare $\overline{\mathbb{S}}$ and $\overline{\mathbb{R}}$ are called "set" and "reset" respectively.
- Note how the circuit "remembers" its signal when going from 10 or 01 to 11.
- Going from 00 to 11 produces unstable behaviour!
 - Depending on which input changes first.

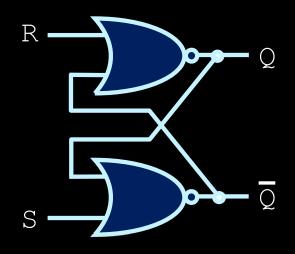


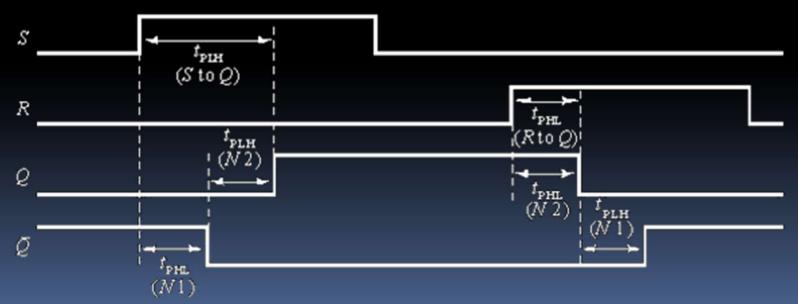
Ø	R	$Q_{\mathtt{T}}$	$\overline{Q}_{\mathtt{T}}$	$Q_{\mathtt{T+1}}$	\overline{Q}_{T+1}
0	0	0	1	0	1
0	0	1	0	1	0
0	1	Χ	Χ	0	1
1	0	Χ	Χ	1	0
_1	1	V	V	0	0
4		Λ	Λ		

- In this case, S and R are "set" and "reset".
- In this case, the circuit "remembers" previous output when going from 10 or 01 to 00.
- As with \overline{SR} latch, unstable behaviour is possible, but this time when inputs go from 11 to 00.

SR latch timing diagram

Important to note that the output signals don't change instantaneously.





More on instability

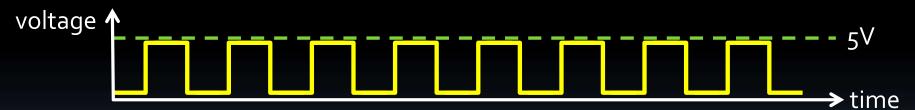
- Unstable behaviour occurs when a \overline{SR} latch's inputs go from 00 to 11, or a SR latch's inputs go from 11 to 00.
 - The signals don't change simultaneously, so the outcome depends on which signal changes first.
- Because of the unstable behaviour, 00 is considered a forbidden state in NAND-based \$\overline{SR}\$ latches, and 11 is considered a forbidden state in NOR-based SR latches.

Introducing the Clock

- Now we have circuit units that can store high or low values. How can we read from them?
 - For instance, when do we know when the output is ready to be sampled?
 - If the output is high, how can we tell the difference between a single high value and two high values in a row?
- Need some sort of timing signal, to let the circuit know when the output may be sampled.
 - → clock signals.

Clock signals

- "Clocks" are a regular pulse signal, where the high value indicates when to update the output of the latch.
- Usually drawn as:



But looks more like:

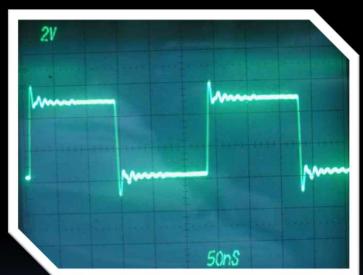


Signal restrictions

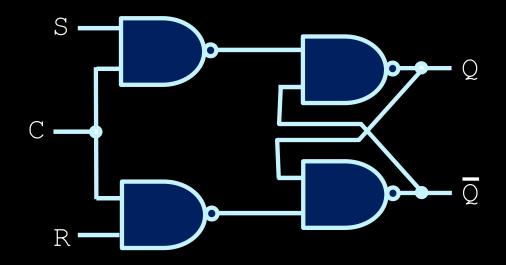
What's the limit to how fast the latch circuit can be sampled?

- Determined by:
 - latency time of transistors
 - Setup and hold time
 - setup time for clock signal
 - Jitter
 - Gibbs phenomenon





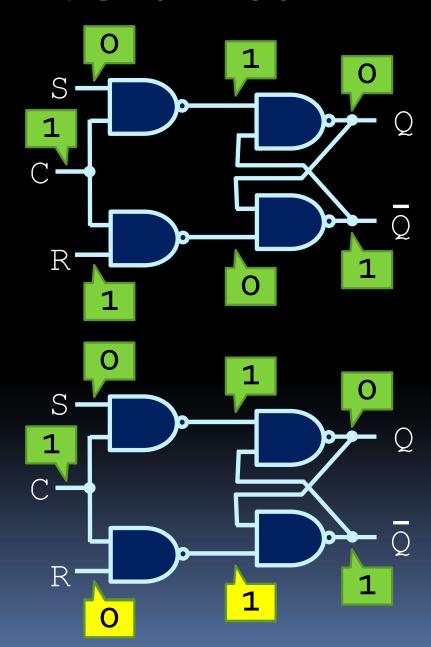
Clocked SR latch



- Adding another layer of NAND gates to the SR latch gives us a clocked SR latch or gated SR latch)
 - Basically, a latch with a control input signal C.
- The input C is often connected to a pulse signal that alternates regularly between 0 and 1 (clock)

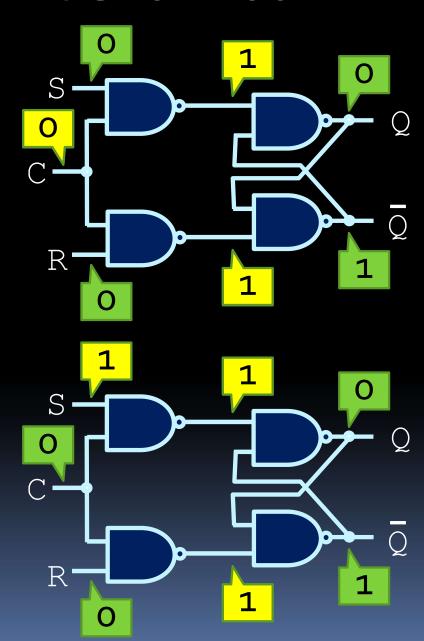
Clocked SR latch behaviour

- Same behaviour as SR latch, but with timing:
 - Start off with S=0 and
 R=1, like earlier example.
 - If clock is high, the first NAND gates invert those values, which get inverted again in the output.
 - Setting both inputs to 0
 maintains the output
 values.

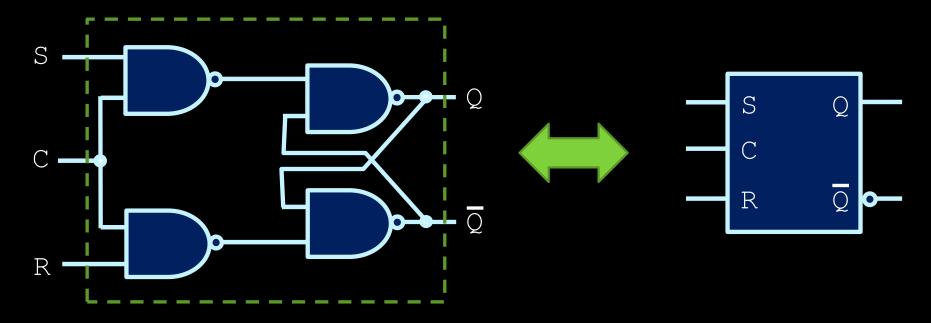


Clocked SR latch behaviour

- Continued from previous:
 - Now set the clock low.
 - Even if the inputs change, the low clock input prevents the change from reaching the second stage of NAND gates.
 - Result: the clock needs to be high in order for the inputs to have any effect.

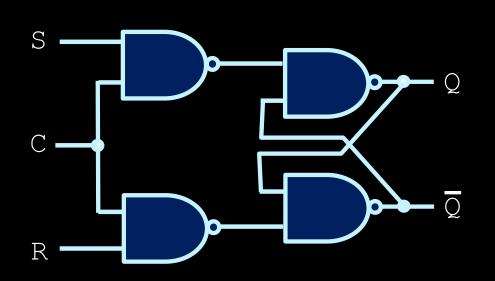


Clocked SR latch



- This is the typical symbol for a clocked SR latch.
- This only allows the S and R signals to affect the circuit when the control input (C) is high.
- Note: the small NOT circle after the Q output is simply the notation to use to denote the inverted output value. It's not an extra NOT gate.

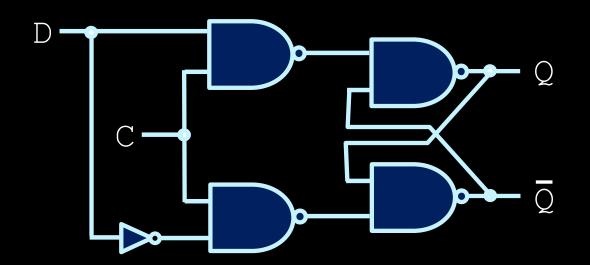
Clocked SR latch behaviour



C	S	R	$Q_{\scriptscriptstyle \mathrm{T+1}}$	Result
0	X	X	$Q_{\mathtt{T}}$	no change
1	0	0	$Q_{\mathtt{T}}$	no change
1	0	1	0	reset
1	1	0	1	set
1	1	1	?	Undefined

- Assuming the clock is 1, we still have a problem when S and R are both 1, since the state of Q is indeterminate.
 - Better design: prevent S and R from both going high.

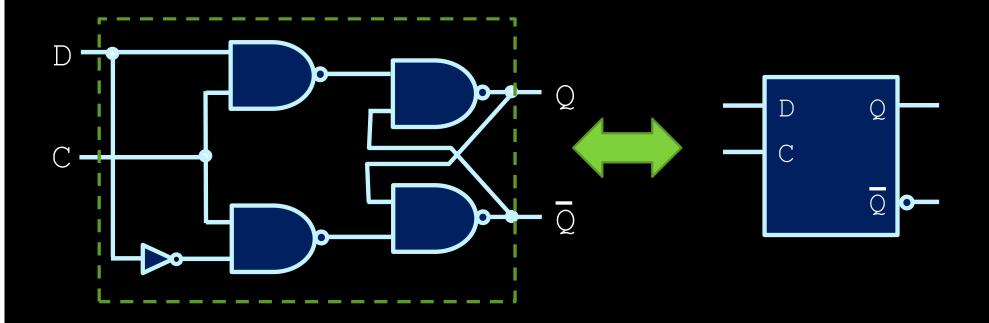
D latch (or gated D-latch)



$Q_{\mathtt{T}}$	D	Q_{T+1}
0	0	0
0	1	1
1	0	0
1	1	1

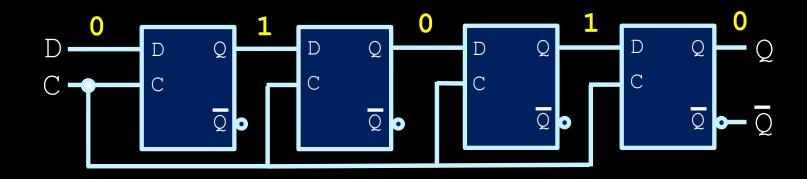
- By making the inputs to R and S dependent on a single signal D, you avoid the indeterminate state problem.
- The value of D now sets output Q low or high whenever C is high.

D latch



- This design is good, but still has problems.
 - i.e. timing issues.

Transparency example



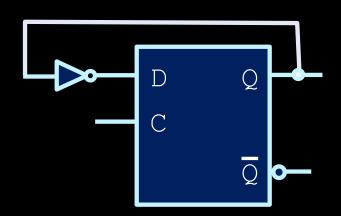
■ If the wires have the values 01010 when the clock goes from 0 to 1, what do you expect the latch values to change to?

D-Latch is transparent!

- Transparent means that
 - Any changes to its inputs are visible to the output when control signal (Clock) is 1.
- Key Take-away: The "output of a latch should not be applied directly or through combinational logic to the input of the same or another latch when they all have the same control (clock) signal."

Latch timing issues

- Consider the circuit on the right:
- When the clock signal is high, the output looks like the waveform below:

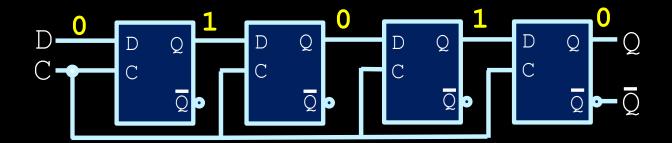


Output keeps toggling back and forth.

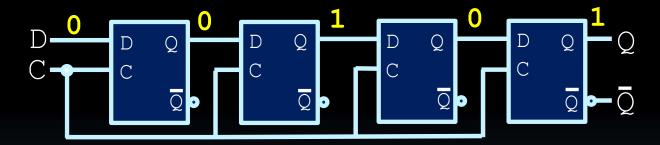
C

...what happens next?

Value- vs Edge-triggered



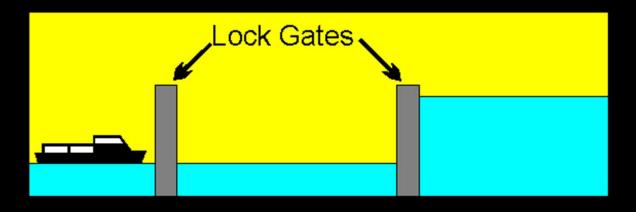
 Instead of having all these latches flooded by the 0 value, we'd rather have the clock shifting the latch values over by one....



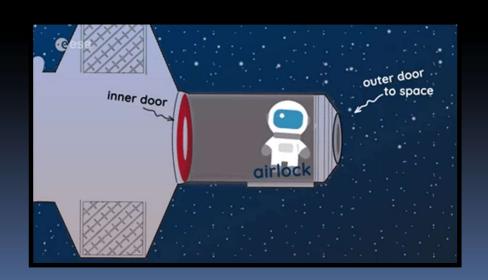
- We'd also imagine this happening at the moment the clock changes, not for the duration of the clock being high.
 - Edge-triggered vs value-triggered.
- So how can we make this happen?

Canal (or airlock) model

 Picture how boats travel through a canal in stages, one stage at a time.

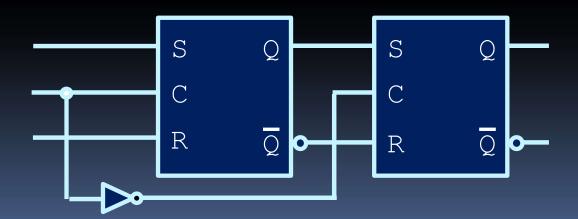


- Boats enter the middle section (aka the lock),
- First gate is closed,
- Second gate is opened,
- Boat exits the canal.
- Same idea as airlocks on a space station.



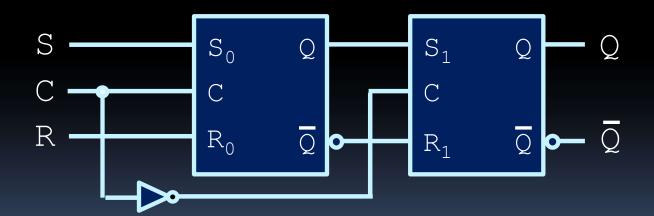
Latch timing issues

- How does this work with latches?
 - We want the output to change only once when the clock pulse changes, at the moment it changes.
 - Solution: create disconnect between circuit output and circuit input, to prevent unwanted feedback and changes to output.

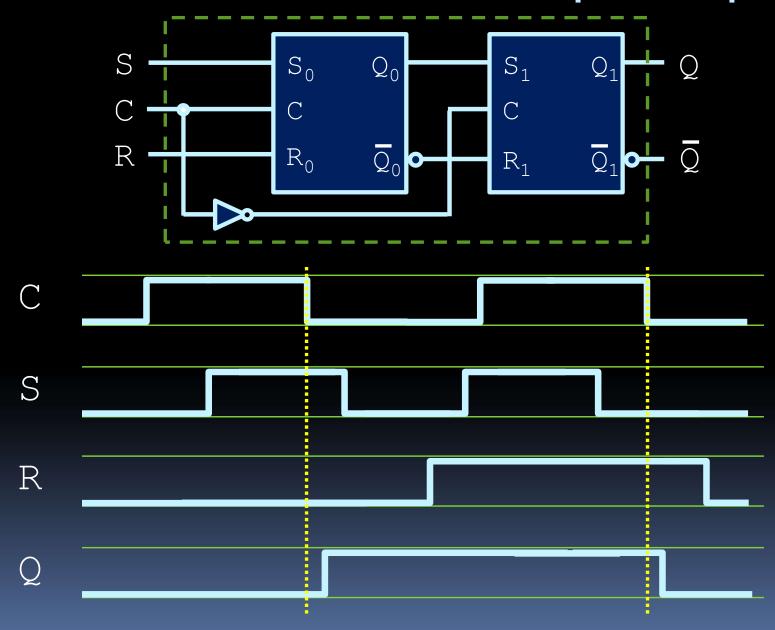


SR master-slave flip-flop

- A flip-flop is a latched circuit whose output is triggered with the rising edge or falling edge of a clock pulse.
- Example: The SR master-slave flip-flop

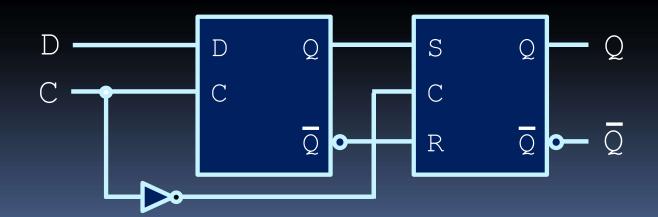


SR master-slave flip-flop



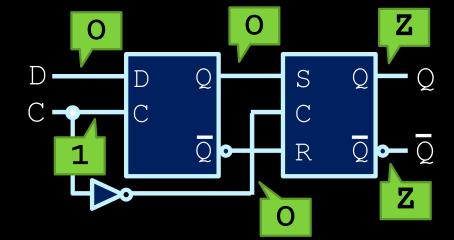
Edge-triggered D flip-flop

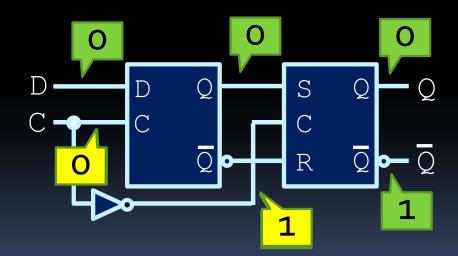
- SR flip-flops still have issues of unstable behaviour.
- Solution: D flip-flop
 - Connect D latch to the input of a SR latch.
 - Negative-edge triggered flip-flop (like the SR)



Flip-flop behaviour

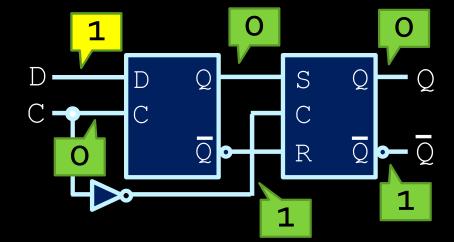
- Observe the behaviour:
 - If the clock signal is high, the input to the first flip-flop is sent out to the second.
 - The second flip-flop doesn't do anything until the clock signal goes down again.
 - When it clock goes from high to low, the first flip-flop stops transmitting a signal, and the second one starts.

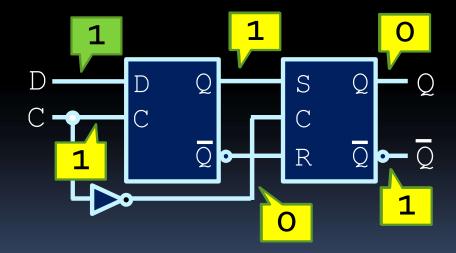




Flip-flop behaviour

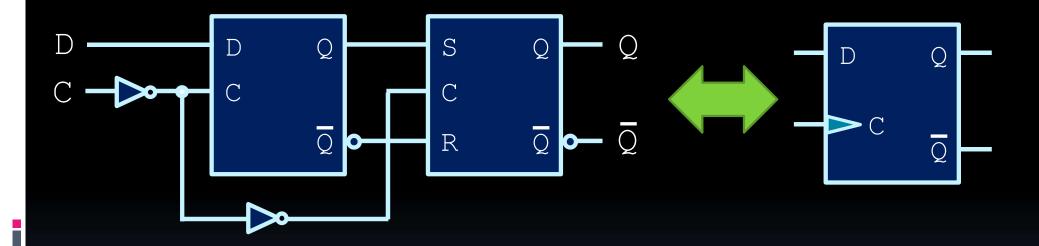
- Continued from previous:
 - If the input to D changes, the change isn't transmitted to the second flip-flop until the clock goes high again.
 - Once the clock goes high, the first flip-flop starts transmitting at the same time as the second flipflop stops.





Edge-triggered flip-flop

Alternative: positive-edge triggered flip-flops

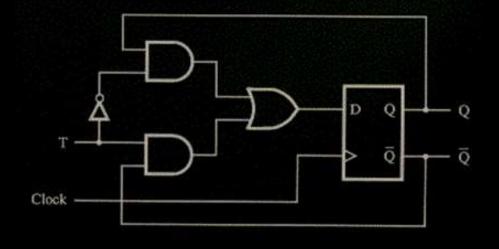


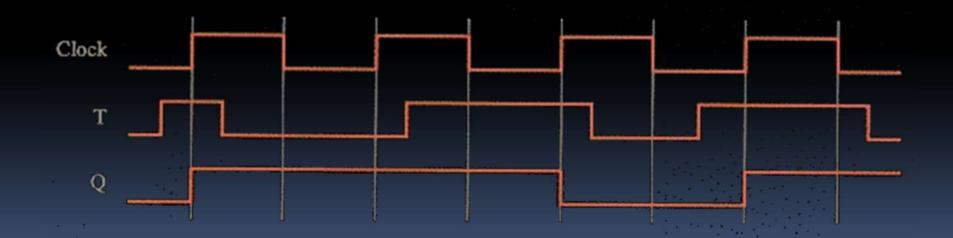
 These are the most commonly-used flip-flop circuits (and our choice for the course).

Other Flip-Flops

The T flip-flop:

 Like the D flip-flop, except that it toggles its value whenever the input to T is high.

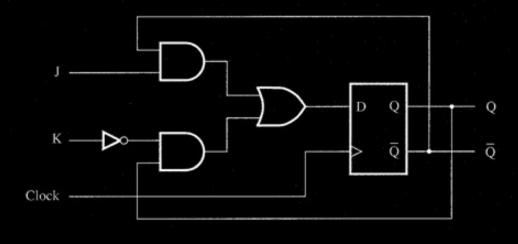




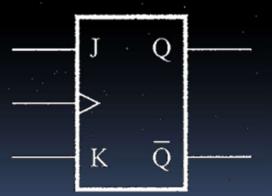
Other Flip-Flops

The JK Flip-Flop:

 Takes advantage of all combinations of two inputs (J & K) to produce four different behaviours:



- if J and K are 0, maintain output.
- if J is 0 and K is 1, reset output to 0.
- if J is 1 and K is 0, set output to 1.
- if J and K are 1, toggle output value.



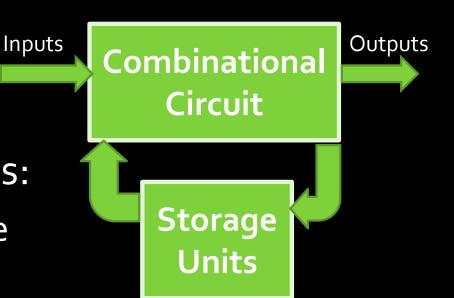
Sequential circuit design

 Similar to creating combinational circuits, with extra considerations:

 The flip-flops now provide extra inputs to the circuit

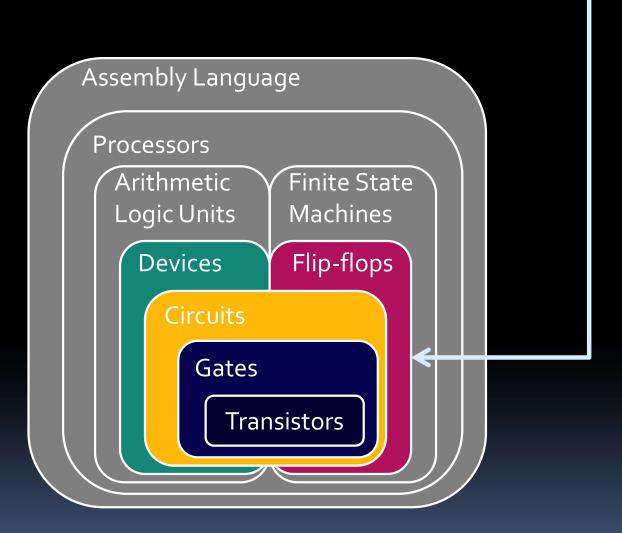
 Extra circuitry needs to be designed for the flip-flop inputs.

...which is the next topic ©



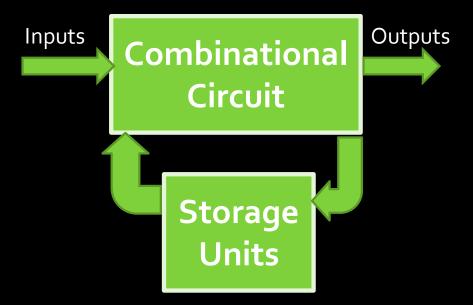
Sequential Circuit Design

We are here



Circuits using flip-flops

Now that we know about flip-flops and what they do, how do we use them in circuit design?



What's the benefit in using flip-flops in a circuit at all?



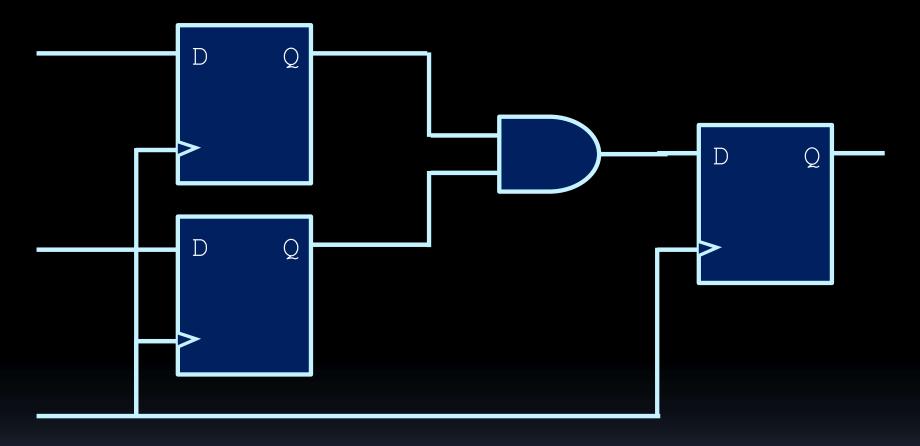
Flip-Flop Timing

 Input should NOT be changing at the same time as the active edge of the clock.

 Setup Time: Input should be stable for some time before active clock edge

 Hold Time: Input should be stable for some time immediately after the active clock edge.

Maximum clock frequency



 Time period between two active clock edges cannot be shorter than longest propagation delay between any two flip-flops + <u>setup time</u> of the flip-flop

Resetting inputs

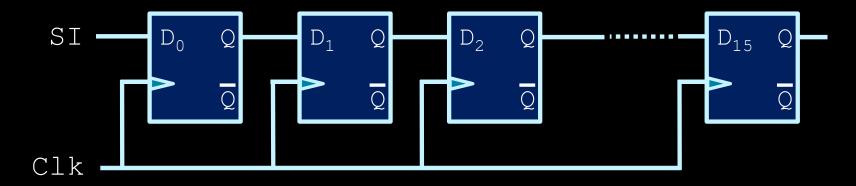
- Since flip-flops (FFs) have unknown state when they are first powered up, we need a convenient way to initialize them
- Reset signal resets the flip flop output to 0
 - This is unrelated to R input of SR latch
- Synchronous reset
 - The output is reset to 0 only on the active edge of the clock
- Asynchronous reset
 - The output is reset to 0 immediately (as soon as the asynchronous reset signal becomes active), independent of the clock signal





Shift registers

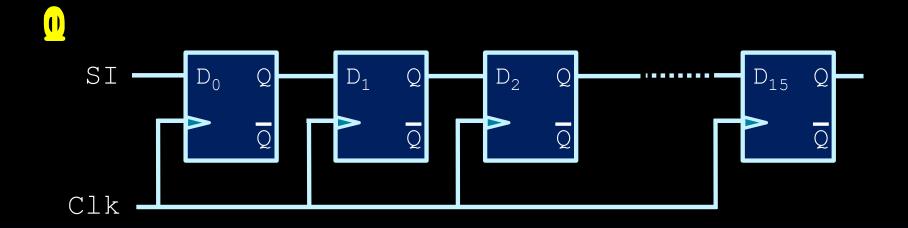
 A series of D flip-flops can store a multi-bit value (such as a 16-bit integer, for example).



- Data can be shifted into this register one bit at a time, over 16 clock cycles.
 - Known as a shift register.

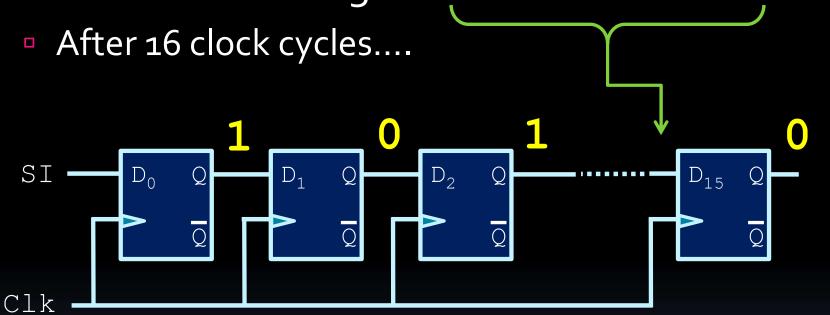
Shift registers

• Illustration: shifting in 0101010101010101



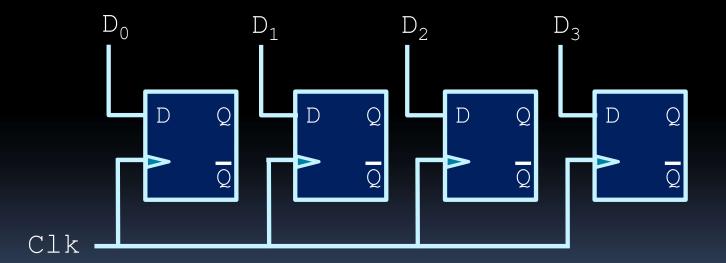
Shift registers

Illustration: shifting in 010101010101010101



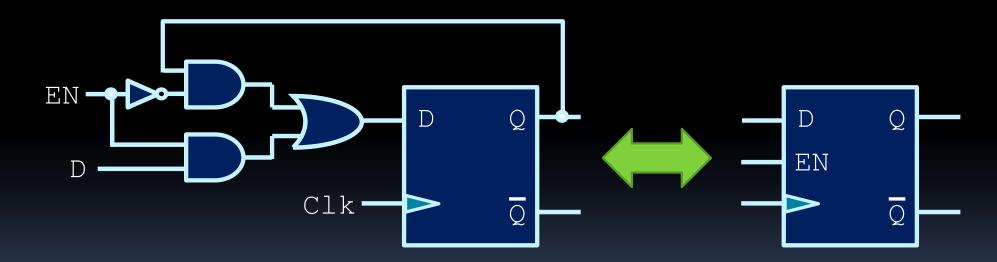
Load registers

- One can also load a register's values all at once, by feeding signals into each flip-flop:
 - In this example: a 4-bit load register.

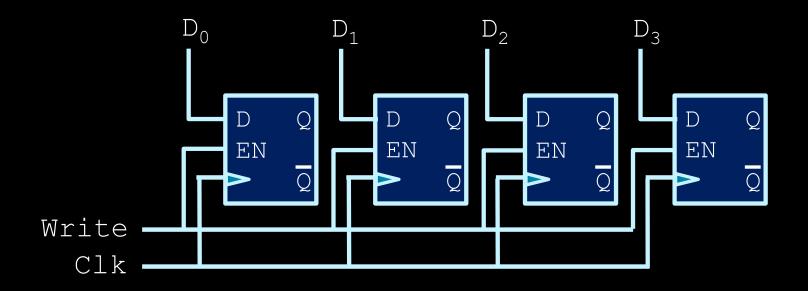


Load registers

To control when this register is allowed to load its values, we introduce the D flip-flop with enable:



Load registers



Implementing the register with these special D flip-flops will now maintain values in the register until overwritten by setting EN high.