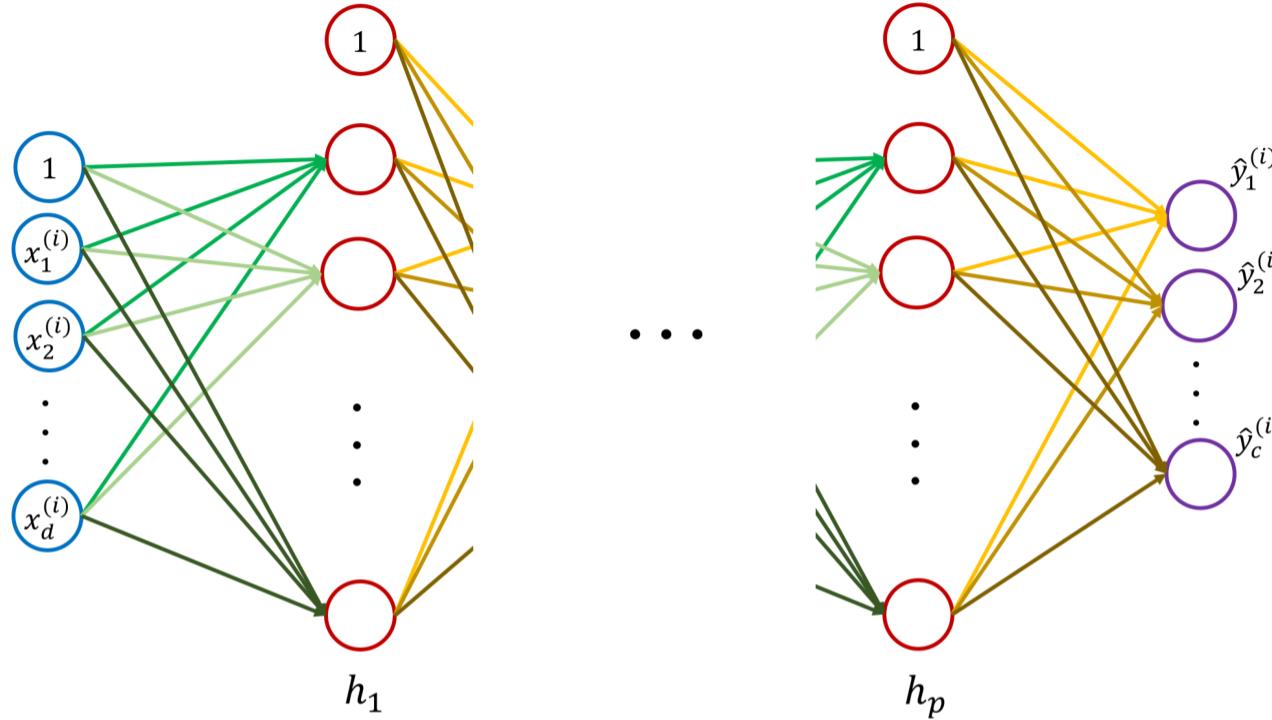


Machine Learning

15 – Neural Networks and Deep Learning

November 04, 2022

Multi-Layered Perceptrons



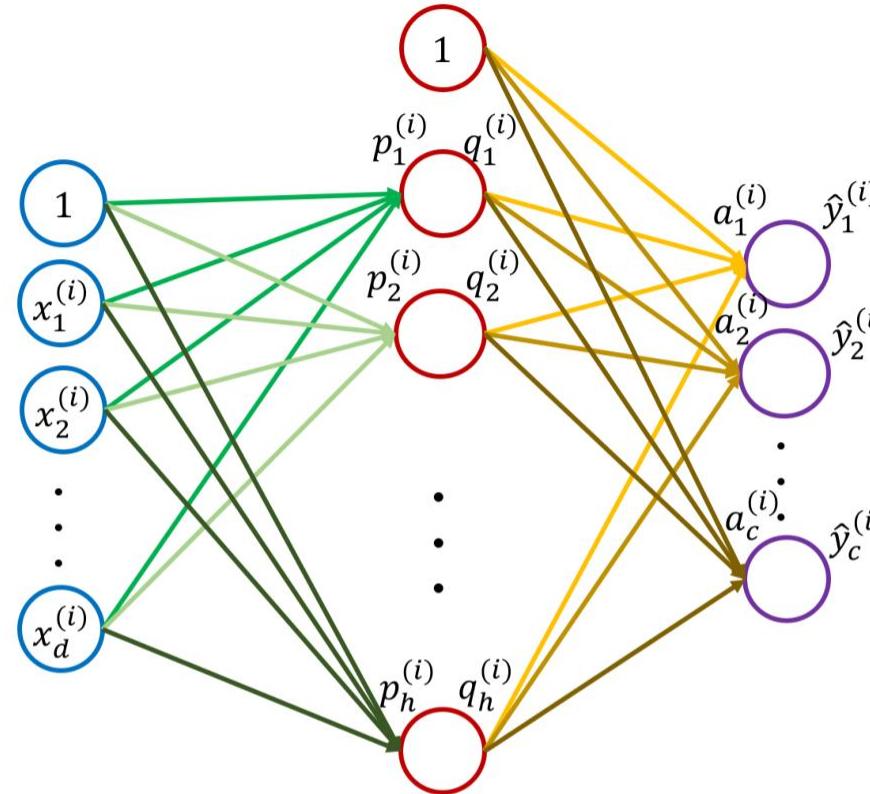
A Multi-Layered Perceptron with p number of hidden layers can be represented as,

$$\hat{\mathbf{y}} = f_{p+1}(\dots f_2(f_1(\mathbf{x})))$$

where each layer is an affine transformation followed by a possible non-linear transformation σ ,

$$f_i(\mathbf{z}) = \sigma((W^i)^T \mathbf{z} + b^i)$$

Motivation: Deep Neural Networks



A single hidden layer network can be represented as,

$$\mathbf{q} = f_1(\mathbf{x}), \quad \hat{\mathbf{y}} = f_2(\mathbf{q})$$

or,

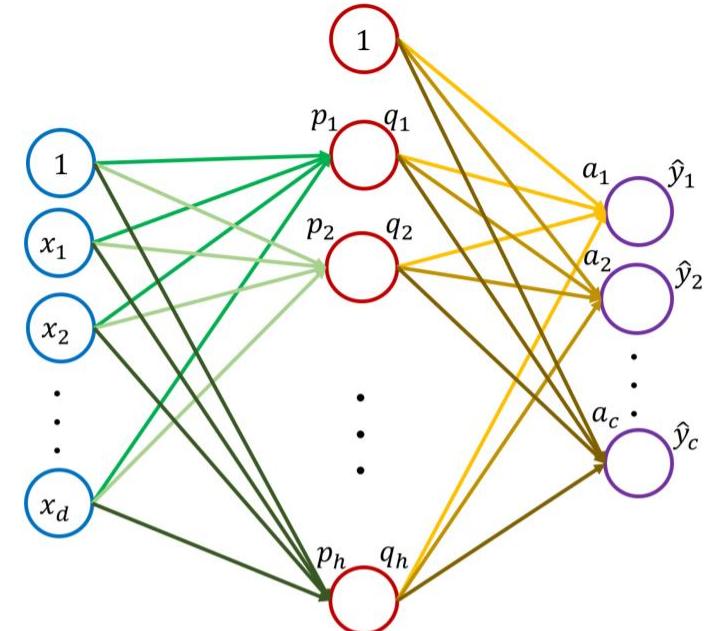
$$\hat{\mathbf{y}} = f_2(f_1(\mathbf{x}))$$

Multi-Layered Perceptron

Feedforward:

$$p_j = \sum_{l=1}^d W_{lj}^{(1)} x_l + b_j^{(1)}, \quad q_j = \sigma(p_j)$$

$$a_k = \sum_{l'=1}^h W_{l'k}^{(2)} q_{l'} + b_k^{(2)}, \quad \hat{y}_k = \sigma(a_k), \quad J = \frac{1}{2} \sum_{k=1}^c (t_k - \hat{y}_k)^2$$



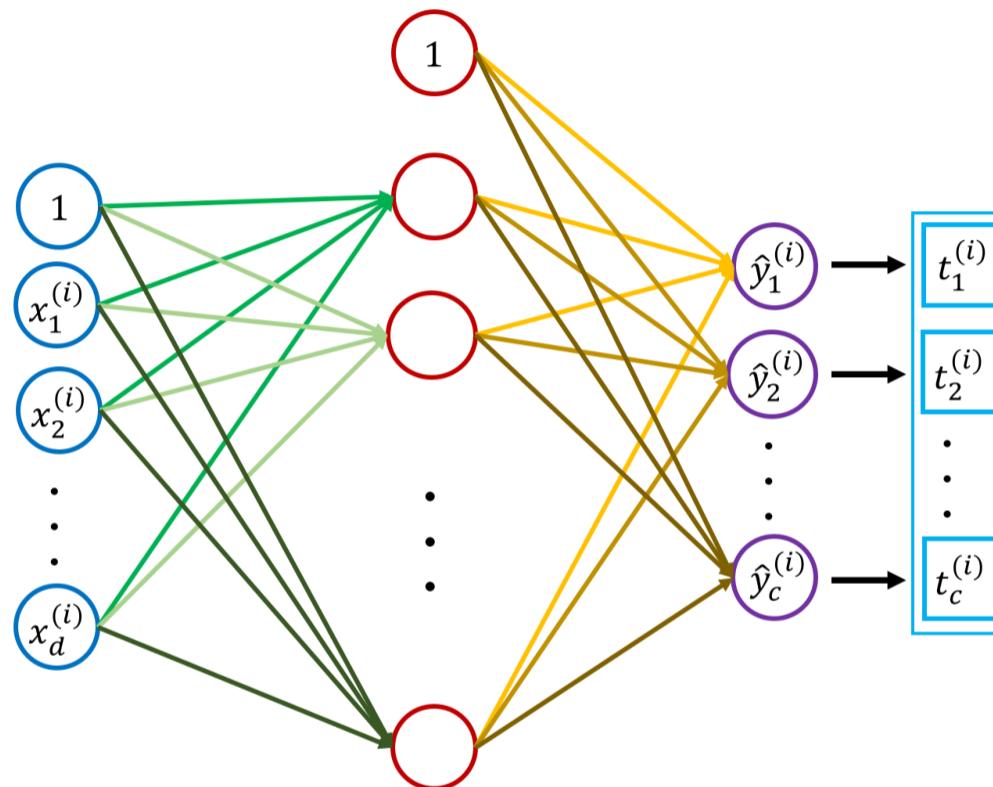
Backpropagation:

$$\frac{\partial}{\partial W_{l'k}^{(2)}} J = -(t_k - \hat{y}_k) \hat{y}_k (1 - \hat{y}_k) q_{l'}, \quad \frac{\partial}{\partial b_k^{(2)}} J = -(t_k - \hat{y}_k) \hat{y}_k (1 - \hat{y}_k),$$

$$\frac{\partial}{\partial W_{lj}^{(1)}} J = \sum_{k=1}^c \left[-(t_k - \hat{y}_k) \hat{y}_k (1 - \hat{y}_k) W_{jk}^{(2)} \right] q_j (1 - q_j) x_l,$$

$$\frac{\partial}{\partial b_j^{(1)}} J = \sum_{k=1}^c \left[-(t_k - \hat{y}_k) \hat{y}_k (1 - \hat{y}_k) W_{jk}^{(2)} \right] q_j (1 - q_j).$$

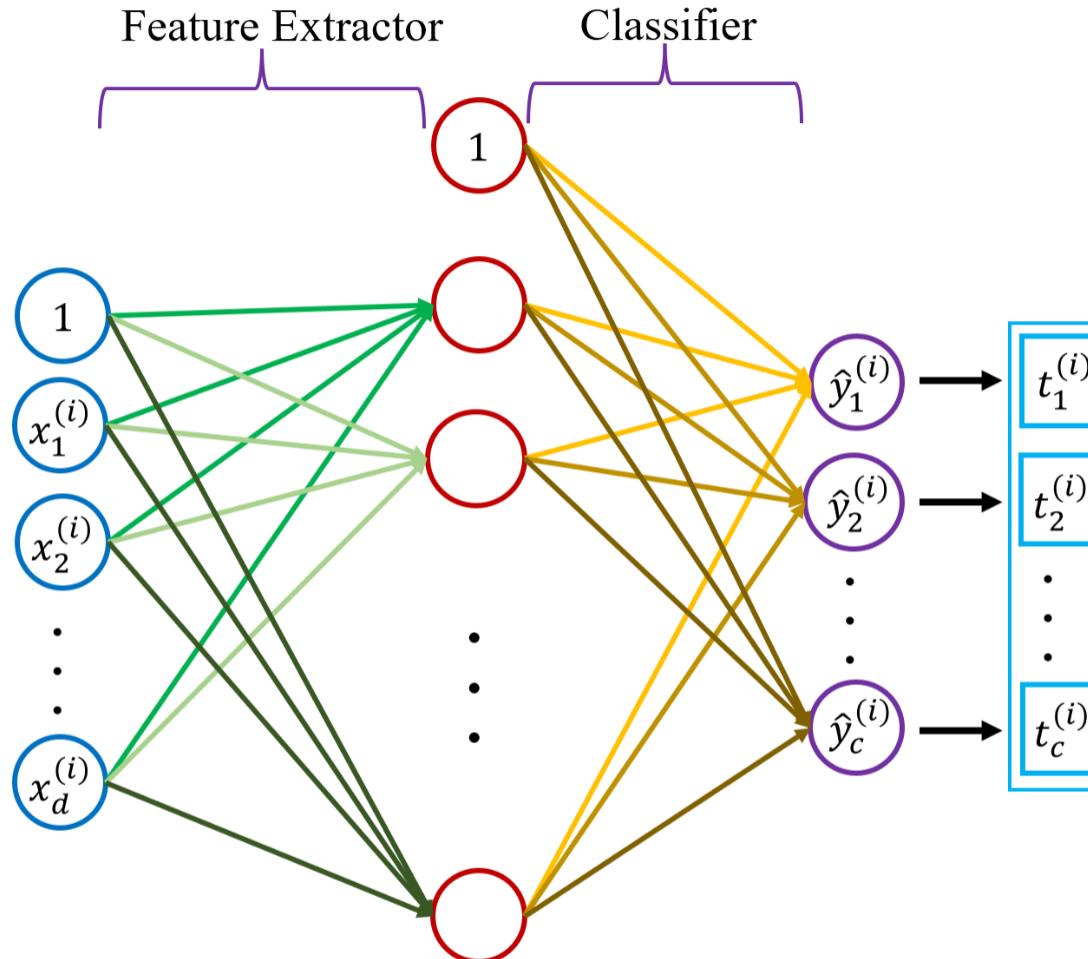
Mult-Layered Perceptron for Classification



For each data instance $\mathbf{x}^{(i)}$, the MLP estimates a vector $\hat{\mathbf{y}}^{(i)}$, and compares it with the ground truth one-hot vector $\mathbf{t}^{(i)}$.

Several loss functions are available that can be used: MSE, CE, ...

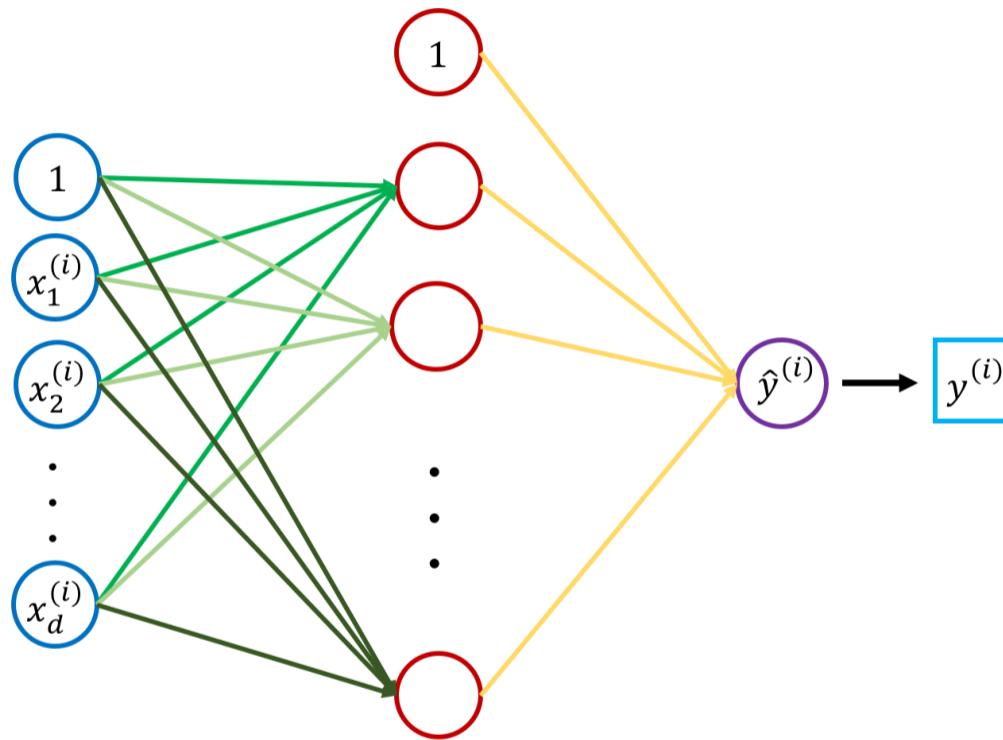
Multi-Layered Perceptron for Classification



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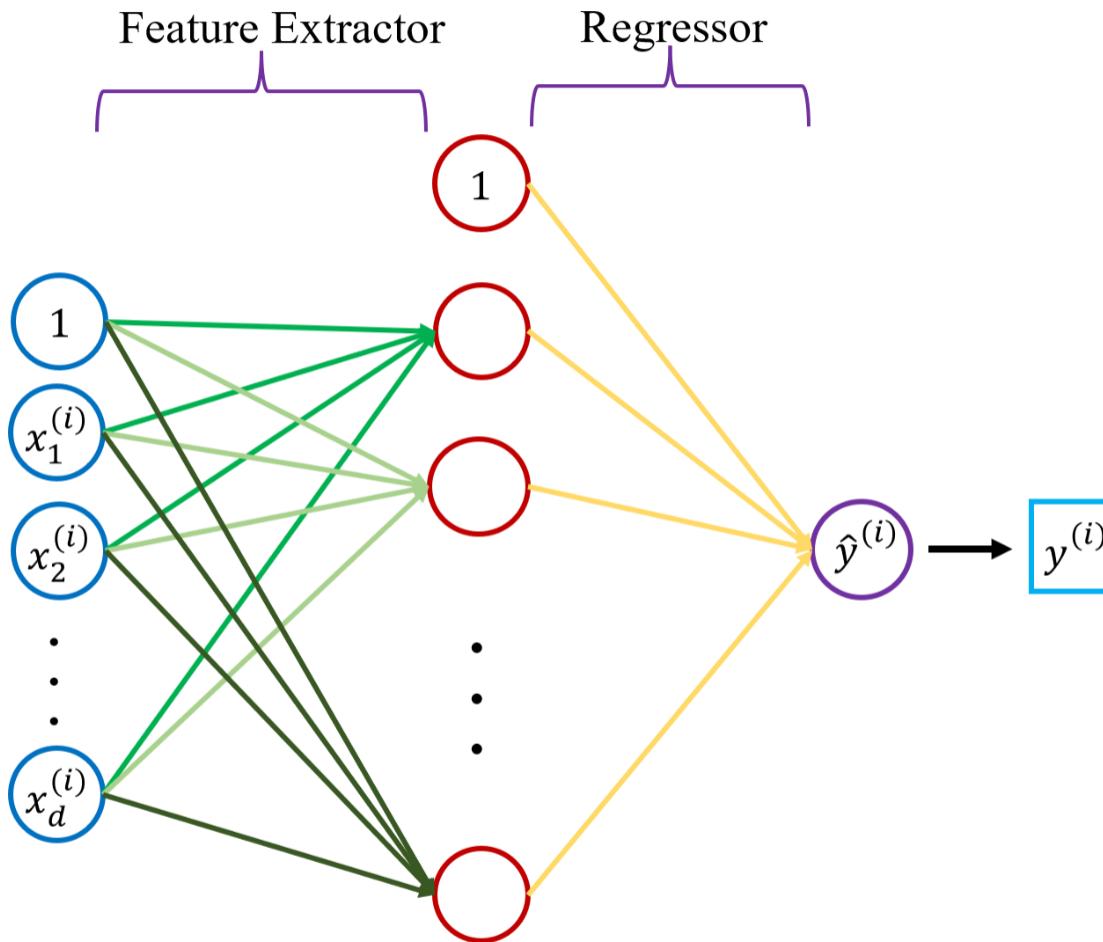
Several loss functions are available that can be used: MSE, CE, ...

Multi-Layered Perceptron for Regression



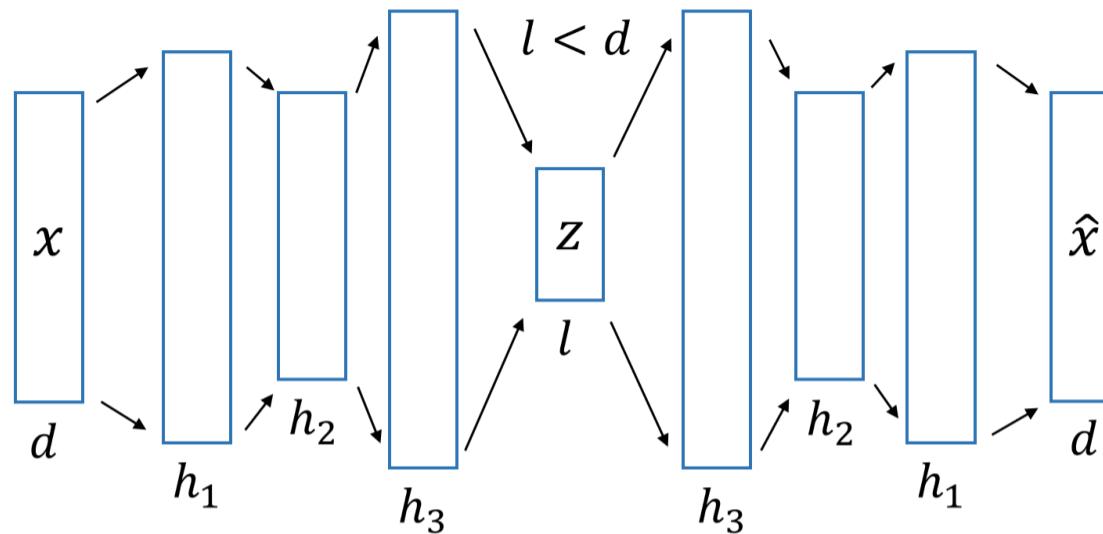
For each data instance $\mathbf{x}^{(i)}$, the MLP estimates a target value $\hat{y}^{(i)}$, and compares it with the ground truth target $y^{(i)}$.

Multi-Layered Perceptron for Regression



For each data instance $\mathbf{x}^{(i)}$, the MLP estimates a target value $\hat{y}^{(i)}$, and compares it with the ground truth target $y^{(i)}$.

Mult-Layered Perceptron for Dimension Reduction: Autoencoders

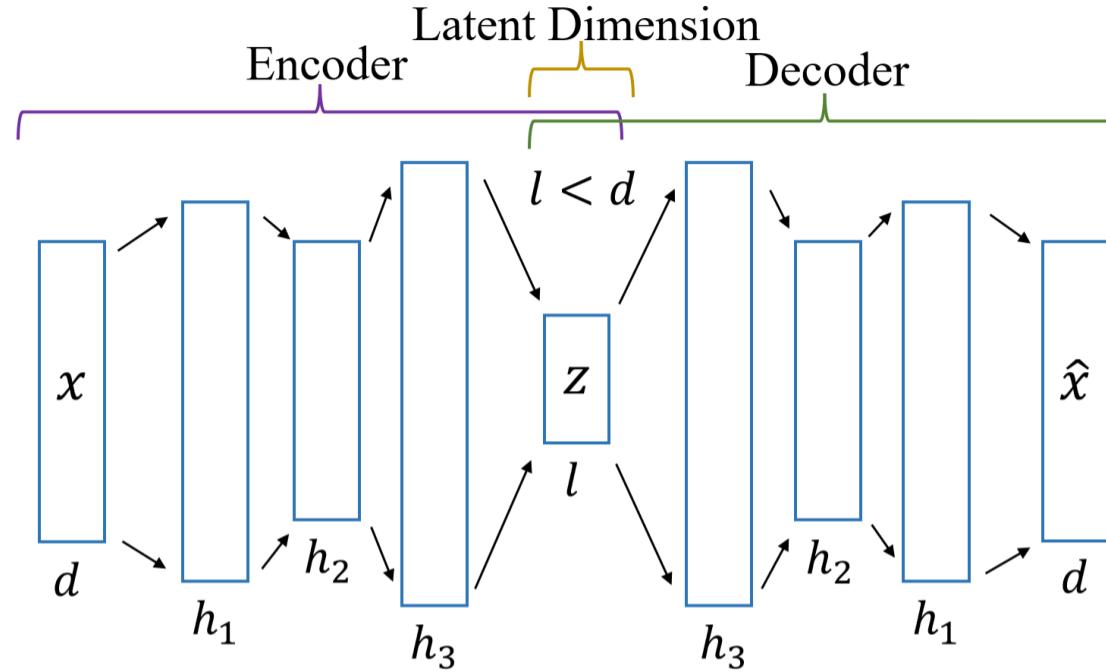


Each data instance $\mathbf{x}^{(i)} \in \mathbb{R}^d$ is mapped by an *encoder network* to a lower dimensional latent vector $\mathbf{z}^{(i)} \in \mathbb{R}^l$, $l < d$. A *decoder network* maps the latent vector $\mathbf{z}^{(i)}$ back to the original dimension $\hat{\mathbf{x}}^{(i)}$. [MSE / CE loss can be used]

Reproducing the data instances makes the autoencoder network learn to:

- ▶ Map each data instance $\hat{\mathbf{x}}^{(i)}$ to a unique $\mathbf{z}^{(i)}$.
- ▶ Map similar data instances close to each other in the latent space.

Multi-Layered Perceptron for Dimension Reduction: Autoencoders

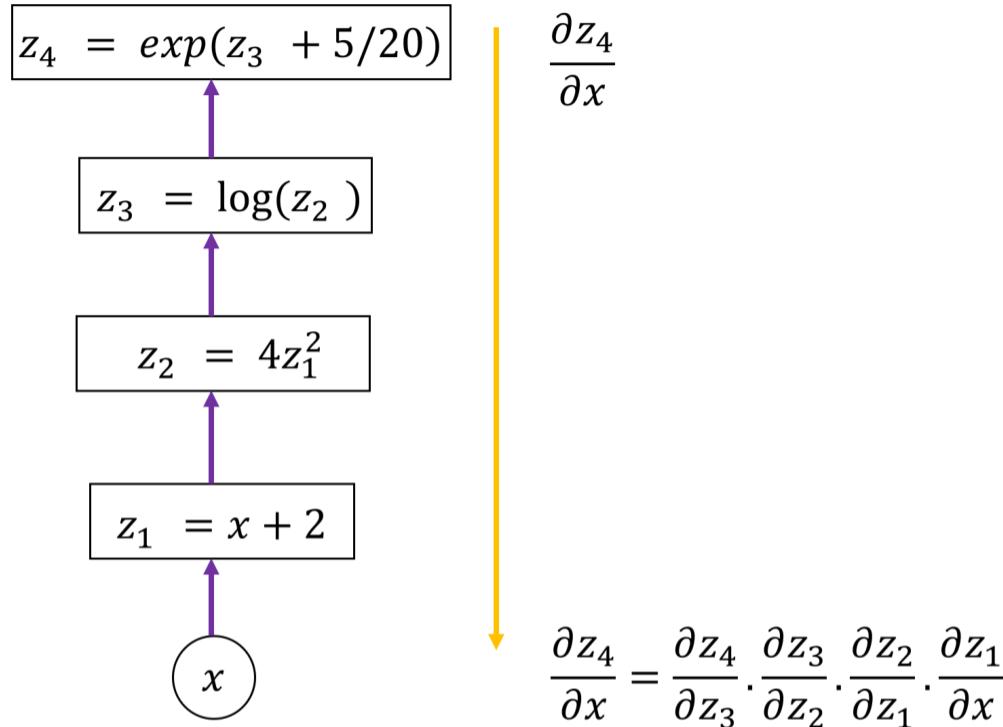


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Reproducing the data instances makes the autoencoder network learn to:

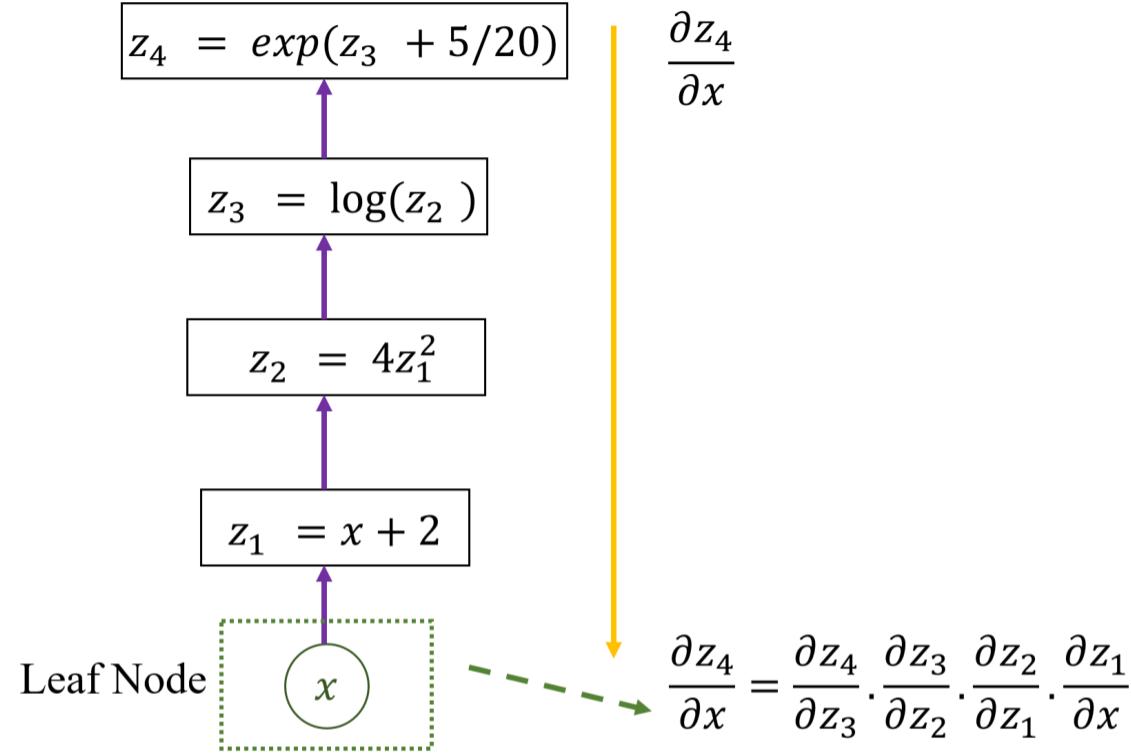
- ▶ Map each data instance $\hat{\mathbf{x}}^{(i)}$ to a unique $\mathbf{z}^{(i)}$.
- ▶ Map similar data instances close to each other in the latent space.

Implementing Neural Networks: Automatic Differentiation



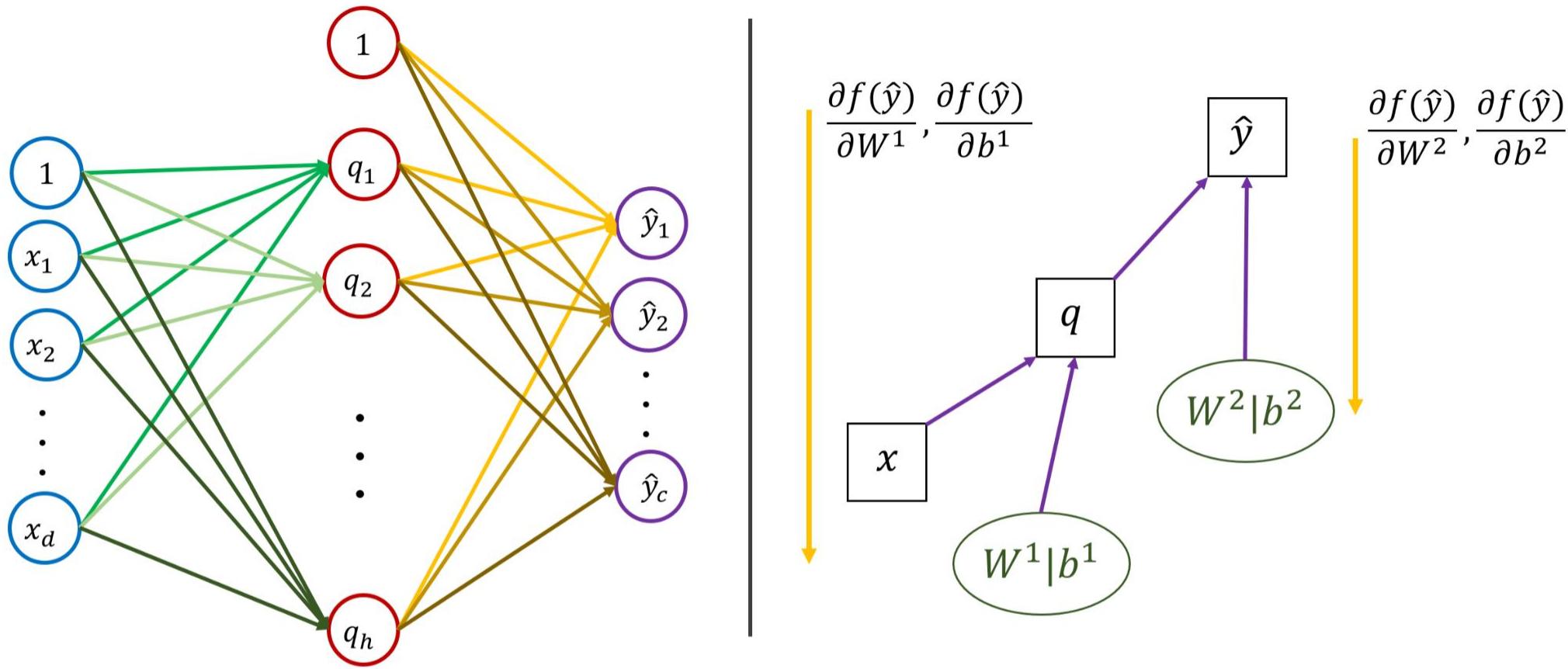
- ▶ Deep Learning libraries keep track of a series of operations that occur on a variable in the form of a **computational graph**.
- ▶ At the end of the series of operations, the gradient with respect to the initial variable can be automatically computed.

Implementing Neural Networks: Automatic Differentiation



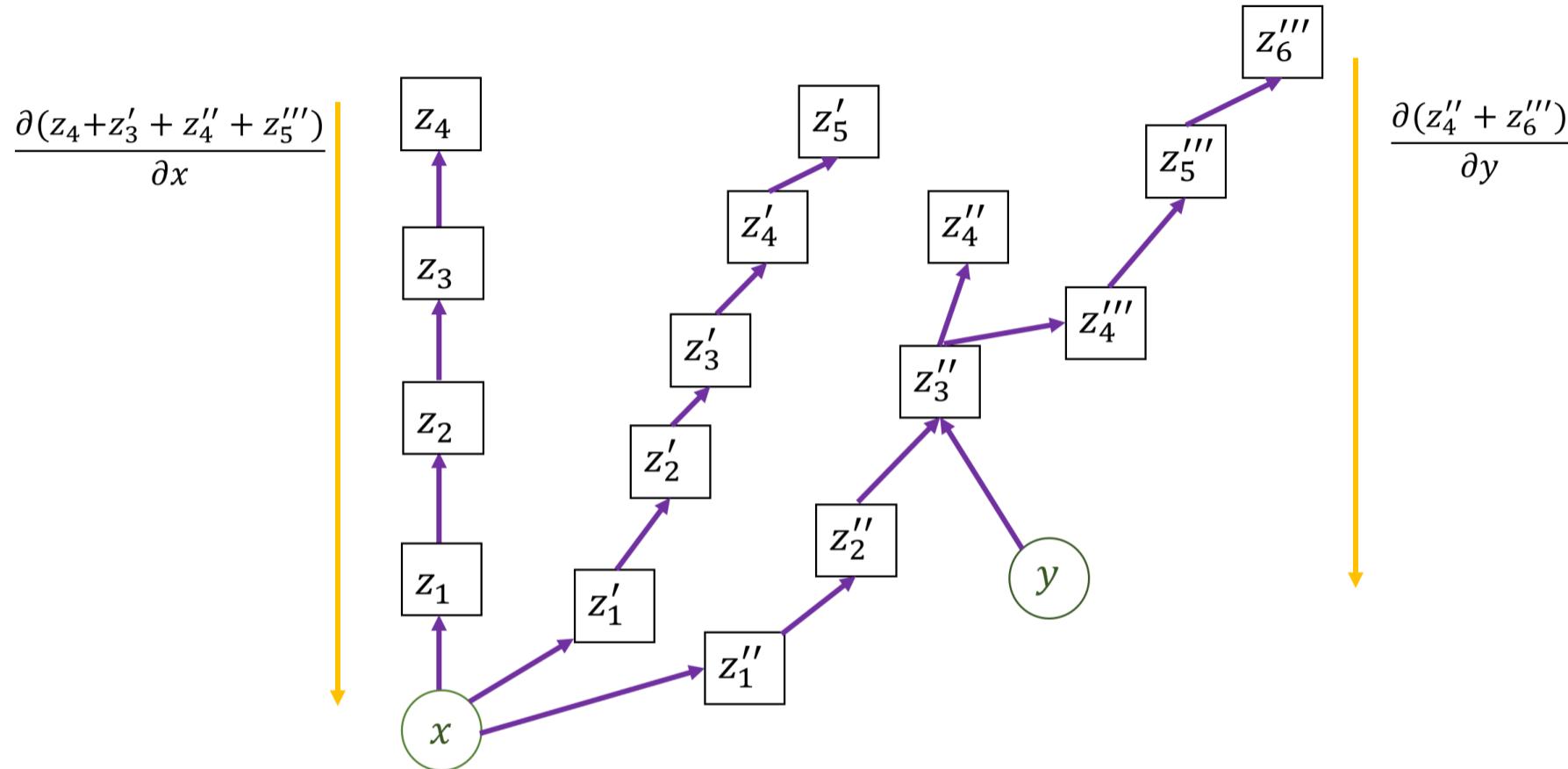
- ▶ Deep Learning libraries keep track of all operations that occur on a variable in the form of a **computational graph**.
- ▶ At the end of the series of operations, the gradient with respect to **any leaf variable** of the computational graph can be automatically computed.

Automatic Differentiation for MLPs



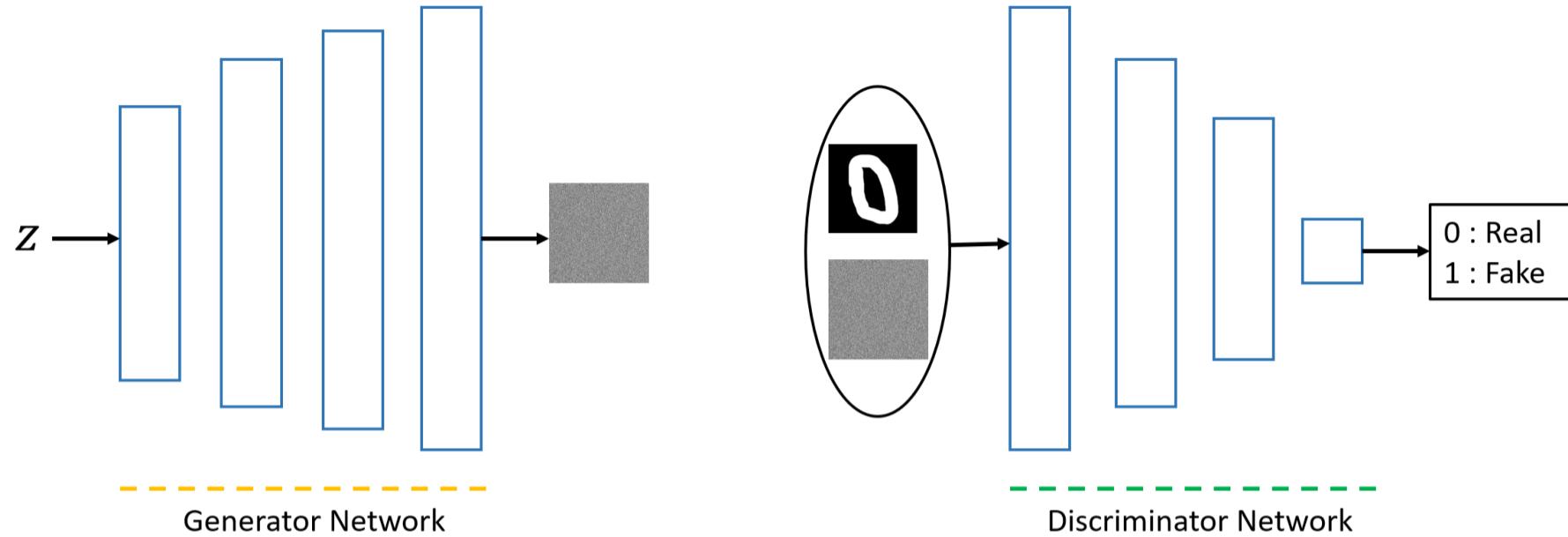
- ▶ The leaves of the computational graph are the network variables $W^{(1)}, b^{(1)}, W^{(2)}, b^{(2)}$.
- ▶ The gradients of the leaves with respect to any function of \hat{y} (such as any loss function) can be automatically computed.

Automatic Differentiation



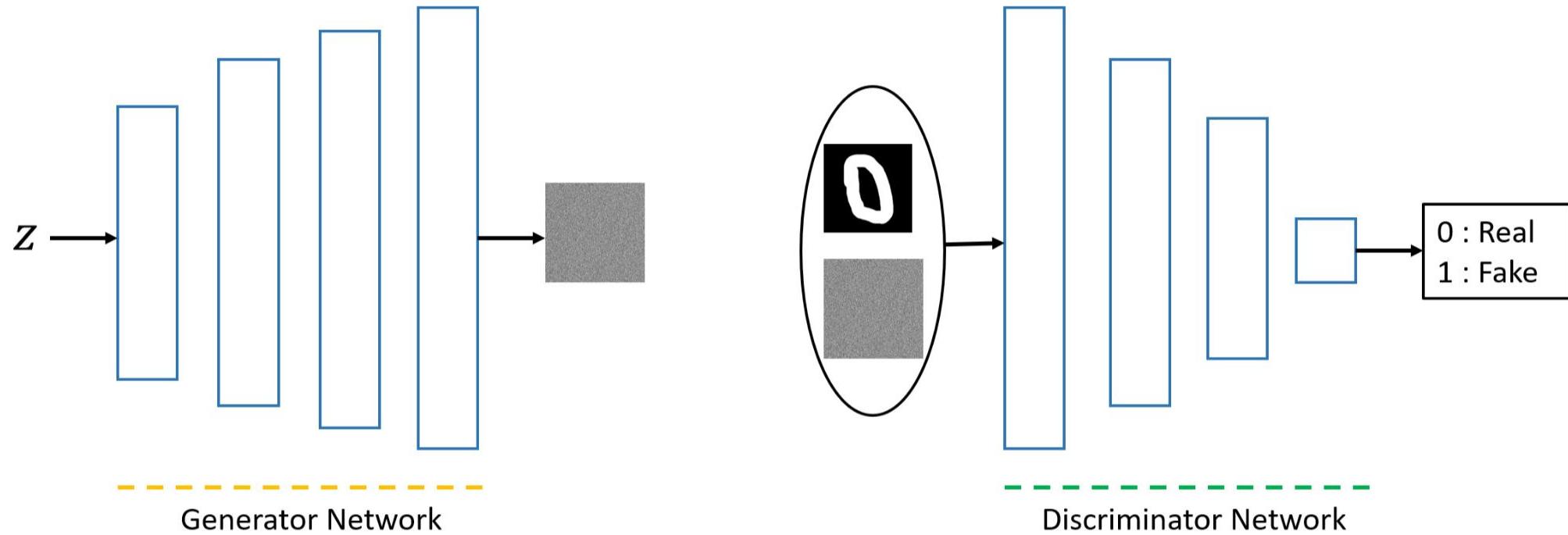
- ▶ In general, automatic differentiation can be done for any number of leaves, along any number of paths.
- ▶ The gradients along only some of the paths can also be computed.

Estimating data distributions: Generative Adversarial Networks



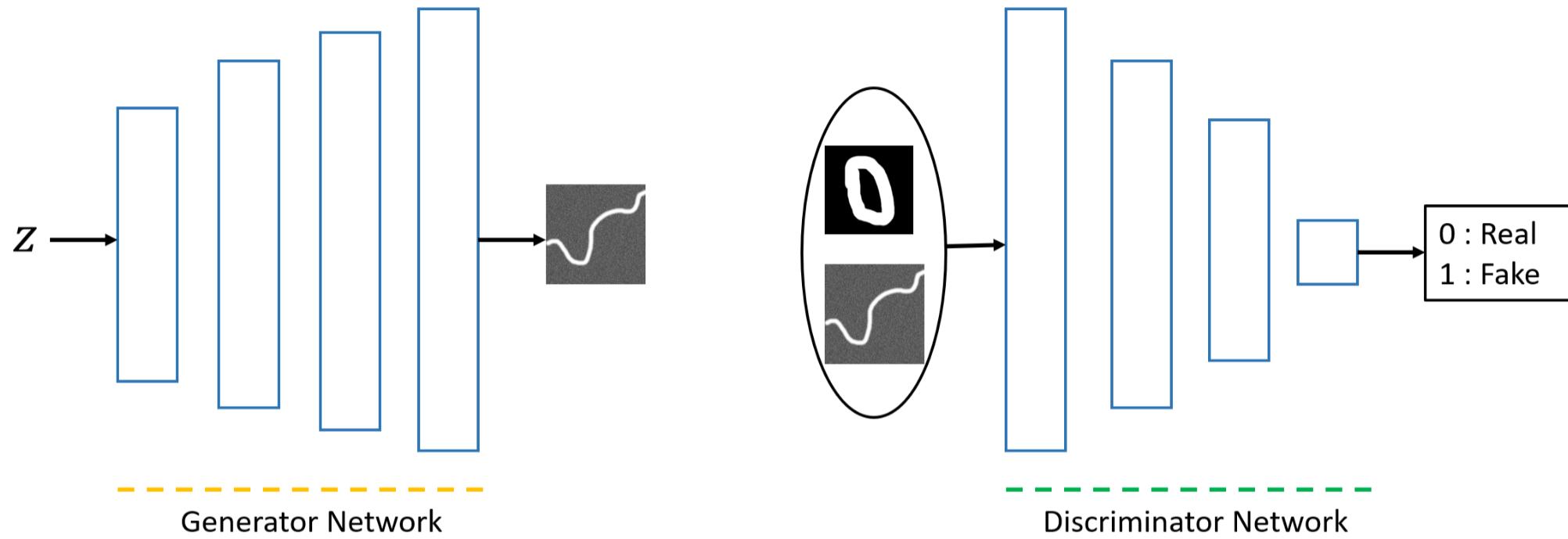
- ▶ We wish to estimate the distribution of the data p_{data} using a Generator Network which follows a distribution p_G ; the learning task is to obtain $p_G \approx p_{data}$.
- ▶ The Generator learns the data distribution by mapping $z \in \mathbb{R}^l$ to the data space.
- ▶ A Discriminator network is trained to discriminated between the (fake) data generated by the Generator, and data from a real data set.

Generative Adversarial Networks



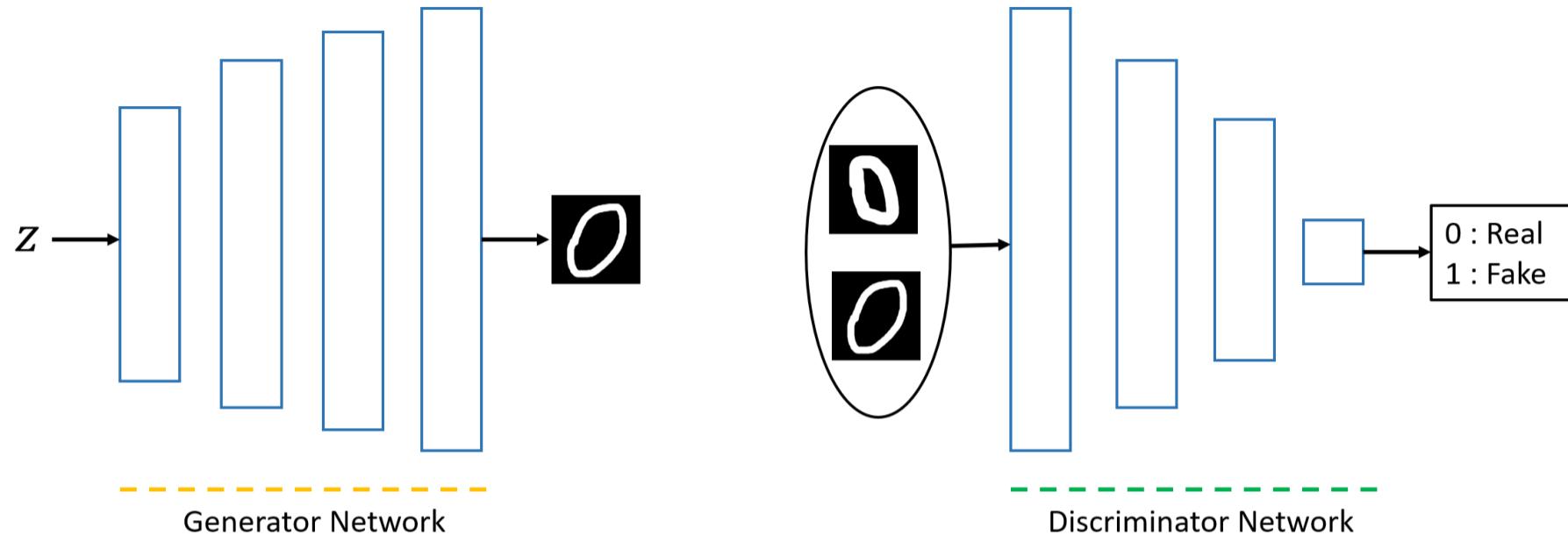
- ▶ The Discriminator is trained for k_1 iterations, so that it learns to properly discriminate between real and generated images.

Generative Adversarial Networks



- ▶ The Discriminator is trained for k_1 iterations, so that it learns to properly discriminate between real and generated images.
- ▶ The Generator is trained for k_2 iterations, so that it learns to fool the Discriminator.

Generative Adversarial Networks



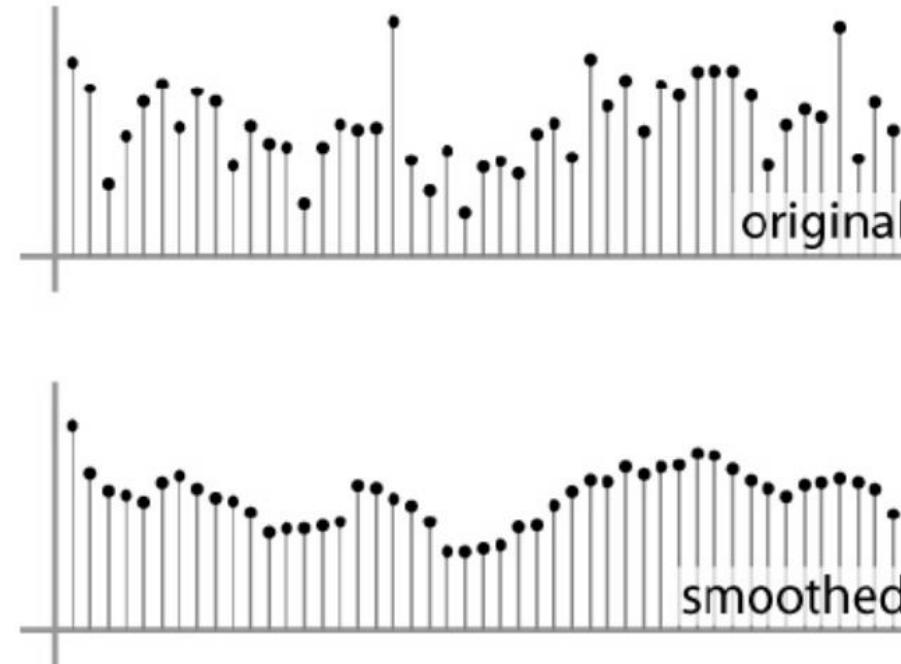
- ▶ The Discriminator is trained for k_1 iterations, so that it learns to properly discriminate between real and generated images.
- ▶ The Generator is trained for k_2 iterations, so that it learns to fool the Discriminator.
- ▶ The Discriminator D and the Generator G are alternately trained to optimize a joint objective function:

$$\min_G \max_D \mathbb{E}_{x \sim p_{data}(x)}[\log D(x)] + \mathbb{E}_{z \sim p_z(z)}[\log(1 - D(G(z)))]$$

A short view on Deep Learning

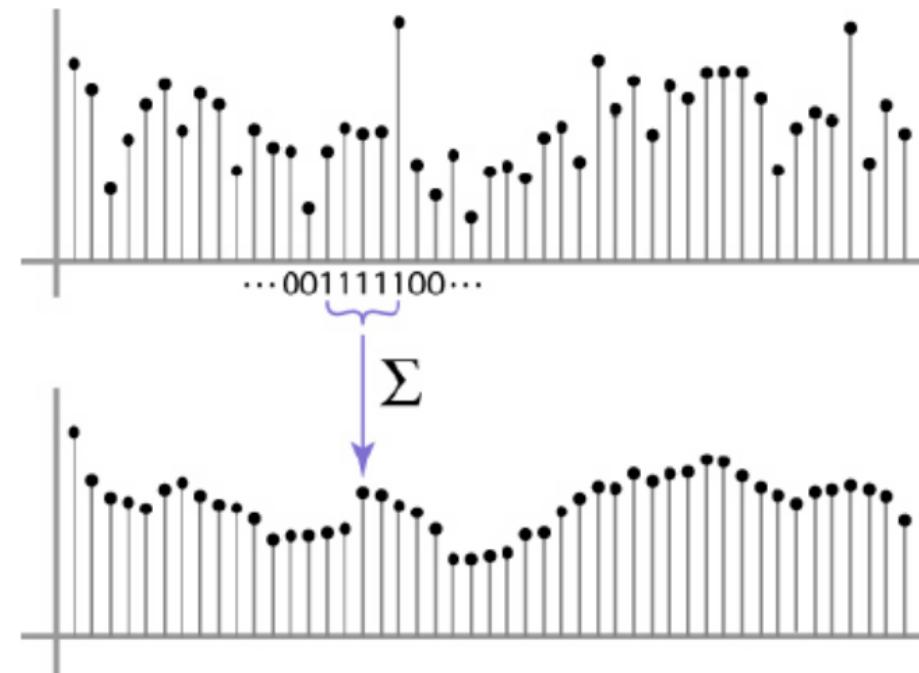
A Signal Processing Perspective of kernels

- How can we smooth a quantized signal?



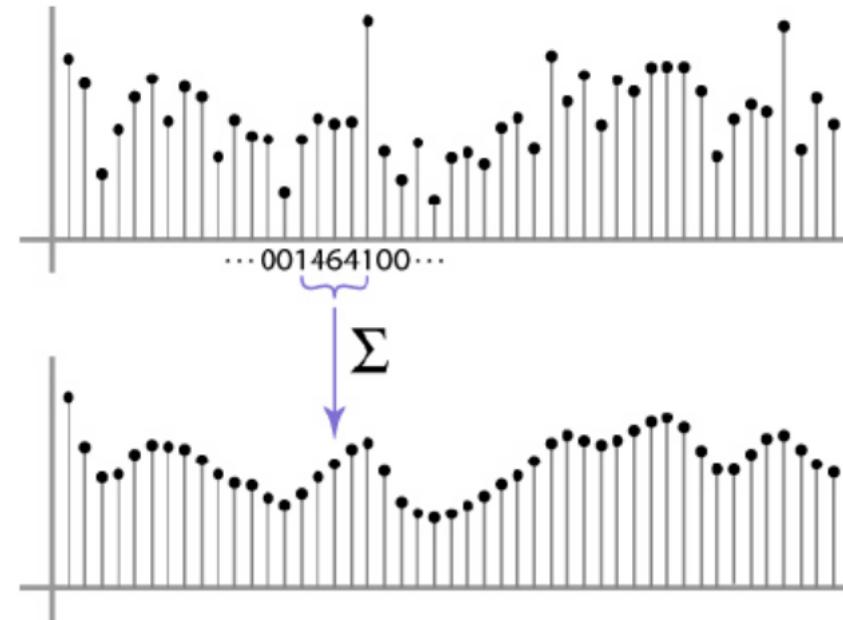
A Signal Processing Perspective of kernels

- How can we smooth a quantized signal?
 - Moving Average



A Signal Processing Perspective of kernels

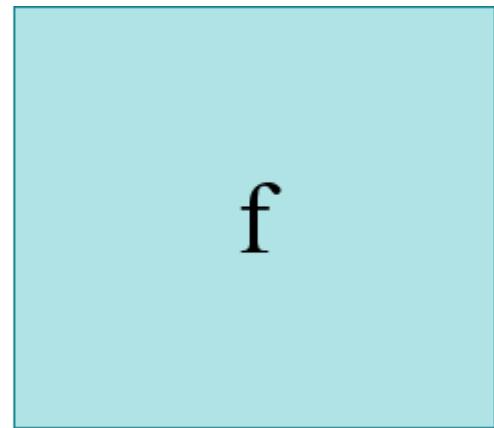
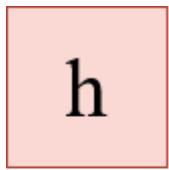
- How can we smooth a quantized signal?
 - *Weighted Moving Average*



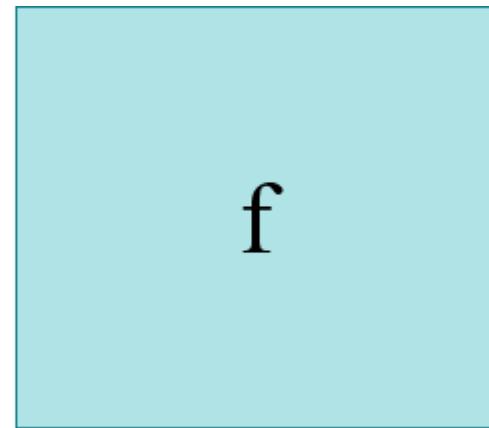
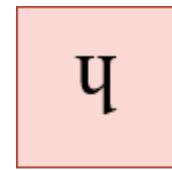
Correlation & Convolution Operators

Correlation:
$$g(i, j) = \sum_{k,l} f(i + k, j + l)h(k, l)$$

Convolution:
$$g(i, j) = \sum_{k,l} f(i - k, j - l)h(k, l)$$



Correlation



Convolution

Weighted averages of 2D signals

$F[x, y]$

0	0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0	0
0	0	0	90	90	90	90	90	0	0	0
0	0	0	90	90	90	90	90	0	0	0
0	0	0	90	90	90	90	90	0	0	0
0	0	0	90	0	90	90	90	0	0	0
0	0	0	90	90	90	90	90	0	0	0
0	0	0	0	0	0	0	0	0	0	0
0	0	90	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0	0

$G[x, y]$

0										

Weighted averages of 2D signals

$F[x, y]$

0	0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0	0
0	0	0	90	90	90	90	90	90	0	0
0	0	0	90	90	90	90	90	90	0	0
0	0	0	90	90	90	90	90	90	0	0
0	0	0	90	0	90	90	90	90	0	0
0	0	0	90	90	90	90	90	90	0	0
0	0	0	0	0	0	0	0	0	0	0
0	0	90	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0	0

$G[x, y]$

0	10									

Weighted averages of 2D signals

$F[x, y]$

0	0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0	0
0	0	0	90	90	90	90	90	90	0	0
0	0	0	90	90	90	90	90	90	0	0
0	0	0	90	90	90	90	90	90	0	0
0	0	0	90	0	90	90	90	90	0	0
0	0	0	90	90	90	90	90	90	0	0
0	0	0	0	0	0	0	0	0	0	0
0	0	90	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0	0

$G[x, y]$

0	10	20								

Weighted averages of 2D signals

$F[x, y]$

0	0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0	0
0	0	0	90	90	90	90	90	0	0	0
0	0	0	90	90	90	90	90	0	0	0
0	0	0	90	90	90	90	90	0	0	0
0	0	0	90	0	90	90	90	0	0	0
0	0	0	90	90	90	90	90	0	0	0
0	0	0	0	0	0	0	0	0	0	0
0	0	90	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0	0

$G[x, y]$

	0	10	20	30						

Weighted averages of 2D signals

$$F[x, y]$$

$$G[x, y]$$

Weighted averages of 2D signals

$F[x, y]$

0	0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0	0
0	0	0	90	90	90	90	90	0	0	0
0	0	0	90	90	90	90	90	0	0	0
0	0	0	90	90	90	90	90	0	0	0
0	0	0	90	0	90	90	90	0	0	0
0	0	0	90	90	90	90	90	0	0	0
0	0	0	0	0	0	0	0	0	0	0
0	0	90	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0	0

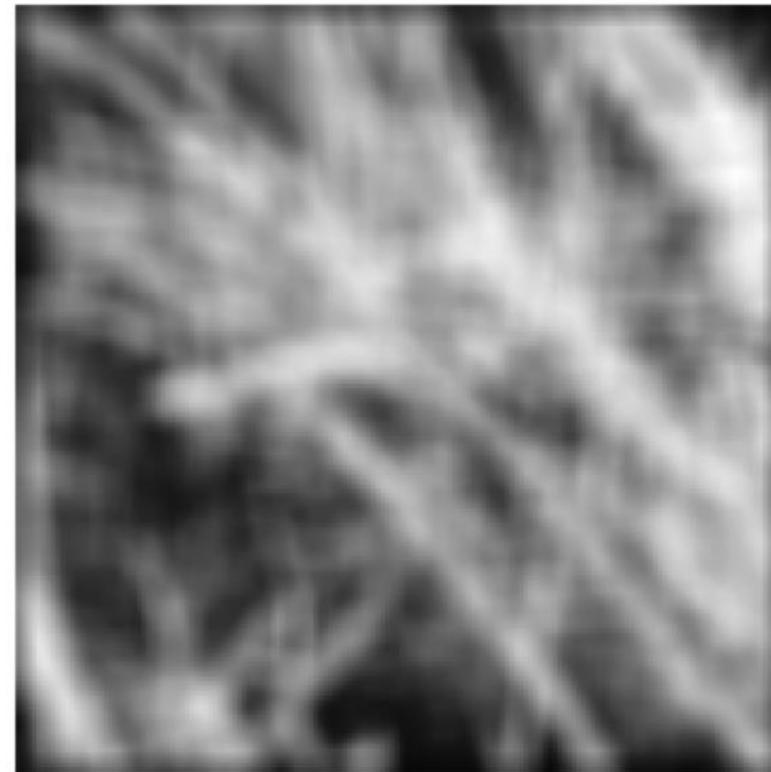
$G[x, y]$

	0	10	20	30	30	30	20	10		
	0	20	40	60	60	60	40	20		
	0	30	60	90	90	90	60	30		
	0	30	50	80	80	90	60	30		
	0	30	50	80	80	90	60	30		
	0	20	30	50	50	60	40	20		
	10	20	30	30	30	30	20	10		
	10	10	10	0	0	0	0	0		

Effect of Convolutions: A Smoothed Signal

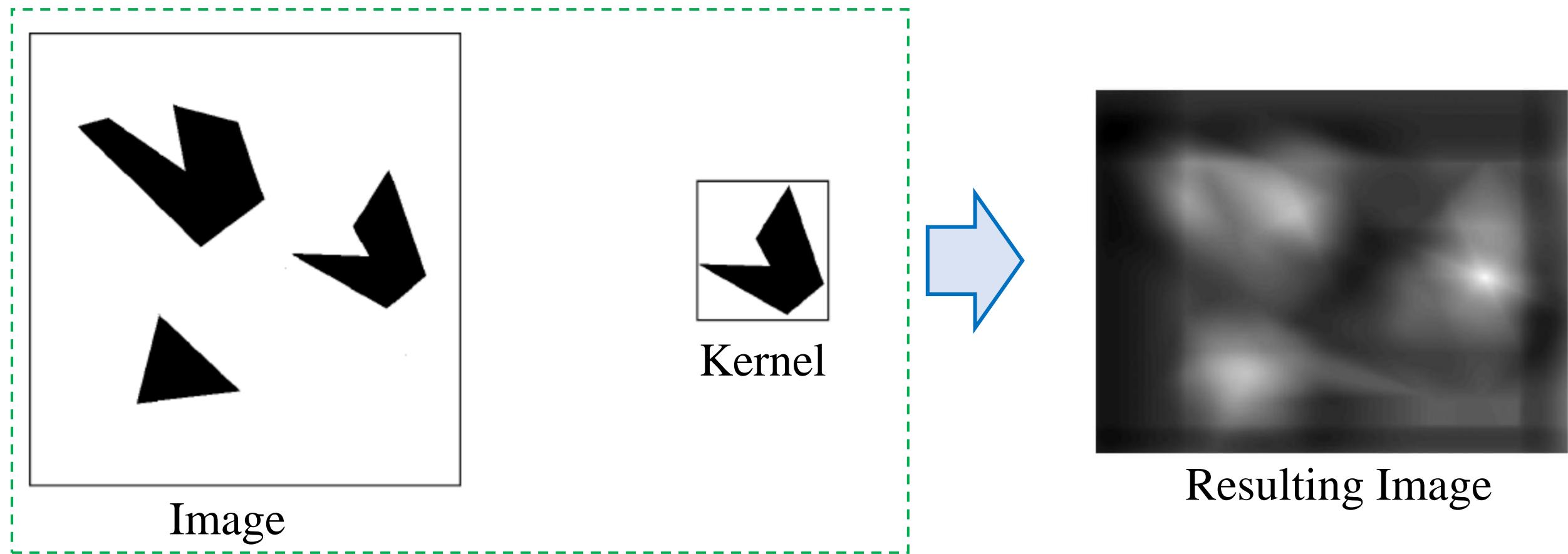


original

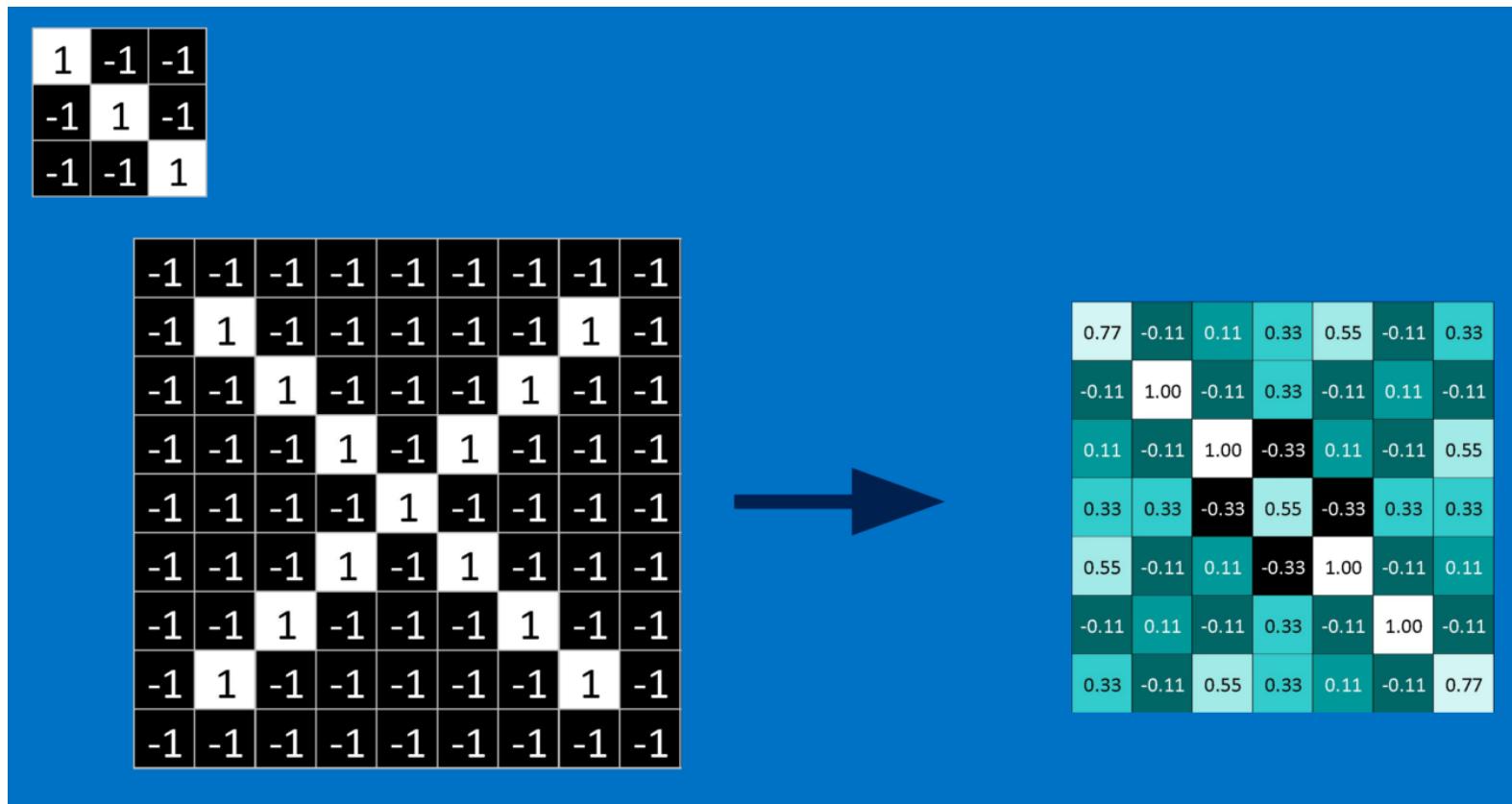


filtered

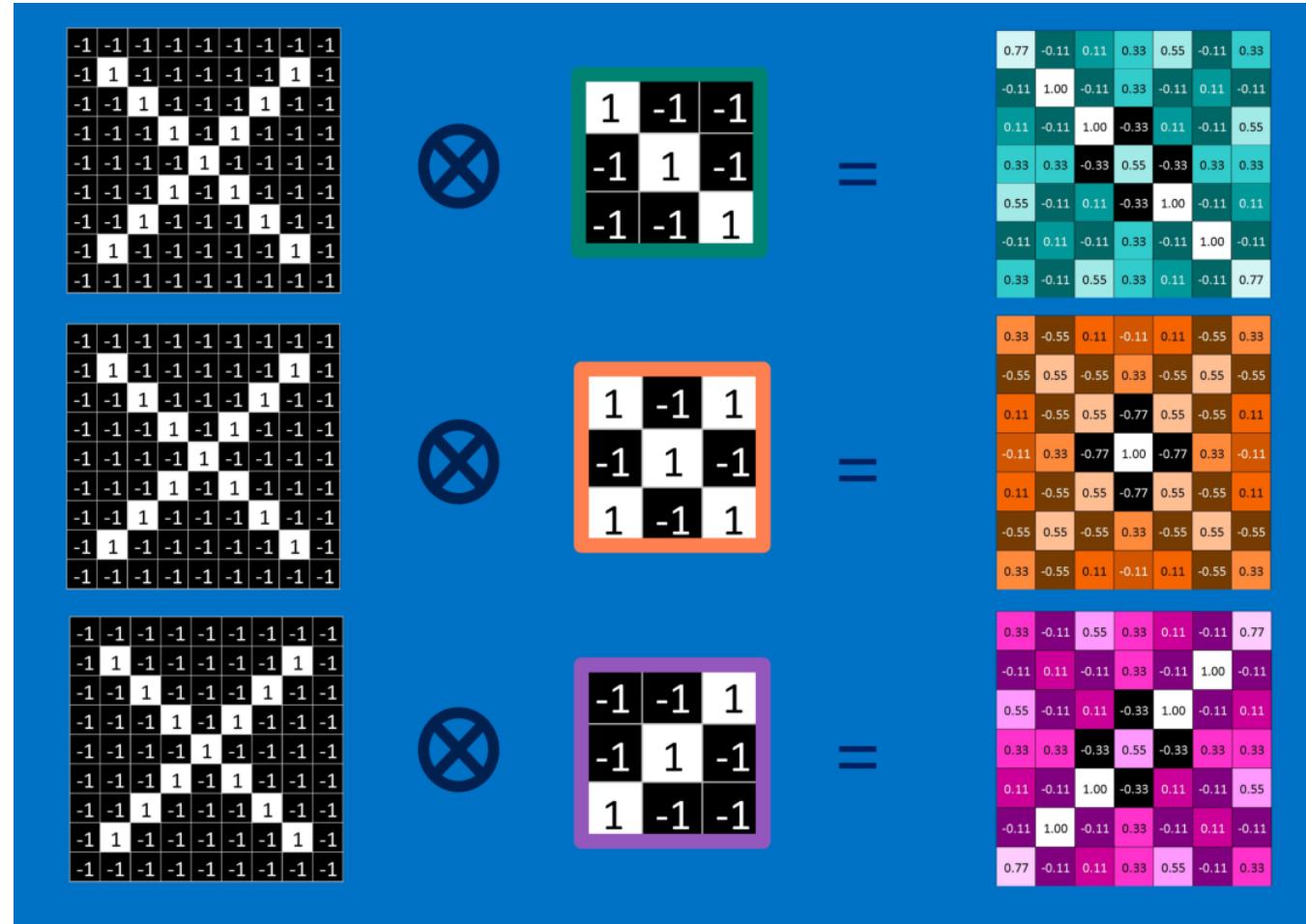
Normalized Correlation for Template Matching



Convolution operation

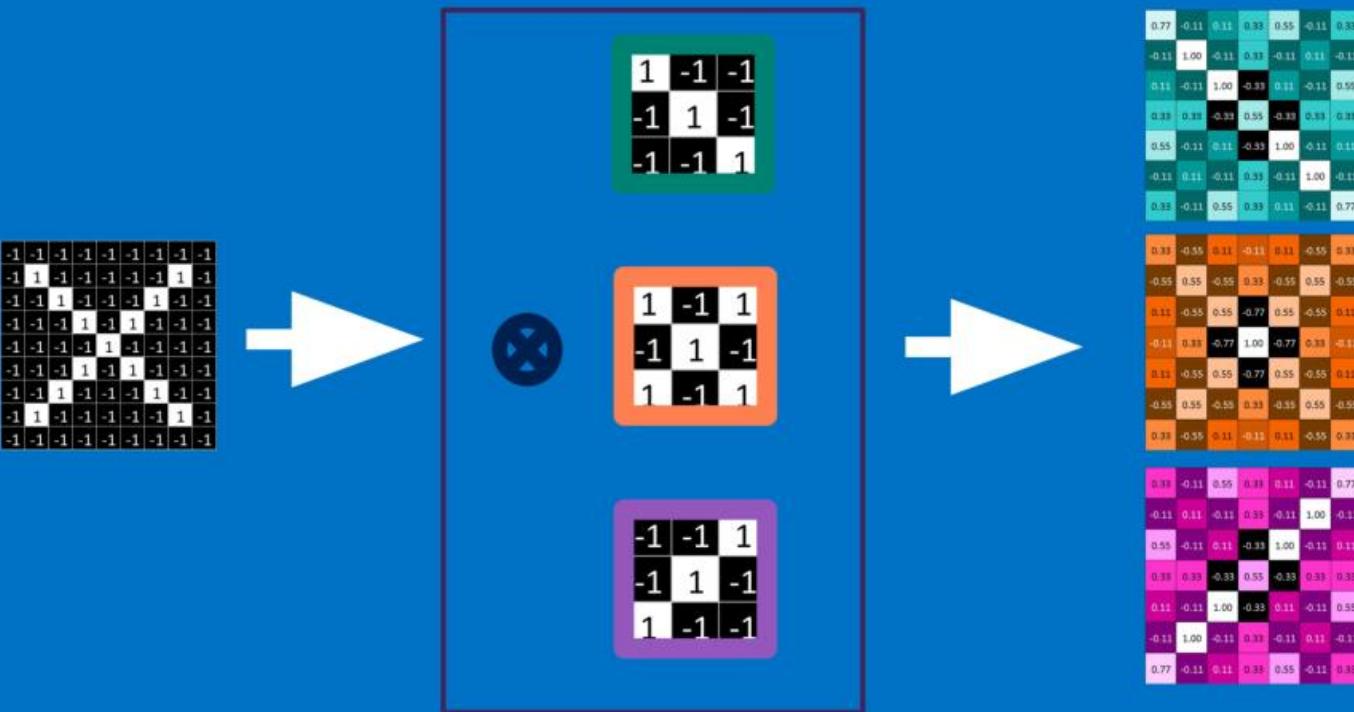


Convolution operation

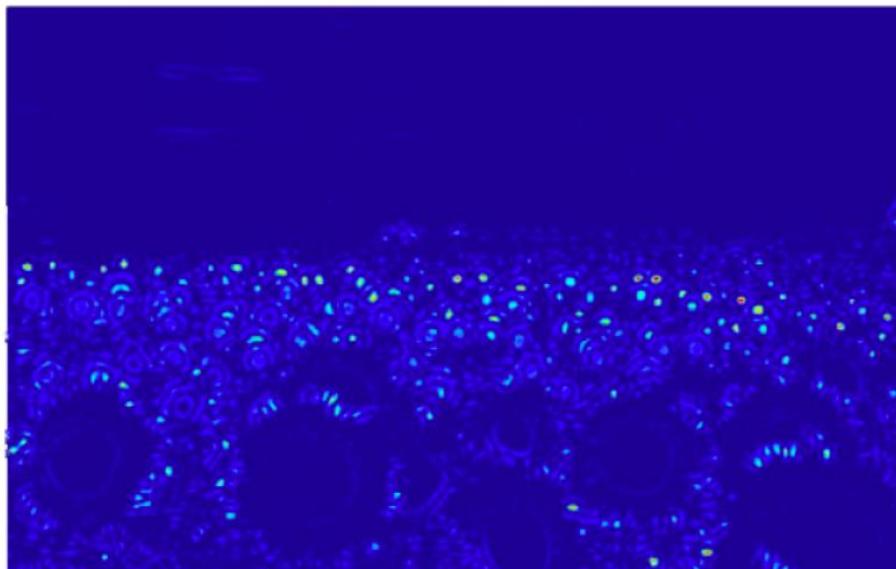
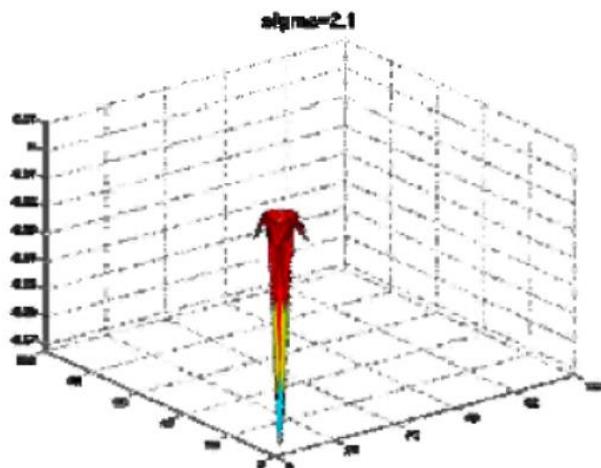


Convolution operation

One image becomes a stack of filtered images

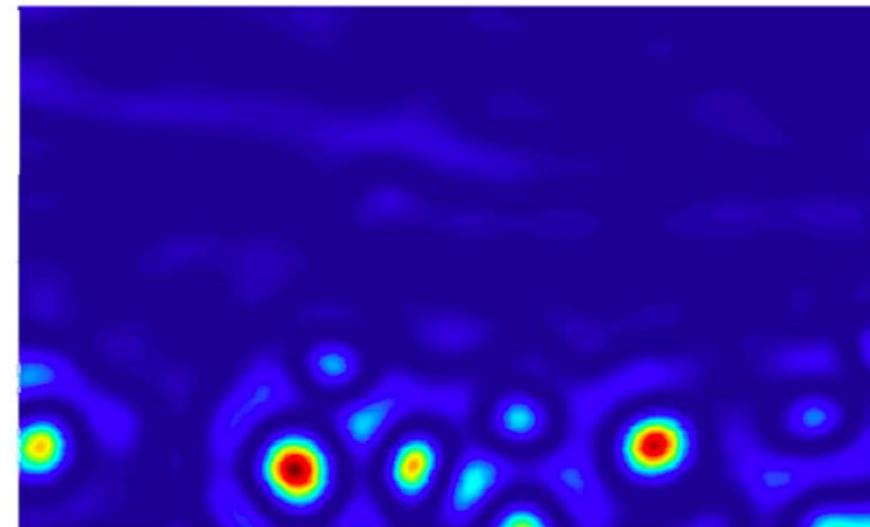
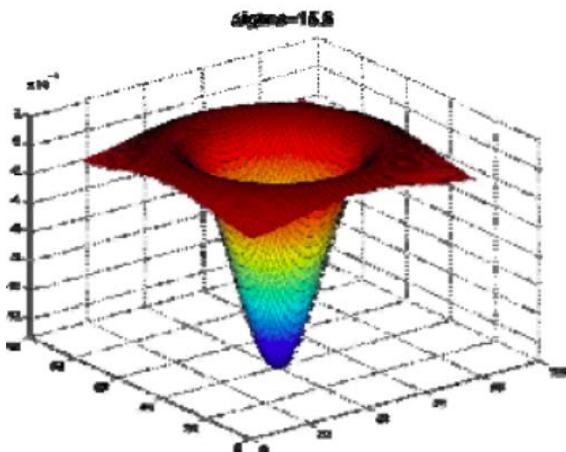


Different features may exist at different scales

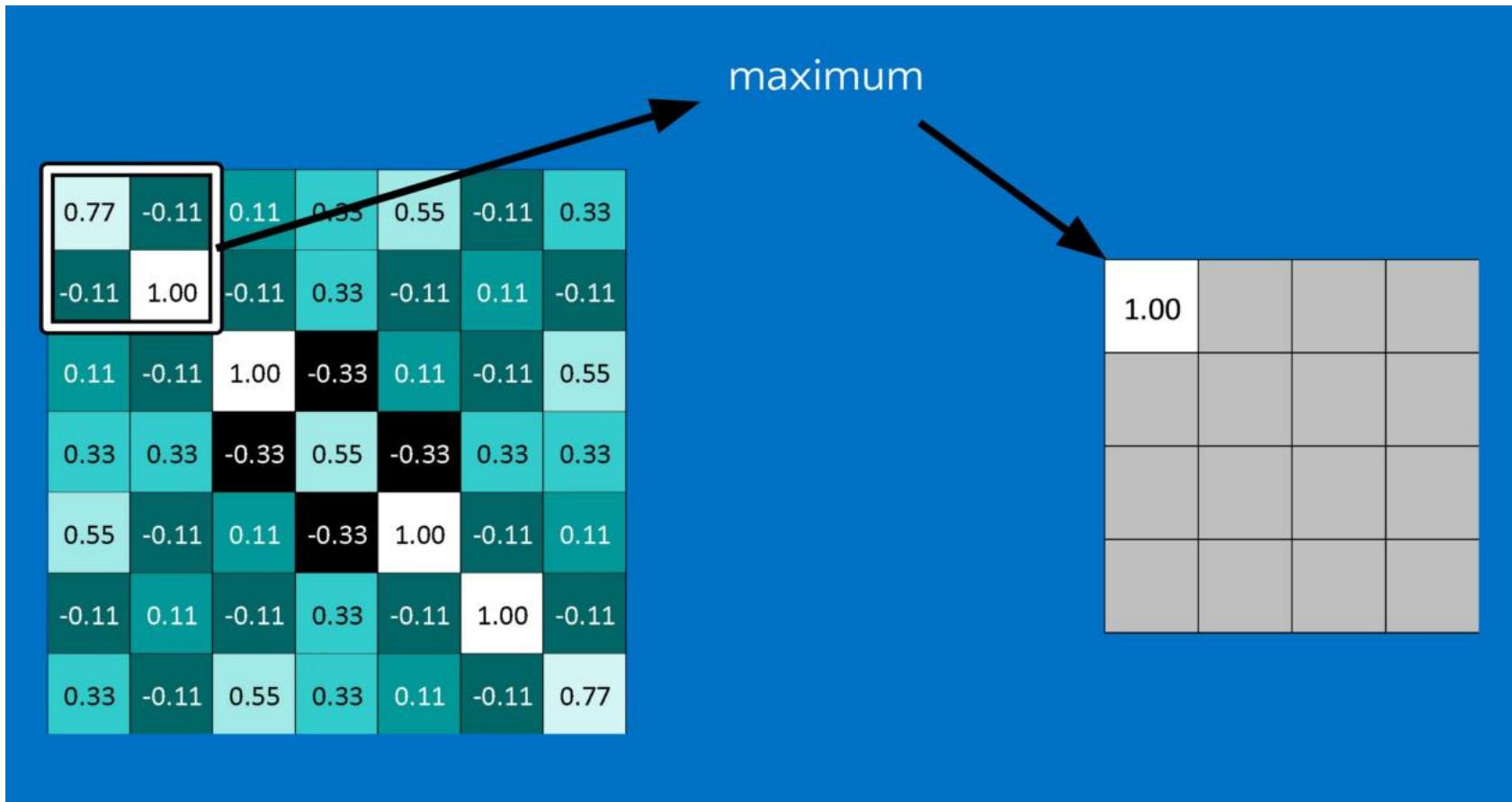


Source: K. Graumann

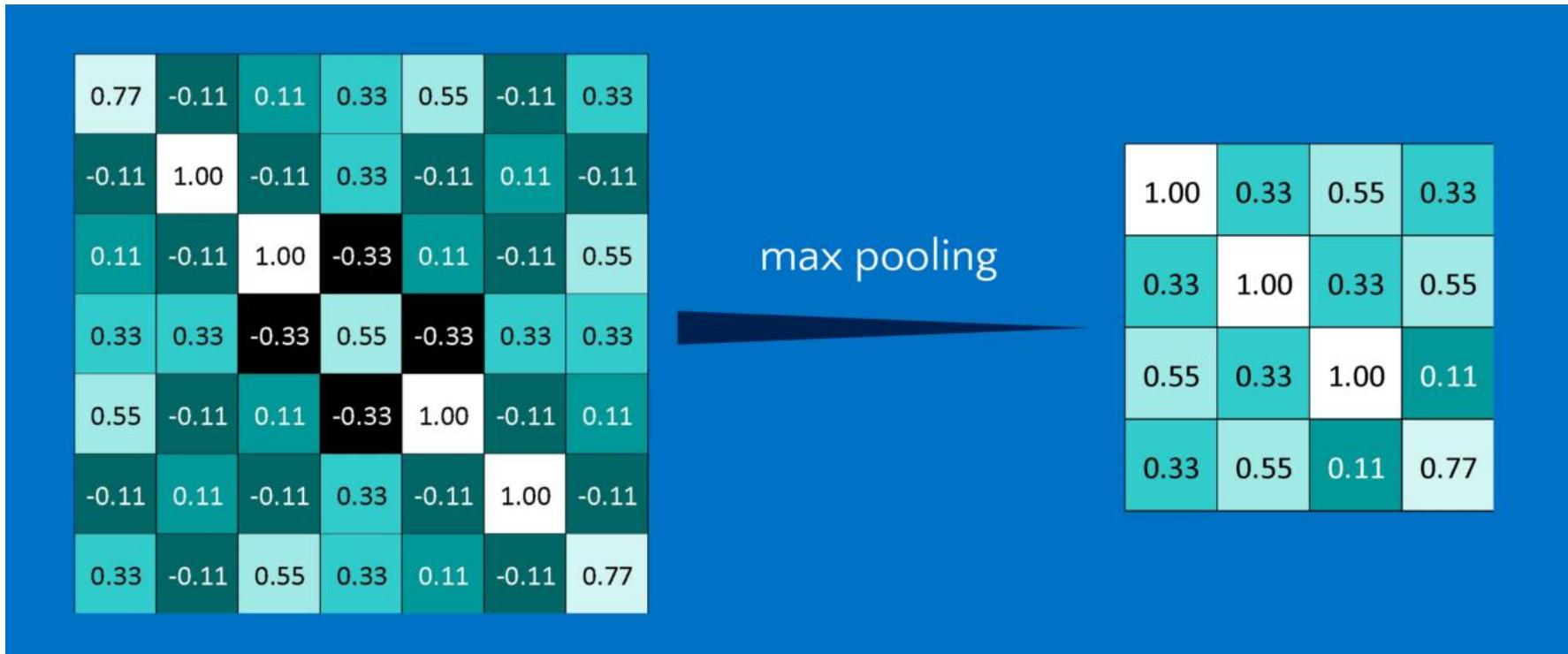
Different features may exist at different scales



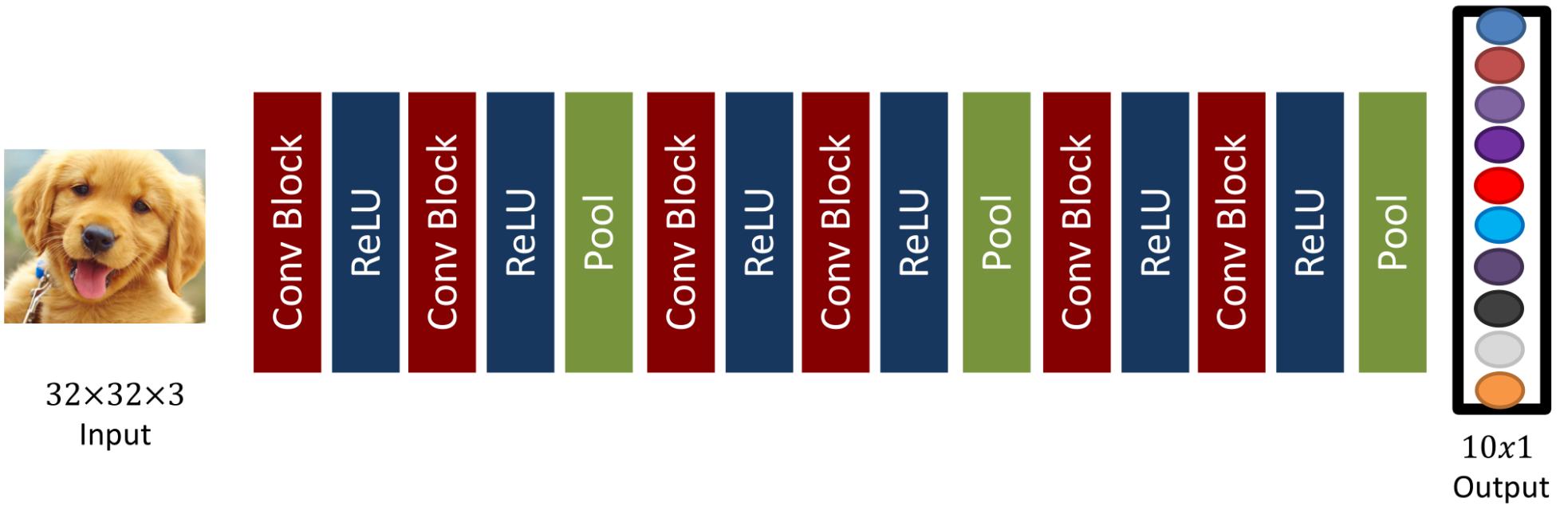
Max Pool operation



Max Pool operation



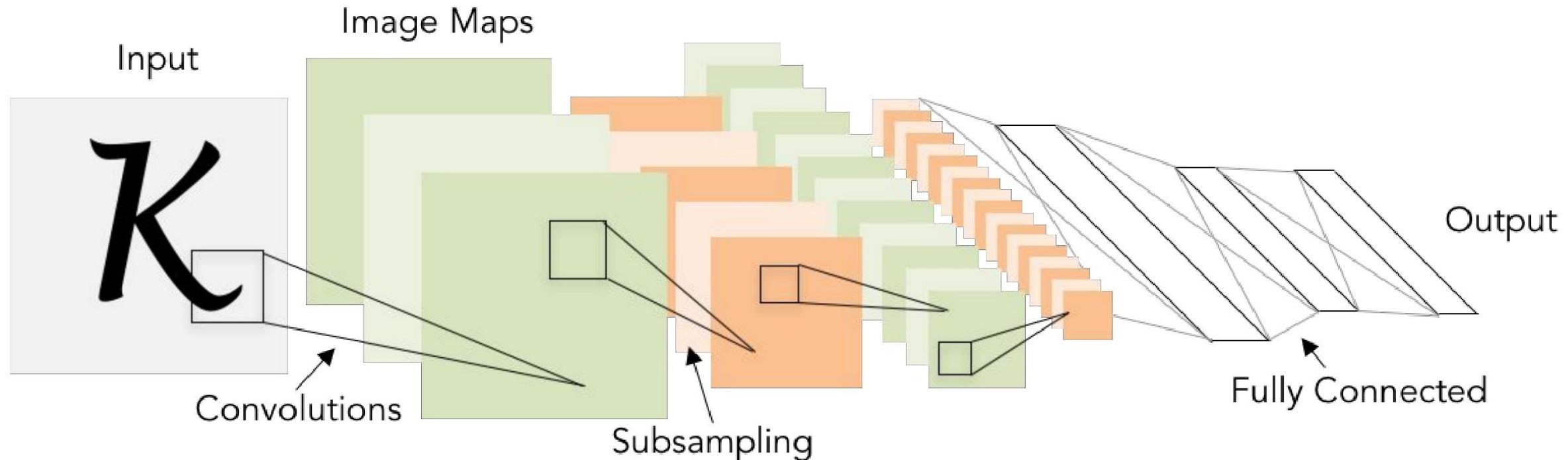
Convolution Neural Networks



Review: LeNet-5

[LeCun et al., 1998]

- ❖ 70% test accuracy on the MNIST dataset
- ❖ Used average pooling instead of max pooling



Conv filters were 5x5, applied at stride 1

Subsampling (Pooling) layers were 2x2 applied at stride 2
i.e. architecture is [CONV-POOL-CONV-POOL-FC-FC]



IMAGENET

www.image-net.org

22K categories and **14M** images

- Animals
 - Bird
 - Fish
 - Mammal
 - Invertebrate
- Plants
 - Tree
 - Flower
 - Food
 - Materials
- Structures
 - Artifact
 - Tools
 - Appliances
 - Structures
- Person
- Scenes
 - Indoor
 - Geological Formations
- Sport Activities



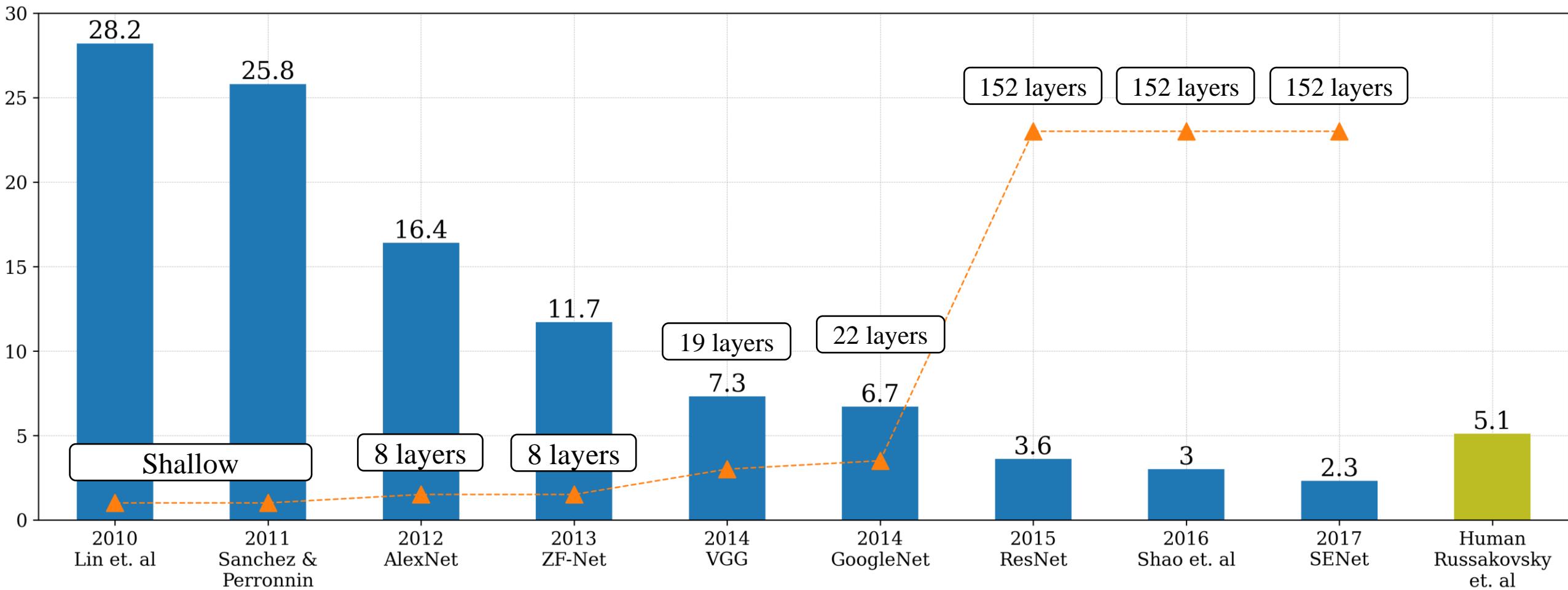
Deng, Dong, Socher, Li, Li, & Fei-Fei, 2009

<https://image-net.org/index.php>

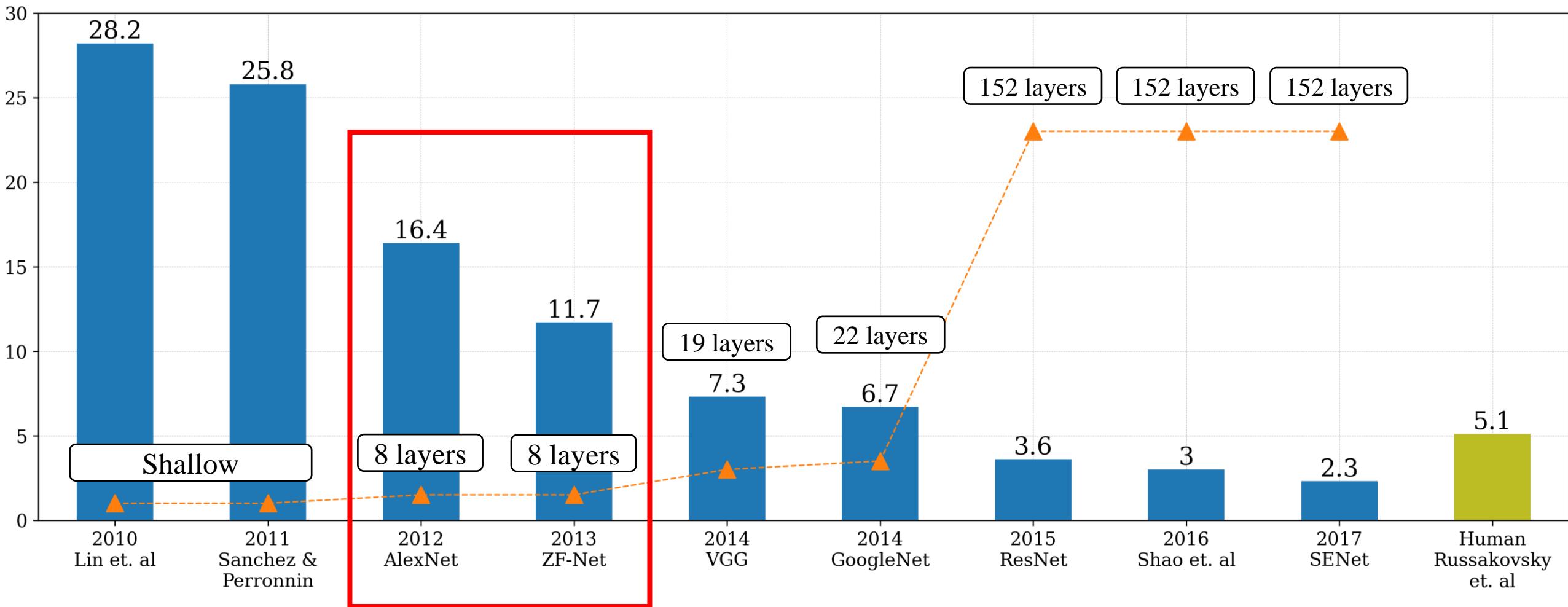
<https://www.kaggle.com/c/imagenet-object-localization-challenge>

<https://pytorch.org/vision/stable/generated/torchvision.datasets.ImageNet.html>

ImageNet Challenge Error Rates over time



ImageNet Challenge Error Rates over time



Case Study: AlexNet

[Krizhevsky et al. 2012]

Full (simplified) AlexNet architecture:

[227x227x3] INPUT

[55x55x96] CONV1: 96 11x11 filters at stride 4, pad 0

[27x27x96] MAX POOL1: 3x3 filters at stride 2

[27x27x96] NORM1: Normalization layer

[27x27x256] CONV2: 256 5x5 filters at stride 1, pad 2

[13x13x256] MAX POOL2: 3x3 filters at stride 2

[13x13x256] NORM2: Normalization layer

[13x13x384] CONV3: 384 3x3 filters at stride 1, pad 1

[13x13x384] CONV4: 384 3x3 filters at stride 1, pad 1

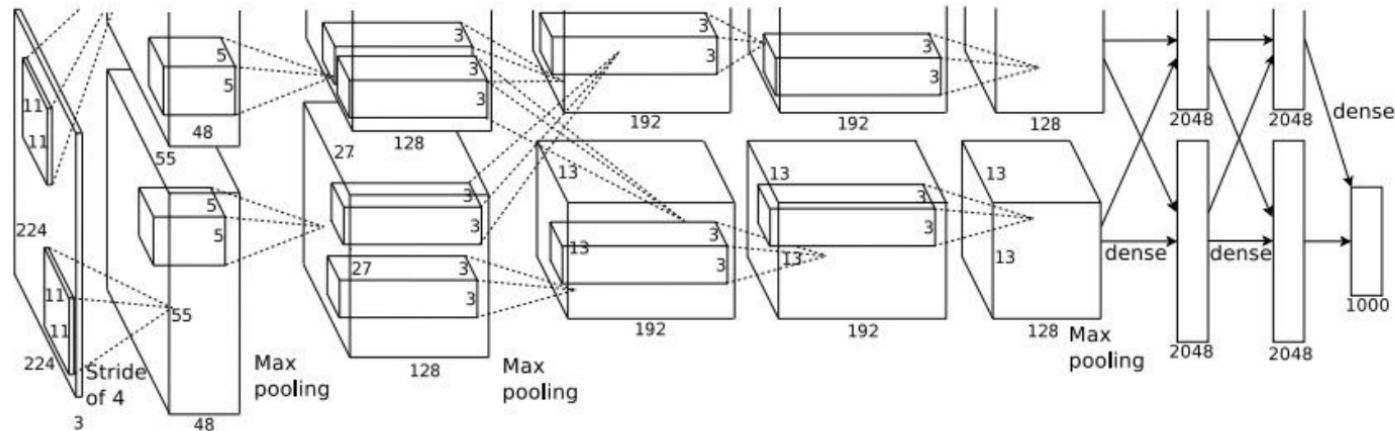
[13x13x256] CONV5: 256 3x3 filters at stride 1, pad 1

[6x6x256] MAX POOL3: 3x3 filters at stride 2

[4096] FC6: 4096 neurons

[4096] FC7: 4096 neurons

[1000] FC8: 1000 neurons (class scores)



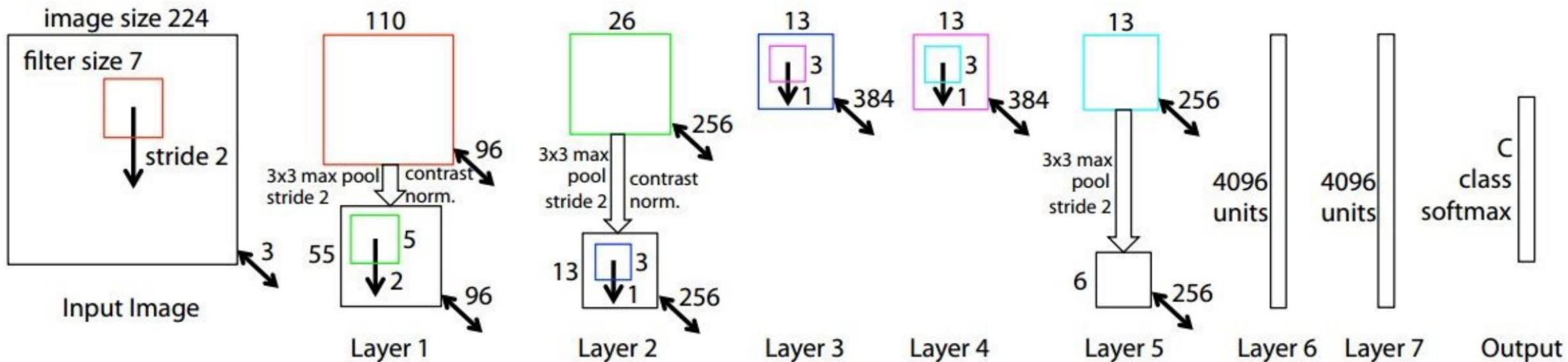
Details/Retrospectives:

- first use of ReLU
- used LRN layers (not common anymore)
- heavy data augmentation
- dropout 0.5
- batch size 128
- SGD Momentum 0.9
- Learning rate 1e-2, reduced by 10 manually when val accuracy plateaus
- L2 weight decay 5e-4
- 7 CNN ensemble: 18.2% -> 15.4%

Figure copyright Alex Krizhevsky, Ilya Sutskever, and Geoffrey Hinton, 2012. Reproduced with permission.

ZFNet

[Zeiler and Fergus, 2013]



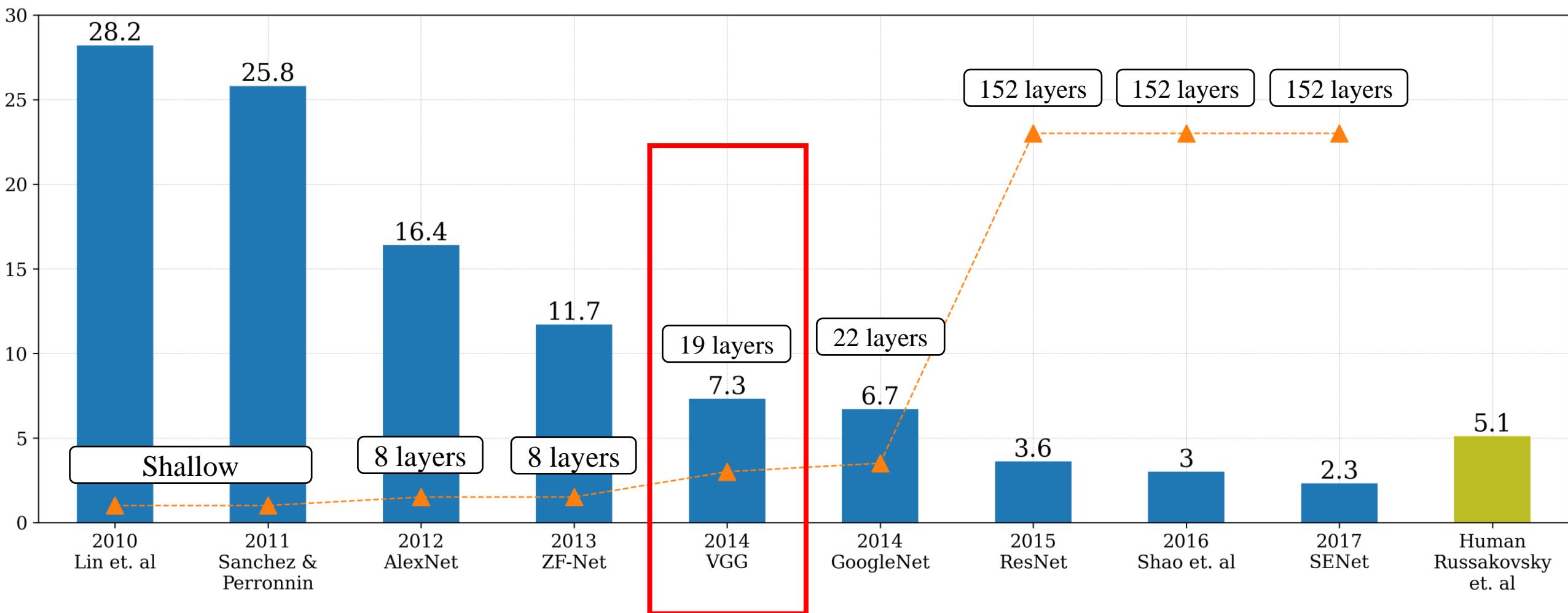
AlexNet but:

CONV1: change from (11x11 stride 4) to (7x7 stride 2)

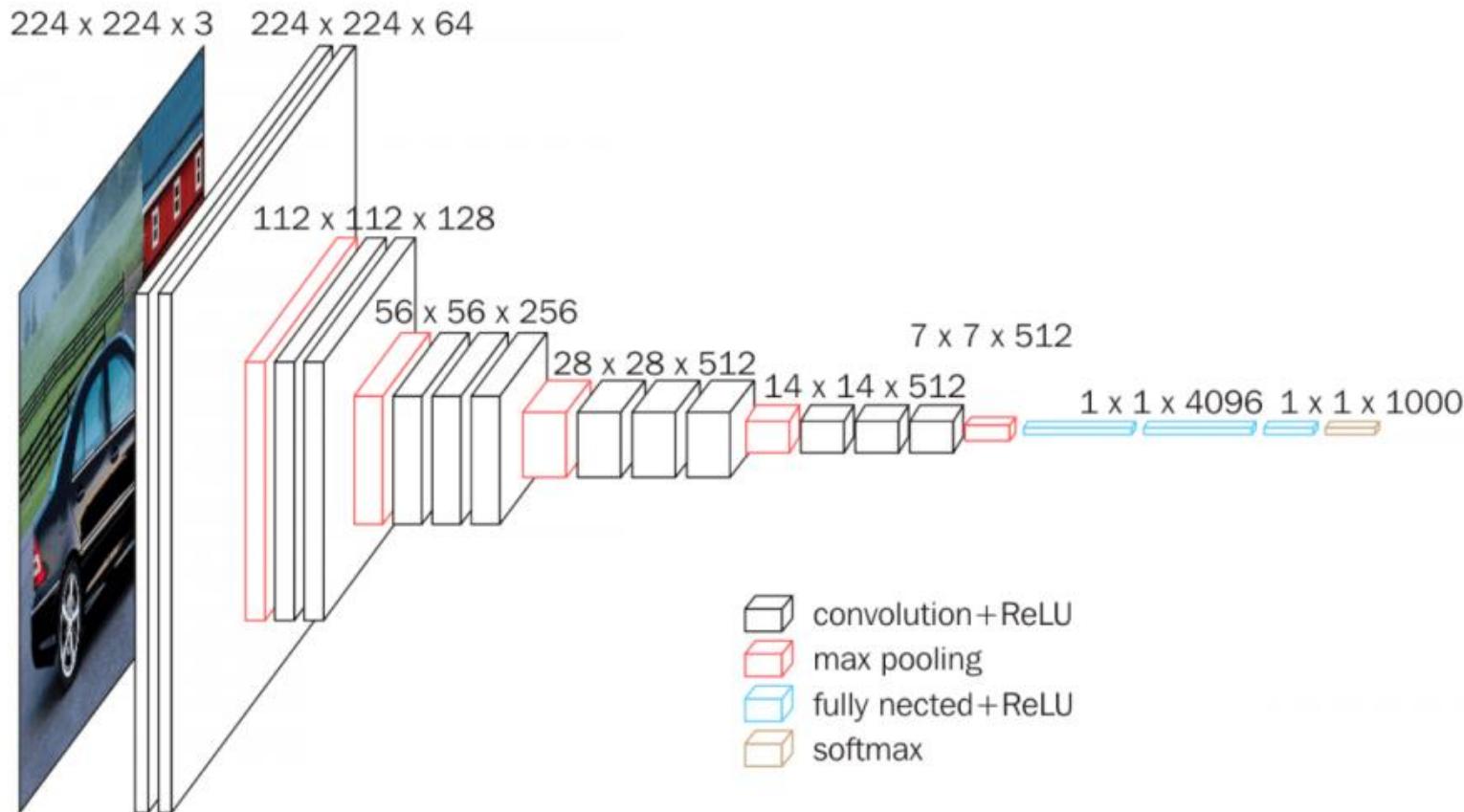
CONV3,4,5: instead of 384, 384, 256 filters use 512, 1024, 512

ImageNet top 5 error: 16.4% \rightarrow 11.7%

ImageNet Challenge Error Rates over time

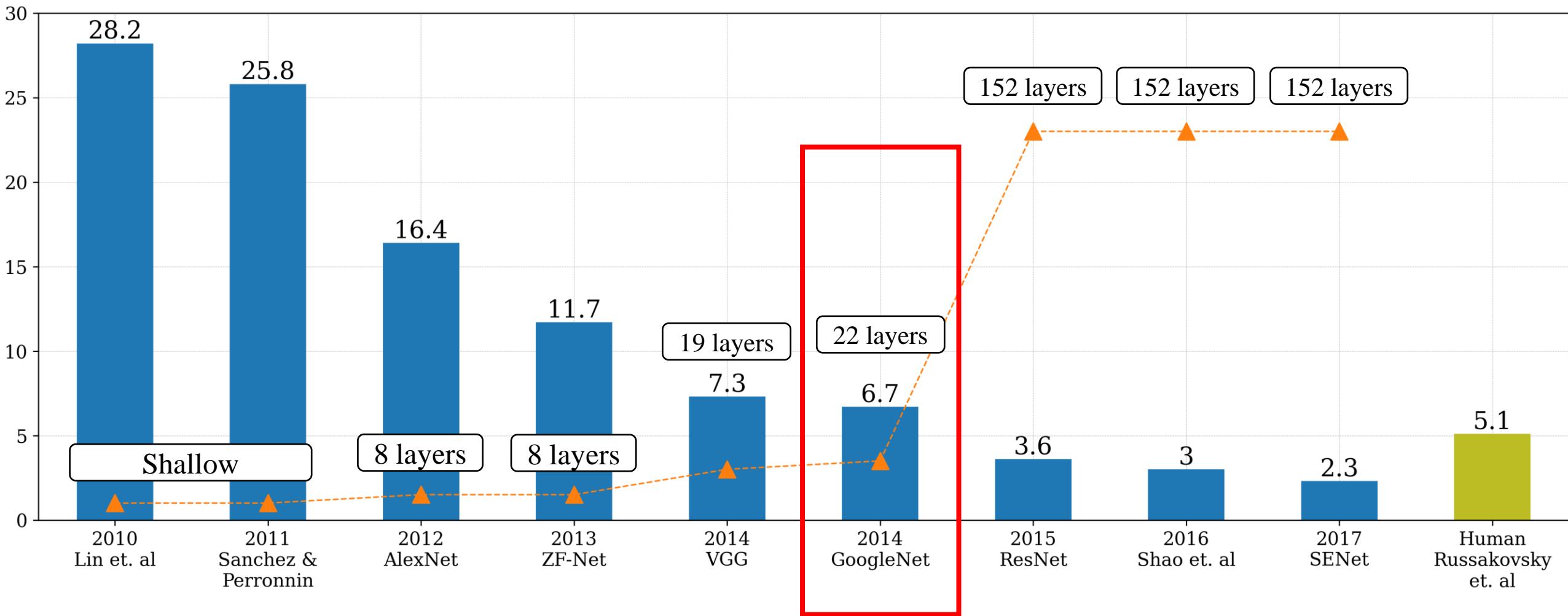


VGG-Net 2014

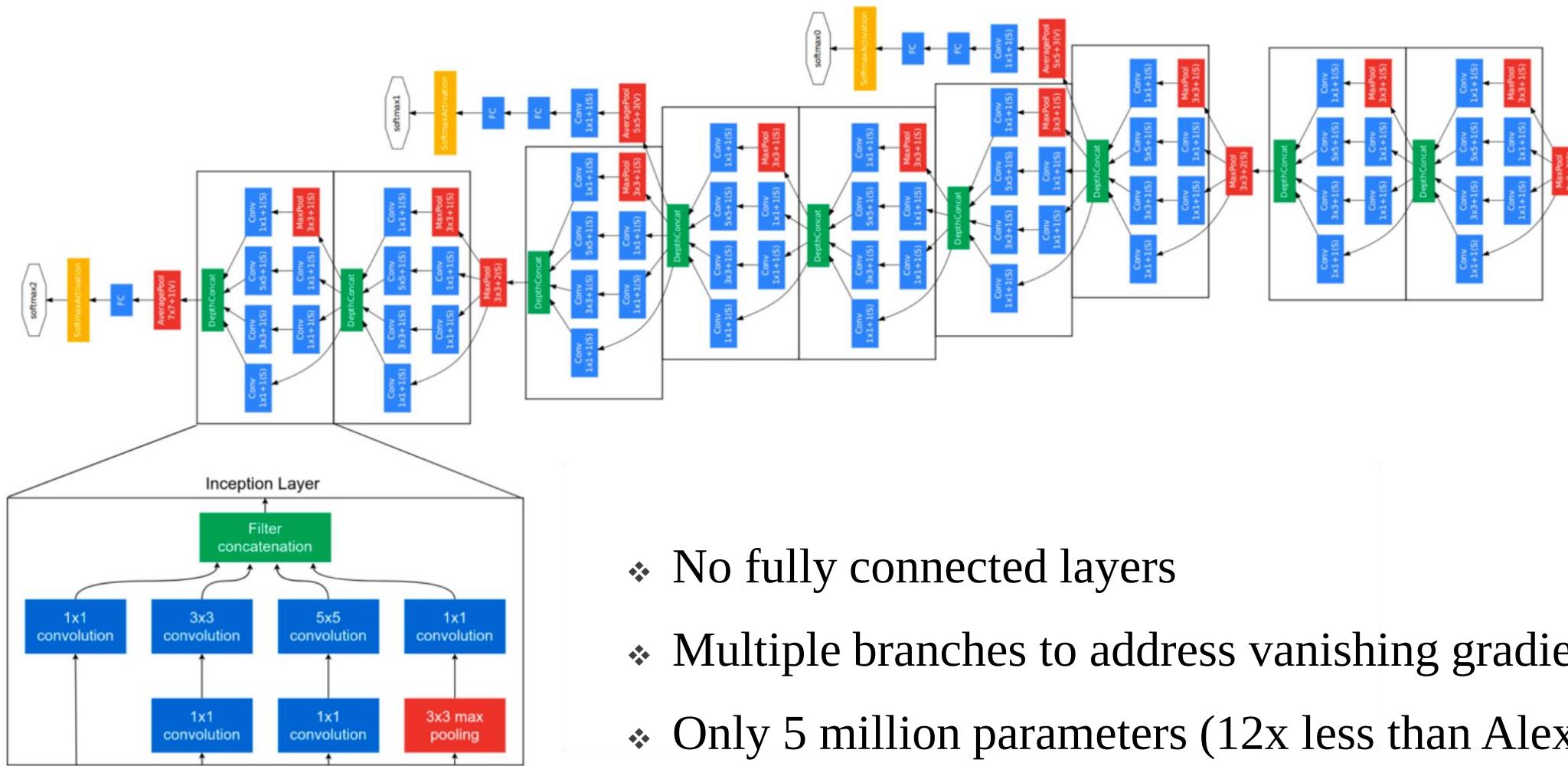


- ❖ Used 3×3 convolution kernels

ImageNet Challenge Error Rates over time

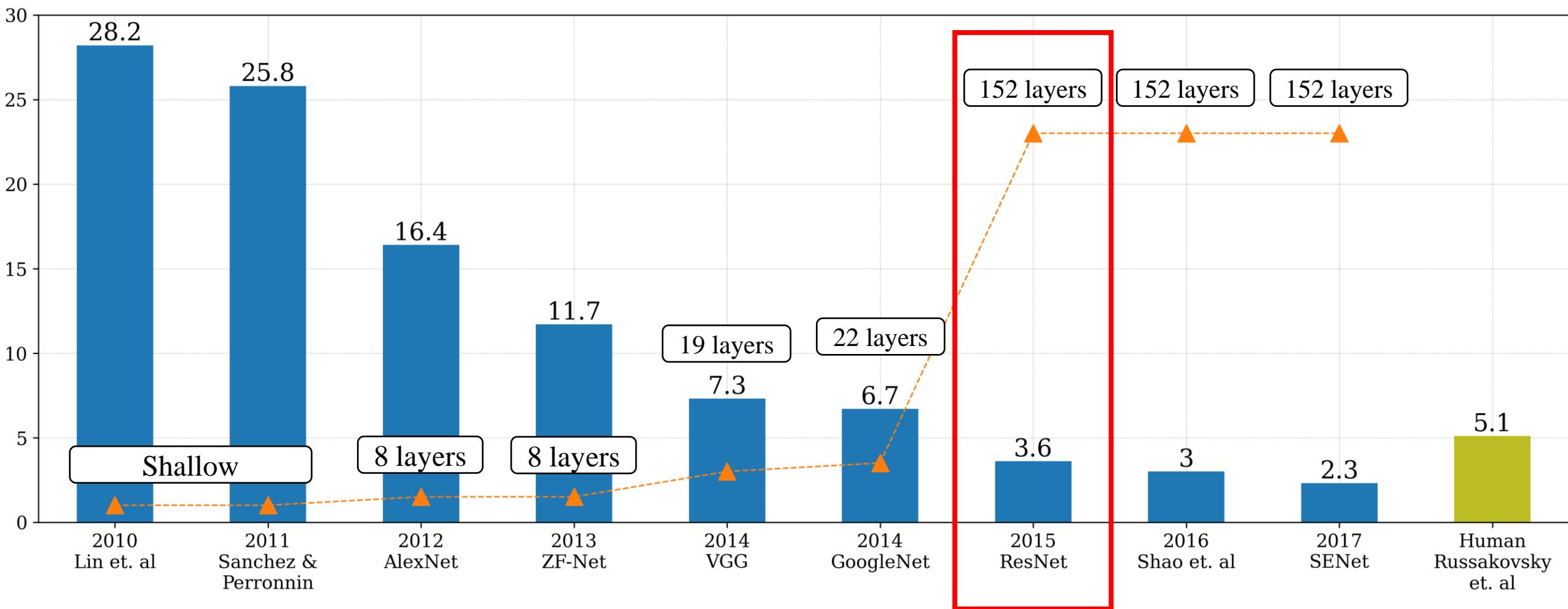


GoogLeNet / InceptionNet v1 (and v2, v3) 2014

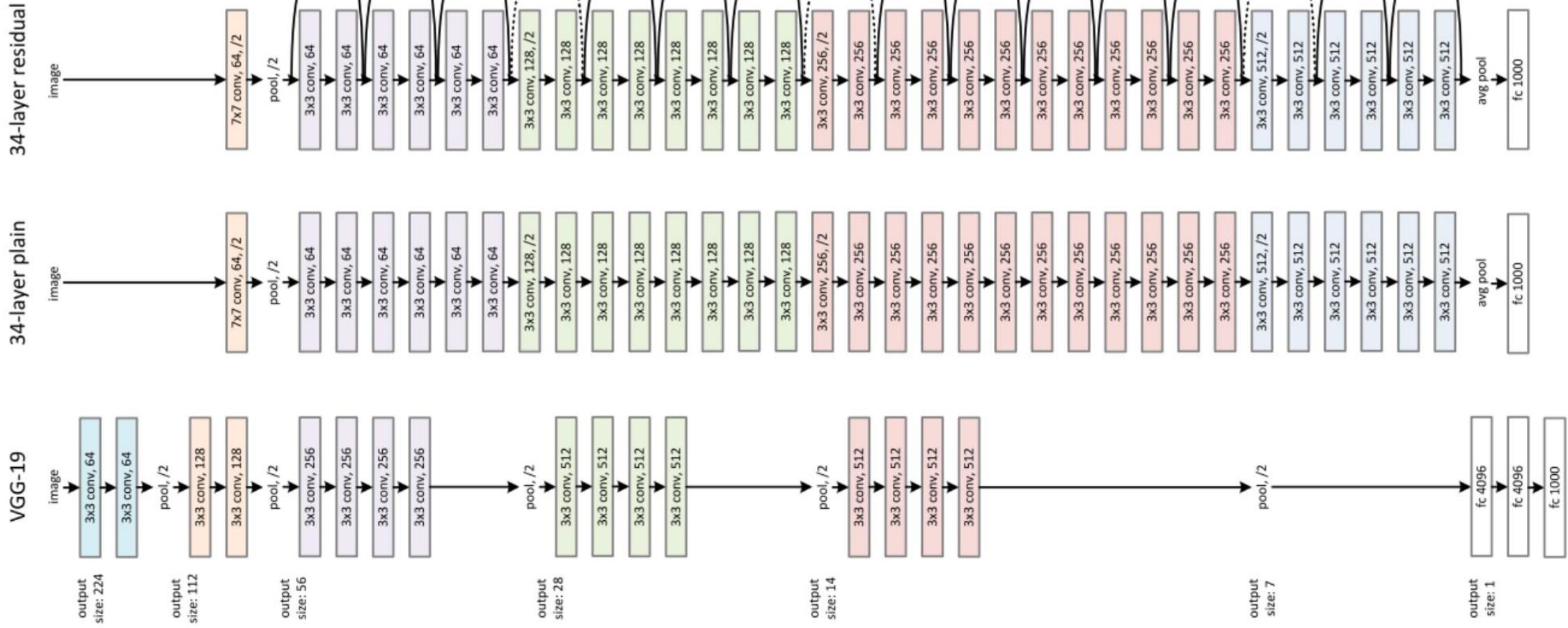


- ❖ No fully connected layers
 - ❖ Multiple branches to address vanishing gradients
 - ❖ Only 5 million parameters (12x less than AlexNet, 27x less than VGG-16)

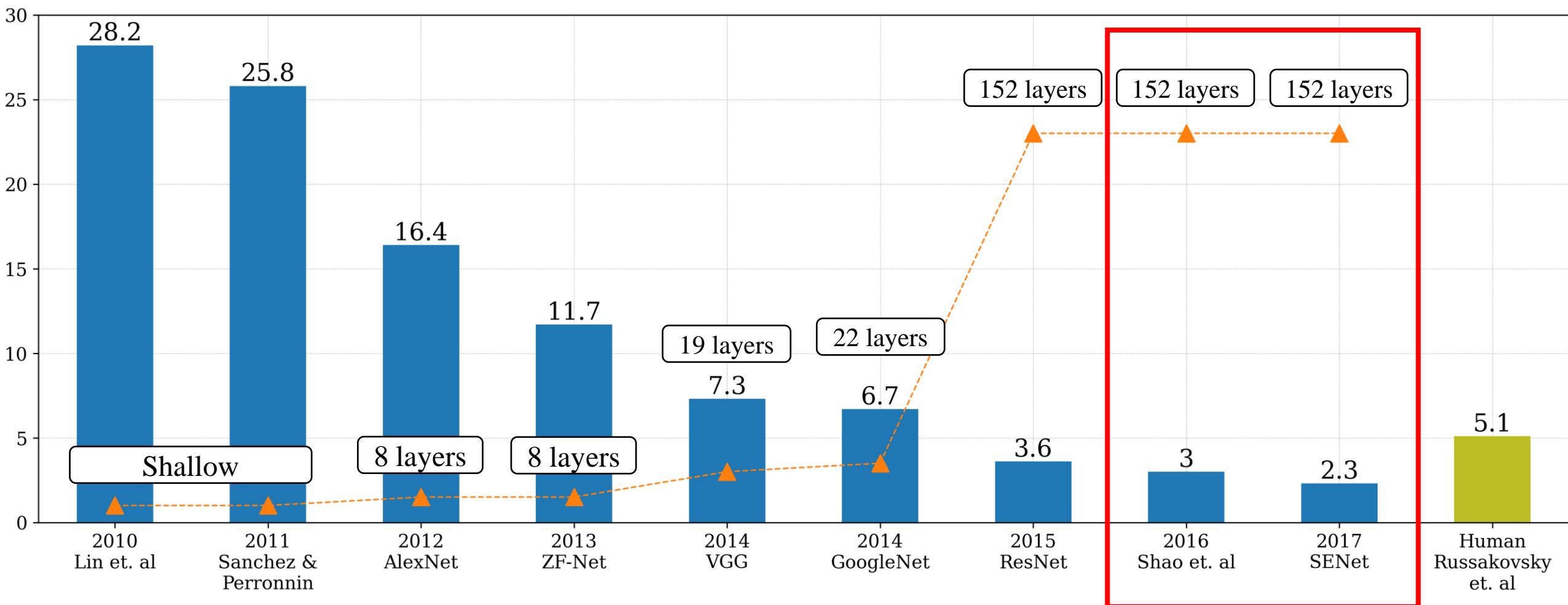
ImageNet Challenge Error Rates over time



He et al. 2015 – ResNet



ImageNet Challenge Error Rates over time



Improving ResNets...

“Good Practices for Deep Feature Fusion”

[Shao et al. 2016]

- Multi-scale ensembling of Inception, Inception-Resnet, Resnet, Wide Resnet models
- ILSVRC'16 classification winner

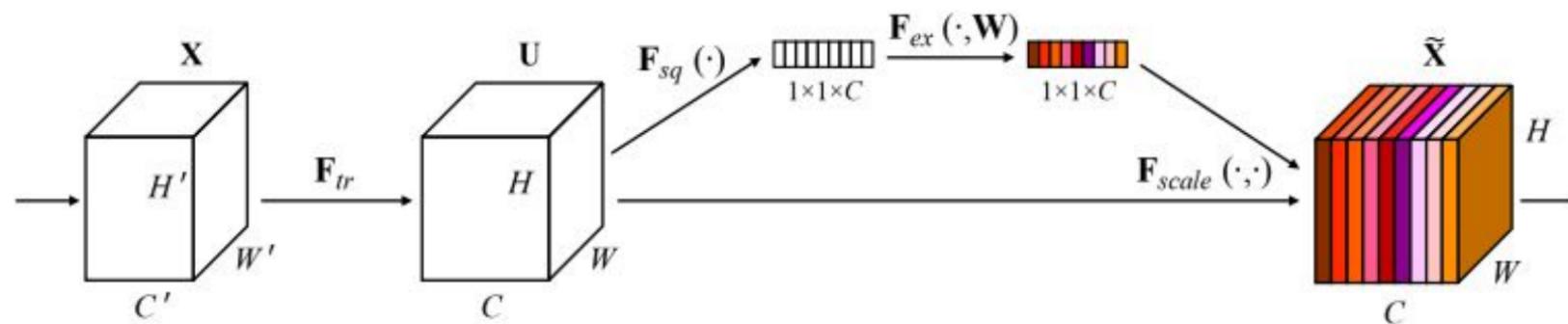
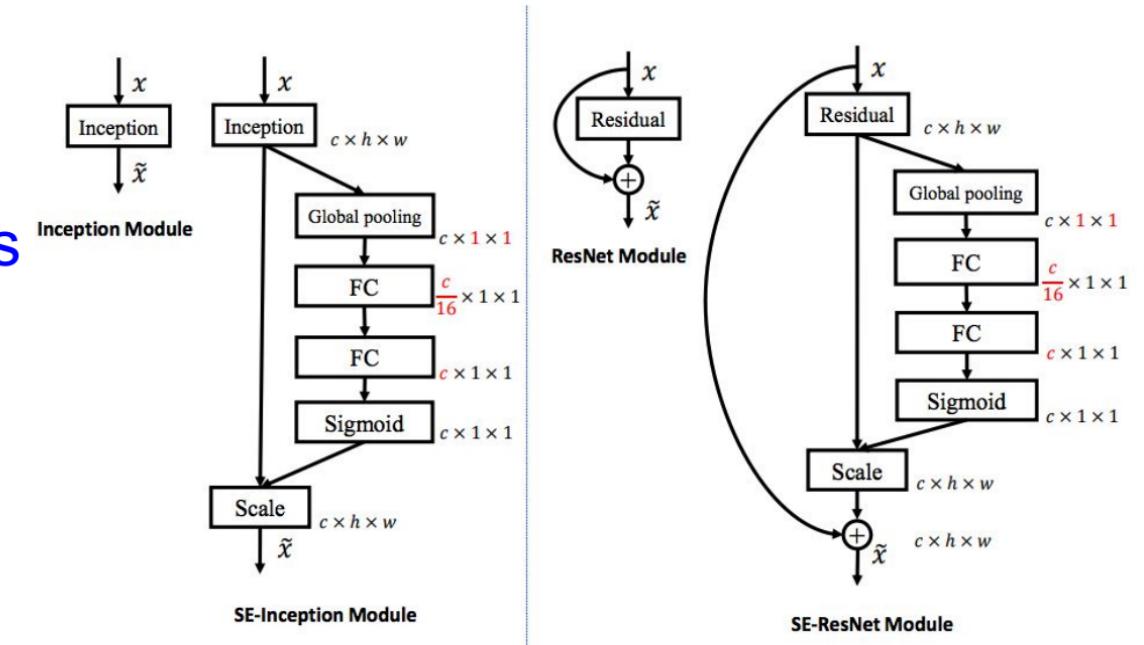
	Inception-v3	Inception-v4	Inception-Resnet-v2	Resnet-200	Wrn-68-3	Fusion (Val.)	Fusion (Test)
Err. (%)	4.20	4.01	3.52	4.26	4.65	2.92 (-0.6)	2.99

Improving ResNets...

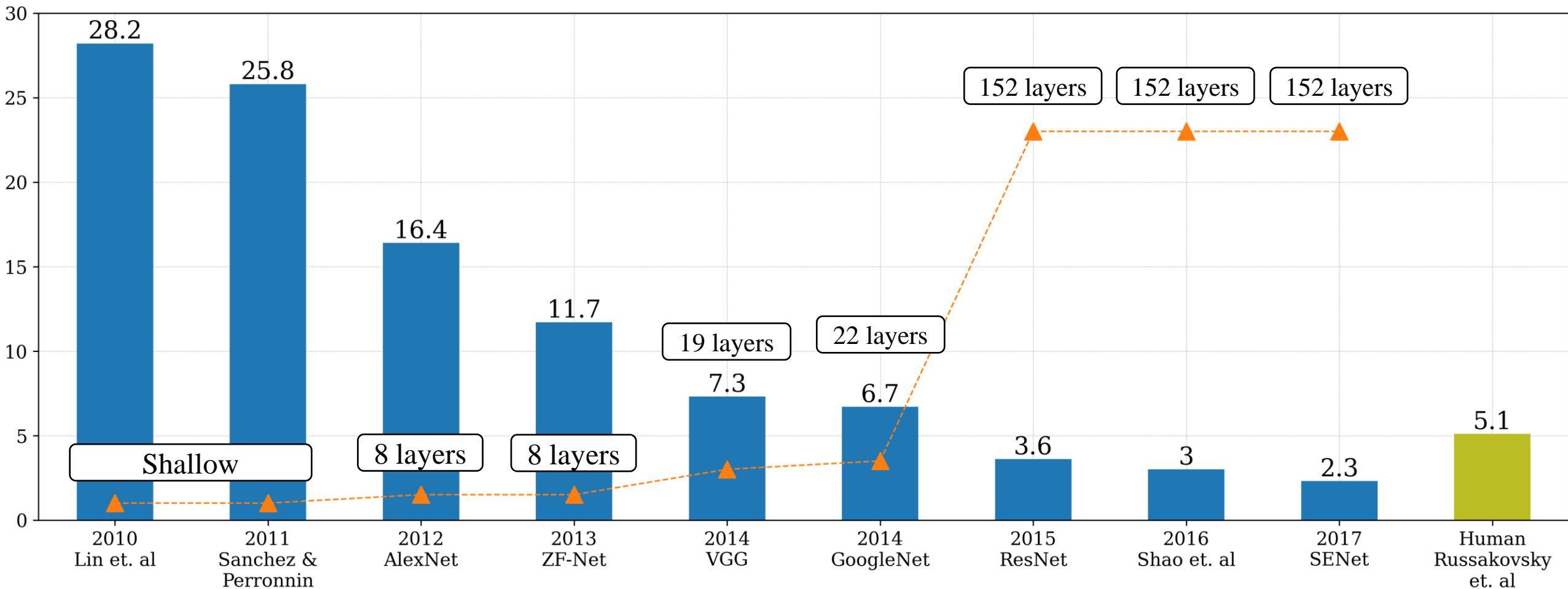
Squeeze-and-Excitation Networks (SENet)

[Hu et al. 2017]

- Add a “feature recalibration” module that learns to adaptively reweight feature maps
- Global information (global avg. pooling layer) + 2 FC layers used to determine feature map weights
- ILSVRC’17 classification winner (using ResNeXt-152 as a base architecture)

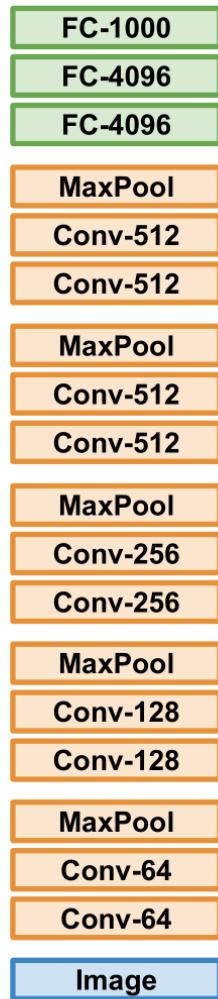


ImageNet Challenge Error Rates over time



Completion of the challenge: Annual ImageNet competition no longer held after 2017
-> now moved to Kaggle.

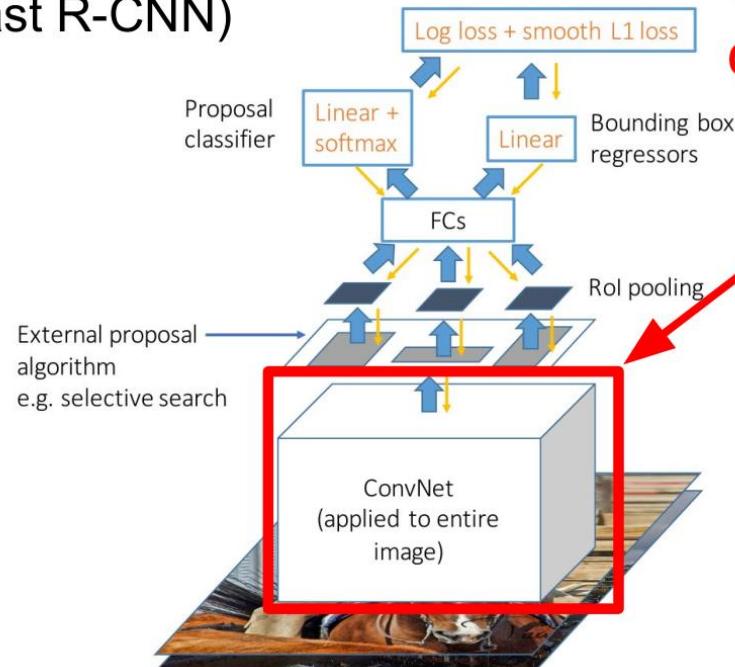
Transfer Learning



	very similar dataset	very different dataset
very little data	Use Linear Classifier on top layer	You're in trouble... Try linear classifier from different stages
quite a lot of data	Finetune a few layers	Finetune a larger number of layers

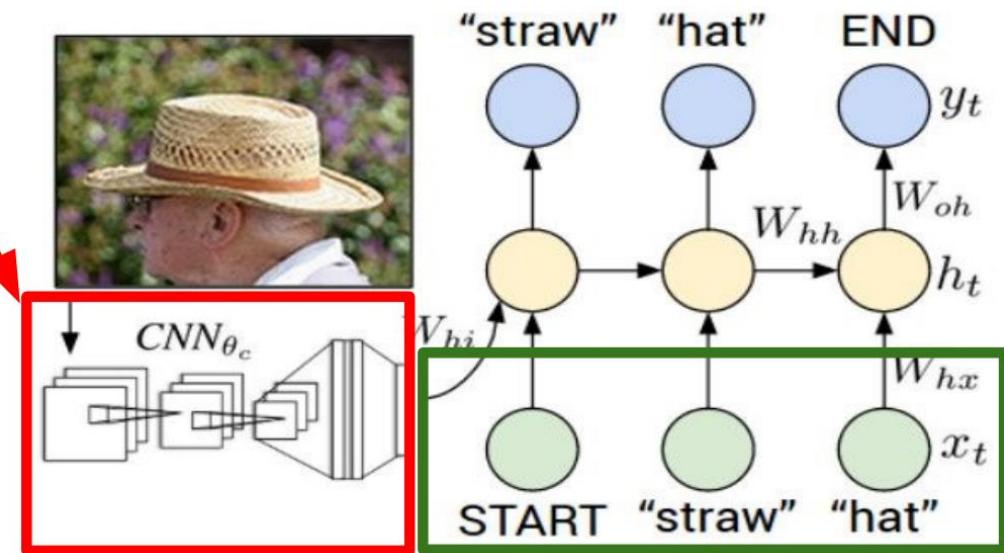
Transfer learning with CNNs is pervasive... (it's the norm, not an exception)

Object Detection
(Fast R-CNN)



CNN pretrained
on ImageNet

Image Captioning: CNN + RNN

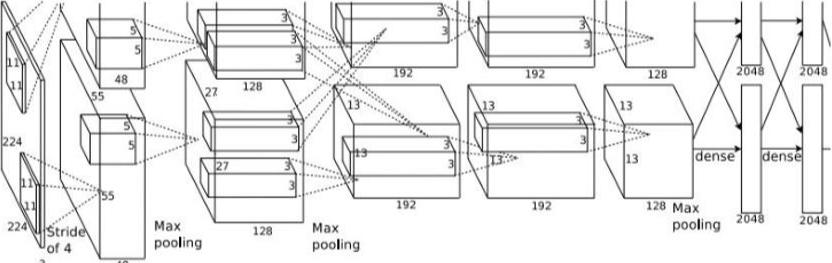
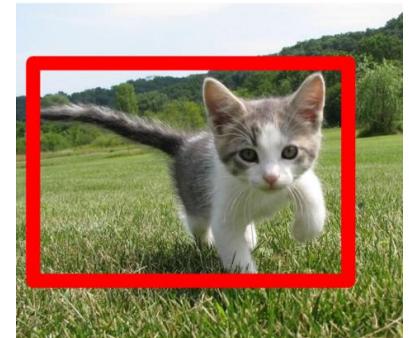


Word vectors pretrained
with word2vec

Girshick, "Fast R-CNN", ICCV 2015
Figure copyright Ross Girshick, 2015. Reproduced with permission.

Karpathy and Fei-Fei, "Deep Visual-Semantic Alignments for Generating Image Descriptions", CVPR 2015
Figure copyright IEEE, 2015. Reproduced for educational purposes.

Image Classification + Localization



Vector:
4096

**Fully
Connected:**
4096 to 1000

**Fully
Connected:**
4096 to 4

Class Scores

Cat: 0.9
Dog: 0.05
Car: 0.01
...

Box

Coordinates → L2 Loss
(x, y, w, h)

Correct label:
Cat

**Softmax
Loss**

+ → **Loss**

Correct box:
(x', y', w', h')

Semantic Segmentation

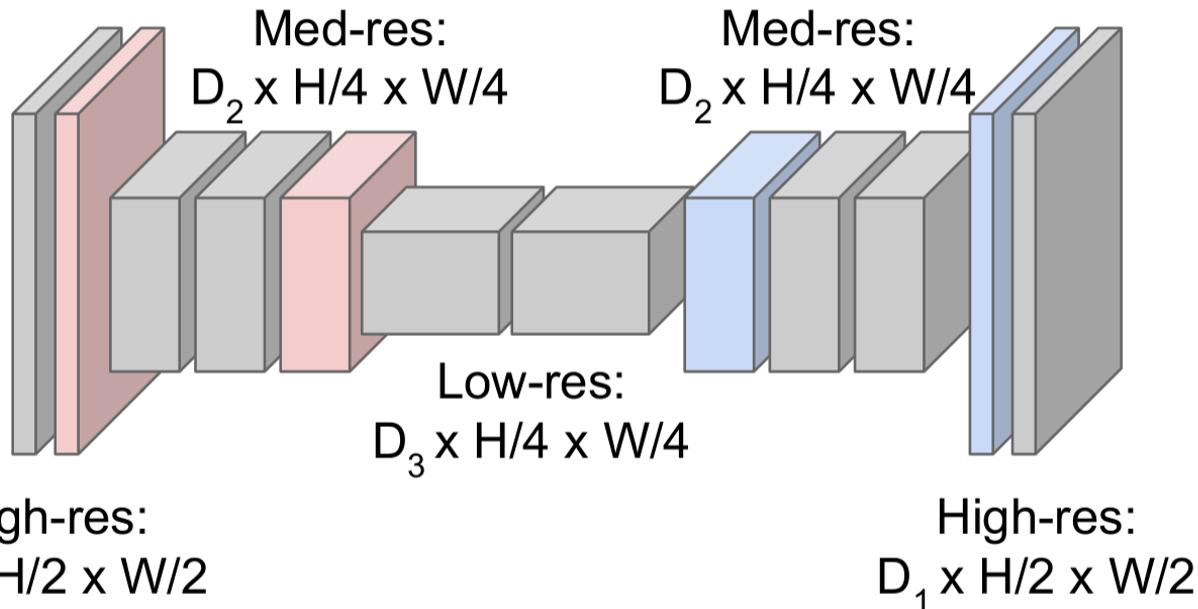
Downsampling:
Pooling, strided convolution



Input:
 $3 \times H \times W$

High-res:
 $D_1 \times H/2 \times W/2$

Design network as a bunch of convolutional layers, with
downsampling and **upsampling** inside the network!



Upsampling:
Unpooling or strided transposed convolution



Predictions:
 $H \times W$

Long, Shelhamer, and Darrell, "Fully Convolutional Networks for Semantic Segmentation", CVPR 2015
Noh et al, "Learning Deconvolution Network for Semantic Segmentation", ICCV 2015

Deep Learning

- Typical Deep Learning networks formed using Convolutional and Max Pool layers
- Deep Learning models show higher generalization capabilities compared to classical Machine Learning methods
- Deep Learning models have been highly successful in problems across several domains - Computer Vision, Natural Language Processing, Information retrieval, Computational Biology and Chemistry, Astrophysics,...