

```

import numpy as np
import pandas as pd
import seaborn as sns
import matplotlib.pyplot as plt
from mpl_toolkits.mplot3d import Axes3D
from sklearn.model_selection import train_test_split
from sklearn.linear_model import LinearRegression
from sklearn.preprocessing import PolynomialFeatures
from sklearn.metrics import mean_squared_error

data = pd.read_csv('/content/displacement_data.csv')
dfx= data[["x","y","u_x"]]
dfy= data[["x","y","u_y"]]

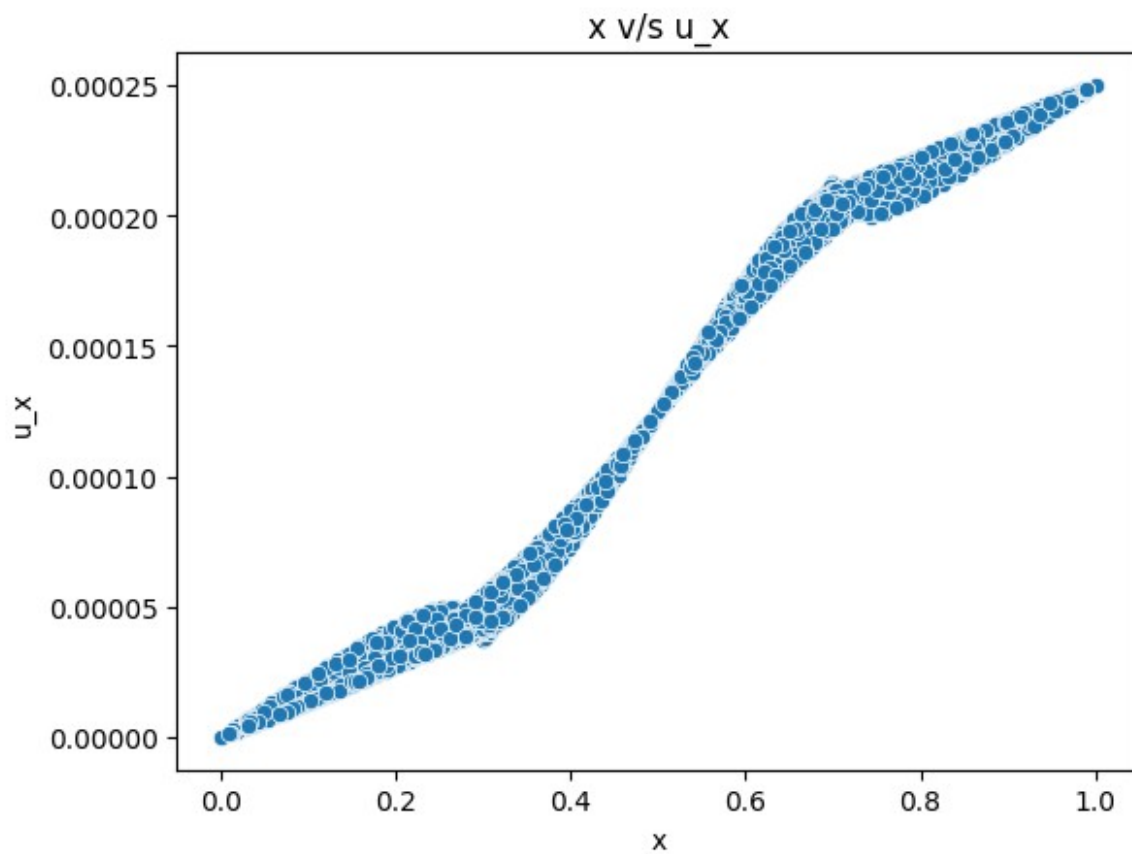
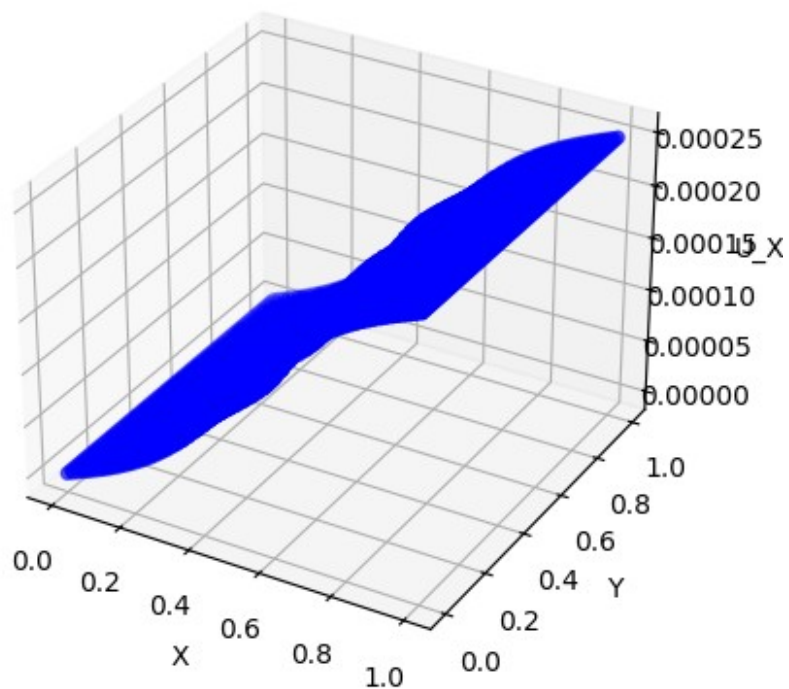
x1 = dfx[['x', 'y']]
y1 = dfx['u_x']
fig = plt.figure()
ax = fig.add_subplot(111, projection='3d')
ax.scatter(dfx['x'], dfx['y'], dfx['u_x'], c='b', marker='o')
ax.set_xlabel('X')
ax.set_ylabel('Y')
ax.set_zlabel('U_X')
plt.title("3D Scatter Plot of X, Y and UX")
plt.show()

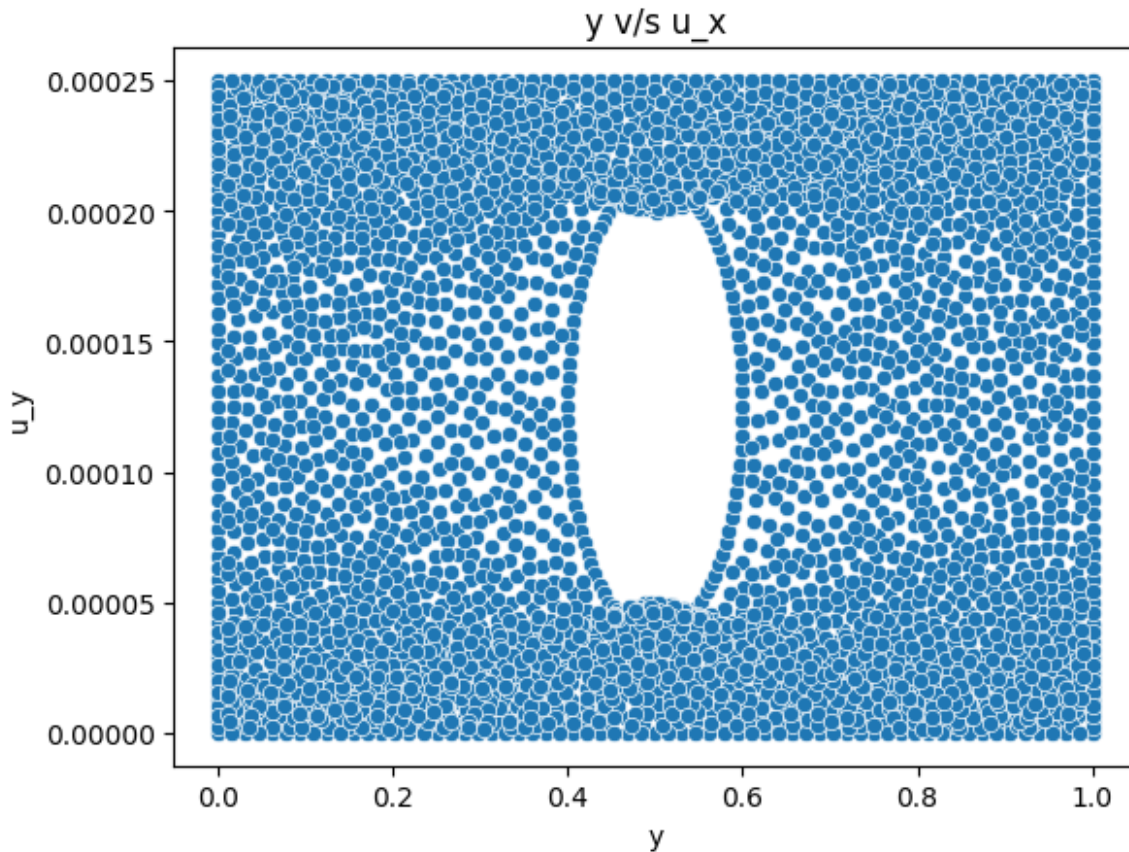
sns.scatterplot(x="x",y="u_x",data=dfx)
plt.title("x v/s u_x")
plt.xlabel("x")
plt.ylabel("u_x")
plt.show()

sns.scatterplot(x="y",y="u_x",data=dfx)
plt.title("y v/s u_x")
plt.xlabel("y")
plt.ylabel("u_y")
plt.show()

```

3D Scatter Plot of X, Y and UX





```
degree = 3
poly = PolynomialFeatures(degree)
X_poly = poly.fit_transform(x1)
model_x = LinearRegression()
model_x.fit(X_poly,y1)
x_range = np.linspace(dfx['x'].min(), dfx['x'].max(), 100)
y_range = np.linspace(dfx['y'].min(), dfx['y'].max(), 100)
X_grid, Y_grid = np.meshgrid(x_range, y_range)
X_grid_poly = poly.transform(np.c_[X_grid.ravel(), Y_grid.ravel()])
Z_grid = model_x.predict(X_grid_poly).reshape(X_grid.shape)

# Plot the original data and the polynomial plane
fig = plt.figure(figsize=(10, 7))
ax = fig.add_subplot(111, projection='3d')

# Plot the original scatter data
ax.scatter(dfx['x'], dfx['y'], dfx['u_x'], color='blue', alpha=0.5,
label="Original Data")

# Plot the polynomial plane
ax.plot_surface(X_grid, Y_grid, Z_grid, color='orange', alpha=0.7,
rstride=100, cstride=100, edgecolor='k')
ax.set_xlabel('X')
```

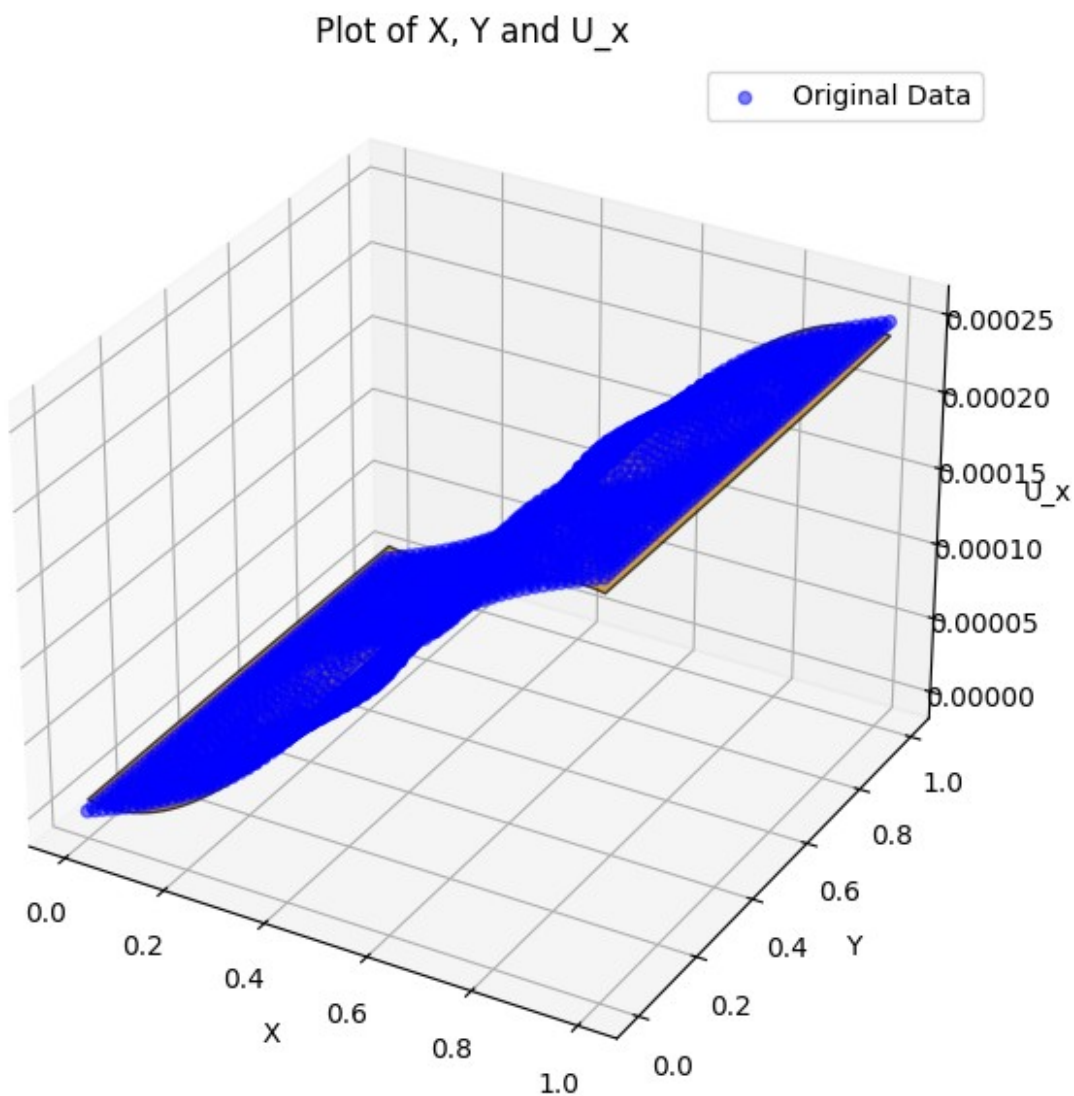
```

ax.set_ylabel('Y')
ax.set_zlabel('U_x')
ax.set_title('Plot of X, Y and U_x')

plt.legend()
plt.show()
u_x_pred = model_x.predict(X_poly)
print("Mean Squared Error:", mean_squared_error(y1, u_x_pred))

/usr/local/lib/python3.10/dist-packages/sklearn/base.py:493:
UserWarning: X does not have valid feature names, but
PolynomialFeatures was fitted with feature names
warnings.warn(

```



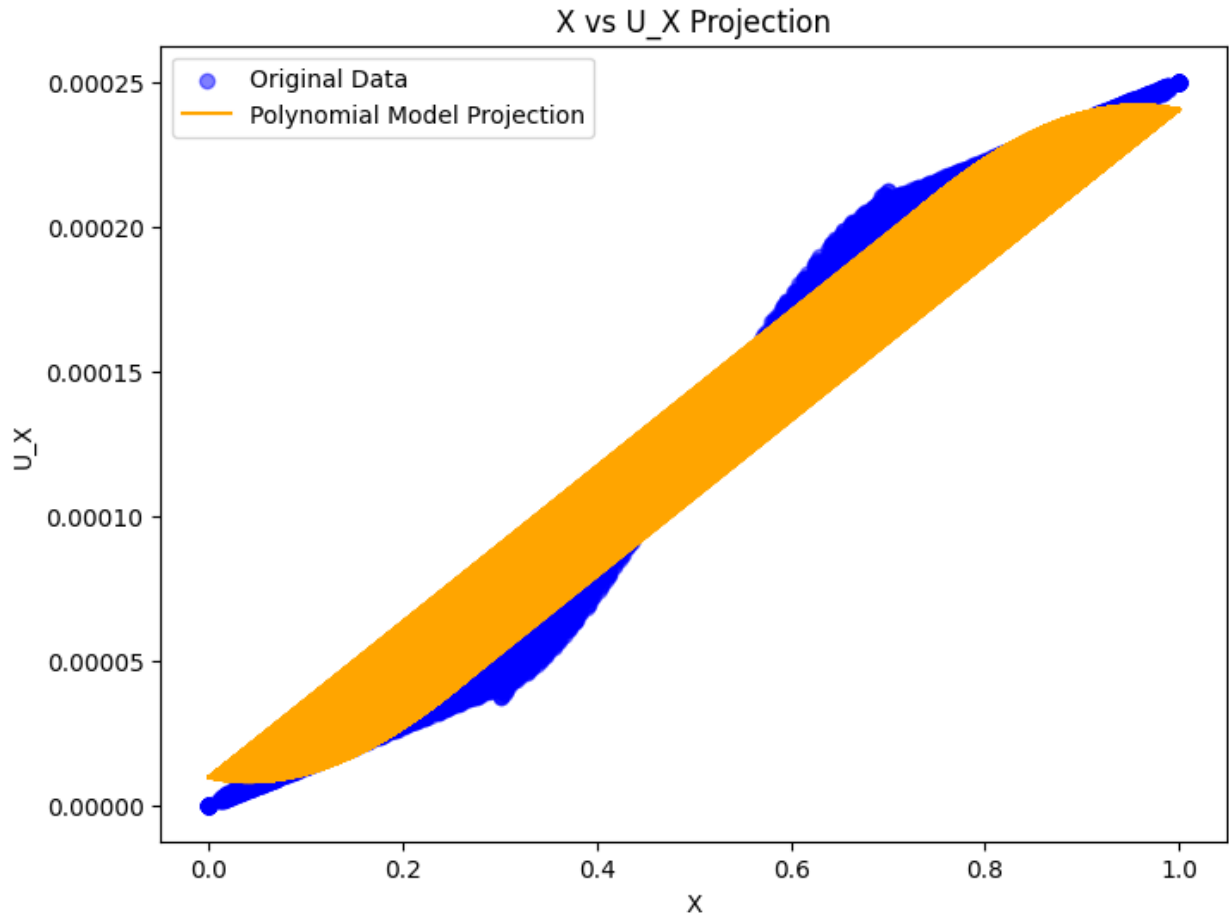
Mean Squared Error: 4.370743975156152e-11

```
# Define a fixed value for y (e.g., the mean of y)
y_fixed = np.full_like(dfx['x'], dfx['y'].mean())

# Create a DataFrame with varying x and fixed y
X_x_projection = pd.DataFrame({'x': dfx['x'], 'y': y_fixed})
X_x_projection_poly = poly.transform(X_x_projection) # Transform for
polynomial terms

# Predict u_y along x-axis using the fixed y value
u_y_x_projection = model_x.predict(X_x_projection_poly)

# Plot the original data projection along the x-axis
plt.figure(figsize=(8, 6))
plt.scatter(dfx['x'], dfx['u_x'], color='blue', alpha=0.5,
label='Original Data')
plt.plot(dfx['x'], u_y_x_projection, color='orange', label='Polynomial
Model Projection')
plt.xlabel('X')
plt.ylabel('U_X')
plt.title('X vs U_X Projection')
plt.legend()
plt.show()
```



```
# Extract terms and construct the polynomial equation string
coefficients_x = model_x.coef_
print(coefficients_x)
intercept_x = model_x.intercept_
print(intercept_x)
terms = poly.get_feature_names_out(['x', 'y'])
equation = f"{intercept_x} " # Start with the intercept

for coef, term in zip(coefficients_x[1:], terms[1:]): # Skip the
first term as it corresponds to the intercept
    equation += f"+ ({coef}) * {term} "

print("Polynomial Regression Equation for u_x:")
print(equation)

[ 0.00000000e+00 -6.84884216e-05  4.52592461e-06  9.05295434e-04
 -8.83532967e-06 -5.30562790e-06 -6.04113774e-04  1.62172312e-06
  6.97569233e-06  1.42521744e-06]
8.460540936082437e-06
Polynomial Regression Equation for u_x:
8.460540936082437e-06 + (-6.848842155234383e-05) * x +
```

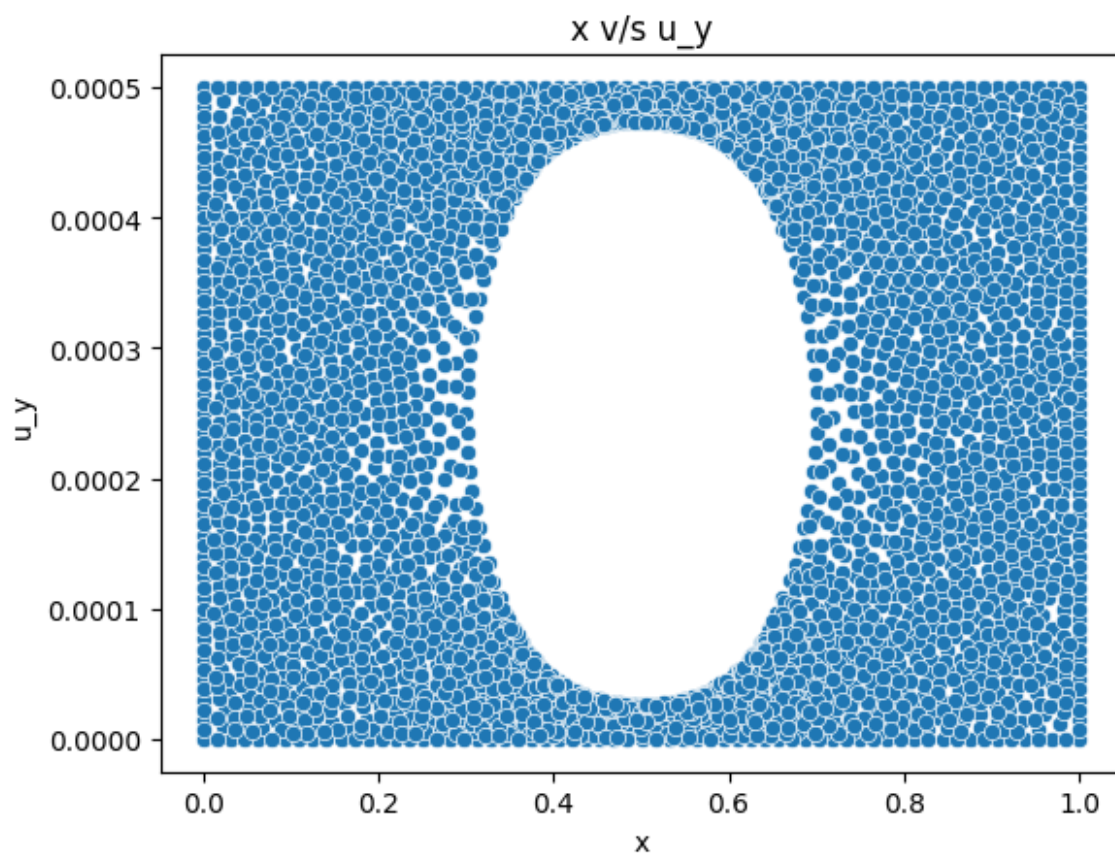
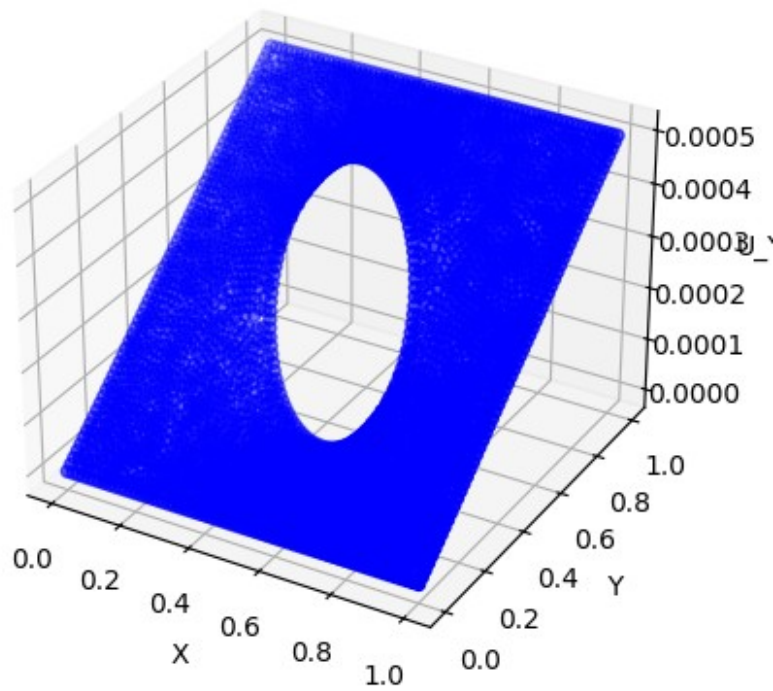
$$(4.525924607056562e-06) * y + (0.0009052954339239371) * x^2 + (-8.835329667708504e-06) * x * y + (-5.305627904812533e-06) * y^2 + (-0.000604113774394459) * x^3 + (1.6217231226933467e-06) * x^2 * y + (6.975692333959068e-06) * x * y^2 + (1.4252174363363996e-06) * y^3$$

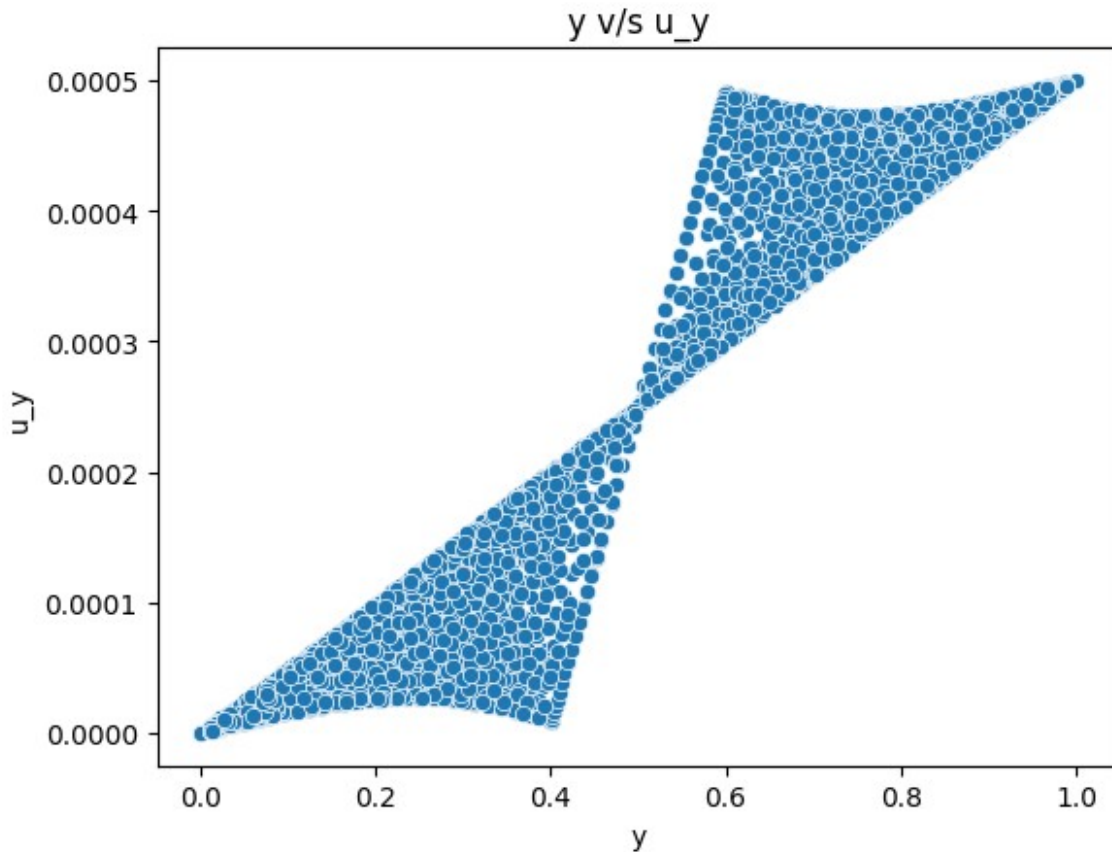
```
x2 = dfy[['x', 'y']]
y2 = dfy['u_y']
fig = plt.figure()
ax = fig.add_subplot(111, projection='3d')
ax.scatter(dfy['x'], dfy['y'], dfy['u_y'], c='b', marker='o')
ax.set_xlabel('X')
ax.set_ylabel('Y')
ax.set_zlabel('U_Y')
plt.title("3D Scatter Plot of X, Y and UY")
plt.show()
```

```
sns.scatterplot(x="x",y="u_y",data=dfy)
plt.title("x v/s u_y")
plt.xlabel("x")
plt.ylabel("u_y")
plt.show()
```

```
sns.scatterplot(x="y",y="u_y",data=dfy)
plt.title("y v/s u_y")
plt.xlabel("y")
plt.ylabel("u_y")
plt.show()
```


3D Scatter Plot of X, Y and UY





```
degree = 3
poly = PolynomialFeatures(degree)
X_poly = poly.fit_transform(x2)

# Fit a linear regression model on the transformed features
model_y = LinearRegression()
model_y.fit(X_poly, y2)

# Predict u_y values for original X
u_y_pred = model_y.predict(X_poly)

# Print model coefficients
print("Polynomial Coefficients:", model_y.coef_)
print("Intercept:", model_y.intercept_)
print("Mean Squared Error:", mean_squared_error(y2, u_y_pred))
coefficients_y = model_y.coef_
intercept_y = model_y.intercept_
terms = poly.get_feature_names_out(['x', 'y'])
equation = f"{intercept_y} " # Start with the intercept

for coef, term in zip(coefficients_y[1:], terms[1:]): # Skip the
first term as it corresponds to the intercept
    equation += f"+ ({coef}) * {term} "
```

```

print("Polynomial Regression Equation for u_y:")
print(equation)

Polynomial Coefficients: [ 0.00000000e+00 -3.70363452e-04 -
2.72410585e-04  3.69608397e-04
 7.47060063e-04  1.82211430e-03  3.08186846e-06 -7.53188828e-04
 6.29740827e-06 -1.21642074e-03]
Intercept: 8.202013844248461e-05
Mean Squared Error: 1.3275583407638332e-09
Polynomial Regression Equation for u_y:
8.202013844248461e-05 + (-0.00037036345175428444) * x + (-
0.00027241058504434164) * y + (0.00036960839708307964) * x^2 +
(0.0007470600625728789) * x y + (0.0018221143010444876) * y^2 +
(3.0818684579309014e-06) * x^3 + (-0.0007531888275400206) * x^2 y +
(6.297408271846958e-06) * x y^2 + (-0.0012164207378863269) * y^3

x_range = np.linspace(dfy['x'].min(), dfy['x'].max(), 100)
y_range = np.linspace(dfy['y'].min(), dfy['y'].max(), 100)
X_grid, Y_grid = np.meshgrid(x_range, y_range)
X_grid_poly = poly.transform(np.c_[X_grid.ravel(), Y_grid.ravel()])
Z_grid = model_y.predict(X_grid_poly).reshape(X_grid.shape)

# Plot the original data and the polynomial plane
fig = plt.figure(figsize=(10, 7))
ax = fig.add_subplot(111, projection='3d')

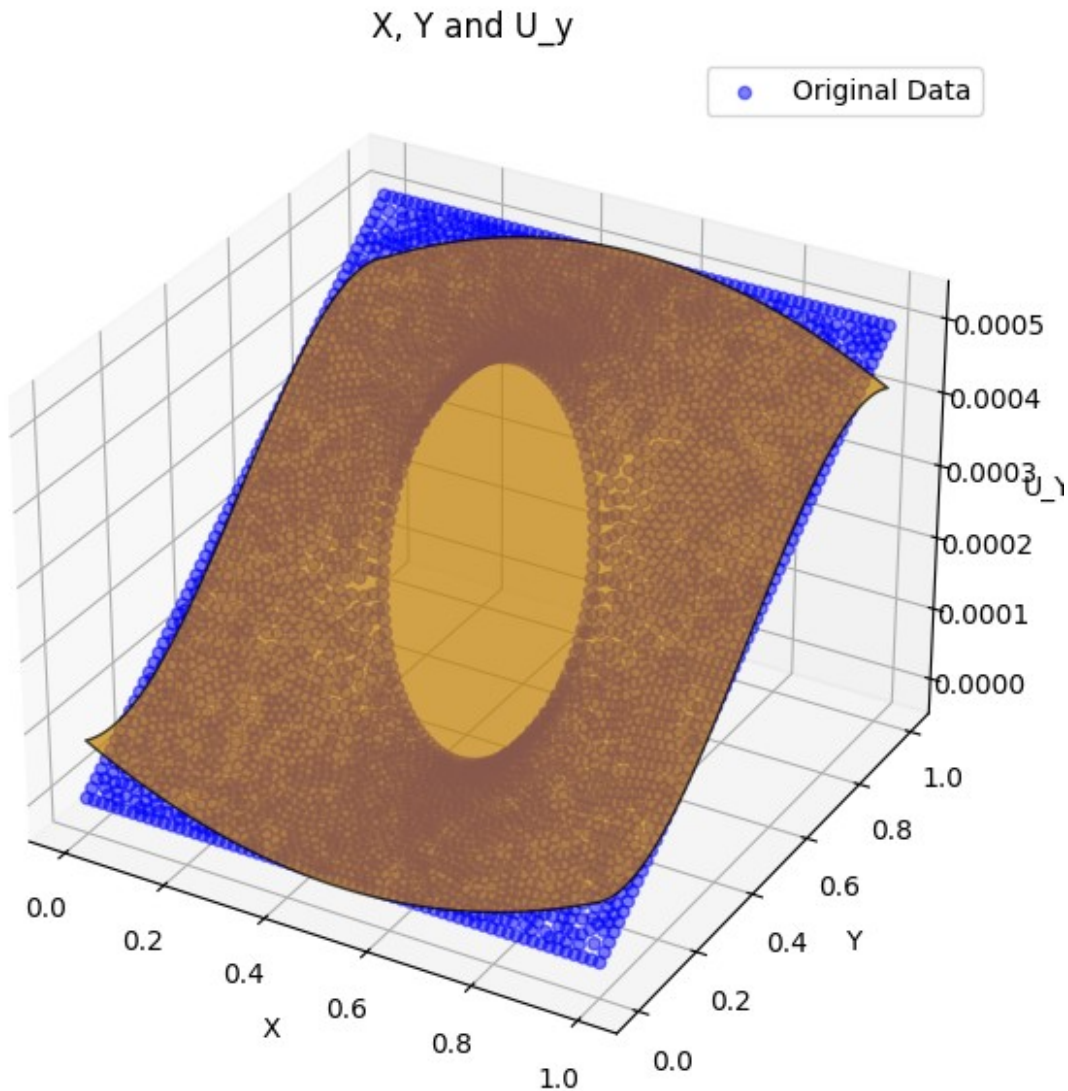
# Plot the original scatter data
ax.scatter(dfy['x'], dfy['y'], dfy['u_y'], color='blue', alpha=0.5,
label="Original Data")

# Plot the polynomial plane
ax.plot_surface(X_grid, Y_grid, Z_grid, color='orange', alpha=0.7,
rstride=100, cstride=100, edgecolor='k')
ax.set_xlabel('X')
ax.set_ylabel('Y')
ax.set_zlabel('U_Y')
ax.set_title('X, Y and U_y')

plt.legend()
plt.show()

/usr/local/lib/python3.10/dist-packages/sklearn/base.py:493:
UserWarning: X does not have valid feature names, but
PolynomialFeatures was fitted with feature names
warnings.warn(

```



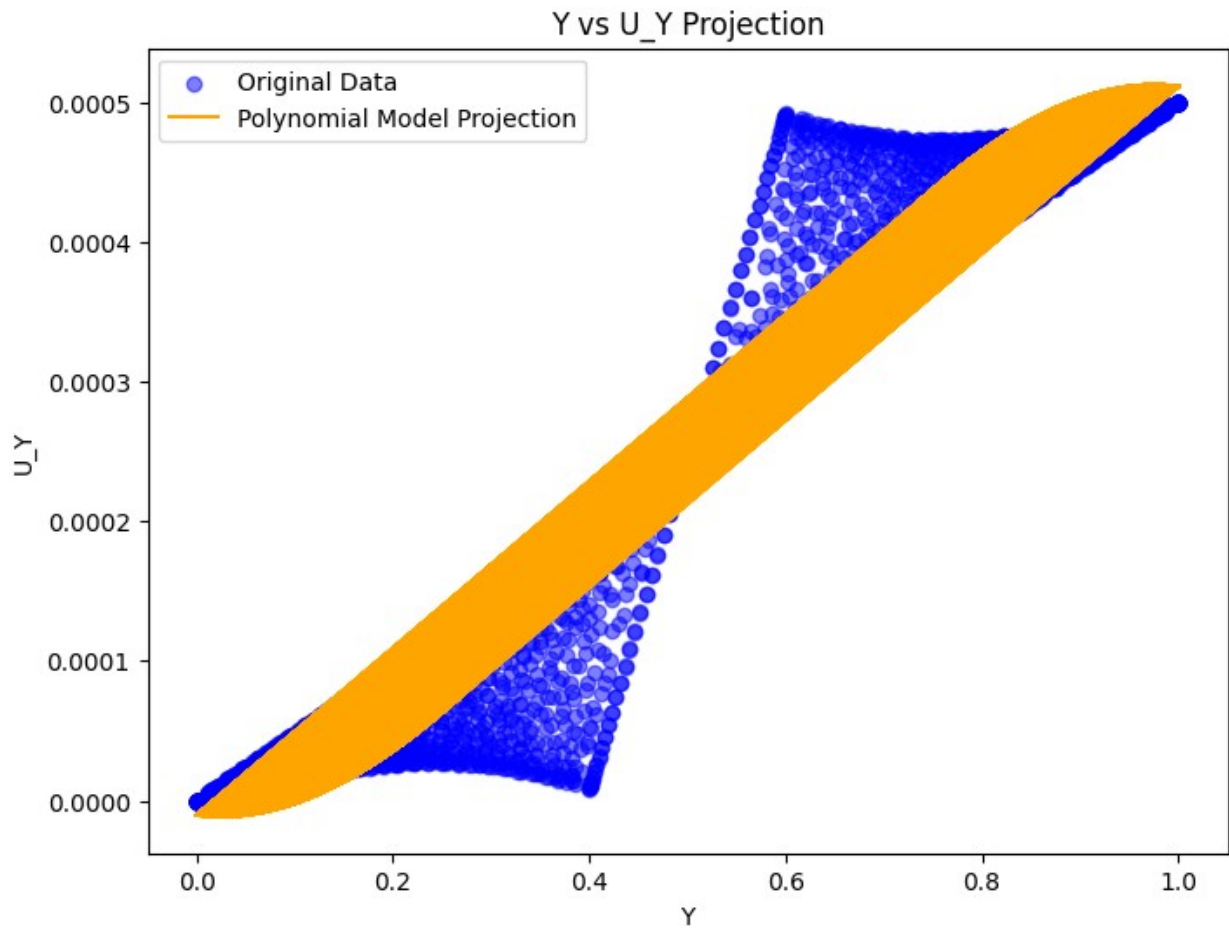
```
x_fixed = np.full_like(dfy['y'], dfy['x'].mean())

# Create a DataFrame with fixed x and varying y
X_y_projection = pd.DataFrame({'x': x_fixed, 'y': dfy['y']})
X_y_projection_poly = poly.transform(X_y_projection) # Transform for
polynomial terms

# Predict u_y along y-axis using the fixed x value
u_y_y_projection = model_y.predict(X_y_projection_poly)

# Plot the original data projection along the y-axis
plt.figure(figsize=(8, 6))
plt.scatter(dfy['y'], dfy['u_y'], color='blue', alpha=0.5,
label='Original Data')
plt.plot(dfy['y'], u_y_y_projection, color='orange', label='Polynomial
Model Projection')
```

```
plt.xlabel('Y')
plt.ylabel('U_Y')
plt.title('Y vs U_Y Projection')
plt.legend()
plt.show()
```



```
from sympy import symbols, diff
x,y = symbols('x y')
ux=(
    intercept_x+
    coefficients_x[1]*x+
    coefficients_x[2]*y+
    coefficients_x[3]*x**2+
    coefficients_x[4]*x*y+
    coefficients_x[5]*y**2+
    coefficients_x[6]*x**3+
    coefficients_x[7]*x**2*y+
    coefficients_x[8]*x*y**2+
    coefficients_x[9]*y**3
```

```

)
print(ux)

-0.000604113774394459*x**3 + 1.62172312269335e-6*x**2*y +
0.000905295433923937*x**2 + 6.97569233395907e-6*x*y**2 -
8.8353296677085e-6*x*y - 6.84884215523438e-5*x + 1.4252174363364e-
6*y**3 - 5.30562790481253e-6*y**2 + 4.52592460705656e-6*y +
8.46054093608244e-6

uy=(
    intercept_y+
    coefficients_y[1]*x+
    coefficients_y[2]*y+
    coefficients_y[3]*x**2+
    coefficients_y[4]*x*y+
    coefficients_y[5]*y**2+
    coefficients_y[6]*x**3+
    coefficients_y[7]*x**2*y+
    coefficients_y[8]*x*y**2+
    coefficients_y[9]*y**3
)
print(uy)

3.0818684579309e-6*x**3 - 0.000753188827540021*x**2*y +
0.00036960839708308*x**2 + 6.29740827184696e-6*x*y**2 +
0.000747060062572879*x*y - 0.000370363451754284*x -
0.00121642073788633*y**3 + 0.00182211430104449*y**2 -
0.000272410585044342*y + 8.20201384424846e-5

exx_1=diff(ux,x)
eyy_1=diff(uy,y)
exx = sum(term for term in exx_1.as_ordered_terms() if term.has(x, y))
eyy = sum(term for term in eyy_1.as_ordered_terms() if term.has(x, y))
print(exx)
print(eyy)

-0.00181234132318338*x**2 + 3.24344624538669e-6*x*y +
0.00181059086784787*x + 6.97569233395907e-6*y**2 - 8.8353296677085e-
6*y
-0.000753188827540021*x**2 + 1.25948165436939e-5*x*y +
0.000747060062572879*x - 0.00364926221365898*y**2 +
0.00364422860208898*y

s_xx_lambda= sum([exx,eyy])
s_yy_lambda= s_xx_lambda
s_xx_mew= 2*exx
s_yy_mew= 2*eyy

print(s_xx_lambda)
print(s_yy_lambda)

```

```

print(s_xx_mew)
print(s_yy_mew)

-0.0025655301507234*x**2 + 1.58382627890806e-5*x*y +
0.00255765093042075*x - 0.00364228652132502*y**2 +
0.00363539327242127*y
-0.0025655301507234*x**2 + 1.58382627890806e-5*x*y +
0.00255765093042075*x - 0.00364228652132502*y**2 +
0.00363539327242127*y
-0.00362468264636675*x**2 + 6.48689249077339e-6*x*y +
0.00362118173569575*x + 1.39513846679181e-5*y**2 - 1.7670659335417e-
5*y
-0.00150637765508004*x**2 + 2.51896330873878e-5*x*y +
0.00149412012514576*x - 0.00729852442731796*y**2 +
0.00728845720417795*y

R_x_1=s_xx_lambda.subs(x,1)
R_x_2=s_xx_mew.subs(x,1)
print(R_x_1,R_x_2)

-0.00364228652132502*y**2 + 0.00365123153521035*y - 7.87922030264432e-
6 1.39513846679181e-5*y**2 - 1.11837668446436e-5*y -
3.50091067100565e-6

from sympy import integrate
R_x_lambda=integrate(R_x_1, (y, 0, 1))
R_x_mew=integrate(R_x_2, (y, 0, 1))
print(R_x_lambda)
print(R_x_mew)

0.000603641040194189
-4.44233253735475e-6

R_y_1=s_yy_lambda.subs(y,1)
R_y_2=s_yy_mew.subs(y,1)
R_y_lambda=integrate(R_y_1, (x, 0, 1))
R_y_mew=integrate(R_y_2, (x, 0, 1))
print(R_y_lambda)
print(R_y_mew)

0.000424674630793363
0.000247461770949882

Reaction = pd.read_csv('/content/reaction_data.csv')
Reaction.head()

{"summary":{"name": "Reaction", "rows": 4, "fields": [{"column": "Reaction", "properties": {"dtype": "string", "num_unique_values": 4, "samples": ["R4", "R2", "R3"]}], "semantic_type":

```

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{"column": "Value", "properties": {"dtype": "number", "std": 135309492.47251204, "min": -126885800.9, "max": 126885800.9, "num_unique_values": 4, "samples": [106597287.3, 126885800.9, -106597287.3]}, "semantic_type": "", "description": ""}, {"column": "Reaction", "properties": {"dtype": "number", "std": 135309492.47251204, "min": -126885800.9, "max": 126885800.9, "num_unique_values": 4, "samples": [106597287.3, 126885800.9, -106597287.3]}, "semantic_type": "", "description": ""}]
n}, {"type": "dataframe", "variable_name": "Reaction"}

R_x=Reaction.iloc[1,1]
R_y=Reaction.iloc[3,1]
C=np.array([R_x,R_y],dtype = float)
print(C)

[1.06597287e+08 1.26885801e+08]

A=np.array([[R_x_lambda,R_x_mew],[R_y_lambda,R_y_mew]],dtype = float)
print(A)

[[ 6.03641040e-04 -4.44233254e-06]
 [ 4.24674631e-04  2.47461771e-04]]

l= np.linalg.solve(A, C)
print(f"Lame's constants are:- {l}")

Lame's constants are:- [1.78114494e+11 2.07082871e+11]

s_xx= l[0]*s_xx_lambda+(l[1]*s_xx_mew)
s_yy= l[0]*s_yy_lambda+(l[1]*s_yy_mew)
from sympy import lambdify
s_x= lambdify((x,y),s_xx)
s_y = lambdify((x,y),s_yy)
e_x= lambdify((x,y),exx)
e_y = lambdify((x,y),eyy)
data['stress_x'] = np.vectorize(s_x)(data['x'], data['y'])
data['stress_y'] = np.vectorize(s_y)(data['x'], data['y'])
data['e_x'] = np.vectorize(e_x)(data['x'], data['y'])
data['e_y'] = np.vectorize(e_y)(data['x'], data['y'])

data.head()

{"summary":{"name": "data", "rows": 3877, "fields": [{"column": "x", "properties": {"dtype": "number", "std": 0.29956252910327485, "min": 0.0, "max": 1.0, "num_unique_values": 3623, "samples": [0.1261502602372457, 0.2118536552724418]}, "semantic_type": "", "description": ""}, {"column": "y", "properties": {"dtype": "number", "std": 0.2990539284472939, "min": 0.0, "max": 1.0, "num_unique_values": 3623, "samples": [0.1261502602372457, 0.2118536552724418]}}, {"column": "Reaction", "properties": {"dtype": "number", "std": 135309492.47251204, "min": -126885800.9, "max": 126885800.9, "num_unique_values": 4, "samples": [106597287.3, 126885800.9, -106597287.3]}, "semantic_type": "", "description": ""}]}

```



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{"min": 0.0, "max": 1.0, "num_unique_values": 3599, "samples": [0.978615252350456, 0.0629078544311327, 0.6518433923214456], "semantic_type": "", "description": "", "column": "u_x", "properties": {"dtype": "number", "std": 8.76668755251157e-05, "min": 0.0, "max": 0.00025, "num_unique_values": 3749, "samples": [0.0001899880142324, 0.0002078897079883, 0.0001959290626733], "semantic_type": "", "description": "", "column": "u_y", "properties": {"dtype": "number", "std": 0.00017773824527321313, "min": 0.0, "max": 0.0005, "num_unique_values": 3749, "samples": [2.8615189560658114e-05, 0.000124605793524, 6.456947463821828e-05], "semantic_type": "", "description": "", "column": "stress_x", "properties": {"dtype": "number", "std": 102039047.44935083, "min": -2128381.9687199593, "max": 455883453.03339076, "num_unique_values": 3877, "samples": [325707655.10467905, 374467589.65642756, 361902141.43790364], "semantic_type": "", "description": "", "column": "stress_y", "properties": {"dtype": "number", "std": 171798527.209521, "min": -3941727.8274259567, "max": 709113021.2813777, "num_unique_values": 3877, "samples": [301494922.0285871, 673689720.8464397, 601723624.7294936], "semantic_type": "", "description": "", "column": "e_x", "properties": {"dtype": "number", "std": 0.00013845097691847017, "min": -2.8708962527433496e-06, "max": 0.0004522101031280899, "num_unique_values": 3877, "samples": [0.00043629645305618374, 0.00031903813033681556, 0.0003358868454118599], "semantic_type": "", "description": "", "column": "e_y", "properties": {"dtype": "number", "std": 0.000281138060976661, "min": -6.128764967142032e-06, "max": 0.001068086451726443, "num_unique_values": 3877, "samples": [0.0003778349952341343, 0.0010415076651478154, 0.0009149339726490342], "semantic_type": "", "description": ""}}, "type": "dataframe", "variable_name": "data"}

```

```

plt.figure(figsize=(10, 6))
contour = plt.tricontourf(data['x'], data['y'], data['stress_x'],
levels=20, cmap="jet")

```

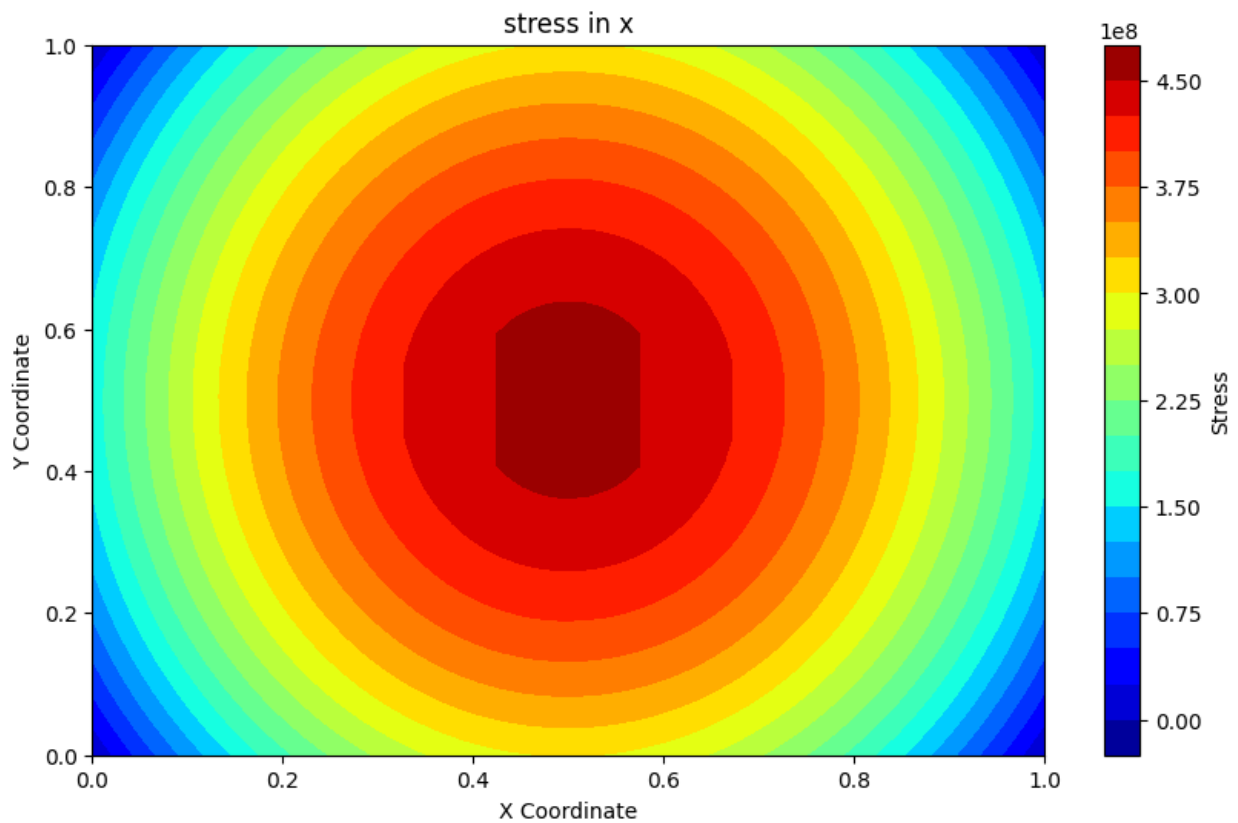
```

# Step 2: Add a color bar for reference
cbar = plt.colorbar(contour)
cbar.set_label("Stress")

# Optional: Add labels, title, etc.
plt.xlabel("X Coordinate")
plt.ylabel("Y Coordinate")
plt.title("stress in x")

plt.show()

```



```

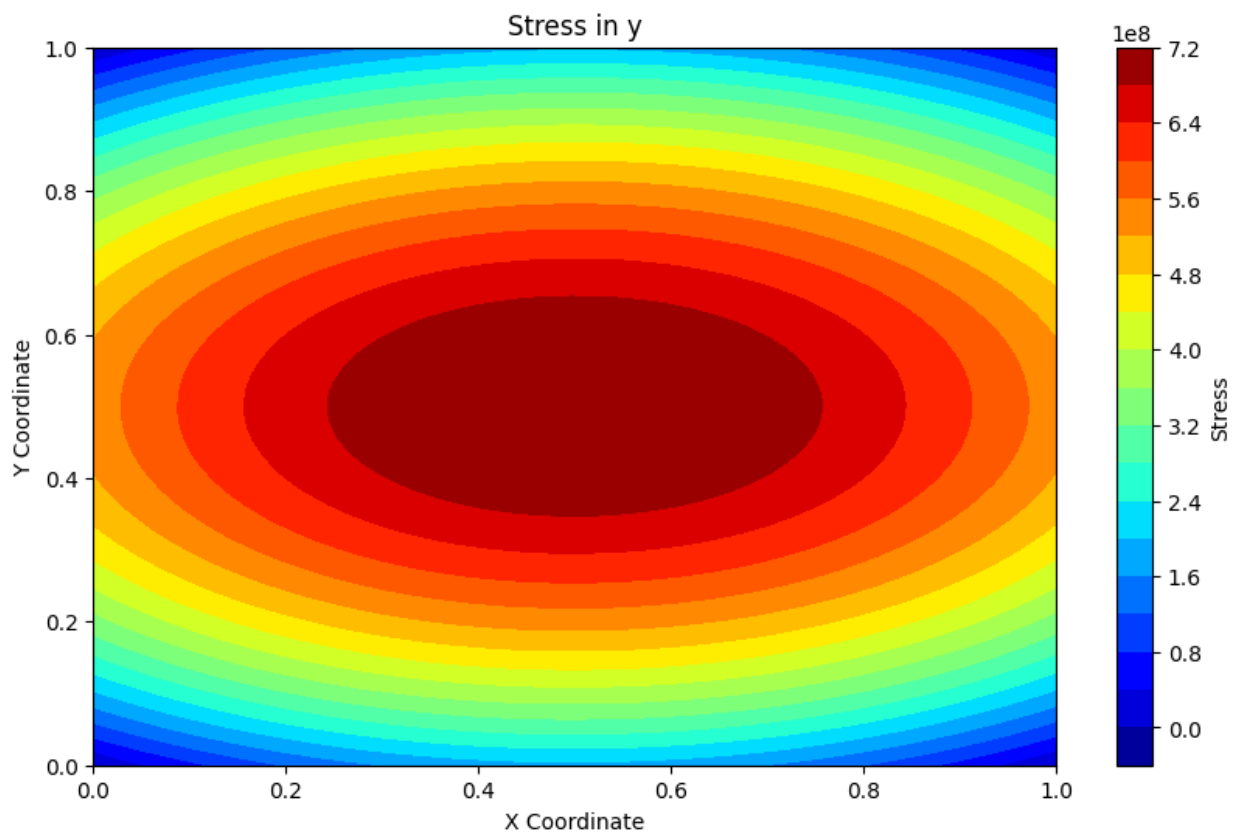
plt.figure(figsize=(10, 6))
contour = plt.tricontourf(data['x'], data['y'], data['stress_y'],
levels=20, cmap="jet")

# Step 2: Add a color bar for reference
cbar = plt.colorbar(contour)
cbar.set_label("Stress")

# Optional: Add labels, title, etc.
plt.xlabel("X Coordinate")
plt.ylabel("Y Coordinate")
plt.title("Stress in y")

```

```
plt.show()
```



```
Txy=(l[1])*(diff(ux,y)+diff(uy,x))
T_xy=lambdify((x,y),Txy)
data['Txy'] = np.vectorize(T_xy)(data['x'], data['y'])
data.head()

{"summary":{"\n  \"name\": \"data\", \n  \"rows\": 3877, \n  \"fields\": [\n    {\n      \"column\": \"x\", \n      \"properties\": {\n        \"dtype\": \"number\", \n        \"std\": 0.29956252910327485, \n        \"min\": 0.0, \n        \"max\": 1.0, \n        \"num_unique_values\": 3623, \n        \"samples\": [\n          0.0508864939110139, \n          0.1261502602372457, \n          0.2118536552724418\n        ], \n        \"semantic_type\": \"\", \n        \"description\": \"\"\n      }\n    }, \n    {\n      \"column\": \"y\", \n      \"properties\": {\n        \"dtype\": \"number\", \n        \"std\": 0.2990539284472939, \n        \"min\": 0.0, \n        \"max\": 1.0, \n        \"num_unique_values\": 3599, \n        \"samples\": [\n          0.978615252350456, \n          0.0629078544311327, \n          0.6518433923214456\n        ], \n        \"semantic_type\": \"\", \n        \"description\": \"\"\n      }\n    }, \n    {\n      \"column\": \"u_x\", \n      \"properties\": {\n        \"dtype\": \"number\", \n        \"std\": 8.76668755251157e-05, \n
```



```

levels=20, cmap="jet")

# Step 2: Add a color bar for reference
cbar = plt.colorbar(contour)
cbar.set_label("Stress")

# Optional: Add labels, title, etc.
plt.xlabel("X Coordinate")
plt.ylabel("Y Coordinate")
plt.title("Txy")

plt.show()

```

